heometrical Transformation

\* Transformation! - Transformation means changes in orientation, size & shape of the object. At is the Geometric changes of an Object from a current state to modified state.

-> Basic Geometric transformation are:-(i) Translation (ii) Rotation (iii) Scaling

(1) Translation: It is repositioning of an object from one place to another in called

Translation. To transcate a point from Coordinate position P(n,y) to another P'(n,'y'), we add the algebraically translation distance to and ty to original co-ordinad.

tn and ty called as shift vector. or Tramlation vector.

The matrix ocpruentation will be:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} 4\pi \\ 4y \end{bmatrix}$$

Q. Translate the triangle [A(10,10), B(15,15), C(20,10)]
2 unit in n-direction and 1 unit in y
direction.

Solh:- we know that 
$$P' = P + T$$

$$P' = [P] + [tr]$$

$$\mathsf{A}_1 = \begin{bmatrix} 70 \\ 70 \end{bmatrix} + \begin{bmatrix} 7 \\ 7 \end{bmatrix}$$

$$A' = \begin{bmatrix} 10+2 \\ 10+1 \end{bmatrix} = \begin{bmatrix} 12 \\ 11 \end{bmatrix}$$

$$\mathbf{S}' = \begin{bmatrix} 15 \\ 15 \end{bmatrix} + \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

$$B^{\dagger} = \begin{bmatrix} 15+2 \\ 15+1 \end{bmatrix} = \begin{bmatrix} 17 \\ 16 \end{bmatrix}$$

for point ( (20, 40)

$$C' = \begin{bmatrix} 20+2 \\ 20+1 \end{bmatrix} = \begin{bmatrix} 22 \\ 21 \end{bmatrix}$$

final Coordinate after translation are A'(12,11), B'(14,16), C'(22,11)



(ii) Rotation! - It is a process of changing the angle of the object. Rolation Can clockwise or anticlockwise.

for Rotadiola we have to specify the angle of Hotation and Holation point.

$$\pi' = \tau \cos(\theta + \phi)$$

$$= \tau (\cos\theta \cos\phi - \sin\theta \sin\phi)$$

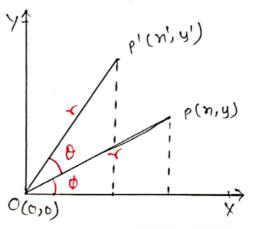
- =) T COSO. COSO Tring. sind
- =) ncoso ysino r cost fring

y'= x (sin & sin (0+0)

- =) ~ ( sino.cos \$ + coso.sin \$)
- =) & sino.cosp + x coso.sind
- =) Asino + y cuso T. cosp s. sind

m = n coro - yrino y = nsino + y coro

$$\begin{bmatrix} n' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} \eta \\ y \end{bmatrix}$$



D. A point P(4,3) is stated clockwise direction by the angle of 450. find the station mass R and the steellant points.

$$P^{1} = R \cdot P$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$= \begin{bmatrix} \cos 45^{\circ} & -\sin 45^{\circ} \\ \sin 45^{\circ} & \cos 45^{\circ} \end{bmatrix} \begin{bmatrix} 4 \\ 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix} \begin{bmatrix} 4 \\ 3 \end{bmatrix}$$

$$= \begin{pmatrix} \frac{4}{\sqrt{2}} - \frac{3}{2} \\ \frac{4}{\sqrt{2}} + \frac{3}{\sqrt{2}} \end{pmatrix}$$

Q. obtain the final Coordinate after two rotation on point p(6,9) with sociation of angles are 300 and 60° suspectively.

$$P' = \begin{bmatrix} \cos(\theta_1 + \theta_2) & -\sin(\theta_1 + \theta_2) & 0 \\ \sin(\theta_1 + \theta_2) & \cos(\theta_1 + \theta_2) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 6 \\ 9 \\ 1 \end{bmatrix}$$

$$P' = \begin{bmatrix} \cos(30+60) & -\sin(30+60) & 0 \\ \sin(30+60) & \cos(30+60) & 0 \\ 0 & 0 & 1 \end{bmatrix}. \begin{bmatrix} 6 \\ 9 \\ 1 \end{bmatrix}$$

$$P^{1} = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 6 \\ 9 \\ 1 \end{bmatrix} = \begin{bmatrix} -9 \\ 6 \\ 1 \end{bmatrix}$$

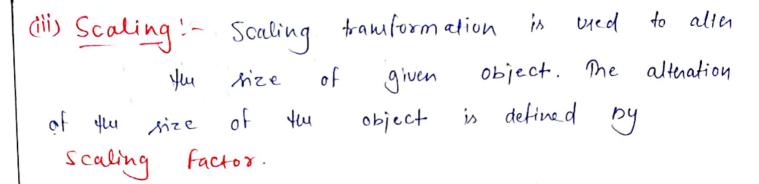
final Co-ordinates after rotations are (-9,6).

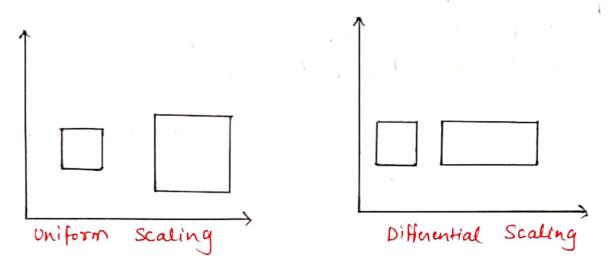
\* matrix for Homogeneous Co-ordinate Rotation Clockwhe!

$$R = \begin{cases} c010 & -3in0 & 0 \\ 8in0 & c010 & 0 \\ 0 & 0 & 1 \end{cases}$$

\* Matrix for Homogeneous Co-ordinate stotation Anticlockwise:

$$R = \begin{bmatrix} coso & sino & o \\ -sino & coso & o \\ o & o & 1 \end{bmatrix}$$





There are two Scaling fractors i.e. Sx in no direction, Syd in y direction.

-> matrix for scaling !-

$$S = \begin{bmatrix} Sn & 0 & 0 \\ 0 & Sy & 0 \\ 0 & 0 & 1 \end{bmatrix}, \begin{bmatrix} n1 \\ y1 \end{bmatrix} = \begin{bmatrix} Sn & 0 & 0 \\ 0 & Sy & 0 \\ 0 & 0 & 1 \end{bmatrix}, \begin{bmatrix} n1 \\ 1 \\ 1 \end{bmatrix}$$

sn and sy is scaling matter, [PI = Snsy.P]

Q. obtain the final co-ordinates after two scaling on line pg [p(2,2), g(8,8)] with scaling factors are (2,2) and (3,3) respectively.

P= S(Sn1. Sn2, Sy1. Syz). P



$$b_1 = \begin{bmatrix} 0 & 2\lambda 1 \cdot 2\lambda 5 & 0 & 0 \\ 0 & 2\lambda 1 \cdot 2\lambda 5 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 3 & 0 \\ 5 & 0 \\ 5 & 0 \end{bmatrix}$$

$$P' = \begin{bmatrix} 6 & 0 & 0 \\ 0 & 6 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 2 & 8 \\ 2 & 8 \\ 1 & 1 \end{bmatrix}$$

$$P' = 
 \begin{bmatrix}
 12 + 0 + 0 & 40 + 0 + 0 \\
 0 + 12 + 0 & 0 + 40 + 0 \\
 0 + 0 + 1 & 0 + 0 + 1
 \end{bmatrix}
 = 
 \begin{bmatrix}
 12 & 40 \\
 12 & 40 \\
 1 & 1
 \end{bmatrix}$$

G. Scale a polygon with co-ordinate 
$$A(2,5)$$
,  $B(7,10)$ ,  $C(10,2)$  by 2 with in  $n-$ 

$$R = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad P = \begin{bmatrix} 2 & 4 & 10 \\ 5 & 10 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

$$p' = 
 \begin{bmatrix}
 2 & 0 & 0 \\
 0 & 3 & 0 \\
 0 & 0 & 1
 \end{bmatrix}
 \begin{bmatrix}
 2 & 4 & 10 \\
 5 & 10 & 2 \\
 1 & 1 & 1
 \end{bmatrix}$$



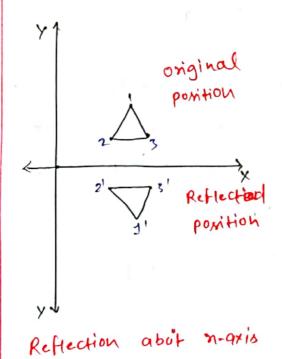
$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 4+0+0 & 14+0+0 & 20+0+0 \\ 0+15+0 & 0+30+0 & 0+6+0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 31 \\ 4 \end{bmatrix} = \begin{bmatrix} 4 & 14 & 20 \\ 15 & 30 & 6 \\ 4 & 1 & 1 \end{bmatrix}$$

final co-ordinates are A(4,15), B(14,30), c(20,6)

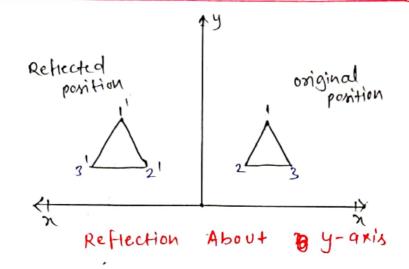
(IV) Reflection! - Reflection is a transformation which produces mirror image of a giver Object. Mis translation can be produce Rela to n-axis or y-axis. The axis wound which reflection takes place is

called angle of Reflection.



This transformation keeps n-val agre some, but flips (change the sign) y value of coordinate positions.

Transformation Matrix is!



This transformation keeps y values are same, but felips (change the sign) or value of coordinate position.

Transformation Matrix !-

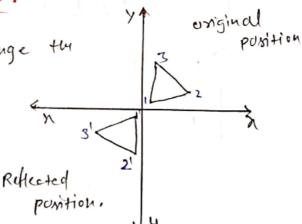
$$\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

-> Reflection About origin:-

This transformation flips (change tu

righ) in and y both values

or co-ordinate pusition.

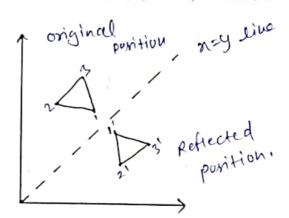


Reft

Transformation Matrix:



## -> Transformation matrix for reflection above the line.

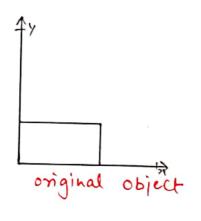


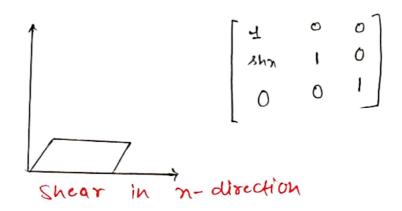
Q. find the Co-ordinate after reflection of the triangle [A(±0,±0), B(15,15), C(20,±0)] about n-axis.

$$P = \begin{bmatrix} 10 & 15 & 20 \\ -10 & -15 & -10 \\ 1 & 1 & 1 \end{bmatrix}$$

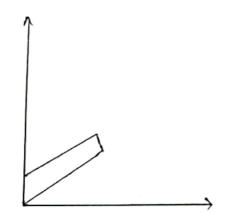
final co-ordinate ofthe reflection are A(40,-40), B(15,-15), C(20,-10)

- (V) Shear Transformation! It is transformation which changes the shape of the object. The shear can be in one direction or two directions.
- -> Shearing in the n-direction:-





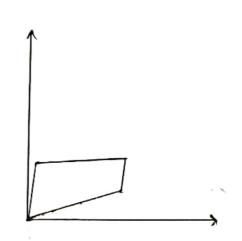
-> Shearing in y-direction:



$$\begin{bmatrix} 1 & shy & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

-> Shearing in n-y directions:

$$\begin{bmatrix}
1 & Shy & O \\
Ohn & 1 & O \\
O & O & 1
\end{bmatrix}$$



- \* Homogeneous Co-ordinales:- To perform a Sequence of transformation such as translation followed by rotation and Scaling. we need to follow a Sequential process like:-
  - -> Rotate tu translated coordinale.
  - -> Men scale the rotated coordinates to complete the Composite transformation.
- To shorten this process, we have to use 3x3 transformation matrix instead of 2x2.
- \*\*Companie Transformation! A Number of transformation can be combined into single one called as Compasition. The Resultant matrix called as Compasite matrix.
- Q. find Companie matrix?
  - (i) Apply translation by Y(Y,Y)
  - (ii) Rotate 'the translation by 45° in anticlockwise direction.
  - (111) Scaling the Gotated Object by (1,1/2).

$$T_{1} = \begin{bmatrix} 1 & 0 & T_{2} \\ 0 & 1 & T_{2} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

$$T_{2} = \begin{bmatrix} \cos 0 & -\sin 0 & 0 \\ \sin 0 & \cos 0 & 0 \end{bmatrix} = \begin{bmatrix} \cos 45^{\circ} & -\sin 45^{\circ} & 0 \\ \sin 45^{\circ} & \cos 45^{\circ} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\eta_3 = 
 \begin{bmatrix}
 s_n & 0 & 0 \\
 o & sy & 0 \\
 o & 0 & 1
 \end{bmatrix} = 
 \begin{bmatrix}
 1 & 0 & 0 \\
 0 & 1/2 & 0 \\
 0 & 0 & 1
 \end{bmatrix}$$

$$T = T_3 \cdot T_2 \cdot T_1$$

$$T = T_1 \cdot T_2 \cdot T_3$$

$$T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1/2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1/12 & -1/1\sqrt{2} & 0 \\ 1/1\sqrt{2} & 1/\sqrt{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1/2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1/\sqrt{2} & -4/\sqrt{2} & 1/\sqrt{2} + (-1/\sqrt{2}) + 0 \\ 1/\sqrt{2} & 1/\sqrt{2} & 1/\sqrt{2} & 1/\sqrt{2} + (-1/\sqrt{2}) + 0 \\ 0 & 0 & 1 \end{bmatrix}$$



$$T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1/2 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 0 \\ 1/\sqrt{2} & 1/\sqrt{2} & \sqrt{2} \\ 0 & 0 & 1 \end{bmatrix}$$

$$T = \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 0 \\ 1/2 \times 1/\sqrt{2} & 1/2 \times 1/\sqrt{2} & \frac{2}{2} \times \sqrt{2} \\ 0 & 0 & 1 \end{bmatrix}$$

$$T = \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 0 \\ 1/2\sqrt{2} & 1/2\sqrt{2} & \sqrt{2}/2 \\ 0 & 0 & 1 \end{bmatrix}$$

$$T = \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & -1 & 0 \\ 1/2 & 1/2 & 1 \\ 0 & 0 & 0 \end{bmatrix}$$

$$T = \frac{1}{2} \begin{bmatrix} 1 & -1 & 0 \\ 1/2 & 1/2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

\* Jwe? :-

Q-find the transformation at triangle A(1,0), B(0,±) c(1,1) by translating ± unit in n and y direction and then relate 45' aboute origin.

801= Translation by I unit in n,y direction.

$$\begin{bmatrix} \chi' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & Ex \\ 0 & 1 & Ey \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ y_2 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}, \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ \frac{1}{2} \end{bmatrix} = \begin{bmatrix} 1+1 & 1 & 1+1 \\ 1 & 1+1 & 1+1 \\ 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

Coordinate after transformation A(2,1), B(1,2), G(2,2)

-> Now Rotation about 45' antidockwine.

about the origin (antidockwine)

$$\begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \\ 3 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ 2 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} y' \\ y' \\ \pm \end{bmatrix} = \begin{bmatrix} \cos 45 & \sin 45 & 0 \\ -\sin 45 & \cos 45 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} & 0 \\ -1/\sqrt{2} & 1/\sqrt{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

$$=) \begin{cases} \frac{3}{\sqrt{52}} & \frac{3}{\sqrt{52}} & \frac{4}{\sqrt{52}} \\ -\frac{1}{\sqrt{52}} & -\frac{1}{\sqrt{52}} & 0 \end{cases}$$

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Q. perform 45' rotation of triangle A(0,0), B(1,1), C(5,2).

- @ About the origin
- (B) About tu point (-1,-1)

Solh @ Rotation About the oxigin.

$$\begin{bmatrix} x_1' & x_{12}' & x_{13}' \\ x_1' & x_{22}' & x_{23}' \end{bmatrix} = \begin{bmatrix} cox 0 & -xin 0 & 0 \\ sin 0 & cox 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} x_1' & x_{12} & x_{13} \\ y_1' & y_{12} & y_{23} \\ 1 & 1 & 1 \end{bmatrix}$$

$$=) \begin{cases} 0 & \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} & \frac{5}{\sqrt{2}} - \frac{2}{\sqrt{2}} \\ 0 & \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} & \frac{5}{\sqrt{2}} + \frac{2}{\sqrt{2}} \\ 1 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{cases}$$

coordinates after Rotation about the origin are: A(0,0),  $B(0,\sqrt{2})$ ,  $C(3/12,7/\sqrt{2})$ 

$$T_{1} = \begin{bmatrix} 1 & 0 & t_{7} \\ 0 & 1 & t_{9} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 - (-1) \\ 0 & 1 & 0 - (-1) \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

$$T_{2} = \begin{bmatrix} \cos 45' & -\sin 45' & D \\ \sin 45' & \cos 45' & D \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 0 \\ 1/\sqrt{2} & 1/\sqrt{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$M = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1/\sqrt{12} & -1/\sqrt{12} & 0 \\ 1/\sqrt{12} & 1/\sqrt{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}$$

$$M = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & 1/\sqrt{2} & 1/\sqrt{2} \\ 0 & 0 & 1 \end{bmatrix}$$

$$M = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 0 \\ 1/\sqrt{2} & 1/\sqrt{2} & \sqrt{2} \\ 0 & 0 & 1 \end{bmatrix}$$

(9)

And C(5,2) to twice its size while clipping C(5,2) fixed.

for point c(5,2

New triangle Co-ordinater = positive translation matrix \* scaling

matrix \* Negative translation matrix

for point

C(5,2)

$$= \begin{bmatrix} 1 & 0 & tn \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & -tn \\ 0 & 1 & -ty \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 5 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & -5 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{bmatrix}$$

$$=) \begin{bmatrix} 1 & 0 & 5 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 2 & 0 & -10 \\ 0 & 2 & -4 \\ 0 & 0 & 1 \end{bmatrix}$$

$$=) \begin{bmatrix} 2 & 00 & -10 + 5 \\ 0 & 2 & -4 + 2 \\ 0 & 0 & 4 \end{bmatrix}$$

NOW multiply the resultant matrix with triangle matrix.

$$M = \begin{bmatrix} 1/\sqrt{2} & -1/\sqrt{2} & -1 \\ 1/\sqrt{2} & 1/\sqrt{2} & \sqrt{2} -1 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix}
 A'B'C'
 \end{bmatrix} = \begin{bmatrix}
 1/\sqrt{2} & -1/\sqrt{2} & -1 \\
 1/\sqrt{2} & 1/\sqrt{2} & \sqrt{2}-1 \\
 0 & 0 & 1
 \end{bmatrix} \cdot \begin{bmatrix}
 0 & 1 & 5 \\
 0 & 1 & 2 \\
 1 & 1 & 1
 \end{bmatrix}$$

$$=) \begin{bmatrix} -1 & -1 & \frac{5}{2} - 1 \\ 52 - 1 & 2 \cdot 1 - 1 & \frac{7}{2} - 1 \\ 4 & 1 & 4 \end{bmatrix}$$

$$= \begin{cases} -1 & -1 & \frac{\sqrt{3}-2}{2} \\ \sqrt{2}-1 & 2\sqrt{2}-1 \\ 1 & 1 \end{cases}$$

final coordinates after rotation About point 
$$(-1,-1)$$
 are.  $A(-1,\sqrt{2}-1)$ ,  $B(-1,2\sqrt{2}-1)$ ,  $C(\frac{\sqrt{2}-2}{2},\sqrt{2}-1)$ 



$$= \begin{bmatrix} 2 & 0 & -5 \\ 0 & 2 & -2 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 0 & 1 & 5 \\ 0 & 1 & 2 \\ 1 & 1 & 1 \end{bmatrix}$$

New Coordinate of Triangle =) A(-5,-2), B(-3,0), C(5,2)