

COMP 2402 w22
Assignment 3 Workshop

Part A

Q1:

Example 1:

`x = 3` → this tells us the length of the chain is 3

input:

`5` → first element in the chain is always index 0
element % length = `5 % 6 = 5` → so the next element
is
at index 5
→ third and final element

`4`

`8`

`10`

`2`

`6` → second element in the chain
element % length = `6 % 6 = 0` → so next element is
at
index 0

Chain:

`[5, 6, 5]`

`(5 + 6 + 5) mod 2402 = 16`

output: `16`

Example 2:

$x = 3$

input:

5 → first element in the chain

$5 \% 6 = 5 \rightarrow$ got to index 5

4 → third and final element

8

10

2

7 → second element in the chain

$7 \% 6 = 1 \rightarrow$ go to index 1

Chain:

[5, 7, 4]

$(5 + 7 + 4) \bmod 2402 = 16$

output: 16

Example 3:

$x = 0$

Input:

1

2

3

4

5

Output: 0 ← Since $x = 0$

Example 4:

x = 1

Input:

1

2

3

4

5

Output: **1**

Q2:

Example 1:

$x = 3 \rightarrow$ this tells us the length of the chain is 3

input:

5 \rightarrow first element in the chain
 $5 \% 6 = 5 \rightarrow$ got to index 5
 \rightarrow third and final element

4

8

10

2

6 \rightarrow second element in the chain
 $6 \% 6 = 0 \rightarrow$ go to index 0

Chain:

[5, 6, 5]

5 (index 0) contributes 0 (no previous values)

6 (index 1) contributes 0 (only previous value = 5 < 6)

5 (index 2) contributes 5 (5 \geq 5 and closer to 5 than 6)

$$(0 + 0 + 5) \bmod 2402 = 5$$

output: 5

Q2:

$x=3$

5

4

8

10

2

6

chain is selected same as in Q1:

5 6 5

no previous values in chain, contributes 0

no previous values \geq in chain, contributes 0

5 and 6 are ≥ 5 , 5 is closer to 5, so contributes 5.

$$(0+0+5) \bmod 2402 = \underline{5}$$

Example 2:

$x = 3 \rightarrow$ this tells us the length of the chain is 3

Input:

index

0 5 \rightarrow 1st element in the chain, $5\%6=5 \rightarrow$ go to index 5

1 4 \rightarrow Third element in chain

2 8

3 10

4 2

5 1 \rightarrow second element in the chain

$1 \% 6 = 1 \rightarrow$ go to index 1

Chain:

[5, 1, 4]

5 (index 0) contributes 0 (no previous values)

1 (index 1) contributes 5 ($1 < 5$)

4 (index 2) contributes 5 ($4 < 5$)

$(0 + 5 + 5) \bmod 2402 = 10$

output: 10

Example 3:

$x = 0$

Input:

1

2

3

Output: 0 since $x = 0$

Example 4:

`x = 1`

Input:

`1`

`2`

`3`

Output: `0` since `x = 1` contributes `0` (no previous values)

Q3:

Example 1:

$x = 3 \rightarrow$ this tells us the length of the chain is 3 and we're

inserting $x-1=2$ times

input:

8
4
7
10
2
9

Step 1: Get first element in the chain

8 \rightarrow first element in the chain

Get value to insert:

$l.size()-1-i = 6 - 1 - 0 = 5$

value at index 5 = 9

Get position to insert at:

$(i+1)\%l.size() = (0+1)\%6 = 1$

Insert 9 at index 1

4
7
10
2
9

Step 2: Insert first time

8

9 \rightarrow inserted 9 at index 1

4
7
10
2
9

Step 3: Get second element in chain

$element \% length = 8 \% 7 = 1 \rightarrow$ go to position 1 for 2nd element

8

9 \rightarrow second element in the chain

Get value to insert:

$l.size()-1-i = 7 - 1 - 1 = 5$

value at index 5 = 2

Get position to insert at:

```
(i+1)%l.size() = (1+1)%7 = 2  
Insert 2 at index 2
```

```
4  
7  
10  
2  
9
```

Step 4: Insert second time

```
8  
9  
2 → inserted 2 at index 2  
4  
7  
10  
2  
9
```

Step 5: Get third (final) element in chain

element % length = 9 % 8 = 1 → go to position 1 for 3rd element

```
8  
9 → third element in the chain  
Note we don't need to get value to insert this  
time  
because we have completed the chain, any other  
work  
on this list is now unnecessary
```

```
2  
4  
7  
10  
2  
9
```

Chain:

```
[8, 9, 9]
```

```
(8 + 9 + 9) mod 2402 = 26
```

output: 26

Q4:

Example 1:

x = 5

First step:

	index	
10	0	← 1st element of chain 10 mult of 5 (correct)
20	1	
5	2	
3	3	
2	4	
24	5	

Chain: 10

Second step:

	index	
10	0	← $(10 \% 6) = 4$ next element is index 4
20	1	
5	2	
3	3	
2	4	← 2nd element, check the chain, add 10 to sum, add 2 to chain
24	5	

Chain: 10, 2

Sum: 10

Third step:

	index	
10	0	
20	1	
5	2	← check chain, add 10 to sum, add 5 to chain then 5 mult 5 is correct
3	3	
2	4	← $2 \% 6 = 2$, next element is index 2
24	5	

Chain: 10, 2, 5

Sum: 10, 10

Fourth step:

index

10	0
20	1
5	$2 \leftarrow 5 \% 6 = 5$, next element is index 5
3	3
2	4

24 5 \leftarrow check chain, add 5 to sum, and 24 div by 24,
remove the minimum multiple of 5 in chain, add 24 to chain

Sum: 10, 10, 5

Chain: 10, 2, 5 \leftarrow remove , 24

Chain:10, 2, 24

Fifth step:

index	
10	0 \leftarrow check chain, add 10 to sum, and add 10 to chain
20	1
5	2
3	3
2	4
24	$5 \leftarrow 24 \% 6 = 0 \leftarrow$ next element is index 0

Sum: 10, 10, 5,10

Chain: 10, 2, 24

Chain:10, 2, 24,10

Part B

Q5:

Example 1:

```
this = {4, 6, 8, 10}
other = {1, 2, 5}
```

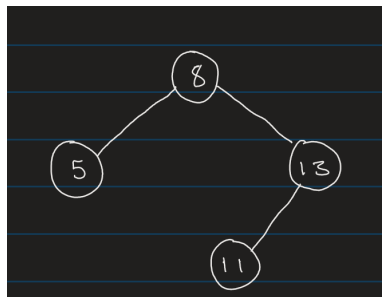
```
{4+1, 6+2, 8+5, 10+1} = {5, 8, 13, 11} → {5, 8, 11, 13}
```

Note that this is a set and not a list:

- No duplicates
- The order in which we write it is not important

Hint: be sure to thoroughly read through the `BinarySearchTree` class → there is an iterator method

Possible visual representation of output:



Note it could look different → remember that a binary search tree is made up of nodes which have a left and right child whose values were not established above, so this tree might look a bit different.

This problem is similar to assignment 1 question 6 and assignment 2 question 5. You can see more “edge cases” and examples from the previous workshops.

The difference / challenge with `sum()` using binary search trees, is that you’re working with sets now as opposed to lists and each element in the set is actually a node - be sure to read the node class.

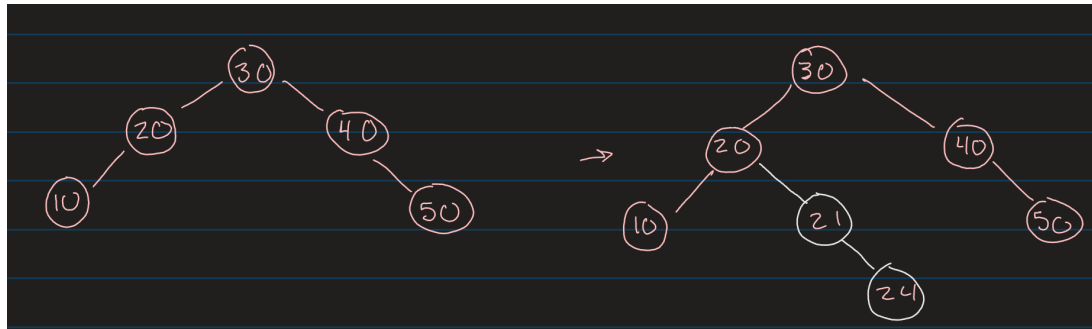
Q6:

Example 1:

```
this = {10, 20, 30, 40, 50}
other = {21, 24}
```

{10, 20, 21, 24, 30, 40, 50}

Possible visual representation of output:

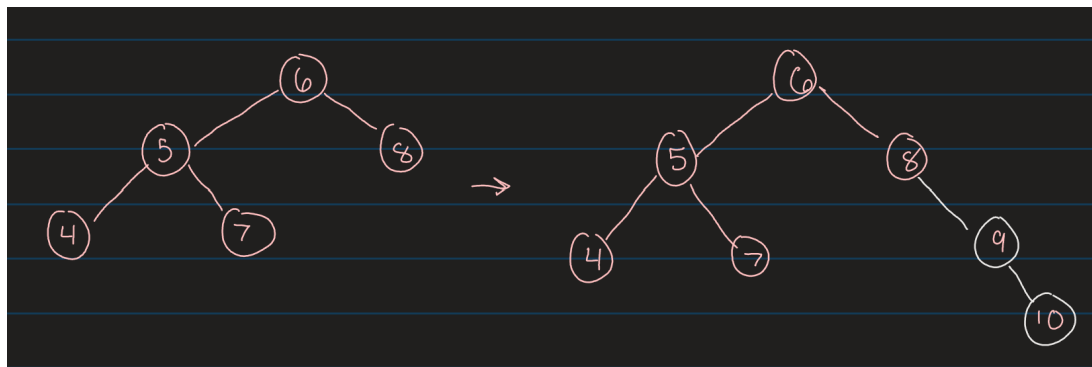


Example 2:

```
this = {4, 5, 6, 7, 8}
other = {9, 10}
```

{4, 5, 6, 7, 8, 9, 10}

Possible visual representation of output:



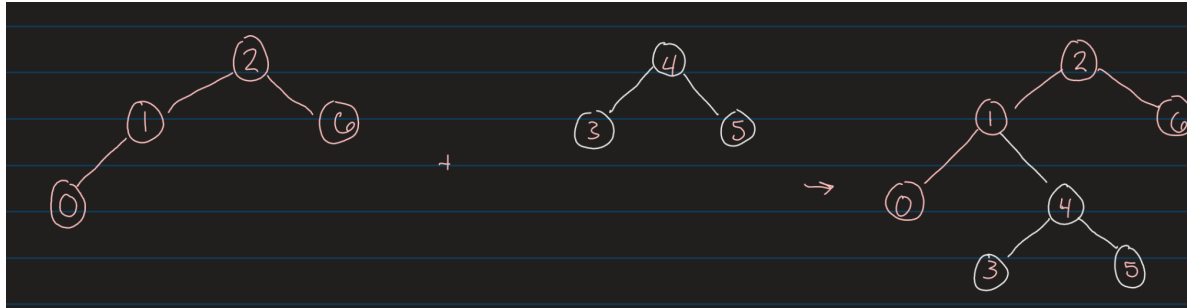
Example 3:

```
this = {0, 1, 2, 6}
```

```
other = {3, 4, 5}
```

```
{0, 1, 2, 3, 4, 5, 6}
```

Possible visual representation of output:



Example 4:

```
this = {0, 1, 2, 6}
```

```
other = {}
```

```
{0, 1, 2, 6}
```

Example 5:

```
this = {}
```

```
other = {1, 2}
```

```
{1, 2}
```

This question is similar to assignment 2 questions 7 and 9, but with binary search trees now.

Q7:

Example 1:

```
this = {2, 4, 5, 6, 7, 8, 9}
y = 2
```

$2 \% 2 = 0$

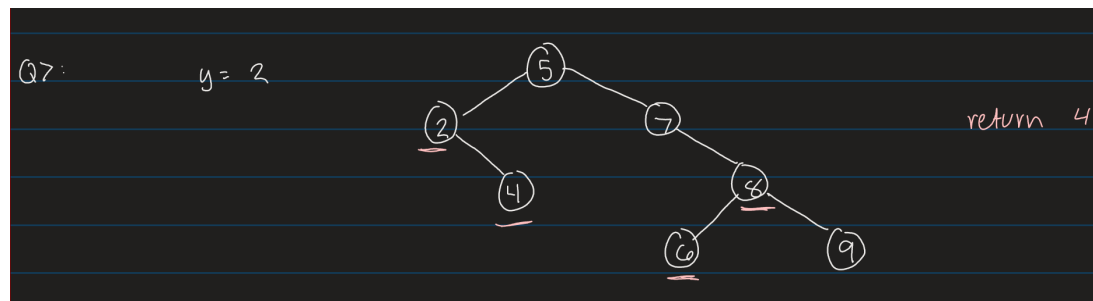
$4 \% 2 = 0$

$6 \% 2 = 0$

$8 \% 2 = 0$

output: **4**

Possible visual representation of output:



This problem is hopefully pretty straightforward to understand, the challenge will be implementing a time efficient algorithm.

Note: you can't use recursion for this problem.

Example 2:

```
this = {3, 5, 7}
y = 2
```

output: **0**

Q8:

Example 1:

```
this = [4, 10, 20, 12, 12, 30, 24]
```

```
smallest(1) = root = 4
```

```
smallest(2) = 10
```

```
smallest(3) = 12
```

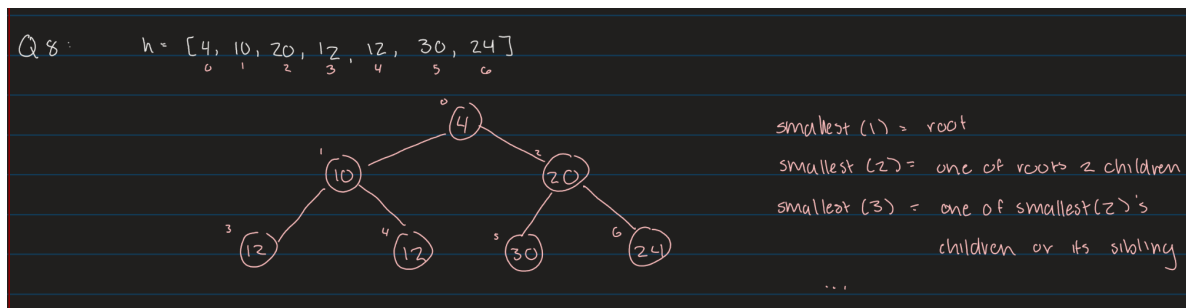
```
smallest(4) = 12
```

```
smallest(5) = 20
```

```
smallest(6) = 24
```

```
smallest(7) = 30
```

Possible visual representation of output:



Note: you can assume k is an integer between 1 and size