

Prob 2:

a)

```
struct stack {  
    unsigned short size (2)  
    T minimum (sizeof T)  
    T data[maxSize] (sizeof T * maxSize)  
}
```

Following type T, the struct stack need size that sizeof (T * (max size + 1) + 4) bytes. Size of stack always be $n \geq 0$. It couldn't be negative. If max size is bigger then 65535, size could be int or more bigger type.

In initializing, size = 0, minimum = MAX_VALUE_OF_TYPE is required.

```
PUSH(T) {  
    stack.data[size] = T;  
    if (T < stack.minimum) T = stack.minimum;  
} -> add T at index 'size' of array data of stack. if size is 0, minimum is T, and size + 1. else T is  
smaller then minimum in stack, minimum is T. Or not ignore.
```

```
POP() {  
    if (!isEmpty()) {  
        T t = stack.data[size];  
        size -= 1;  
        return t;  
    } else  
        return -1; // Means stack is empty.  
}  
}-> return T at index 'size' of array data of stack. And size -1. If size is 0, return error type of  
T.
```

```
TOP() {  
    if (!isEmpty()) return stack.data[size];  
    return -1; // Means stack is empty.  
}-> return T at index 0 of array data of stack. If size is 0, return error type of T.
```

```
SIZE() {  
    return stack.size;  
}-> return size of stack.
```

```
isEmpty() {  
    return SIZE();  
}-> return size of stack. In programming, 0 means false, else means true.  
getMinimum() -> return minimum of stack.
```

b) The correctness follows size of stack. Need to handle 0 size case and max size case. We re-define the max size of stack or expand max size of stack with dynamic array if there is more data then max size of stack.

c) PUSH(T) always add a values in last runs in $O(1)$ time, POP() always remove and return value in last runs in $O(1)$ time, TOP() return last value when size is no 0 runs in $O(1)$ time, SIZE() always constant value of stack runs in $O(1)$ time, isEmpty() always return size of stack runs in $O(1)$ time, getMinimum() always return constant T of stack runs in $O(1)$ time follow a), need size that sizeof (T * (max size + 1) + 4) bytes.

Prob 3:

a) Traverse from last index to first index. On each data(height of lighthouse) traverse current index of data of index 0, start with data -1 and if data[k] is bigger than data[i], data - 1, desl escape inner traverse and so on.

b)

```
int [] func(int arr[]) {
    for (int k = arr.size() - 1; k >= 0; k--) {
        if ( k == 0 ) {
            arr[k] = -1;
            break;
        }
        for( int i = k-1; i >= 0; i--) {
            arr[k]--;

            if (arr[k] > arr[i]) arr[k]--;
            else break;
        }
    }
    return arr;
}
```

b)

func() travels the array only once from bottom to top(index 0) runs in $O(n)$. Though inner travels from current index of data to top. If met bigger one, it will be done. In this case, best one runs in $O(1)$ when meet bigger one at first every single inner traverse. but the Worst one runs in $O(\log n)$ when in every traverse from current index to 0. So it takes time complexity n to $n \log n$. As the Big-O time complexity, the time complexity of algorithm is $O(n \log n)$.