

$$\begin{array}{l}dF=\\-\frac{S}{dT}-\\ \frac{P}{dV}+\\ \frac{\mu}{dN}\\ U=\\ F+\\ \frac{T}{S}\\ 0.45<\\ T/T_c<\\ \frac{1}{T_c^{13}}\\ \frac{1}{\eta_N}=\\ \frac{\overline{\eta}}{\eta}=\\ packingFraction\\ \Lambda =\end{array}$$

$$(1) \quad \frac{F}{N \cdot k \cdot T} = a^{IDEAL} + a^{HS} + \beta \cdot a_1^{SW} + \beta^2 \cdot a_2^{SW}$$

$$(2) \quad a^{IDEAL}=\ln\left(n\cdot\Lambda^3\right)-1$$

$$(3) \quad a^{HS}=-ln(1-4\cdot\eta)$$

$$(4) \quad a_1^{SW}=a_1^{VDW}\cdot g^{HS}(1;\eta_{eff})$$

$$(5) \quad a_1^{VDW}=-4\cdot\eta\cdot\epsilon\cdot(\lambda^3-1)$$

$$(6) \quad g^{HS}(1;\eta_{eff})=\frac{1-\eta_{eff}/2}{(1-\eta_{eff})^3}$$

$$(7) \quad n_{eff}=c1\cdot\eta+c2\cdot\eta^2+c3\cdot\eta^3$$

$$(8) \quad \left(c\right)_1c_2c_3=\left(2\right)\cdot 25855-1.503490.249434-0.6692701.40049-0.82773910.1576-15.04275.30827\times\left(1\right)\lambda\lambda^2$$

$$(9) \quad a_2^{SW}=\frac{1}{2}\cdot\epsilon K^{HS}\eta\cdot\frac{\partial a_1^{SW}}{\partial \eta}$$

$$(10) \quad K^{HS}=\frac{(1-\eta)^4}{1+4\cdot\eta+4\cdot\eta^2}$$

$$Z=Z_{ideal}\cdot Z_{HS}\cdot Z_{disp}$$

$$Z_{ideal}=Z_{ideal}^{SAFTVR}$$

$$Z_{HS}=e^{-S_{HS}/k}$$

$$Z_{disp}=\frac{Z_{interaction}}{Z_{HS}}=\frac{\sum_i\alpha\cdot D(E_i)\cdot e^{-\beta\cdot E_i}}{\lim_{T\rightarrow\infty}\sum_i\alpha\cdot D(E_i)\cdot e^{-\beta\cdot E_i}}=\frac{\sum_iD(E_i)\cdot e^{-\beta\cdot E_i}}{\sum_iD(E_i)}$$

$$\frac{S_{HS}}{T} =$$

$$\frac{P}{\Delta S_{HS}^{success}} =$$

$$\frac{k}{\ln(P_{success})}$$

$$\frac{S_{HS}}{N! \sum_i e^{-\beta \cdot E_i} 11 = \frac{1}{N!} \int \ldots \int e^{-\beta \cdot [\{P_1^2/2m + P_2^2/2m + \ldots\} + V(\vec{R_1}, \vec{R_2}, \ldots)]} d\vec{P_1} \cdot d\vec{P_2} \ldots d\vec{P_N} \cdot d\vec{R_1} \cdot d\vec{R_2} \ldots d\vec{R_N}}$$

$$V^N/V^N$$

$$\frac{id_{\mathbb{A}^1}}{V^N}.$$

$$\int \cdots$$

$$(19) \quad \text{and } Z_{disp} = \frac{Z_{interaction}}{Z_{HS}}$$

$$\frac{T_0}{T_0} = \frac{F_{ideal}}{U_{ideal} - T_{ideal}}$$

$$(20) \quad U_{ideal} = 3/2 \cdot N \cdot k \cdot T$$

$$(21) \quad S_{ideal*} \approx k \cdot N \left(\ln \left[\frac{V}{N} \left(\frac{4 \cdot \pi \cdot m}{3 \cdot h^2} \cdot \frac{U}{N} \right)^{3/2} \right] + \frac{5}{2} \right)$$

$$(22) \quad S_{ideal} = k \cdot N \left(\ln \left[V \cdot N!^{-1/N} \left(\frac{4 \cdot \pi \cdot m}{3 \cdot h^2} \cdot \frac{U}{N} \right)^{3/2} \right] + \frac{3}{2} \right)$$

$$(23) \quad \frac{T_0}{Z_{exc}} \rightarrow Z_{HS} \cdot Z_{disp} \Rightarrow$$

$$(24) \quad F_{exc} = -k \cdot T \cdot \ln(Z_{exc}) = -k \cdot T \cdot \ln(Z_{HS}) - k \cdot T \cdot \ln(Z_{disp}) \Rightarrow$$

$$(25) \quad S_{exc.\infty} = \lim_{T \rightarrow \infty} - \left(\frac{\partial F_{exc}}{\partial T} \right)_{V,N} \text{ but } \lim_{T \rightarrow \infty} Z_{exc} = constant \Rightarrow$$

$$(26) \quad S_{exc.\infty} = -k \cdot \ln(Z_{HS.\infty}) - k \cdot \ln(Z_{disp.\infty})$$

$$(27) \quad \text{but } Z_{HS} \text{ is also constant and } Z_{disp.\infty} = \frac{Z_{interaction.\infty}}{Z_{HS}} = Z_{HS}/Z_{HS} = 1 \Rightarrow$$

$$(28) \quad S_{exc.\infty} = -k \cdot \ln(Z_{HS}) - k \cdot \ln(1) = -k \cdot \ln(Z_{HS}) \Rightarrow$$

$$(29) \quad Z_{HS} = e^{-S_{exc.\infty}/k}$$

$$(30) \quad \frac{T_0}{F} \rightarrow F = U - T \cdot S \Rightarrow S = (U - F)/T \approx -F/T = k \cdot \ln(Z)$$

$$(31) \quad \text{let } Z_{small} = \text{partition function of the smaller box}$$

$$(32) \quad \text{let } Z_{big} = \text{partition function of the bigger box}$$

$$(33) \quad \Delta S = S_{small} - S_{big} = k \cdot \ln(Z_{small}) - k \cdot \ln(Z_{big}) = k \cdot \ln(Z_{small}/Z_{big})$$

$$\frac{Z_{big}}{Z_{small}} = \frac{\Delta S}{Z_{valid}}$$

$$(34) \quad \text{let } Z_{big} = Z_{valid} + Z_{invalid}$$

$$(35) \quad \text{note } Z_{small} \text{ maps into } Z_{valid} \Rightarrow Z_{small} = \alpha \cdot z_{valid} \text{ for some constant } \alpha$$

$$\frac{\alpha}{Z_{small}}$$