

Coding Assignment 1

Due Thursday, Sept. 13, 11:30 p.m. (PT)

This assignment is related to the simulation study described in Section 2.3.1 (the so-called Scenario 2) of “Elements of Statistical Learning” (ESL).

Scenario 2: the two-dimensional data $X \in \mathbf{R}^2$ in each class is generated from a mixture of 10 different bivariate Gaussian distributions with uncorrelated components and different means, i.e.,

$$X|Y = k, Z = l \sim \mathcal{N}(\mathbf{m}_{kl}, s^2 \mathbf{I}_2),$$

where $k = 0, 1$, $l = 1 : 10$, $P(Y = k) = 1/2$, and $P(Z = l) = 1/10$. In other words, given $Y = k$, X follows a mixture distribution with density function

$$\frac{1}{10} \sum_{l=1}^{10} \left(\frac{1}{\sqrt{2\pi s^2}} \right)^2 e^{-\|\mathbf{x} - \mathbf{m}_{kl}\|^2 / (2s^2)}.$$

You can choose your own values for s and the twenty 2-dim vectors \mathbf{m}_{kl} , or you can generate them from some distribution.

I have also discussed this example in class; please check notes from this week on “kNN vs. LinearRegression” and the related Rcode.

Following the data generating process, generate a training sample of size 200 and a test sample of size 10,000.

Evaluate the performance (the averaged 0/1 error¹) for the following three procedures:

- Linear regression with cut-off value 0.5,
- k NN classification with $k = 1, 3, 5, 7, 11, 21, 31, 45, 69, 101, 151$, and
- the Bayes rule (assume you know the values of \mathbf{m}_{kl} ’s and s).

Summarize your result graphically. Design your graph so that it shows the **test** and **training** errors for linear regression and k NN, and **test** error for the Bayes classifier. Check Figure 2.4 of ESL and figures from the notes.

Write R/Python code to simulate the data, compute the errors, and produce a PDF file of your graph.

(Continue on the next page →)

¹For each sample, the incurred error is 1 if there is a mistake, and 0 otherwise.

What you need to submit?

A PDF file and the R/Python code that produces the PDF file. If we source your R file or run your Python script, we should see a PDF file generated in the same directory.

- Name your R/Python file starting with

`Assignment_1_xxxx_netID`

where “xxxx” is the last 4-dig of your University ID.

For example, the submission for Max Y. Chen with UID 672757127 and netID mychen12 would be named as

`Assignment_1_7127_mychen12_MaxChen.R`

You can add whatever characters after your netID.

- Name the PDF file similarly, starting with

`AssignmentOutput_1_xxxx_netID`

where “xxxx” is the last 4-dig of your University ID. Name your submitted PDF file the same as the file that will be generated by your code.

- Set the seed at the beginning of your code to be the last 4-dig of your University ID. So once we run your code, we can get the same PDF file.