# A Simple Utility for Literate Lean

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## 1 Introduction

The literatelean.py Python 3 program reads a literate lean file and produces three files:

- 1. out.tex: a IATEX file meant to be compiled with xelatex and the accompanying report.tex files,
- 2. out.lean: a Lean file with all the literate text stripped away,
- 3. out.bib: a bibliography file containing the citations of the literate lean file.

This very document is compiled from the literate lean file Example.lean.

# 2 Simple Literate Lean

A literate lean file must be first and foremost a legal Lean file [2] that the lean compiler and checker approve of.

The text and its accompanying citations in the LaTeX file are always inside comments.

### 2.1 Human Readable Text

The human readable part of the document must be valid LATEX, but it may not be a complete document. To the user's convenience we supplied a minimal report.tex LATEX document and Makefile that may help you in getting started

All text must appear between the comment delimeters: /-@tex and @-/, or more convienently between  $/-@text{-}@text{-}@text{-}@text{-}@text{-}&tex$ 

Multiple human readable blocks are allowed in a document. The final LATEX document will concatenate all these blocks in the same order that they appear in.

## 2.2 Bibliography

Bibliography data must be valid bibtex [3]. Like human readable text, these must appear inside comments and their delimeters are /-@bib and @-/. Only whitespace may appear around these delimeters on the line they occupy.

Just like human readable text, many bibliography blocks are allowed and the resulting bib file will be the concatenation of all the blocks.

Human-readable text and bibliography commenst may be arbitrarily nested.

#### 2.3 Lean Text

As a literate lean program is a Lean program then Lean code does not appear inside comments.

By default every line of Lean code makes it in the LATEX document inside a formated minted block. It is possible to hide parts of Lean code by wrapping them inside -- {{ and --}}. All the lean lines in between two comments will not be displayed and instead a -- ... will be displayed instead exactly where the opening delimiter is.

Lean comments are equally moved into the LATEX output. That choice was made to encourage moving all comments into a literate format. It may be interesting to look into single line comments annotating some Lean code to be added as footnotes.

The minted block will always have a git logo in its top left that, when clicked, redirects to the relevant lines in the resulting stripped out.lean file.

For example, these three lines of Lean code start by evaluating the identity function to 1, then they check the type of the result of applying the identity function to 2, and finally checks the type of the identity function.

```
#eval (\lambda \times \mapsto x) 1

-- 1

#check (\lambda \times \mapsto x) 2

-- (\text{fun } x \Rightarrow x) 2 : Nat

#check (\lambda \times \mapsto x)

-- (\text{fun } x \Rightarrow x) 2 : Nat

#check (\lambda \times \mapsto x)

-- (\text{fun } x \Rightarrow x) 2 : (\text{fun } x \Rightarrow x) 2 : (\text{fun } x \Rightarrow x) 2 : (\text{fun } x \Rightarrow x) 3 : (\text{fun } x \Rightarrow x) 3 : (\text{fun } x \Rightarrow x) 4 : (\text{fun } x \Rightarrow x) 5 : (\text{fun } x \Rightarrow x) 6 : (\text{fun } x \Rightarrow x) 7 : (\text{fun } x \Rightarrow x) 8 : (\text{fun } x \Rightarrow x) 8 : (\text{fun } x \Rightarrow x) 9 :
```

Sadly, this utility is too simple to use the Lean LSP to show the result of the #eval and #check calls.

Or even to show errors in a nicely formatted way.

But it does have a cool feature that allows you to reference definitions, theorems, inductive types, and type classes from the LATEX code. This can be done using the \lensuremath{lean} macro which the utility expands before passing it to the LATEX compiler.

For example, nat is the definition of the Peano [1] numbers.

```
-- Peano Numbers
inductive nat where
| zero
| succ (n: nat)
```

The definition of addition, in add, is the following:

And the proof that add is commutative, add\_comm, is the following. We omit the proof at the base case as it's obvious. If you wish to see it you may do so by clicking on the git icon

```
-- This is the add_comm from the standard library, not ours!
                                                                               git
#check Nat.add_comm
   Nat.add\_comm (n m : Nat) : n + m = m + n
theorem add_comm: \forall (n m : nat), add n m = add m n := by>
  intros▶ n; induction▶ n
  case▶ zero =>
  case▶ succ n ih =>
   - n : nat
  -- ih : \forall (m : nat), add n m = add m n
  -- \vdash \forall (m : nat), add n.succ m = add m n.succ
    intros▶ m; induction▶ m
    case zero => simp only [add, ih] case succ m' ih' =>
    -- ih : \forall (m : nat), add n m = add m n -- ih' : add n.succ m' = add m' n.succ
     -- - add n.succ m'.succ = add m'.succ n.succ
      unfold▶ add
      rw [ih▶, ←ih'▶]
unfold▶ add
      rw [ih▶]
```

The tool is again simple, it creates a label to definitions, theorems, inductive types, and type classes if and only if the declaration starts on a new line with the keyword def, theorem, inductive, and class keyword (respectively) being the first token of the line and the identifier to be bound is the second token.

#### 2.4 Index

An index is automatically collected of all the definitions, theorems, inductive types, and type classes. If you wish to have them rendered in the final document you must have the two commands \makeindex and \printindex.

For example, in the following code, without even referring to the Printable type class in the text through the \lean macro, the symbol still makes it to the index.

```
class Printable (a: Type) where
  print: a + String

instance : Printable nat where
  print n := toString n
    where toString (n: nat) : String :=
        match n with
        | nat.zero => "0"
        | nat.succ n => "S" ++ toString n

instance : Printable String where
  print x := x

#eval Printable.print (nat.succ (nat.succ nat.zero))
-- "SS0"
#eval Printable.print "Hello, World!"
-- "Hello, World!"
```

# References

- [1] KENNEDY, H. Peano: life and works of Giuseppe Peano, vol. 4. Springer Science & Business Media, 2012.
- [2] MOURA, L. D., AND ULLRICH, S. The lean 4 theorem prover and programming language. In *International Conference on Automated Deduction* (2021), Springer, pp. 625–635.
- [3] PATASHNIK, O. Bibtex 101. TUGboat 15 (1984), 269-273.

## Index

```
\begin{array}{lll} & & & & & & \\ & \text{Add, 3} & & & & & \\ & \text{add\_comm, 3} & & & & \\ & \text{instance: Printable} & & & \\ & \text{instance: Printable} & & & \\ \end{array}
```

# A Proof Goals

#### by

```
\vdash \forall (n m : nat), add n m = add m n
```

## intros

```
n : nat
\vdash \forall (m : nat), add n m = add m n
```

#### induction

#### $\mathbf{case}$

```
\vdash \forall (m : nat), add nat.zero m = add m nat.zero
```

### $\mathbf{case}$

```
n : nat
ih : ∀ (m : nat), add n m = add m n
⊢ ∀ (m : nat), add n.succ m = add m n.succ
```

### intros

#### induction

```
case zero
n : nat
ih : ∀ (m : nat), add n m = add m n
⊢ add n.succ nat.zero = add nat.zero n.succ

case succ
n : nat
ih : ∀ (m : nat), add n m = add m n
n† : nat
n_ih† : add n.succ n† = add n† n.succ
⊢ add n.succ n†.succ = add n†.succ n.succ
```

#### case

```
n : nat
ih : ∀ (m : nat), add n m = add m n

- add n.succ nat.zero = add nat.zero n.succ
```

#### case

```
in : nat
ih : ∀ (m : nat), add n m = add m n
m' : nat
ih' : add n.succ m' = add m' n.succ
⊢ add n.succ m'.succ = add m'.succ n.succ
```

### unfold

```
n: nat
ih: V (m: nat), add n m = add m n
m': nat
ih': add n.succ m' = add m' n.succ
\( \text{(add n m'.succ).succ} = (add m' n.succ).succ
\( \text{(add n m'.succ).succ} = (add m'.succ).succ
\( \text{
```

#### ih

```
in : nat
ih : ∀ (m : nat), add n m = add m n
m' : nat
ih' : add n.succ m' = add m' n.succ
⊢ (add m'.succ n).succ = (add m' n.succ).succ
```

### $\leftarrow$ ih'

```
n : nat
ih : ∀ (m : nat), add n m = add m n
m' : nat
ih' : add n.succ m' = add m' n.succ
⊢ (add m'.succ n).succ = (add n.succ m').succ
```

#### unfold

```
n : nat
ih : ∀ (m : nat), add n m = add m n
m' : nat
ih' : add n.succ m' = add m' n.succ
⊢ (add m' n).succ.succ = (add n m').succ.succ
```

#### ih

```
n: nat
ih: ∀ (m: nat), add n m = add m n
m': nat
ih': add n.succ m' = add m' n.succ
⊢ (add m' n).succ.succ = (add m' n).succ.succ
```