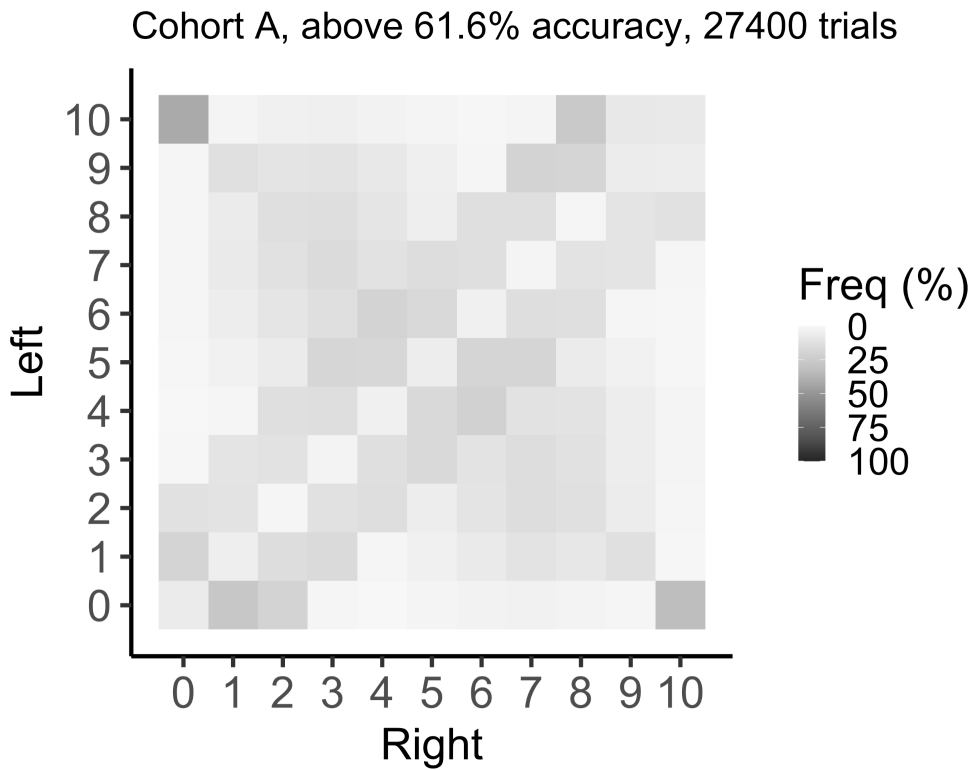


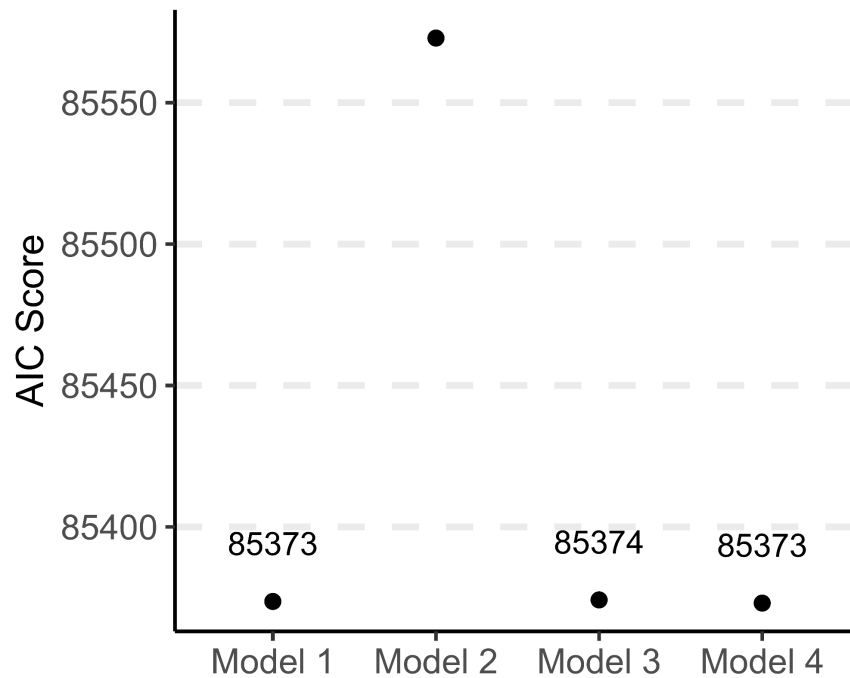
Assessing evidence accumulation and rule learning in humans with an online game
Supplementary materials

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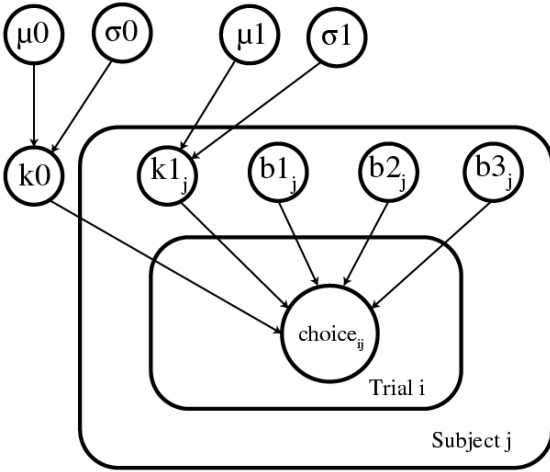
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Supplementary Figure 1. Heatmap showing the frequency of flashes pairings reflecting a Poisson sampling process as well as upsampling of difficult pairings (flash difference of 1 and 2).

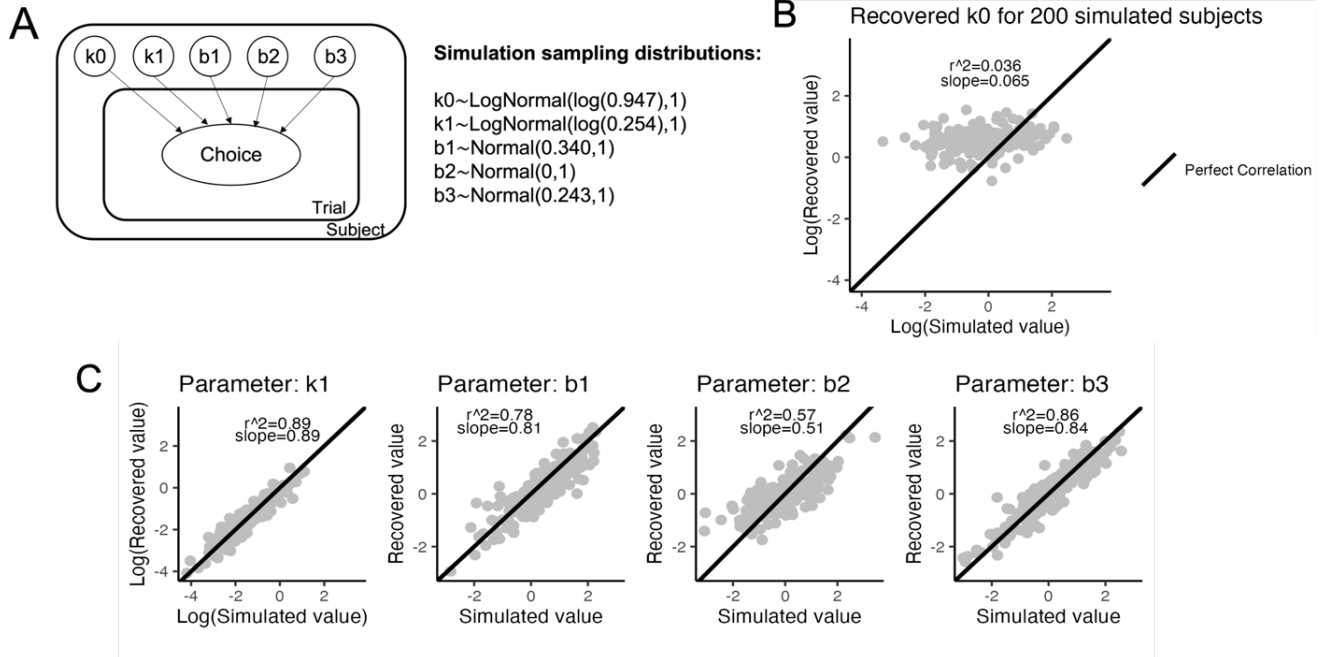


Supplementary Figure 2. Model comparisons for participants in cohort A, B and C, ignoring the first 30 trials to remove any learning dynamics. Fitted parameters returned by Model 1 ($k_1 = 1.679$, $k_0 = 0.284$), Model 2 ($k_2=1.58e-05$, $k_0 = 1.85$), Model 4 ($k_1 = 1.328$, $k_2 = 0.255$, $k_0 = 0.209$), Model 3 ($k = 0.343$, $k_0 = 1.498$, $k_i = 1.903$).

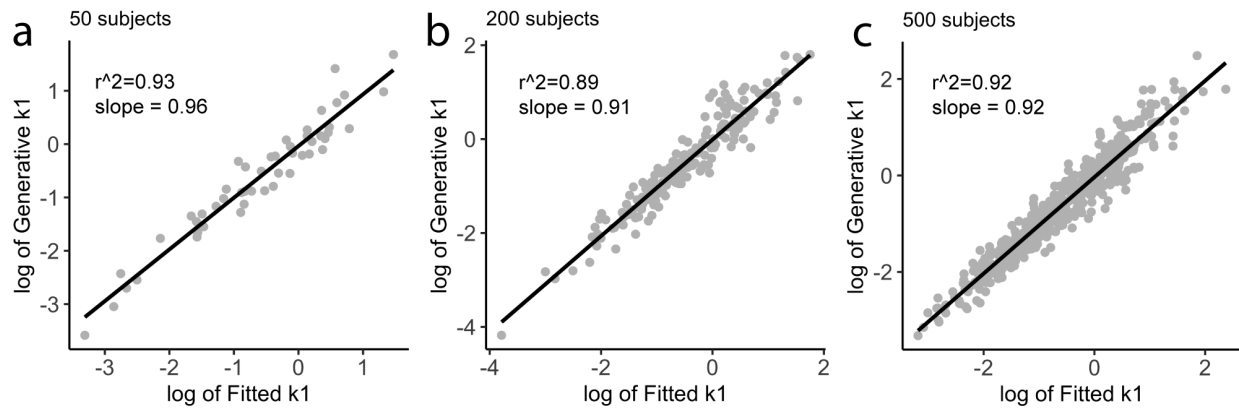
a**b**

$\mu_0 \sim \text{Normal}(-2.3, 0.1)$
 $\mu_1 \sim \text{Normal}(-2.3, 0.1)$
 $\sigma_0 \sim \text{Normal}(0.1, 0.1)$
 $\sigma_1 \sim \text{Normal}(0.1, 0.1)$
 $k_0 \sim \text{LogNormal}(\mu_0, \sigma_0)$ *Initial Noise*
 $k_{1j} \sim \text{LogNormal}(\mu_1, \sigma_1)$ *Perceptual Noise*
 $b_{1j} \sim \text{Normal}(0, 1)$ *Win-stay*
 $b_{2j} \sim \text{Normal}(0, 1)$ *Lose-switch*
 $b_{3j} \sim \text{Normal}(0, 1)$ *Side Bias*
 $\sigma_{ij} = k_0 + k_{1j}[i] \cdot (R_{ij}^2 + L_{ij}^2)$
 $\mu_{ij} = R_{ij} - L_{ij} + b_{1j}[i] \cdot \text{WS}_{ij} + b_{2j}[i] \cdot \text{LS}_{ij} + b_{3j}[i]$
 $\pi_{ij} = 1 - \text{normal_cdf}(0, \mu_{ij}, \sigma_{ij})$ *Probability Went Right*
 $\text{choice}_{ij} \sim \text{Bernoulli}(\pi_{ij})$

Supplementary Figure 3. A) Schematic of the Bayesian hierarchical model - signal detection theory model of perceptual uncertainty. **B)** Fitted parameters and prior distributions for each parameter in the model



Supplementary Figure 4. A) This model fits all parameters, including $k0$, $k1$, $b1$, $b2$ and $b3$, on subject level for 200 simulated subjects. Each parameter has its distribution listed in the graph. **B)** and **C)** Log scaled recovered $k0$ and $k1$ values on subject level versus log scaled simulated values. Recovered $b1$, $b2$ and $b3$ against simulated values.



Supplementary Figure 5. Effect of the number of participants on the accuracy of the recovered parameter using the Bayesian Hierarchical Model. **A-C)** Fitted k_1 from the Hierarchical Model versus Generative k_1 in log-scaling for 50 participants, 200 participants and 500 participants doing 200 trials each.