

Conditions need to be fulfilled for LL(1) Grammar

If the grammar is ϵ - free:

For every pair of productions $A \rightarrow \alpha \mid \beta$

$\text{FIRST}(\alpha) \cap \text{FIRST}(\beta) = \varnothing$ (i.e., $\text{FIRST}(\alpha)$ and $\text{FIRST}(\beta)$ should be disjoint sets for every pair of productions $A \rightarrow \alpha \mid \beta$)

When the grammar is not ϵ -free:

For every pair of productions $A \rightarrow \alpha \mid \beta$, the following 2 conditions must hold

- (i) $\text{FIRST}(\alpha) \cap \text{FIRST}(\beta) = \varnothing$, and
- (ii) if $\text{FIRST}(\beta)$ contains ϵ , and $\text{FIRST}(\alpha)$ does not contain ϵ , then $\text{FIRST}(\alpha) \cap \text{FOLLOW}(A) = \varnothing$

Example:

Consider the following grammar, and test whether the grammar is LL(1) or not.

$$S \rightarrow 1AB / \epsilon, \quad A \rightarrow 1AC / 0C, \quad B \rightarrow 0S, \quad C \rightarrow 1$$

Since the given grammar is not ϵ free.

For a pair of productions $S \rightarrow 1AB \mid \epsilon$:

$$\text{FIRST}(1AB) \cap \text{FIRST}(\epsilon) = \{1\} \cap \{\epsilon\} = \varnothing \text{ and}$$

$$\text{FIRST}(1AB) \cap \text{FOLLOW}(S) = \{1\} \cap \{\$ \} = \varnothing$$

Similarly, for a pair of productions $A \rightarrow 1AC \mid 0C$:

$$\text{FIRST}(1AC) \cap \text{FIRST}(0C) = \{1\} \cap \{0\} = \varnothing$$

Hence the grammar is LL(1).