

Experimental investigation of solitary breaking waves in the swash zone

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Abstract

This study presents an experimental investigation of plunging breakers on a sloping beach with an inclination of 5.1° . The incident waves are solitary waves with various amplitudes from non-breaking waves to plunging breakers, and the area investigated is the swash zone. PIV (Particle Image Velocimetry) is performed on images captured at four different field of views (FOV). The PIV measurements are compared with computed velocity fields from a Boundary Integral Model (BIM). There is excellent agreement between the experimental and the computed result for the non-breaking waves. The experimental results from the breaking waves indicate that the motion becomes more irregular as we move further up the beach. In addition, there are more irregularities present for waves with larger amplitude. Shoreline position and maximum runup are measured, and are repeatable in both time and height, although cross-sectional variations of the shoreline shape are observed at maximum runup. Length and velocity of air bubbles entrapped by the plunger breakers are extracted from an image series captured with large a FOV. The images showed that a large air bubble remains intact for a time period during runup for the breaking waves.

Keywords: Breaking solitary waves, PIV, Boundary layers, Runup, Bubble entrainment.

1. Introduction

In shallow water with constant depth, the nonlinear effect and dispersion will be balanced for solitary waves (Peregrine, 1983). If the depth decreases as the wave travels towards the shore, the wave will steepen, and at some critical point breaking may occur. Breaking waves are one of the most important physical features in the swash zone (Elfrink and Baldock, 2002). Breaking waves have a large impact on sediment transport onshore, which can result in erosion on cliffs and affect construction located near the shore. Although breaking waves is a well-known phenomenon from our daily life, many physical aspects regarding wave breaking are still poorly understood.

Several experimental studies of breaking waves have been performed in the recent years. A broad range of different experimental methods have been utilized to measure quantities such as surface elevation, runup, shear stress, and velocities. Techniques such as Laser Doppler Velocimetry (Petti and Longo, 2001), PIV (Cowen et al., 2003) and shear sensors (Barnes et al., 2009) has been utilized. The swash zone is defined as the region where the beach is partly wetted during runup and rundown. Aeration and the small flow depth makes the swash zone a challenging region to study experimentally with the techniques mentioned

above. A further development of the PIV method is Bubble image Velocimetry (BIV), which Rivillas-Ospina et al. (2012) use to investigate velocity fields in plunging breakers. They compared the measurements with numerical simulations conducted with Reynolds Average Navier Stokes Equations Model. The model gave fairly good agreement with the measurements in the surf zone, but the model overpredicts the velocities in the swash zone compared to the BIV measurements. One of the latest work on solitary waves on a plane beach has been conducted by Pujara et al. (2015). They investigated the flow evolution of the runup and run down of solitary waves in the range from non breaking to plunging breakers. A shear plate was located at different positions along the beach and measurements revealed that the maximum positive bed shear stress was obtained in the tip of the swash tongue during runup, and is due to the developing of a boundary layer, and due to bore driven turbulence. The maximum negative bed shear stress was obtained at the end of the withdrawal. The flow is accelerated during downrush by gravity and the bed shear stress increases during rundown until a maximum is reached right before the water runs out of the measuring area.

Until now, PIV measurements with high resolution close to the beach have not been reported for plunging breakers waves in the swash zone. This paper presents PIV measurements where the amplitude of the solitary breaking waves varies. The paper starts with a description of both the experimental set-up and the computational Boundary Integral Model used in this study (chapter 2). Further on, results from different parts of the experiment will be presented, herein the surface elevation of the incident waves in chapter 3.1, surface development and maximum runup in chapter 3.2, velocity profiles from the swash zone in chapter 3.3, and air bubble investigation in chapter 3.4. Finally, a discussion of the findings will be presented in chapter 4.

2. Experimental set-up and formulation

2.1. The wave tank

Laboratory experiments of non-breaking to plunging breaking waves in the swash zone were conducted in a 25m long and 0.51m wide wave tank located at the Hydrodynamics Laboratory at the University of Oslo. Incident waves were generated in an equilibrium depth of 20.5cm by a piston type wave paddle using the method described in Jensen et al. (2003). A PETG (Polyethylene Terephthalate Glycol-modified) beach with an inclination of 5.1° was placed in the wave tank with its toe 529.81cm from the start position of the wave paddle. Two coordinate systems were introduced, one parallel to the still water level (x', z'), and one parallel to the beach (x, z) (See Figure 1). The origin of both is at the equilibrium shoreline.

Nominally, the amplitude to depth ratios should equal ($\alpha = 0.1, 0.12, 0.2, 0.3, 0.4, 0.5$). However, imperfection in the generation and frictional effects along the wave tank reduced the heights slightly such that $\alpha \approx A/H$. An acoustic wave gauge (ultra Banner U-Gage S18U, sample frequency of 200Hz) measured the wave height at the toe of the beach and the amplitudes were found to be $A/H = (0.0986, 0.1184, 0.1977, 0.2959, 0.3930, 0.4863)$.

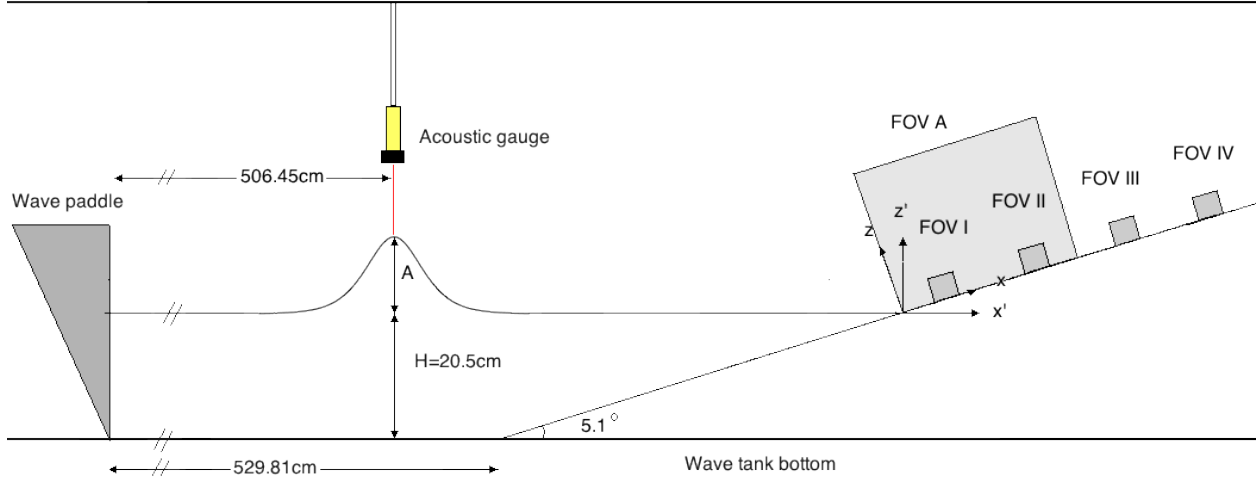


Figure 1: Sketch of the experimental set-up.

FOV:	I	II	III	IV
Location, x :	[8.49 - 13.04]	[36.35 - 40.26]	[77.55 - 81.53]	[117.76 - 121.80]
Location, z :	[-0.05 - 3.78]	[-0.16 - 3.54]	[-0.04 - 3.79]	[-0.85 - 3.09]

Table 1: Location of the different FOVs in cm. The dimensions of the FOVs are approximately 4cm x 4cm.

2.2. Instrumentation, measurements

To obtain velocity fields in the swash zone, images were captured at four different field of views (FOV), located upward along the beach (Table 1). The different FOV's are denoted with roman numbers. The water in the tank was seeded with polymid particles with diameters of approximately $50 \mu\text{m}$. A Quantronix Darwin Duo pulsed laser generated a light sheet parallel to the centreline of the wave tank, and a Photron SA5 high speed camera (1024 x 1024) synchronized with the laser, captured images of the illuminated particles. A Carl Zeiss Makro- Planer 2/50 zf lens was used. Images were collected at 3000 frames per seconds (fps). The image processing were performed in DigiFlow (Dalziel, 2006). PIV was performed using interrogation windows of 32×8 pixels with a 75% overlap. Oblong interrogation windows are beneficial in boundary layer flow and have been employed previously in Liu et al. (2007) and Pedersen et al. (2013). An averaging of 10 images was applied to reduce noise from the data. The number of images used in the average was carefully selected, such that the mean results were not affected by the averaging.

To investigate air bubbles encapsulated by the plunging breakers, the camera was moved further away from the wave tank, resulting in much larger FOV than the FOVs installed to obtain velocity fields. This FOV will be referred to as FOV A and is located at $x = [0 - 60]\text{cm}$. 500 fps were used in this investigation, and a continuous dedolight 400D was used as illumination, replacing the laser. A white background sheet was attached to the side wall of the wave tank and the water was dyed dark blue to increase the contrast in the images.

The maximum runup was measured by capturing images of the shoreline at its maximum position. A high speed Photron APX camera was mounted on rails above the beach in the wave tank with same inclination as the beach. A high pulsed white light was used as illumination. The field of views were based on estimates of the runup height for each case. The camera captured 125 frames per second. The maximum shoreline profiles were tracked manually for each wave. The experiments were repeated at least three times. The scatter δ_i for some measured quantity, x_i , is then calculated in the following manner,

$$\delta_i = \frac{x_i - \bar{x}}{\bar{x}} \quad (1)$$

where \bar{x} is the mean over the repetitions.

To find a measure of the irregularities present in the PIV measurements, the standard deviations are calculated at the different FOV for the strongest plunging breaker. Deviations are extracted at times where the mean flow in an area near the beach ($z=[0 - 0.6]\text{cm}$) has a specified velocity ($[40, 0, -40]\text{cm/s}$).

$$\sigma = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})^2} \quad (2)$$

The average deviations in the z-direction are calculated from the same area ($z=[0 - 0.6]\text{cm}$), and M corresponds to number of vertically grid-points within this area.

$$\bar{\sigma} = \frac{1}{M} \sum_{j=1}^M (\sigma_j) \quad (3)$$

2.3. The potential flow and boundary layer models

The evolution of the waves during shoaling, as well as the runup for the smallest amplitude, were computed by a BIM (Boundary Integral Model) for fully nonlinear, inviscid flow. This model breaks down when a plunger re-attaches with fluid or impacts the beach. Moreover, the model becomes singular when the contact angle at the shoreline exceeds 90° and the results also become unreliable for contact angles slightly smaller.

The potential flow model also provides the outer flow and the pressure gradient which are used as input to a FDM viscous boundary layer model. However, the coupling between the models is only one way as there is no feed-back from the boundary layer to the potential flow model. More details on both models are given in Pedersen et al. (2013).

Simulations are conducted with a range of various spatial resolutions. Grid refinements are engaged up to the point where the runup height and time was deterministic with a 0.2% error. The same resolutions was applied to the breaking waves, and the finest resolution $\delta x'$ was approximately $0.07H$. For all the waves the temporal increment was set to 0.0073s, which is twice as large as the temporal averaging used in PIV. The viscous boundary layer model generated 600 grid points along the beach, with a spatial increment of $0.0042H$. The time resolution was kept the same as for BIM.

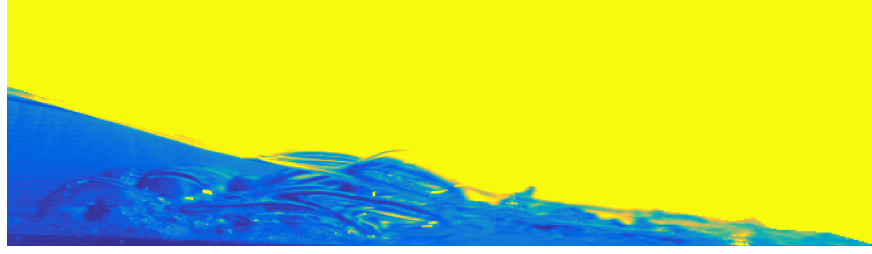


Figure 2: Image of the swash tongue for $\alpha = 0.50$.

3. Results

Visual inspection of the experiments revealed that the cases with normalized amplitude $\alpha = 0.10$ and $\alpha = 0.12$ did not break until the draw-down, while all the other cases developed into plunging breakers at or before the equilibrium shoreline. The plunger breakers encapsulated large amounts of air, which resulted in air bubbles in the swash tongue of the breaking waves (Figure 2).

3.1. Surface elevation of the incident waves

The amplitude of the smallest amplitude wave is determined by a simple correction scheme. First the maximum of the series from the acoustic gauge A_m is used as solitary wave amplitude in the BIM model. For the lowest wave this value is $A_m/H = 0.0998$. When BIM data are extracted at the gauge position we obtain a slightly too large surface elevation $A_b = 0.1008$, due to the reflection from the beach. We then adjust the amplitude according to $A = A_m(1 - \frac{(A_b - A_m)}{A_m})$. The result is $A/H = 0.09865$ and the comparison with BIM results, obtained with this amplitude for the incident wave, is shown in Figure 3. When the surface elevation of the incident waves are very steep, the ultra sonic signal will not get reflected back and registered by the sensor. This leads to dropouts in the measurements, which have been filled in by linear interpolation. Cubic polynomial regression is used to remove noise from the signal. The surface elevation measurements are in agreement with computed surface elevation from the BIM simulations. The corrected and measured amplitudes for all the other waves are given in Table 2.

3.2. Surface development and maximum runup

To investigate shoaling and runup of the waves both simulation and measurements have been conducted. BIM simulations of the near-shore evolution model is shown in Figure 4. For reasons explained previously we only compute the runup for the smallest wave $\alpha = 0.10$. The computed time, inundation length and height for maximum runup were $t = 8.93s$, $r = 112.78cm$ (measured along the beach), and $R/A = 4.95$ respectively. The BIM model had some difficulties with the waves with amplitude $\alpha = 0.12$. For the other cases shown the numerical model describes the evolution of the plunger, but nothing beyonds its impact onshore.

The measured maximum runup heights and deviations for each waves are available in Table 2. Compared to the teoretical values above, for $\alpha = 0.10$, the maximum runup height is reduced by 22% and the maximum occurs 0.07s later. The BIM model does not account for viscous effect or surface tension, and this is the likely

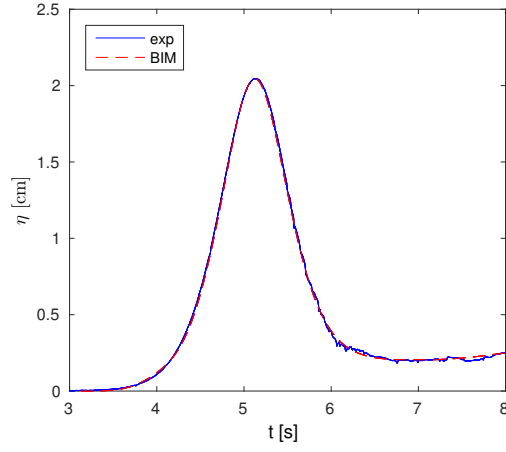


Figure 3: Measured and computed surface elevation for $\alpha = 0.10$.

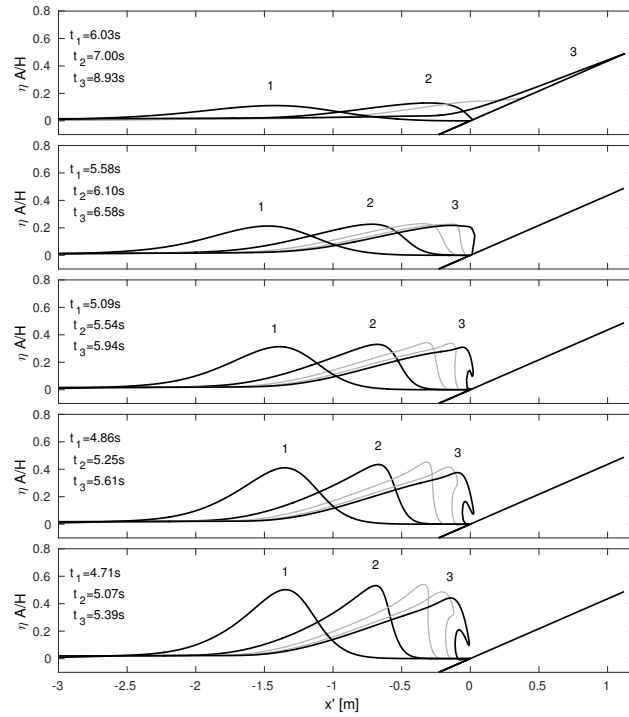


Figure 4: BIM simulation of the waves the upper to lower figures correspond to $\alpha = (0.10, 0.20, 0.30, 0.40, 0.50)$, respectively. In the top panel the curve marked 3 corresponds to the time of maximum runup.

α	A/H	A_m/H	$r[cm]$	R/A	$e_r[\%]$	t	$e_t[\%]$
0.10	0.09865	0.0998	87.25	3.82	1.68	8.86 s	0.15
0.12	0.1184	0.1194	105.67	3.85	0.27	8.67 s	0.15
0.20	0.1977	0.1984	147.37	3.22	0.93	8.53 s	0.31
0.30	0.2959	0.2967	191.67	2.80	1.08	8.03 s	0.78
0.40	0.3930	0.3936	227.42	2.50	0.11	7.82 s	0
0.50	0.4863	0.4869	267.46	2.37	2.27	7.30 s	1.64

Table 2: *Maximum runup measurements, where A incident wave amplitude, A_m is the measured amplitude at the toe of the beach, r is the inundation length, R is the vertical maximum runup, t is the time corresponding to max runup and e is the estimated error in the measurement*

reason for the differences. Pedersen et al. (2013) reported differences that were similar, but were smaller in magnitude due to a steeper slope angle of 10.54° which leads to thicker flow depths and shorter inundation. In fact, in Figure 5 we observe transverse variations in the experiments and the average run up height is more than 5% smaller than the maximum one. Table 2 shows that the maximum runup is repeatable for all waves including the breaking ones.

The shoreline at maximum runup are shown in Figure 5. It is fairly repeatable for the amplitude close to 0.1 times the depth (Figure 5a), but has a wedge-like shape. This is presumably due to a cross-wise deformation of the beach which has been measured using a straightedge and a feeling gauge. The typical maximum suppression in each transect of the beach was 3mm. If we assume that the depressions were unsystematic and that the later stages of runup are governed by gravity alone (see, for instance, Jensen et al. (2003)) this should correspond to a variation of 3cm on a 1 in 10 slope beach. However, even though the flow depth is small during runup, the momentum transport due to the pressure is still noticeable (inferred from the simulations, results not shown). More importantly, there is a systematic suppression at the center-line of the beach and the beach width is 51cm, which is comparable to the inundation length for the smallest amplitude. Hence, another relevant estimate of the runup variation is the suppression times the contact angle (angle of fluid wedge during runup) in radians. In the simulations this angle approaches 0.5° at maximum runup, which yields a variation in x of 30cm. This is modified by the the capillary affects that affects the contact angle and shape of fluid body near the shoreline. Unfortunately, we cannot quantify this effect from the experiments. From Figure 5 it is clear that transverse variation is more in line with the latter estimate than the first one. The runup varies much more for the three repetitions of the breaking wave $\alpha = 0.50$, resulting in irregularly shaped shorelines (Figure 5b).

An estimate of the arrival time of the wave for FOV II, III and IV, were measured based on the intensity changes in images captured at each FOV. Each image in each time series was compared to the initial image taken before the wave paddle starts. The image where the sum of light intensity differs more than a given threshold (1000) from the initial image, correspond to the time when the wave enters that FOV. The

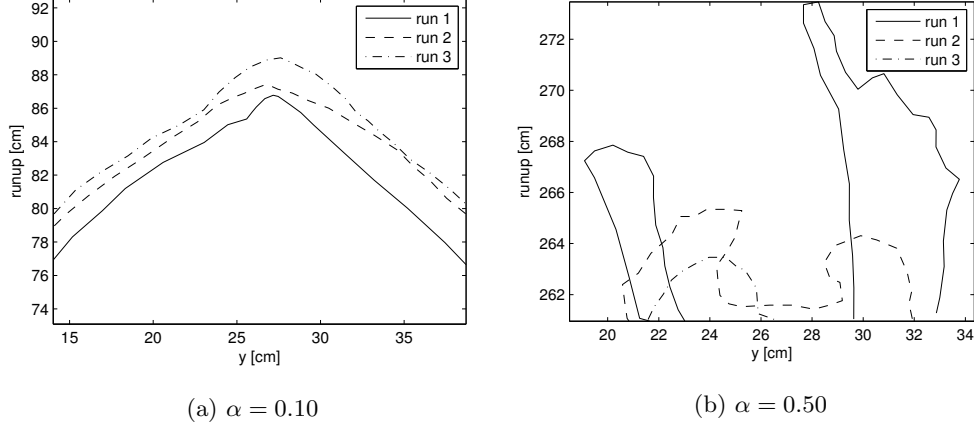


Figure 5: *Shoreline shapes at max runup.*

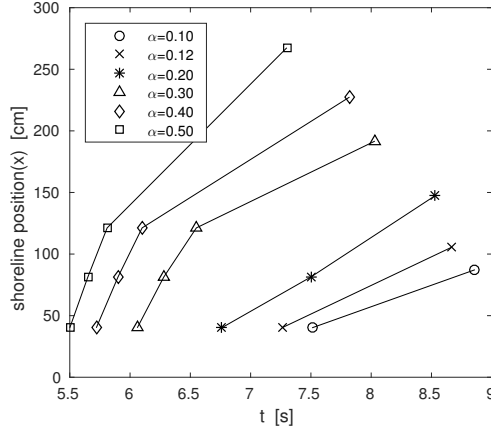


Figure 6: *Shoreline position as a function of time for all cases. The first measurements correspond to the swash tongue arrival time for FOV II, III, IV. The last measuring point for all cases correspond to measurement of maximum runup*

measured shoreline positions as a function time are presented in Figure 6. The maximum error obtained for three different runs was 0.18%. This indicate that the shoreline motion was repeatable for each of the FOV.

3.3. Velocity profiles from the swash zone

Velocity profiles are extracted from the PIV data that are obtained from the four different FOV, approximately from 10cm to 120cm from the equilibrium shoreline. First, a comparison between computed BIM and measured PIV velocities for $\alpha = 0.10$ will be given for FOV I and II, (See Figure 7). There is good agreement between the measured and the computed velocity profiles. The computed velocities are higher in the front of the wave for both FOVs. The maximum deviation between measured and computed outer flow was at the begining of PIV timeseries, and was 4.7% for FOV I and 6.8% for FOV II (not shown). Deviation decreased for both FOVs as time increased. This complies with corresponding results in Pedersen et al. (2013) where the delay of the experimental wave was linked to capillary effects, while an accumulative

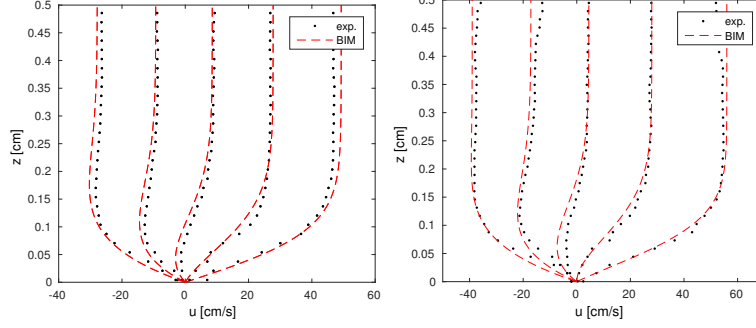


Figure 7: Velocity profiles for $\alpha = 0.10$

Left: FOV I $x=8.7\text{cm}$ $t=[7.48, 7.82, 8.15, 8.48, 8.81]\text{s}$

Right: FOV II $x=40.1\text{cm}$ $t=[7.76, 8.10, 8.76, 9.10]\text{s}$

$\bar{\sigma} \left[\frac{\text{cm}}{\text{s}} \right]$	$40 \frac{\text{cm}}{\text{s}}$	$0 \frac{\text{cm}}{\text{s}}$	$-40 \frac{\text{cm}}{\text{s}}$
FOV I	0.52	0.24	0.51
FOV II	1.03	0.56	1.06
FOV III	2.10	1.03	0.75
FOV IV	3.48	1.70	0.79

Table 3: Irregularity for $\alpha = 0.50$, the mean deviation from $z=0-0.6$ for the three repetitions

reduction of velocity, and hence runup height, was related to the viscous boundary layers at the beach. Hence, the BIM computation over-predicts the maximum runup as given in the previous section.

The PIV analysis of the breaking waves was difficult due to air bubbles in the flow, and challenges with particle seeding within the thin swash zone. $\alpha = 0.50$ has the longest runup of all the breaking waves, and that makes it the wave where most data can be extracted from all the FOVs. Velocity profiles for $\alpha = 0.50$ are shown in Figure 8. The velocity profiles are extracted at times after all the air bubbles have passed each of the FOV. It is clear that the velocities at FOV I resembles the velocities obtained for $\alpha = 0.10$. The boundary layer is well defined and the deviation between the different runs is really small. For FOV II-IV the deviations tends to increase as we move further up the beach, however the largest irregularities are typically at the beginning of runup and decreases as the flow decelerates. The withdrawal has a well defined boundary layer and outer flow for all the FOVs. The deviation between different runs are indeed reduced. A measure of the irregularities (or the average deviations of the different runs) are presented in Table 3. The findings substantiate the interpretation made of the data shown in Figure 8.

The velocities near flow reversal for all the different wave amplitudes will be discussed in the following. FOV II is located approximately 40cm from the origin, and velocity profiles obtained from this FOV are shown in Figure 9. For $\alpha = 0.20$ the particle density was too sparse close to the surface, which led to spurious vacillations in the velocity profiles near $z \approx 1$. Some distance below the surface a region of uniform flow is apparent for all cases. Boundary layers are apparent for all the cases and they all display a flow reversal

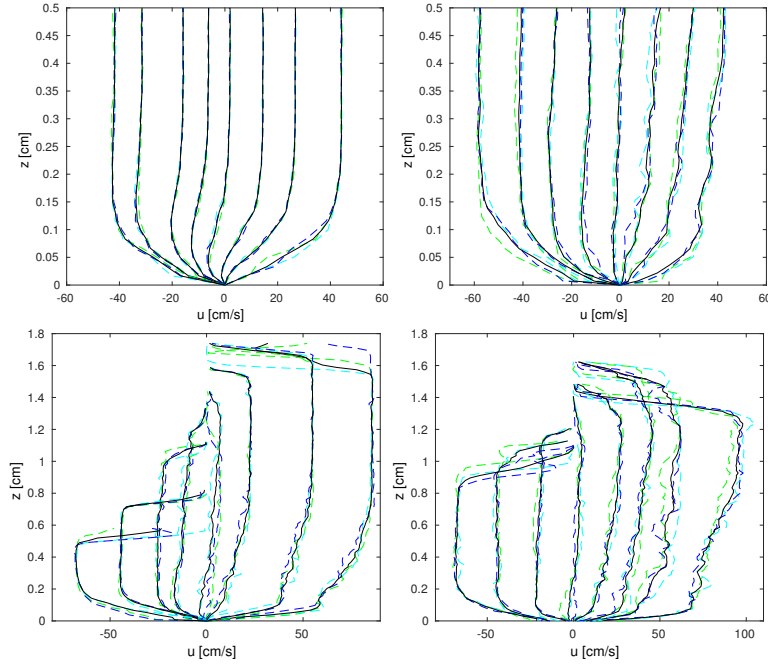


Figure 8: Velocity profiles for $\alpha = 0.50$ Colors: blue, cyan and green correspond to run 1,2 and 3.

Upper Left: FOV I $x=8.7\text{cm}$ $t=[6.12, 6.34, 6.50, 6.69, 6.84, 7.00, 7.27, 7.45]\text{s}$

Upper Right: FOV II $x=40.1\text{cm}$ $t=[6.43, 6.57, 6.74, 6.92, 7.14, 7.36, 7.56, 7.80]\text{s}$

Lower Left: FOV III $x=81.4\text{cm}$ $t=[6.34, 6.60, 6.94, 7.12, 7.34, 7.50, 7.80, 8.16]\text{s}$

Lower Right: FOV IV $x=121.2\text{cm}$ $t=[6.50, 6.78, 6.94, 7.10, 7.32, 7.60, 7.91, 8.20]\text{s}$

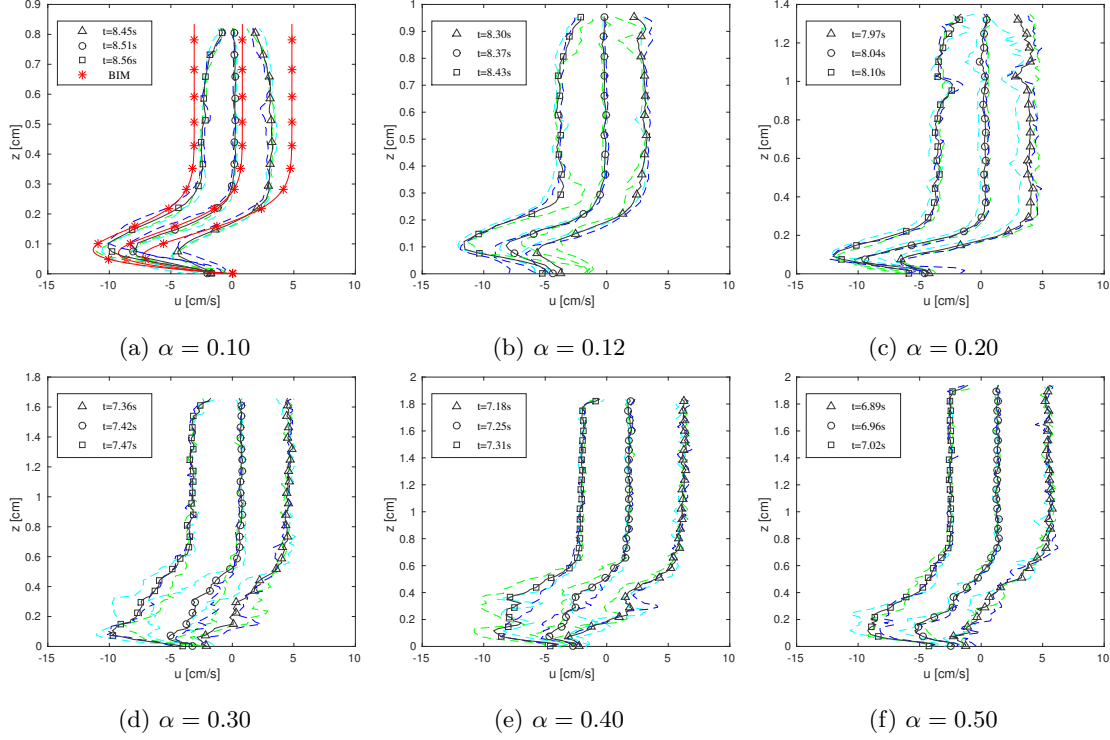


Figure 9: *FOV II*, mean velocity profiles before and after the outer flow reverses ($\triangle, \circ, \square$). Colors: blue, cyan, green and red correspond to run 1, 2, 3 and BIM respectively. $x = 40.1\text{cm}$.

prior to that of the outer flow. However, the evolution of the boundary layers for the amplitudes up to just below $\alpha = 0.2$ and those close to $\alpha = 0.3$ and higher differ. The boundary layers for the higher amplitudes appear more irregular with a thicker and less pronounced region of reversed flow in the boundary layers. While the boundary layer for the lower amplitudes, including that of $\alpha = 0.20$, appears laminar the higher waves have boundary layers that presumably are in a transition to turbulence.

FOV III is located about 80cm from origo along the beach. For $\alpha = 0.10$ and $\alpha = 0.12$, the swash tongues were too thin, and particles within the tongue were impossible to detect. Consequently, only $\alpha = 0.20 - 0.50$ will be presented for this FOV. None of the cases had an outer flow with constant velocity at times close to outer flow reversal (Figure 10). This indicates that the motion was more irregular for this FOV than for FOV II.

FOV IV is located about 120cm from where the still water reaches the beach. At this FOV, only $\alpha = 0.30 - 0.50$ will be presented due to the thin swash tongue for the other waves. Velocity profiles are given in Figure 11. The velocity was less repeatable at this location than for the other FOVs. The velocity profiles were more irregular, especially for $\alpha = 0.50$, where the average velocity profile obtained before flow reversal resembles the parabolic velocity profiles from fully developed turbulent channel flow, as described in White and Corfield (2006).

Inspection of movies of the front of the swash tongue from FOV IV (furthest up the beach) shows that

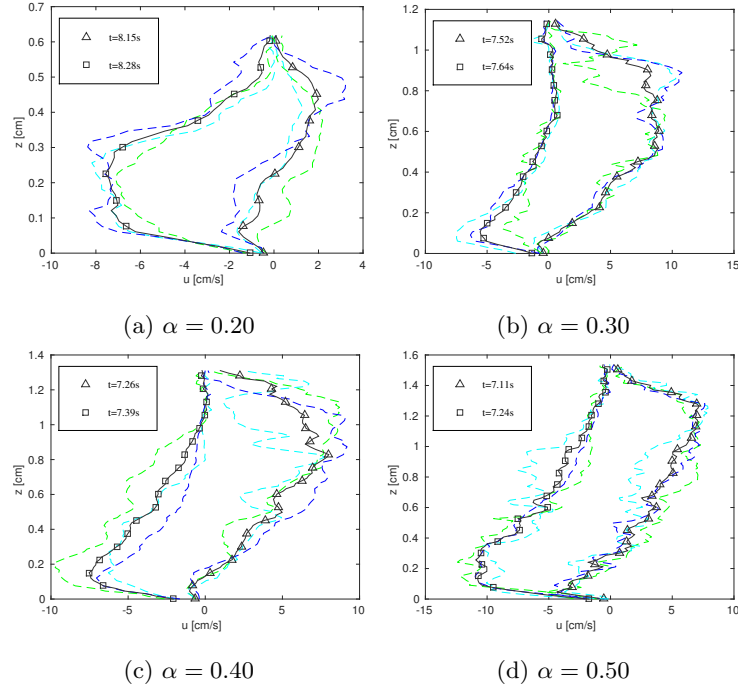


Figure 10: *FOV III*, mean velocity profiles before and after the outer flow reverses (Δ, \square). Colors: blue, cyan and green correspond to run 1, 2 and 3. $x = 81.4cm$

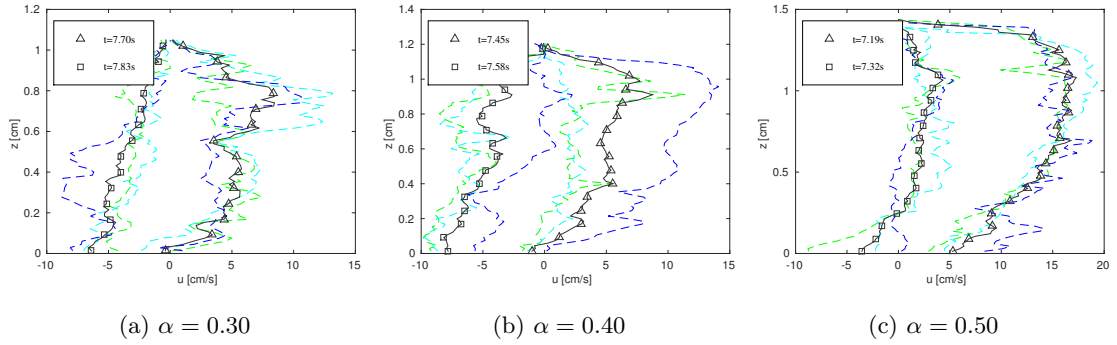


Figure 11: *FOV IV*, mean velocity profiles before and after the outer flow reverses (Δ, \square). Colors: blue, cyan and green correspond to run 1, 2 and 3. $x = 121.2cm$

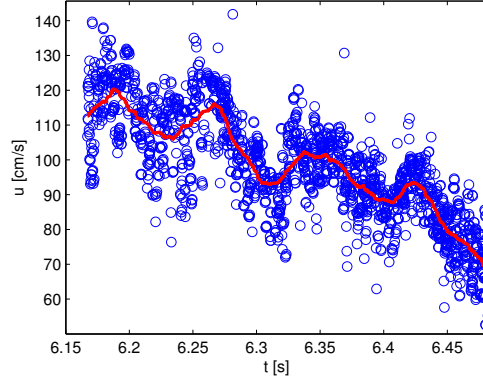


Figure 12: *FOV IV Collection of velocities of particles within a distance of 0.05cm from the point(x,z)=(120,0.3)cm. The data is collected from $\alpha = 0.50$, run 2. Blue circles: Raw data points. Red line: 2 order interpolation with 40 evaluation points*

a systematic swirling effect were present in the front of the swash tongue for $\alpha = 0.50$. To investigate this phenomenon, Particle Tracking Velocimetry (PTV) has been utilized on images captured close to arrival of the swash tongue (5.33s). In the front of the swash tongue, sparse seeding of particles prevented us from obtaining velocities right after flow arrival. So the first time where enough particles were within the tongue for this PTV analysis was at $t=6.16s$, but this is still long before the large bubble arrives at this FOV. For each image pair after this, the velocity for all the particles within a distance of 0.05cm from a given evaluation point $(x,y)=(120,0.3)cm$ are assessed. Figure 12 shows how the velocities vary as a function of time. Superimposed a steady deceleration of the fluid there is an oscillation. Flow in decelerating boundary layers are prone to instabilities. However, the oscillations do not increase in magnitude and are present from the beginning. This indicates that the wave breaking induces irregularities, possibly in the form of vortices, that prevails during the subsequent motion.

3.4. Bubble investigation

For the plunging breakers ($\alpha = 0.20-0.50$) one large air bubble is encapsulated. As the waves propagated upward the beach, this bubble disintegrated into smaller and smaller bubbles. Before maximum runup, all the bubbles have escaped the surface. The images captured with the large FOV A provides some information about this air bubble formation, (see Figure 13 and 14). To enhance the shape of the bubbles the gradient magnitude image is represented. The shape of the main bubble is oval with a thin tongue in the front, for $\alpha = 0.30$. The shape of the main air bubble appears less repeatable for $\alpha = 0.50$. In particular, in run 2 the large air bubble cannot be identified in the image at all. The length of the main bubble for three different runs is given in Table 4. It is clear from the images and Table 4, that the three different runs are more similar for $\alpha = 0.30$ than for $\alpha = 0.50$. This supports the assertion that larger plungers are more irregular. The air bubbles will eventually rise to the surface, and consequently the air bubbles must have a vertically velocity component at some point. This may introduce irregularities in the flow regime, since velocities in the fluid must equal the velocity of the bubbles close to the bubble surface.

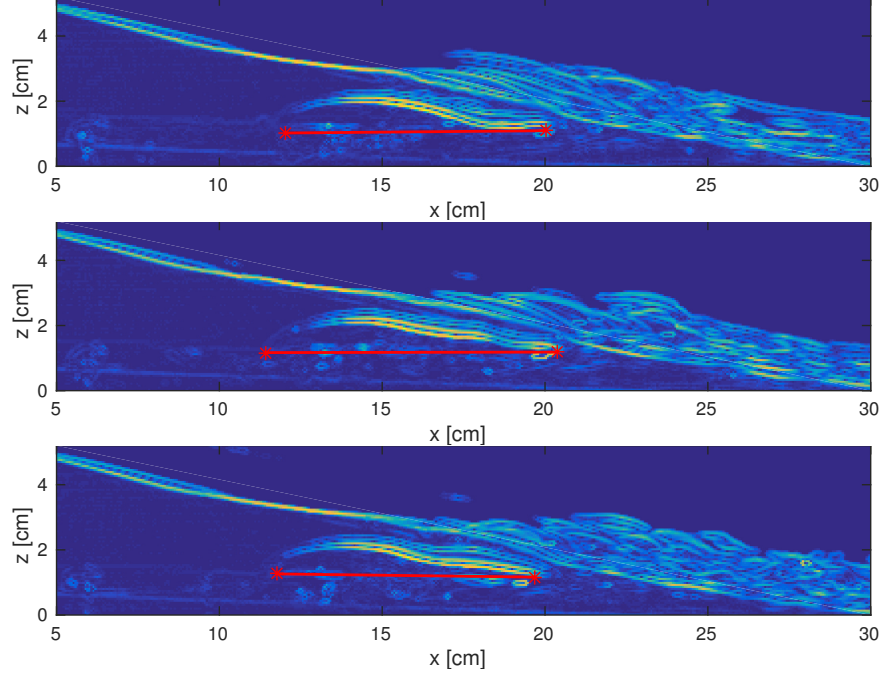


Figure 13: $\alpha = 0.30$, run 1,2 and 3. $t=6.06s$

Main bubble size	Run 1 [cm]	Run 2 [cm]	Run 3 [cm]
$\alpha = 0.30$:	8.00	8.94	7.90
$\alpha = 0.50$:	9.24		8.17

Table 4: Size of the main bubble measured at $t=6.06s$ for $\alpha = 0.30$, and $t=5.54s$ for $\alpha = 0.50$

217 The air bubble velocity in the direction along the beach is given in Table 5. The largest velocities were
 218 obtained in the front of the bubbles for most of the runs, and may explain the shape of the thin tongue in
 219 the front of the air bubble observed for $\alpha = 0.30$. The bubbles velocities are comparable to the velocities of
 220 the developing shoreline (See Figure 6). The average shoreline velocity from FOV II to FOV III was found to
 221 be $1.87m/s$ for $\alpha = 30$ and $2.75m/s$ for $\alpha = 50$, and the average is taken within a time interval close to the
 222 times of bubble investigation. The average shoreline motion was smaller than the average bubble velocity for
 223 $\alpha = 30$, which interpret that the bubbles will not be lagged relative to the swash tongue for this wave, and
 224 the bubbles may not affect the later stages of the runup as much as we first presumed. However for $\alpha = 0.50$
 225 the average bubble velocity is smaller than the shoreline velocity which makes the bubble lagged relative to
 226 the swash tongue, and the area of the swash tongue where air bubbles are present may be extended. This
 227 may be one of the reasons for the large irregularities measured with the PIV system in the beginning of the
 228 swash tongue (see Figure 8).

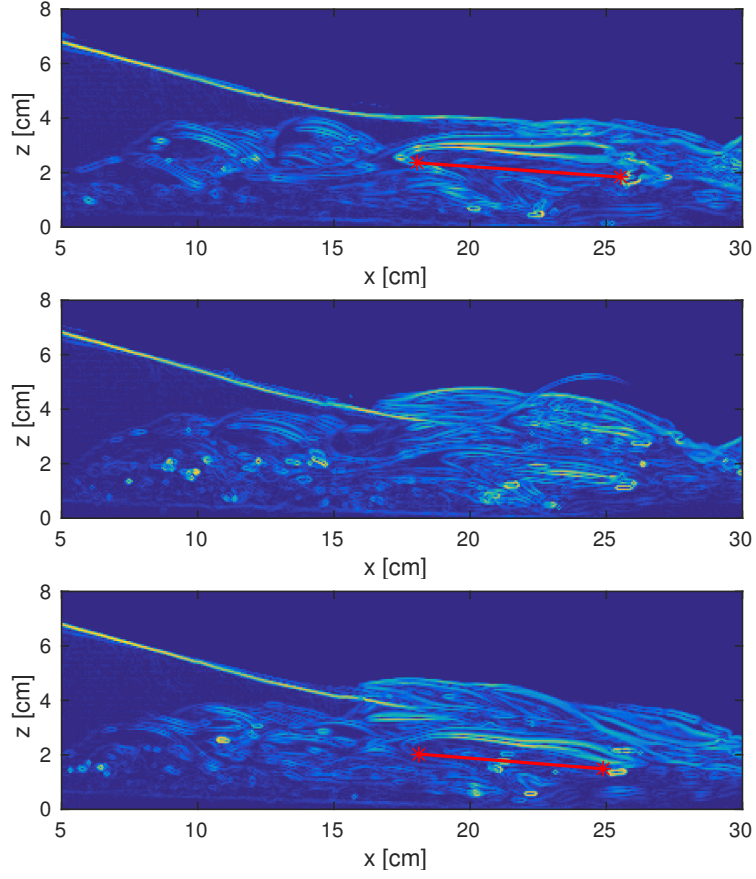


Figure 14: $\alpha = 0.50$, run 1,2 and 3. $t=5.54s$

$\alpha = 0.30$	Run 1	Run 2	Run 3
Front velocity [m/s]	2.05	2.20	2.48
Tail velocity [m/s]	2.10	2.05	2.23
$\alpha = 0.50$			
Front velocity [m/s]	3.26		2.01
Tail velocity [m/s]	1.58		2.23

Table 5: Velocities along the beach for the main air bubble. $t=6.06s$ for $\alpha = 0.30$, and $t=5.54s$ for $\alpha = 0.50$

4. Discussion

For runup of non-breaking solitary waves on a 5.1° slope we observe laminar boundary layers. The presumption of laminarity is supported by the good agreement found with boundary layers computed by combining a potential flow model with a standard boundary layer model on the beach. However, in accordance with Pedersen et al. (2013) the potential flow model, without any feed back from the boundary layer model, overpredicts the maximum runup height by 30%. The discrepancies between computations and measurements, which is mainly due to viscosity and capillary effects, are in reality larger since tiny deformation of the beach increases the maximum runup height in the experiments..

The measurement of the breaking waves showed that the fluid motion becomes more irregular and less repeatable as we move further up the beach. In addition, the motion was more irregular for the waves with the stronger plunger breakers than for those with smaller amplitude. The maximum runup was fairly repeatable, but marked an irregular transverse variations were observed for the breaking waves. The bubble investigation indicated that the air bubble shapes were repeatable for the waves with amplitude $\alpha = 0.30$ but not for waves with amplitude $\alpha = 0.50$. Overall, irregular motion increases with larger breaking waves and as the waves propagate upwards the beach.

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