

①

a) $x = \text{collegiat}$
 $y = \text{mini}$

b) Max Profit

$$\max Z = 32x + 24y$$

c) Constraints

$$3x + 2y \leq 5000 \quad \leftarrow \text{material}$$

$$45x + 40y \leq (40 \cdot 35 \cdot 60) = 212400 \quad \leftarrow \text{Labor}$$

$$\text{non-negativity } x, y \geq 0$$

d) $\max Z = 32x + 24y$

$$3x + 2y \leq 5000$$

$$45x + 40y \leq 212400$$

$$x, y \geq 0$$

②

a) $Lp1, Lp2, Lp3 = \text{Large plants 1, 2, 3}$

$mp1, mp2, mp3 = \text{Medium plants}$

$Sp1, Sp2, Sp3 = \text{Small plants}$

b) Objective function

$$\max Z = 420(Lp1 + Lp2 + Lp3) + 360(mp1 + mp2 + mp3) + 300(Sp1 + Sp2 + Sp3)$$

Constraints

$$\left. \begin{aligned} Lp1 + mp1 + Sp1 &\leq 750 \\ Lp2 + mp2 + Sp2 &\leq 900 \\ Lp3 + mp3 + Sp3 &\leq 450 \end{aligned} \right\} \text{Capacity}$$

$$\left. \begin{aligned} 20(Lp1) + 15(mp1) + 12(Sp1) &\leq 13000 \\ 20(Lp2) + 15(mp2) + 12(Sp2) &\leq 12000 \\ 20(Lp3) + 15(mp3) + 12(Sp3) &\leq 5000 \end{aligned} \right\} \text{Storage}$$

$$\left. \begin{aligned} Lp1 + Lp2 + Lp3 &\leq 900 \\ mp1 + mp2 + mp3 &\leq 1200 \\ Sp1 + Sp2 + Sp3 &\leq 7500 \end{aligned} \right\} \text{sales}$$

all variables are non-negative ≥ 0