AE1MCS: Tutorial 3

Question 1:

- 1. Use quantifiers to express the statement that "There is a woman who has taken a flight on every airline in the world."
- 2. Use quantifiers to express the statement that "There does not exist a woman who has taken a flight on every airline in the world."

Question 2:

Use rules of inference to show that if $\forall x (P(x) \rightarrow (Q(x) \land S(x)))$ and $\forall x (P(x) \land R(x))$ are true, then $\forall x (R(x) \land S(x))$ is true.

Question 3:

Use rules of inference to show that if $\forall x (P(x) \lor Q(x)), \forall x (\neg Q(x) \lor S(x)), \forall x (R(x) \to \neg S(x)), \text{ and } \exists x \neg P(x) \text{ are true, then } \exists x \neg R(x) \text{ is true.}$