IPUMS Health Data

MATH 301 Data Confidentiality

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```
## read data
data <- read.csv("nhis_00001.csv")
## REMOVE THIS LATER. ONLY TAKING 1000 SAMPLES B/C JAGS TOOK TOO LONG
data <- sample_n(data, 2000, replace = FALSE, prob = NULL)
## log income
## data$LOGINC<- log(data$EARNIMPOINT1)
#load("tp.RData")</pre>
```

Our goal is to generate synthetic data from the estimated Bayesian synthesizer from the posterior predictive distribution. To produce a good synthesizer, there will be trade-offs between utility and risks.

```
## Remove all NIU (00) values
data <- data[!data$EDUCREC2 == 00, ]</pre>
data <- data[!data$HOURSWRK == 00, ]</pre>
data <- data[!data$HINOTCOVE == 0, ]</pre>
data <- data[!data$HRSLEEP == 00, ]</pre>
data <- data[!data$WORFREQ == 0, ]</pre>
## Create new column RACE and recode into 6 categories
## 1 = White, 2 = Black, 3 = American Indian, 4 = Asian,
## 5 = Other races, 6 = Two or more races
data <- data %>% mutate(RACE = ifelse(RACEA %in% 100, 1, ifelse(RACEA %in% 200, 2, ifelse(RACEA %in% c(
## Create new column EDUC and recode into 3 categories
## 1 = 4 years of high school or less, 2 = 4 years of college,
## 3 = 5 + years of college
data <- data %>% mutate(EDUC = ifelse(EDUCREC2 %in% c(10,20,30,31,32,40,41,42), 1, ifelse(EDUCREC2 %in%
data <- data %>% mutate(INCOME = ifelse(EARNIMPOINT1 %in% 0, 0, 1))
head(data)
     AGE SEX RACEA EDUCREC2 HOURSWRK POORYN EARNIMP1 EARNIMPOINT1 USUALPL
## 1 22
           2
                100
                          51
                                    36
                                             1
                                                      3
                                                                14000
           2
                200
                          54
                                    35
                                             1
                                                      21
                                                                37000
                                                                             2
## 2
      32
               100
                                                                             2
## 3
      19
                          42
                                    30
                                             1
                                                      2
                                                                 7000
           1
                                                                             2
                200
                          60
                                             1
                                                      52
                                                                70000
## 4
      66
           1
                                    40
                                                                             2
## 5
      52
           2
                100
                          51
                                    47
                                             1
                                                      31
                                                                47000
## 6
      20
                100
                          42
                                    15
                                             9
                                                       0
     DELAYCOST HINOTCOVE ALCDAYSWK CIGDAYMO HRSLEEP WORFREQ DEPFREQ RACE EDUC
## 1
             2
                        1
                                  80
                                            22
                                                      6
                                                              1
                                                                       2
                                                                            1
                                                     7
                                                              5
                                                                            2
                                                                                  2
## 2
             1
                        1
                                  96
                                            96
                                                                       5
## 3
             1
                        1
                                   0
                                            96
                                                     8
                                                              5
                                                                            1
                                                                                  1
## 4
                        1
                                  80
                                            96
                                                     8
                                                              5
                                                                       5
                                                                            2
                                                                                  3
             1
## 5
                        1
                                            96
                                                     6
                                                              2
                                                                            1
                                                                                  2
                                                              2
## 6
                        2
                                   0
                                                     6
                                                                       2
                                                                            1
                                                                                  1
             2
                                            96
     INCOME
##
```

summary(data)

```
##
                           SEX
         AGE
                                          RACEA
                                                          EDUCREC2
##
    Min.
           :18.00
                     Min.
                             :1.00
                                     Min.
                                             :100.0
                                                              :10.00
##
    1st Qu.:31.00
                     1st Qu.:1.00
                                     1st Qu.:100.0
                                                       1st Qu.:42.00
    Median :42.00
                     Median:1.00
                                     Median :100.0
                                                       Median :51.00
##
    Mean
            :43.78
                             :1.49
                                             :137.1
                                                              :50.67
                     Mean
                                     Mean
                                                       Mean
##
    3rd Qu.:56.00
                     3rd Qu.:2.00
                                      3rd Qu.:100.0
                                                       3rd Qu.:54.00
                                             :600.0
##
    Max.
            :78.00
                             :2.00
                                     Max.
                                                       Max.
                                                              :60.00
                     Max.
##
       HOURSWRK
                         POORYN
                                          EARNIMP1
                                                         EARNIMPOINT1
##
    Min.
           : 1.00
                             :1.000
                                      Min.
                                              : 0.00
                     Min.
                                                        Min.
    1st Qu.:35.25
                                       1st Qu.: 5.00
                                                        1st Qu.: 21451
##
                     1st Qu.:1.000
##
    Median :40.00
                     Median :1.000
                                      Median :22.00
                                                        Median : 40000
##
    Mean
            :40.36
                     Mean
                            :1.315
                                      Mean
                                              :29.07
                                                        Mean
                                                               : 49986
##
    3rd Qu.:50.00
                     3rd Qu.:1.000
                                       3rd Qu.:52.00
                                                        3rd Qu.: 70000
##
    Max.
            :95.00
                     Max.
                             :9.000
                                      Max.
                                              :70.00
                                                        Max.
                                                               :149000
##
       USUALPL
                       DELAYCOST
                                         HINOTCOVE
                                                          ALCDAYSWK
##
    Min.
            :1.000
                     Min.
                             :1.000
                                      Min.
                                              :1.000
                                                        Min.
                                                               : 0.00
##
    1st Qu.:2.000
                     1st Qu.:1.000
                                       1st Qu.:1.000
                                                        1st Qu.: 0.00
                     Median :1.000
##
    Median :2.000
                                      Median :1.000
                                                        Median :10.00
##
    Mean
           :1.859
                     Mean
                            :1.126
                                      Mean
                                              :1.113
                                                        Mean
                                                               :32.85
    3rd Qu.:2.000
                                                        3rd Qu.:70.00
##
                     3rd Qu.:1.000
                                       3rd Qu.:1.000
##
    Max.
            :3.000
                     Max.
                             :2.000
                                      Max.
                                              :2.000
                                                        Max.
                                                               :99.00
##
       CIGDAYMO
                        HRSLEEP
                                           WORFREQ
                                                            DEPFREQ
    Min.
           : 4.00
                             : 3.000
                                        Min.
                                               :1.000
                                                         Min.
                                                                 :1.000
                     Min.
##
    1st Qu.:96.00
                     1st Qu.: 6.000
                                        1st Qu.:3.000
                                                         1st Qu.:4.000
    Median :96.00
                     Median : 7.000
                                        Median :4.000
                                                         Median :5.000
##
##
    Mean
            :94.16
                     Mean
                            : 6.928
                                        Mean
                                               :3.677
                                                         Mean
                                                                 :4.308
    3rd Qu.:96.00
                                        3rd Qu.:5.000
                     3rd Qu.: 8.000
                                                         3rd Qu.:5.000
##
    Max.
            :96.00
                             :12.000
                                        Max.
                                               :5.000
                                                                 :5.000
                     Max.
                                                         Max.
         RACE
                           EDUC
                                           INCOME
##
##
            :1.000
                             :1.000
                                              :0.0000
    Min.
                     Min.
                                      Min.
    1st Qu.:1.000
                     1st Qu.:1.000
                                       1st Qu.:1.0000
##
    Median :1.000
                     Median :2.000
                                      Median :1.0000
           :1.351
##
    Mean
                     Mean
                             :1.905
                                      Mean
                                              :0.9744
##
    3rd Qu.:1.000
                     3rd Qu.:2.000
                                       3rd Qu.:1.0000
    Max.
            :5.000
                     Max.
                             :3.000
                                      Max.
                                              :1.0000
```

Step 1: Synthetic Logistic Regression Model

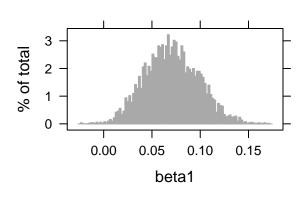
```
## JAGS script
modelString <-"
model {
## sampling
for(i in 1:N){
y[i] ~ dbern(p[i])
logit(p[i]) <- beta0 + beta1*x_age[i] +</pre>
```

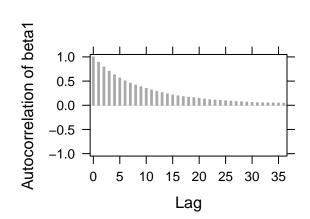
```
beta2*x_sex_male[i] + beta3*x_sex_female[i] +
beta4*x_race_w[i] + beta5*x_race_b[i] +
beta6*x_race_i[i] + beta7*x_race_a[i] +
beta8*x_race_o[i] +
beta10*x_educ_1[i] + beta11*x_educ_2[i] +
beta12*x_educ_3[i] + beta13*x_hourswrk[i] +
beta14*x_health_cov[i] + beta15*x_health_nocov[i] +
beta16*x hrsleep[i] + beta17*x wor daily[i] +
beta18*x_wor_weekly[i] + beta19*x_wor_monthly[i] +
beta20*x_wor_fewtimes[i] + beta21*x_wor_never[i]
}
## priors
beta0 ~ dnorm(mu0, g0)
beta1 ~ dnorm(mu1, g1)
beta2 ~ dnorm(mu2, g2)
beta3 ~ dnorm(mu3, g3)
beta4 ~ dnorm(mu4, g4)
beta5 ~ dnorm(mu5, g5)
beta6 ~ dnorm(mu6, g6)
beta7 ~ dnorm(mu7, g7)
beta8 ~ dnorm(mu8, g8)
beta10 ~ dnorm(mu10, g10)
beta11 ~ dnorm(mu11, g11)
beta12 ~ dnorm(mu12, g12)
beta13 ~ dnorm(mu13, g13)
beta14 ~ dnorm(mu14, g14)
beta15 ~ dnorm(mu15, g15)
beta16 ~ dnorm(mu16, g16)
beta17 ~ dnorm(mu17, g17)
beta18 ~ dnorm(mu18, g18)
beta19 ~ dnorm(mu19, g19)
beta20 ~ dnorm(mu20, g20)
beta21 ~ dnorm(mu21, g21)
#invsiqma2 ~ dqamma(a, b)
#sigma <- sqrt(pow(invsigma2, -1))
y = as.vector(data$INCOME)
x age = as.vector(data$AGE) ## age
x_sex_male = as.vector(data$SEX$.data_1) ## male
x_sex_female = as.vector(data$SEX$.data_2) ## female
x_race_w = as.vector(data$RACE$.data_1) ## white
x_race_b = as.vector(data$RACE$.data_2) ## black/african-american
x_race_i = as.vector(data$RACE$.data_3) ## american indian
x_race_a = as.vector(data$RACE$.data_4) ## asian
x_race_o = as.vector(data$RACE$.data_5) ## other races
x_educ_1 = as.vector(data$EDUC$.data_3) ## 4 years of high school or less
x_educ_2 = as.vector(data$EDUC$.data_1) ## 4 years of college
x_educ_3 = as.vector(data$EDUC$.data_2) ## 5+ years of college
x hourswrk = as.vector(data$HOURSWRK) ## hours of work
x_health_cov = as.vector(data$HEALTH$.data_1) ## has health coverage
x_health_nocov = as.vector(data$HEALTH$.data_2) ## has no health coverage
x_hrsleep = as.vector(data$HRSLEEP) ## hours of sleep
```

```
x_wor_daily = as.vector(data$WORRY$.data_2) ## worry daily
x_wor_weekly = as.vector(data$WORRY$.data_5) ## worry weekly
x_wor_monthly = as.vector(data$WORRY$.data_4) ## worry monthly
x_wor_fewtimes = as.vector(data$WORRY$.data_3) ## worry few times a year
x_wor_never = as.vector(data$WORRY$.data_1) ## worry never
N = length(y) # Compute the number of observations
## Pass the data and hyperparameter values to JAGS
the_data <- list("y" = y,
"x_age" = x_age, "x_sex_male" = x_sex_male,
"x_sex_female" = x_sex_female, "x_race_w" = x_race_w,
"x_race_b" = x_race_b, "x_race_i" = x_race_i,
"x_race_a" = x_race_a, "x_race_o" = x_race_o,
"x_educ_1" = x_educ_1,
x_{educ_2} = x_{educ_2}, x_{educ_3} = x_{educ_3},
"x_hourswrk" = x_hourswrk, "x_health_cov" = x_health_cov,
"x_health_nocov" = x_health_nocov, "x_hrsleep" = x_hrsleep,
"x_wor_daily" = x_wor_daily, "x_wor_weekly" = x_wor_weekly,
"x_wor_monthly" = x_wor_monthly, "x_wor_fewtimes" = x_wor_fewtimes,
"x_wor_never" = x_wor_never,
"N" = N,
"mu0" = 0, "g0" = 1, "mu1" = 0, "g1" = 1,
"mu2" = 0, "g2" = 1, "mu3" = 0, "g3" = 1,
"mu4" = 0, "g4" = 1, "mu5" = 0, "g5" = 1,
"mu6" = 0, "g6" = 1, "mu7" = 0, "g7" = 1,
"mu8" = 0, "g8" = 1,
"mu10" = 0, "g10" = 1, "mu11" = 0, "g11" = 1,
"mu12" = 0, "g12" = 1, "mu13" = 0, "g13" = 1,
"mu14" = 0, "g14" = 1, "mu15" = 0, "g15" = 1,
"mu16" = 0, "g16" = 1, "mu17" = 0, "g17" = 1,
"mu18" = 0, "g18" = 1, "mu19" = 0, "g19" = 1,
"mu20" = 0, "g20" = 1, "mu21" = 0, "g21" = 1)
initsfunction <- function(chain){</pre>
.RNG.seed \leftarrow c(1,2) [chain]
.RNG.name <- c("base::Super-Duper",
"base::Wichmann-Hill")[chain]
return(list(.RNG.seed=.RNG.seed,
.RNG.name=.RNG.name))
}
## Run the JAGS code for this model:
posterior_MLR <- run.jags(modelString,</pre>
n.chains = 1,
data = the data,
monitor = c("beta0", "beta1", "beta2",
"beta3", "beta4", "beta5",
"beta6", "beta7", "beta8", "beta10",
"beta11", "beta12", "beta13", "beta14", "beta15", "beta16", "beta17",
"beta18", "beta19", "beta20", "beta21"),
adapt = 1000,
burnin = 5000,
sample = 5000,
```

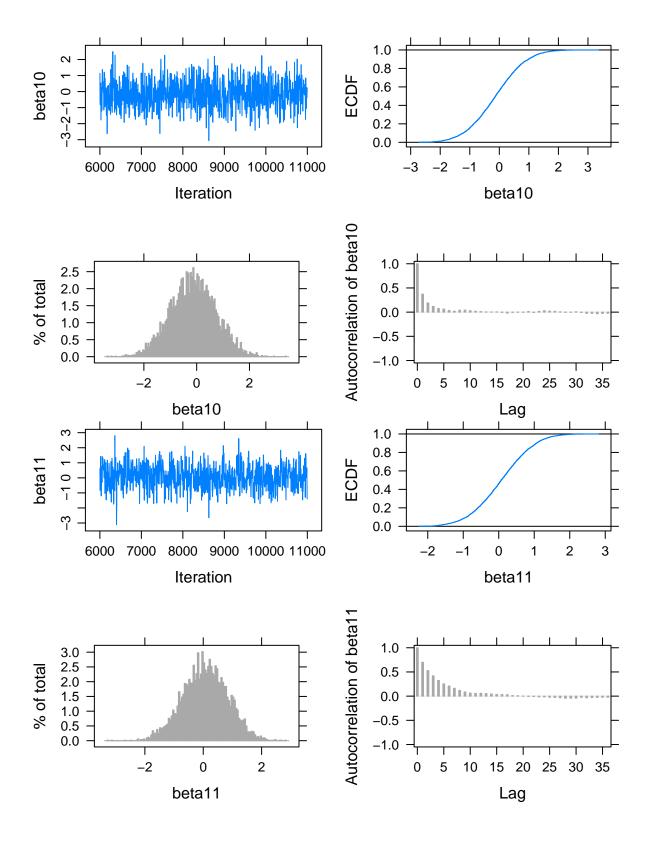
```
thin = 1,
inits = initsfunction)
## Loading required namespace: rjags
## Compiling rjags model...
## Calling the simulation using the rjags method...
## Adapting the model for 1000 iterations...
## Burning in the model for 5000 iterations...
## Running the model for 5000 iterations...
## Simulation complete
## Calculating summary statistics...
## Warning: Convergence cannot be assessed with only 1 chain
## Finished running the simulation
## JAGS output
summary(posterior_MLR)
##
             Lower95
                           Median
                                    Upper95
                                                    Mean
                                                                 SD Mode
## beta0
         -1.94216286 -0.064370798 1.7087691 -0.059244782 0.95755888
          ## beta1
                                                                      NΑ
## beta2
        -1.52081205 -0.010785325 1.5617397 -0.001100925 0.78853927
## beta3 -1.42833200 -0.030058490 1.6036287 -0.037891187 0.76633484
## beta4 -1.70854020 -0.238894845 1.2627460 -0.261122309 0.77038375
## beta5 -1.90242561 -0.266598173 1.3632391 -0.247070020 0.83764811
## beta6 -1.80407664 0.125012061 1.9626125
                                             0.118639226 0.98157860
## beta7 -1.46997316 0.258248644 2.0954143 0.279991684 0.91151560
## beta8 -1.82410712 0.082366429 1.9653833 0.082791730 0.96465078
## beta10 -1.80561893 -0.127869671 1.5390520 -0.129151490 0.86019312
                                                                      NA
## beta11 -1.47775601
                     0.068138162 1.5119147
                                             0.069102320 0.76951951
                                                                      NA
## beta12 -1.46719304
                     0.042431748 1.5549516
                                             0.024320356 0.77475482
## beta13 0.04660710 0.100308705 0.1553877
                                             0.101392498 0.02817009
                                                                      NA
## beta14 -0.91600088 0.532118514 2.0267029
                                             0.551548048 0.77527016
                                                                      NA
## beta15 -2.20148535 -0.584046364 0.9382540 -0.598551876 0.79961200
                                                                      NA
## beta16 -0.67530542 -0.231626161 0.2103327 -0.229364201 0.23163627
## beta17 -1.74548598 -0.333244751 1.0957288 -0.331396086 0.72269332
                                                                      NA
## beta18 -1.65502601 -0.169343372 1.1056249 -0.169482359 0.70711899
                                                                      NA
## beta19 -0.56718725 0.987889468 2.5936241 0.994046300 0.81821663
                                                                      NΑ
## beta20 -1.62605643 0.004998299 1.5255489 0.013384858 0.80716359
## beta21 -1.99993607 -0.575112387 1.0555822 -0.548693811 0.77444022
##
               MCerr MC%ofSD SSeff
                                           AC.10 psrf
## beta0 0.056190074
                               290
                                   2.982882e-01
                         5.9
## beta1 0.001626187
                                    3.489078e-01
                         5.8
                               297
## beta2 0.030278286
                         3.8
                               678
                                    6.002516e-02
                                                   NΑ
## beta3 0.031597559
                         4.1
                               588
                                    1.017022e-01
## beta4 0.034138273
                         4.4
                               509
                                    1.546571e-01
## beta5 0.026542528
                         3.2
                               996
                                    8.377229e-02
## beta6
        0.017770571
                         1.8
                              3051
                                    2.837257e-02
                                                   NA
## beta7
         0.018196566
                         2.0
                              2509
                                    4.529739e-05
                                                   NA
                              2936
## beta8 0.017802231
                         1.8
                                    6.935257e-03
## beta10 0.019769596
                         2.3
                              1893
                                    2.958121e-02
                                                   NA
## beta11 0.029331843
                         3.8
                               688
                                    6.214165e-02
                                                   NA
## beta12 0.027965868
                         3.6
                               767
                                    4.804411e-02
                                                   NΑ
## beta13 0.001304828
                         4.6
                               466
                                   1.538657e-01
```

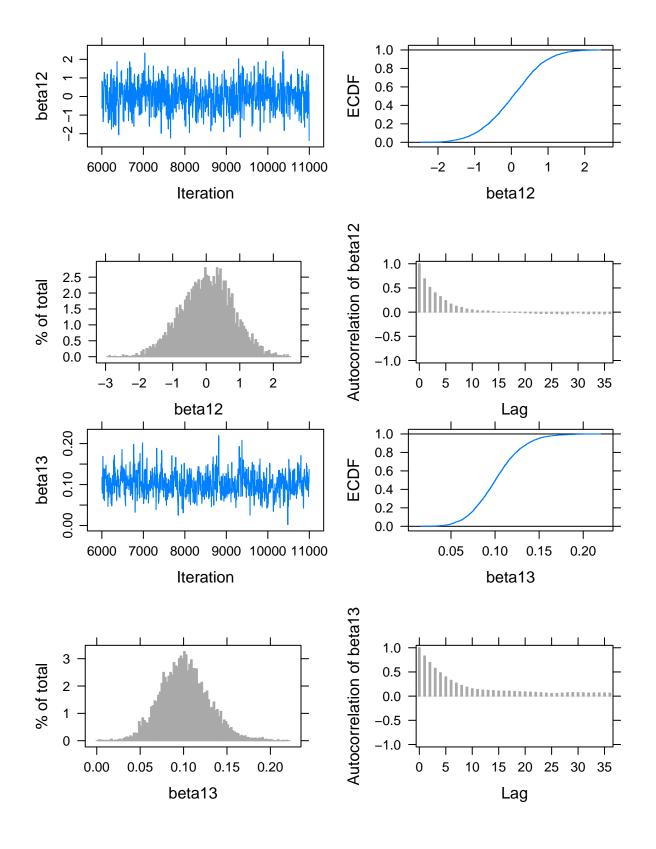
```
## beta14 0.033415330
                           4.3
                                  538
                                       1.097408e-01
                                                       NA
## beta15 0.028190107
                           3.5
                                       5.718940e-02
                                  805
                                                       NA
## beta16 0.022056978
                           9.5
                                       6.568611e-01
                                                       NA
                                  110
## beta17 0.018092380
                           2.5
                                 1596
                                       9.121764e-03
                                                       NA
## beta18 0.020274399
                                       1.647437e-02
                           2.9
                                 1216
## beta19 0.016687399
                           2.0
                                 2404 -2.150645e-02
                                                       NA
## beta20 0.016393582
                           2.0
                                 2424 -4.418488e-02
                                                       NA
                           2.5
## beta21 0.019459208
                                       3.691483e-02
                                1584
                                                       NA
plot(posterior_MLR, vars = "beta1")
## Generating plots...
                                                    1.0
                                                    8.0
     0.10
                                                ECDF
beta1
                                                    0.6
                                                    0.4
     0.00
                                                    0.2
                                                    0.0
        6000 7000
                     8000 9000 10000 11000
                                                           0.00
                                                                   0.05
                                                                          0.10
                      Iteration
                                                                      beta1
```

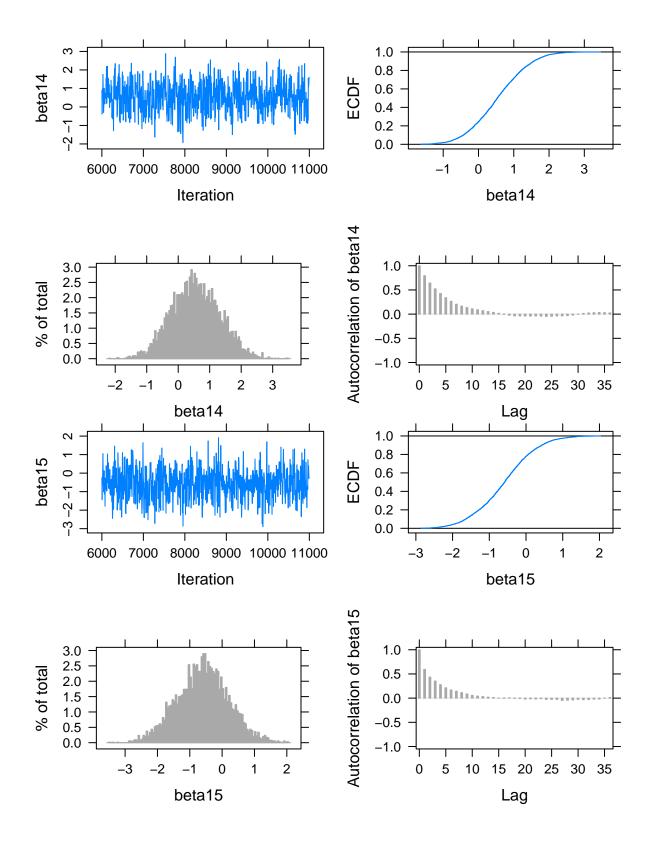


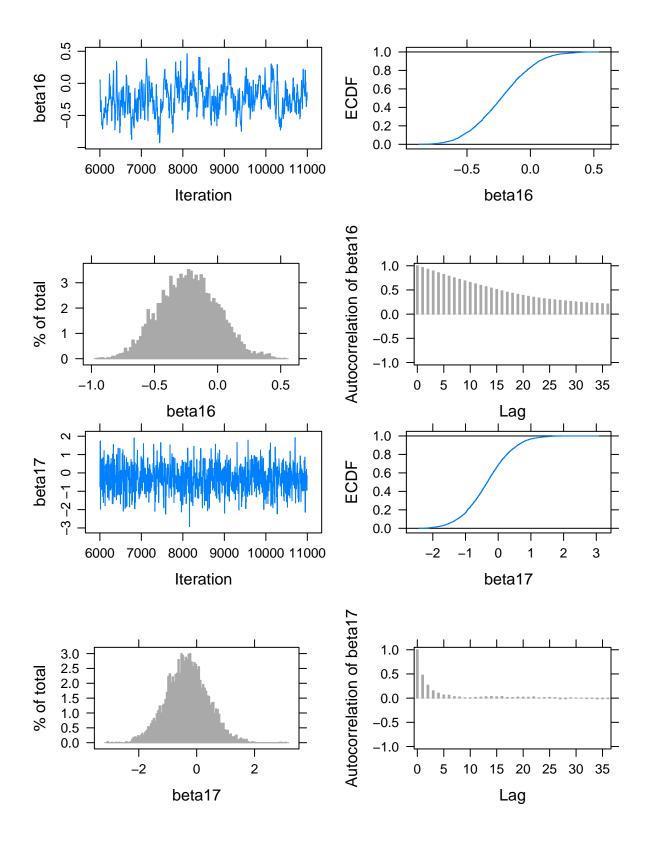


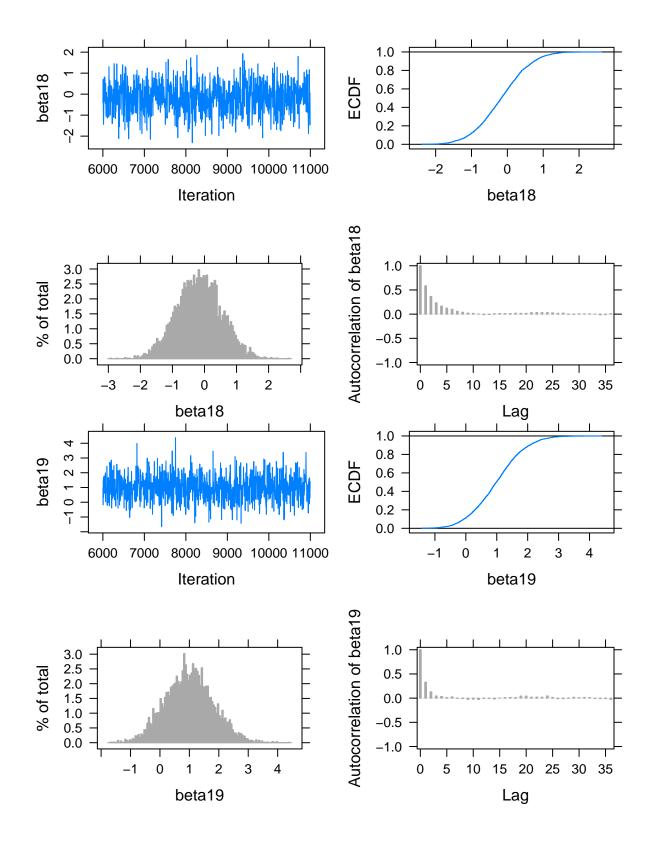
0.15







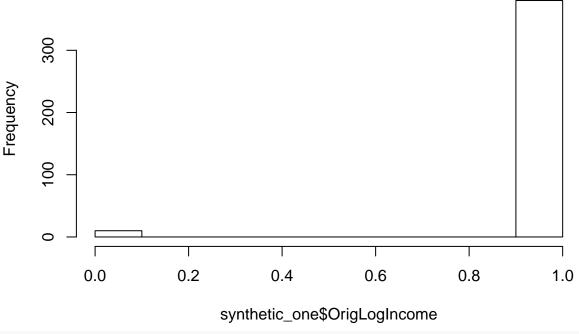




```
beta11
beta12
beta13
                                                                                         beta14
beta15
beta16
                                                                                                                          beta17
                                                                                                                                     beta18
## Saving posterior parameter draws
post <- as.mcmc(posterior_MLR)</pre>
post[1, "beta0"]
## [1] 0.2047922
## Generating one set of sythetic data
synthesize <- function(X, index, n){</pre>
         synthetic_Y <- c()</pre>
        for(i in 1:n){
                     p <- plogis(post[index, "beta0"] + X$x_age[i] * post[index, "beta1"] + X$x_sex_male[i] * post[index, "beta0"] + X$x_sex_male[i] * post[index, "beta1"] + X$x_sex_male[index, "beta1"] + X$x
                      synthetic_Y[i] <- rbinom(1,1,p)</pre>
        }
        data.frame(X$y, synthetic_Y)
}
n <- dim(data)[1]</pre>
params <- data.frame(y, x_age, x_sex_male, x_sex_female, x_race_w, x_race_b, x_race_i, x_race_a, x_race
synthetic_one <- synthesize(params, 1, n)</pre>
names(synthetic_one) <- c("OrigLogIncome", "SynLogIncome")</pre>
```

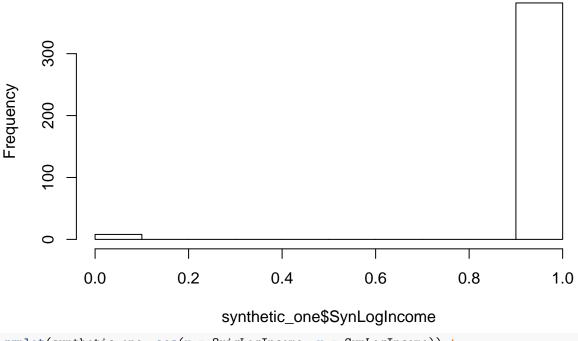
hist(synthetic_one\$OrigLogIncome)

Histogram of synthetic_one\$OrigLogIncome



hist(synthetic_one\$SynLogIncome)

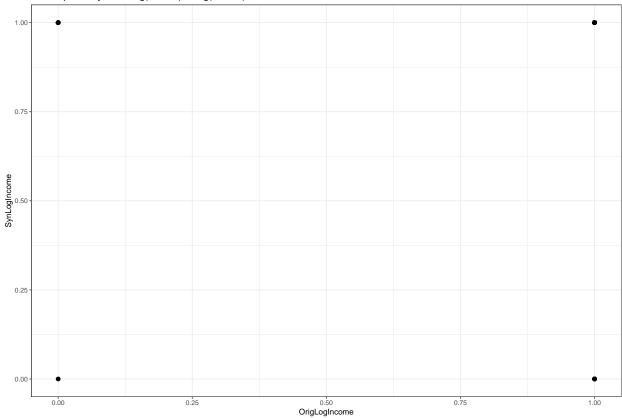
Histogram of synthetic_one\$SynLogIncome



```
ggplot(synthetic_one, aes(x = OrigLogIncome, y = SynLogIncome)) +
  geom_point(size = 1) +
  labs(title = "Scatter plot of Synthetic log(Income) vs log(Income)") +
```

```
theme_bw(base_size = 6, base_family = "")
```

Scatter plot of Synthetic log(Income) vs log(Income)



Utility Evaluation

Analysis-specific measures

Synthetic IPUMS sample: step 1

```
n <- dim(data)[1]
m <- 20
synthetic_m <- vector("list",m)

for(i in 1:m){
    seed <- round(runif(1, 1, 1000))
    synthetic_new <- synthesize(params, 2000 + i, n)
    names(synthetic_new) <- c("params", "LogIncome")
    synthetic_m[[i]] <- synthetic_new
}

q <- rep(NA, m)
v <- rep(NA, m)
for (i in 1:m){
    synthetic_new <- synthetic_m[[i]]
    q[i] <- mean(synthetic_new$LogIncome)
    v[i] <- var(synthetic_new$LogIncome)/n
}</pre>
```

Synthetic IPUMS sample: step 2

```
q_bar_m <- mean(q)
b_m <- var(q)
v_bar_m <- mean(v)</pre>
```

Synthetic IPUMS sample: step 3

```
T_p <- b_m / m + v_bar_m
v_p <- (m - 1) * (1 + v_bar_m / (b_m / m))^2
```

Synthetic CE sample: step 4

• Obtain the point estimate for mean estimand Q, and the 95% confidence interval

```
set.seed(123)
q_bar_m

## [1] 0.9725641

t_score_syn <- qt(p = 0.975, df = v_p)
c(q_bar_m - t_score_syn * sqrt(T_p), q_bar_m + t_score_syn * sqrt(T_p))

## [1] 0.9557478 0.9893804</pre>
```

Synthetic CE sample: step 4-extra

Synthetic mean estimand: 0.974 Synthetic 95% CI: [0.957, 0.990]

Original mean estimand: 0.970 Original 95% CI: [0.952, 0.987]

```
## Obtain the point estimate for mean estimand Q, and the 95%
## confidence internval from the original data
set.seed(123)
mean_org <- mean(data$INCOME)
sd_org <- sd(data$INCOME)
t_score_org <- qt(p = 0.975, df = n-1)
mean_org

## [1] 0.974359
set.seed(123)
c(mean_org - t_score_org * sd_org / sqrt(n), mean_org + t_score_org * sd_org / sqrt(n))
## [1] 0.9586027 0.9901153</pre>
```

Interval overlap utility measure

Combining rules provide point estimate and confidence interval estimates. We can also obtain point estimate and confidence interval estimate from the original, confidential data.

```
L_s = quantile(synthetic_new$params, 0.025)
U_s = quantile(synthetic_new$params, 0.975)
L_o = quantile(data$INCOME, 0.025)
U_o = quantile(data$INCOME, 0.975)
L_i = max(L_s, L_o)
U_i = min(U_s, U_o)
I = (U_i - L_i) / (2 * (U_o - L_o)) + (U_i - L_i)/ (2 * (U_s - L_s))
I
```

```
## 97.5%
## 1
```

It seems like the interval overlap measure is 1 so we have high utility. We can potentially try to calculate multiple estimands and then take the average values of I over all estimands to obtain a summary.

Identification Risk Evaluation

First, we look into identification disclosure through expected match risk, true match rate, and false match rate. Then attribute disclosure will be examined.

Higher expected match risk, higher true match rate, and lower false match rate indicate higher identification disclosure risk for the sample. Since we are doing a two-part synthesis model, we could potentially calculate three summaries on each synthetic dataset, and take the average.

Step 1: calculate key quantities

```
CalculateKeyQuantities <- function(data, params, known.vars, syn.vars, n){ data <- data params <- params n <- n c_vector <- rep(NA, n) T_vector <- rep(NA, n) for (i in 1:n){ match <- (eval(parse(text=paste("data", syn.vars, "[i] == params", syn.vars, sep="", collapse="&")))& eval(parse(text=paste("data", kn params", known.vars, sep="", collapse="&")))) match.prob <- ifelse(match, 1/sum(match), 0)

if (max(match.prob) > 0){
    c_vector[i] <- length(match.prob[match.prob == max(match.prob)])
}

else
    c_vector[i] <- 0
    T_vector[i] <- is.element(i, rownames(data)[match.prob == max(match.prob)])
}

K_vector <- (c_vector * T_vector == 1) F_vector <- (c_vector * (1 - T_vector) == 1) s <- length(c_vector[c_vector == 1 & is.na(c_vector) == FALSE])

res_r <- list(c_vector = c_vector, T_vector = T_vector, K_vector = K_vector, F_vector = F_vector, s = s) return(res_r) }
```

Step 1: calculate key quantities cont'd

known.vars <- c("SEX", "RACE", "AGE", "EDUC", "HOURSWRK", "HEALTH", "HRSLEEP", "WORRY") syn.vars <- c("INCOME") n <- dim(data)[1] KeyQuantities <- CalculateKeyQuantities(data, param, known.vars, syn.vars, n)

Step 2: calculate 3 summary measures

```
IdentificationRisk <- function(c\_vector, T\_vector, K\_vector, F\_vector, s, N) \\ nonzero\_c\_index <- which(c\_vector > 0) exp\_match\_risk <- sum(1/c\_vector[nonzero\_c\_index]*T\_vector[nonzero\_c\_index] \\ true\_match\_rate <- sum(na.omit(K\_vector))/N false\_match\_rate <- sum(na.omit(F\_vector))/s res\_r \\ <- list(exp\_match\_risk = exp\_match\_risk, true\_match\_rate = true\_match\_rate, false\_match\_rate = false\_match\_rate) \\ return(res\_r) \\ \\ \}
```

Step 2: calculate 3 summary measures cont'd

• each record is a target, therefore N = n

 $\begin{array}{l} c_vector <- \ KeyQuantities[["c_vector"]] \ T_vector <- \ KeyQuantities[["T_vector"]] \ K_vector <- \ KeyQuantities[["K_vector"]] \ F_vector <- \ KeyQuantities[["s"]] \ N <- \ n \ ThreeSummaries <- \ IdentificationRisk(c_vector, T_vector, K_vector, F_vector, s, N) \end{array}$

Step 2: calculate 3 summary measures cont'd

 $Three Summaries [["exp_match_risk"]] \ Three Summaries [["true_match_rate"]] \ Three Summaries [["false_match_rate"]] \ Three Summaries [["false_match_rate"]]$