E26: Advantages and Disadvantages of the designs

| Designs | Brief description | Advantages | Disadvantages | | | |
|------------------------|--|--|---|--|--|--|
| Design 2 - PointCP2 | Stores Polar only and computes Cartesian | Getting polar coordinates is fast; Efficient when creating an instance by inputting polar coordinates. If compared to design 1 (PointCP original), stores only 2 variables, hence less memory is required. The majority of code is simple. | Getting Cartesian coordinates is slow. The functions that require Cartesian coordinates such as getDistance and Rotate are expected to be slow due to required computation before these methods can be implemented. Some memory is used to store the coordinates. Inefficient when an instance created with cartesian coordinates (slow because of computation of rho and theta) | | | |
| Design 3 - PointCP3 | Stores Cartesian only and computes Polar | Getting Cartesian is fast; Methods that utilize Cartesian coordinates are expected to be fast. Efficient when creating an instance by giving cartesian coordinates Compared to original design 1 PointCP, less memory is required Simple Code | Getting Polar coordinates is expected to be slower; Some memory is used to store the coordinates. Inefficient when creating an instance with Polar coordinates (slower); | | | |
| Design 5 - PointCP5 | Is an abstract superclass for subclasses Design 2 and Design 3. | Defines the methods and enforces the subclasses to implement them. Improves code reusability Allows to hide some code due to abstraction property | Cannot be inherited multiple times. As per assignment specifications the computation and getting the coordinates depend on the concrete classes. Hence, the abstract class is not expected to reduce the runtime. | | | |

E28-E30: Performance Analysis

| Operation | S | Time for Design 2 (millisecond s) | Time for Design 3 (milliseconds | Time for Design 5 (Concrete 2) (milliseconds) | Time for Design 5 (Concrete 3) (milliseconds) | |
|---------------------------------------|-----|--|---------------------------------------|---|---|--|
| Construction | Ave | 1801.9 | 29.7 | 1882.2 | 30.2 | |
| by giving Cartesian coordinates | Min | 1553 | 27 | 1597 | 28 | |
| | Max | 2138 | 41 | 2234 | 37 | |
| Construction | Ave | 28.6 | 3836.4 | 29.5 | 3897.1 | |
| by giving | Min | 27 | 3573 | 27 | 3609 | |
| Polar | Max | 32 | 4111 | 38 | 4152 | |
| | Ave | 728.5 | 12.1 | 1130.3 | 20.6 | |
| getX() | Min | 655 | 10 | 1107 | 16 | |
| | Max | 971 | 14 | 1297 | 33 | |
| | Ave | 921.8 | 10 | 1111.1 | 11.8 | |
| getY() | Min | 900 | 6 | 1105 | 10 | |
| | Max | 948 | 26 | 1127 | 15 | |
| | Ave | 7.5 | 11.4 | 12.9 | 15 | |
| getRho() | Min | 7 | 7 | 12 | 11 | |
| | Max | 8 | 19 | 15 | 28 | |
| | Ave | 7 | 218.6 | 12.4 | 211.3 | |
| getTheta() | Min | 6 | 209 | 11 | 206 | |
| | Max | 8 | 240 | 14 | 244 | |
| | Ave | 4407.1 | 14.6 | 4456.2 | 29.8 | |
| getDistance() | Min | 4393 | 9 | 4388 | 18 | |
| | Max | 4421 | 41 | 4596 | 88 | |
| | Ave | 8758.4 | 4624.5 | 6838.7 | 4664.9 | |
| rotatePoint() | Min | 8726 | 4596 | 6774 | 4618 | |
| | Max | 8804 | 4678 | 7050 | 4748 | |

Description of how the test were done

First, the designs 2,3 and 5 were implemented by modifying PointCP according to the table provided in the Book. The PointCPTest was also modified to test each design. After confirming proper implementation of each design, the time efficiency analysis was performed.

For time efficiency analysis, we created several classes:

- **Test** the class generates a large number of random instances for each design. In addition this class generates an array of *point B* necessary for testing the distance between points. It contains the method that constructs the points.
- PointCPTesting the class contains methods to test each design's function and to track the time taken for each method. Here is an example of how a function typical for each design is tested:

```
//GETX TEST
long s_getX = System.currentTimeMillis();
for (int i=0; i<arrayCP2.length;i++){
    arrayCP2[i].getX();
}
long e_getX = System.currentTimeMillis();
System.out.println("Time taken for getX for " +arrayCP2[0].getClass()+" (milliseconds): "+ (e_getX-s_getX));</pre>
```

Analysis - class that contains the Main and performs the time analysis. In this
class, the user can input the number of instances to be created, as well as the
number of tests to be run. It is important to note that the user can test all the
designs in one test run for several times, or test each design separately for several
times by simply removing the testing of other designs. Our group tested each design
separately for 10 times.

To analyze the performance of designs, we have created 2 800 000 instances of points for each design and timed the methods of each design. The reason we chose 2 800 000 is to ensure that tests for each design run for at least 10 seconds to get a good measure of performance.

A total of 10 runs were performed to generate 10 time results per each design and each method. The code for this part of analysis can be found in *Analysis.java*.

Here is an example of the output for 1 test run for design 2 (PointCP2):

```
Time taken to construct PointCP2 (milliseconds) giving Polar coordinates: 27
Time taken to construct PointCP2 (milliseconds) giving Cartesian coordinates: 1553
Time taken for getX for class PointCP2 (milliseconds): 697
Time taken for getY for class PointCP2 (milliseconds): 902
Time taken for getRho for class PointCP2 (milliseconds): 8
Time taken for getTheta for class PointCP2 (milliseconds): 7
Time taken for getDistance for class PointCP2 (milliseconds): 4407
Time taken for rotatePoint for class PointCP2 (milliseconds): 8804
```

At first we tried to run 10 test runs by simply specifying the test run number in Analysis.java. However, It was observed that the time was significantly different for the second test run of PointCP2. After some research, we believe such discrepancy is related to JVM performance. To further investigate this issue and possibly counteract, we have run tests one by one (by changing the functions we call in Analysis) for 10 times in the terminal and scripted the outputs into the files. These outputs can be found in *terminalTimeOutput.txt. We have confirmed that running the Analysis in the terminal loop provided more consistent results as opposed to looping inside Analysis. Hence, for average, minimum and maximum results we used *terminalTimeOutput.txt.

Once the output for 10 runs for each design were completed. The average, minimum and maximum were reported in the table above.

Discussion of Results

Design 2

As can be observed from the table, the fastest operations for Design 2 were constructed when Polar coordinates are given, getRho(), and getTheta, whereas getX() and getY() operations were more time-consuming. This is expected, because class PointCP2 stores Rho and Theta, hence they can be accessed directly without computation. However, to get x and y coordinates, PointCP2 has to perform computations which increases the run time.

When considering the functions getDistance() and rotate(), they are also considerably slower when compared to other operations or to the same methods in Design 3, and Design 5 with concrete class PointCP3. This is also expected since both of these functions call getY() and getX() in the body. In addition, rotate() returns PointCP2 that is constructed using cartesian coordinates (which was shown to be very slow, about 1801.9 ms).

Design 3

As shown in the table, the fastest operations included construction with Cartesian coordinates, getX(), getY(), getRho(), getDistance(). The slowest in increasing order were getTheta(), constructing with Polar coordinates, and rotate(). The results for getX() and getY() were expected as PointCP3 stores x and y coordinates, hence they can be accessed without any computation.

The outcome for getRho() was somewhat unexpected as we initially suggested that it would be considerably slower than getting the stored variables and perhaps it would be similar to getTheta() in terms of running time. This prompted us to further investigate and we came to a conclusion that math operations performed for getting Rho are faster than the operations necessary to compute Theta. In addition, the construction of PointCP3 with Polar coordinates uses Math.toRadians() and sin/cos functions to get x and y; therefore making the construction slower compared to the one which uses cartesian coordinates.

The difference observed in math operations is summarized in the figure below. We tested the time (milliseconds) needed to perform the math functions used in the designs for 1 000 000 random numbers.

```
Math.toDegrees(Math.atan2(a, b)) takes 53
Math.sqrt(Math.pow(a, 2) + Math.pow(b, 2)) takes 6
(Math.sin(Math.toRadians(a)) * b) takes 400
```

It should be noted that getDistance() was fast compared to design 2; and such outcome is attributed to the fact that cartesian coordinates are stored within PointCP3. As for rotate, the method computes trigonometric function and constructs a Point, thus taking more time than other operations. Design 2 rotatePoint() is two times slower than Design 3 rotatePoint() and this is because the Design 2 rotatePoint(), apart from calling getX() and getY(), constructs PointCP2 with Cartesian coordinates (known to be slow from the performance analysis).

Design 3 outperformed design 2 in such methods: getX, getY, Construction with Cartesian coordinates, getDistance(), and rotatePoint().

Design 5

Since PointCP5 is abstract and computation of coordinates depends on concrete classes, we have tested PointCP5 with concrete class PointCP2_5 and with concrete class PointCP3_5. Overall, PointCP3_5 follows the same time trend as PointCP3. This is expected as the computation of coordinates depends on the concrete class used. PointCP2_5 also has a similar time trend as PointCP2: same operations are slowest in both designs.

We implemented rotatePoint() and getDistance() in the abstract superclass and compared the performance of these methods in each design. According to our design 5, PointCP5 abstract superclass implements the rotatePoint() that returns PointCP3 constructed with Cartesian coordinates; this approach is expected to be faster than rotatePoint() in design 2 where a PointCP2 was returned after construction with cartesian coordinates (time-consuming as discussed in Design 2). Therefore, we observe that rotatePoint() in design 5 is slightly faster than in design 2.

Appendix

Test results

| PointCP2 | Const P | Const C | getX | getY | getRho | getTheta | getDistance | rotatePoint |
|----------|---------|---------|-------|-------|--------|----------|-------------|-------------|
| 1 | 32 | 1703 | 694 | 941 | 7 | 7 | 4401 | 8737 |
| 2 | 27 | 1553 | 697 | 902 | 8 | 7 | 4407 | 8804 |
| 3 | 29 | 1893 | 681 | 907 | 8 | 7 | 4395 | 8797 |
| 4 | 29 | 2136 | 694 | 922 | 7 | 7 | 4407 | 8747 |
| 5 6 | 27 | 1628 | 732 | 906 | 7 | 7 | 4402 | 8738 |
| | 30 | 1571 | 971 | 935 | 8 | 7 | 4419 | 8765 |
| 7 | 29 | 1758 | 655 | 943 | 8 | 6 | 4418 | 8768 |
| 8 | 28 | 1592 | 707 | 914 | 7 | 7 | 4408 | 8726 |
| 9 | 28 | 2138 | 675 | 900 | 7 | 8 | 4421 | 8733 |
| 10 | 27 | 2047 | 779 | 948 | 8 | 7 | 4393 | 8769 |
| Avg | 28.6 | 1801.9 | 728.5 | 921.8 | 7.5 | 7 | 4407.1 | 8758.4 |
| Min | 27 | 1553 | 655 | 900 | 7 | 6 | 4393 | 8726 |
| Max | 32 | 2138 | 971 | 948 | 8 | 8 | 4421 | 8804 |
| PointCP3 | Const P | Const C | getX | getY | getRho | getTheta | getDistance | rotatePoint |
| 1 | 3768 | 33 | 13 | 7 | 19 | 213 | 10 | 4678 |
| 2 | 4090 | 27 | 14 | 7 | 19 | 213 | 13 | 4668 |
| 3 | 4111 | 28 | 14 | 7 | 7 | 240 | 13 | 4655 |
| 4 | 3730 | 29 | 12 | 14 | 13 | 217 | 12 | 4609 |
| 5 | 3633 | 28 | 10 | 11 | 7 | 218 | 12 | 4608 |
| 6 | 4064 | 28 | 10 | 6 | 14 | 212 | 9 | 4608 |
| 7 | 3573 | 28 | 11 | 8 | 10 | 216 | 15 | 4596 |
| 8 | 4074 | 41 | 13 | 7 | 9 | 209 | 41 | 4601 |
| 9 | 3719 | 28 | 10 | 26 | 7 | 218 | 11 | 4617 |
| 10 | 3602 | 27 | 14 | 7 | 9 | 230 | 10 | 4605 |
| Avg | 3836.4 | 29.7 | 12.1 | 10 | 11.4 | 218.6 | 14.6 | 4624.5 |
| Min | 3573 | 27 | 10 | 6 | 7 | 209 | 9 | 4596 |
| Max | 4111 | 41 | 14 | 26 | 19 | 240 | 41 | 4678 |

| PointCP2_5 | Const P | Const C | getX | getY | getRho | getTheta | getDistance | rotatePoint |
|------------|---------|---------|--------|--------|--------|----------|-------------|-------------|
| 1 | 38 | 1914 | 1107 | 1106 | 12 | 11 | 4388 | 6843 |
| 2 | 29 | 1609 | 1117 | 1117 | 15 | 12 | 4497 | 6785 |
| | 29 | 2123 | 1110 | 1105 | 12 | 13 | 4426 | 6818 |
| 4 | 28 | 1909 | 1109 | 1105 | 13 | 13 | 4392 | 6813 |
| 5 | 30 | 1597 | 1297 | 1114 | 13 | 14 | 4451 | 6787 |
| 6 | 27 | 2234 | 1113 | 1109 | 12 | 12 | 4402 | 6877 |
| 7 | 28 | 1650 | 1110 | 1111 | 13 | 11 | 4596 | 6774 |
| 8 | 30 | 2095 | 1108 | 1106 | 12 | 12 | 4586 | 7050 |
| 9 | 28 | 1651 | 1119 | 1127 | 14 | 12 | 4423 | 6855 |
| 10 | 28 | 2040 | 1113 | 1111 | 13 | 14 | 4401 | 6785 |
| Avg | 29.5 | 1882.2 | 1130.3 | 1111.1 | 12.9 | 12.4 | 4456.2 | 6838.7 |
| Min | 27 | 1597 | 1107 | 1105 | 12 | 11 | 4388 | 6774 |
| Max | 38 | 2234 | 1297 | 1127 | 15 | 14 | 4596 | 7050 |
| PointCP3 5 | Const P | Const C | getX | getY | getRho | getTheta | getDistance | rotatePoint |
| 1 | 3909 | 37 | 16 | 10 | 28 | 207 | 22 | 4625 |
| 2 | 4130 | 28 | 19 | 13 | 12 | 207 | 32 | 4704 |
| 3 | 3609 | 28 | 33 | 15 | 16 | 210 | 26 | 4748 |
| 4 | 4152 | 34 | 16 | 11 | 12 | 207 | 18 | 4670 |
| 5 | 3642 | 28 | 21 | 12 | 12 | 208 | 22 | 4663 |
| 6 | 4037 | 30 | 25 | 12 | 17 | 209 | 21 | 4653 |
| 7 | 4126 | 29 | 20 | 11 | 12 | 206 | 19 | 4677 |
| 8 | 3982 | 29 | 16 | 11 | 12 | 244 | 88 | 4659 |
| 9 | 3694 | 30 | 19 | 12 | 11 | 206 | 30 | 4618 |
| 10 | 3690 | 29 | 21 | 11 | 18 | 209 | 20 | 4632 |
| Avg | 3897.1 | 30.2 | 20.6 | 11.8 | 15 | 211.3 | 29.8 | 4664.9 |
| Min | 3609 | 28 | 16 | 10 | 11 | 206 | 18 | 4618 |
| Max | 4152 | 37 | 33 | 15 | 28 | 244 | 88 | 4748 |