

#### Representation

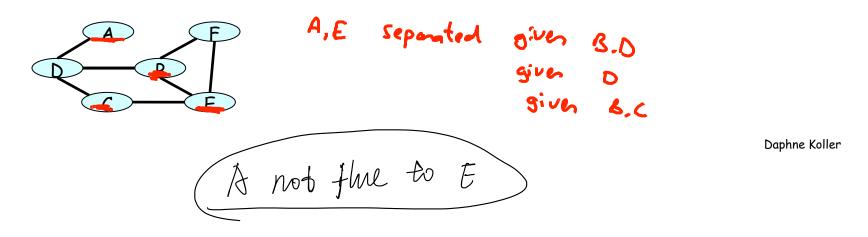
Independencies

# Markov Networks

# Separation in MNs

### Definition:

X and Y are <u>separated</u> in H given Z if there is no active trail in H between X and Y given Z



## Factorization ⇒ Independence: MNS

**Theorem:** If P factorizes over H, and  $sep_H(X, Y \mid Z)$ 

then P satisfies  $(X \perp Y \mid Z)$ 

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## Factorization ⇒ Independence: MNs

$$I(H) = \{(X \perp Y \mid Z) : sep_{H}(X, Y \mid Z)\}$$

If P satisfies I(H), we say that H is an I-map (independency map) of P

Theorem: If P factorizes over H, then H is an I-map of P

# Independence => Factorization

• Theorem (Hammersley Clifford): For a positive distribution P, if H is an I-map for P, then P factorizes over H

P(Z)>0 AZ

# Summary

Two equivalent\* views of graph structure:

- Factorization: Hallows P to be represented
- I-map: Independencies encoded by H hold in P

If P factorizes over a graph H, we can read from the graph independencies that must hold in P (an independency map)

\* for positive distributions