Name:	SID:
Collaborators:	

# Week 2 Problem Set

Probability PHW142

You must put your name and SID at the top of the page.

The exercises in this week's problem set are adapted from our textbook.

Be sure to show your work by stating intermediate steps and reasoning used.

When you upload your problem set solution, the problem set key will be unlocked for you. Because the problem set key will be released when you upload your solution, you may only upload once.

#### No exceptions.

This problem set is worth 24 points.

# **Chapter 10 exercises**

## unintended pregnancies

1. **(5 points)** Birth certificates show that approximately 9% all births in the United States are to teen mothers (ages 15 to 19), 24% to young-adult mothers (age 20 to 24), and the remaining 67% to adult mothers (age 25 to 44). An extensive survey of live births examined pregnancy type, defining an unintended pregnancy as one that was unwanted or mistimed by at least two years. The survey found that "only 23% of births to teen mothers are intended, and 77% are unintended. Among births to young-adult women age 20–24, 50% are intended, and at ages 25–44, 75% are intended."

(exercise 10.12 in the 4th edition of Baldi and Moore)

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Draw a tree diagram representing the age group of the mother (tee and the pregnancy type (intended, unintended) for live births in the Uthe image here.  Suggestion: Draw the tree, scan and upload.	Inited States. Upload

1.3	What is the probability that any given live birth in the United States is unintended? Your tree diagram should be helpful.	1 poin
	blood types	
type	oints) All human blood can be "ABO-typed" as O, A, B, or AB, but the distribution of the s varies a bit among groups of people. Here are the distributions of blood types for a domly chosen person in China and in the United States:	
	O A B AB China probability 0.35 0.27 0.26 0.12 US probability 0.45 0.40 0.11 0.04	
(exe	ercise 10.30 in the 4th edition and 10.28 in the 3rd edition of Baldi and Moore)	
2.1	Choose an American individual and a Chinese individual at random, independently of each other. What is the probability that both have type O blood?	1 poin

		both individuals h		ood typo.	3 poin
		cancer-detec	ting dogs		
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	additional questions: u don't need to use Bayes's Rule to find the answers; just use the values in the table.	
B Fo	or this special group, find the probability that a subject tested really has cancer, given the test result is positive. (This doesn't apply to the entire US population.)	1 poir
	or this special group, find the probability that the subject tested really does not have neer, given that the test is negative. (This doesn't apply to the entire US population.)	1 poir

### world weight situation

4. **(6 points)** Obesity is a growing public health concern worldwide. Adults with a high body mass index (BMI) of 25 or greater are considered overweight or obese. The following table shows the number of adults (in millions) who are overweight or obese in countries with different income levels, based on data from the World Health Organization and the United Nations.

Note: Baldi and Moore's choice of column labels is not appropriate. In this context, the opposite of high BMI is NOT low BMI! A BMI of 24 is in no sense low.

country	millions with	millions whose	total
income level	high BMI	BMI is not high	เบเสเ
high	549	414	963
upper middle	612	1042	1654
lower middle	288	1083	1371
low	63	357	420
all	1512	2896	4408

4.1	What is the probability that a randomly selected adult has a high BMI?	1 point
4.2	What are the conditional probabilities that a randomly selected adult has a high BMI, given	
	each country income level? Write a short summary of your findings in context.	2 points

	BMI). Explain, in words, what these conditional probabilities mean and why they are not the same.	3 points
	Chapter 12	
	Down syndrome	
	points The state of New York reported 1484 live births in which the infants had Down syn-	
W as	rome (trisomy 21) between 2006 and 2010, which averages to about 5.7 cases per week. While the causes of Down syndrome are not fully understood, it is reasonable at this point to ssume that live births are independent and the weekly rate is constant. Let X be the count of abies born with Down syndrome in the state of New York in each week.	
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week?					1

#### vaccination at work

6. **(2 points)** Whooping cough (pertussis) is a highly contagious bacterial infection that was a major cause of childhood deaths before the development of vaccines Approximately 80% of unvaccinated children who are exposed to whooping cough will develop the infection, compared to only 5% of vaccinated children.

A group of 20 children at a nursery school are exposed to whooping cough by playing with an infected child.

(exercise 12.38 in the 4th edition of Baldi and Moore)

Use the binomial functions in R and include your functions in the answers.

	20 children will develop infections?	1 point
6.2	If none of the 20 of the children have been vaccinated, what is the probability that 18 or	
	If none of the 20 of the children have been vaccinated, what is the probability that 18 or more of the 20 children will develop infections?	1 point
		1 point
		1 point