

## Signals and Systems

### Quiz 2

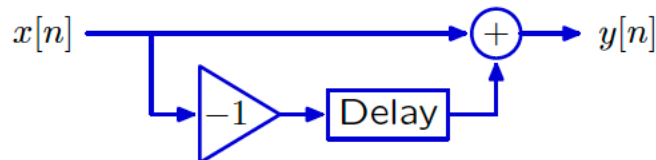
(10 questions to be chosen randomly, 5 from easy, 5 from medium)

#### System Properties (Easy)

1. Consider a system where output  $y(t) = x(t)\cos(\omega(t-3))$ . The system is
  - a. Linear and time invariant
  - b. Nonlinear and time invariant
  - c. Linear and time variant
  - d. Nonlinear and time variant
2. Consider a system where output  $y(t) = (t+1)^2x(t)$ . The system is
  - a. Linear and time invariant
  - b. Nonlinear and time invariant
  - c. Nonlinear and time variant
  - d. Linear and time variant
3. Consider a system where output  $y(t) = x(t+1)+x(-t-1)$ . The system is
  - a. Linear and time variant
  - b. Linear and time invariant
  - c. Nonlinear and time invariant
  - d. Nonlinear and time variant
4. Impulse response of a system is given as  $h[n] = (-3)^{-n}u[n-3]$ , the system is
  - a. Causal & Stable
  - b. Non causal, not stable
  - c. non causal, stable
  - d. causal, not stable
5. Given system  $y(t) = x^4(t+4)+x^3(t-4)$ , the system is
  - a. Stable, causal and invertible
  - b. Stable, non-causal and non-invertible
  - c. Non-stable, non-causal and non-invertible
  - d. Stable, causal and non-invertible
6. Consider a system where output  $y(t) = x(t)+\sin(t)$ . The system is
  - a. Linear and time invariant
  - b. Nonlinear and time invariant
  - c. Nonlinear and time variant
  - d. Linear and time variant
7. Consider a system where output  $y(t) = ax(t)+b$ . For what values of a and b will be system be linear time invariant?
  - a.  $a=2, b=1$
  - b.  $a=2, b=0$
  - c.  $a=\sin(t), b=0$
  - d.  $a=\sin(t), b=1$
8. Given system  $y(t) = x^k(t+m)$ , for what values of k and m will the system be causal and invertible?
  - a.  $k=2, m=-1$
  - b.  $k=3, m=-1$
  - c.  $k=4, m=1$
  - d.  $k=3, m=1$

9. Consider a system where output  $y(t) = x(t+1) * x(-t-1)$ . The system is
- Causal & Stable
  - Non causal, not stable
  - non causal, stable
  - causal, not stable
10. If  $y[n] = 1.5x[n] - x[n-1] + x[n+1]$ , what is the impulse response of the system?
- $h[n] = \delta[n] - \delta[n-1] + \delta[n+1]$
  - $h[n] = \delta[n] + \delta[n-1] + \delta[n+1]$
  - $h[n] = 1.5\delta[n] - \delta[n-1] + \delta[n+1]$
  - $h[n] = 1.5\delta[n] + \delta[n-1] - \delta[n+1]$
11. If  $y[n] = x[n] - x[n-1] + x^2[n+2]$ , the system is
- Causal & Stable
  - Non causal, not stable
  - non causal, stable
  - causal, not stable
12. If  $Y = (1 - 2R + R^2) X$ , the output  $y[n]$  depends upon
- $x[n]$ ,  $y[n-1]$  and  $y[n-2]$
  - $x[n]$ ,  $y[n-1]$  and  $x[n-2]$
  - $x[n]$ ,  $x[n-1]$  and  $y[n-2]$
  - $x[n]$ ,  $x[n-1]$  and  $x[n-2]$

13. For a system with block diagram given below, the difference equation is



- $y[n] = x[n] + 1.2y[n-1]$
  - $y[n] = x[n] - x[n-1]$
  - $y[n] = x[n] + x[n-1]$
  - $y[n] = -x[n] + x[n+1]$
14. If  $y[n] = x[n] - 1.01y[n-1]$ , impulse response of the systems is
- finite length and convergent
  - infinite length and convergent
  - finite length and divergent
  - infinite length and divergent
15. Impulse response of a system is given as  $h[n] = (-1)^n u[n+1]$ , the system is
- Causal & Stable
  - Non causal, not stable
  - non causal, stable
  - causal, not stable

### Convolution (Medium/Hard)

16. Let  $y[n]=x[n]*h[n]$ . The impulse response  $h[n] = (1/2)^n u(n)$  and  $x[n]$  is a causal signal. If  $y[0] = 1$  and  $y[1] = 1$ , the values of  $x[0]$  and  $x[1]$  would be
- $x[0]=1, x[1] = 1$
  - $x[0]=1, x[1] = 1/2$
  - $x[0]=1/2, x[1] = 1$
  - $x[0]=1, x[1] = 0$
17. Let  $y[n]=x[n]*h[n]$ . The impulse response  $h[n] = 2u(n)$  and  $x[n]$  is a causal signal. If  $y[0] = 1$  and  $y[1] = 1$ , the values of  $x[0]$  and  $x[1]$  would be
- $x[0]=1, x[1] = 0$
  - $x[0]=1/2, x[1] = 1/2$
  - $x[0]=1/2, x[1] = 0$
  - $x[0]=1, x[1] = 0$
18. Let  $y[n]=x[n]*h[n]$ . The impulse response  $h[n] = 2^n, -1 \leq n \leq 4$  and  $x[n] = 1, 0 \leq n \leq 2$ . The length of  $y[n]$  and its maximum value will be
- Length = 8, max = 28
  - Length = 7, max = 13
  - Length = 8, max = 13
  - Length = 7, max = 28
19. Given two discrete time signal  $x[n] = 2^{-n}u[n]$  and  $h[n] = u[n]$ , the convolved signal  $y[n]=x[n]*h[n]$  would be,
- $2^{-n}$
  - $2^{-n}u[n]+u[n]$
  - $(2-2^{-n})u[n]$
  - $(1/2 - (1/2)^n)u[n]$
20. Given two continuous time signals  $x(t) = e^{-\alpha t}u(t)$  and  $h(t)=u(t)$ , the convolved signal  $y(t)=x(t)*h(t)$  would be,
- $\alpha^{-t}u(t)$
  - $(1/\alpha)(1-e^{-\alpha t})u(t)$
  - $(1/\alpha)(1+e^{-\alpha t})u(t)$
  - $(1/\alpha)(1-e^{\alpha t})u(t)$
21. Two systems  $h_1[n]$  and  $h_2[n]$  are connected in cascade. If  $h_1[n] = h_2[n] = u[n]$ , the response of the combined system is
- $h[n]=u[n]$
  - $h[n] = u^2[n]$
  - $h[n]=nu[n]$
  - $h[n]=(n+1)u[n]$
22. Two systems  $h_1[n]$  and  $h_2[n]$  are connected in parallel, If  $h_1[n]=2^{-n}u[n+2]$  and  $h_2[n]=2^n u[n-2]$ , the combined system will be
- Stable and causal
  - Non causal, not stable
  - non causal, stable
  - causal, not stable
23. Let  $y[n]=x[n]*h[n]$ . The impulse response  $h[n] = (-1)^n, -2 \leq n \leq 4$  and  $x[n] = 1, 0 \leq n \leq 3$ . The length of  $y[n]$  and its maximum value will be
- Length = 10, max = 1

- b. Length = 11, max = 2
  - c. Length = 10, max = 4
  - d. Length = 11, max = 3
24. Let  $y[n] = x[n] * h[n]$ . The impulse response  $h[n] = (-2)^n, -2 \leq n \leq 4$  and  $x[n] = 1, 0 \leq n \leq 3$ . The length of  $y[n]$  and its smallest value will be
- a. Length = 10, min = -2
  - b. Length = 11, min = -4
  - c. Length = 10, min = 0
  - d. Length = 11, min = -6
25. The system is represented by the following equation  $Y = X + 1.2RY - 0.32R^2Y$ . The poles of the system are at
- a. 0.8 and 0.4
  - b. -0.8 and 0.4
  - c. 0.8 and -0.4
  - d. -0.8 and -0.4
26. For  $x_1[n] = \delta[n]$ , the output  $y_1[n] = (-0.5)^n$ . If the new input  $x_2[n] = \delta[n] + \delta[n-1]$ ,  $y_2[1]$  and  $y_2[2]$  will be
- a. -1/2, -1/2
  - b. 1/2, -1/4
  - c. 1, -1/2
  - d. -1/2, 1/4
27. For  $x_1[n] = \delta[n]$ , the output  $y_1[n] = (-1)^n$ . If the new inputs  $x_2[n] = \delta[n] + \delta[n-2]$ ,  $y_2[0]$ ,  $y_2[1]$  and  $y_2[2]$  will be
- a. 0, -1, 1
  - b. 1, 2, 2
  - c. 2, -2, 2
  - d. 1, 0, 0
28. For  $x[n] = u[n]$ , the output  $y[n] = \delta[n]$ . The impulse response of the system is
- a.  $h[n] = \delta[n]$
  - b.  $h[n] = \delta[n-1]$
  - c.  $h[n] = \delta[n] + \delta[n-1]$
  - d.  $h[n] = \delta[n] - \delta[n-1]$
29. Two systems  $h_1(t)$  and  $h_2(t)$  are connected in cascade. If  $h_1(t) = \delta(t-4)$  and  $h_2(t) = u(t)$  the response of the combined system is
- a.  $h(t) = u(t-4)$
  - b.  $h(t) = u(t+4)$
  - c.  $h(t) = u(t) + \delta(t-4)$
  - d.  $h(t) = u(t)$