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Pre-Lab 1)

//assuming all our numbers are uint32_t, 32 bit natural numbers (including 0)

N = number of primes to test

```
Types_of_primes{
    bitvector(N) Fibonacci_till_N;
    bitvector(N) Lucas_till_N;
```

```
    int prev_term = 0;
    int term = 1;
    int sum = 1;
```

```
    set_bit(prev_term, Fibonacci_till_N);
    set_bit(term, Fibonacci_till_N);
```

```
    while(prev_term + term < N){ //filling Fibonacci bit vector
        sum = prev_term + term;
        prev_term = term;
        term = sum;
        set_bit(term, Fibonacci_till_N);
    }
```

```
    int prev_term = 2;
    int term = 1;
```

```
    set_bit(prev_term, Lucas_till_N);
    set_bit(term, Lucas_till_N);
```

```
    while(prev_term + term < N){ //filling Lucas bit vector
        sum = prev_term + term;
        prev_term = term;
        term = sum;
        set_bit(term, Lucas_till_N);
    }
```

```
    For every prime p up to N
        successor = p+1;
        bits_in_successor = 0;
        for(int i = 0; i < 32; i++){ //counting bits in successor
            bit_i = 1 << i; //a number where only bit i is 1
```

```

        if(bit_i & successor){
            bits_in_successor++;
        }
    }
    if(bits_in_successor == 1)
        p is a mersenne prime;
    if(is_bit_set(N,Fibonacci_till_N)
        p is a Fibonacci prime;
    if(is_bit_set(N, Lucas_till_N)
        p is a Lucas prime;
}

```

2) Fibonacci and Lucas implementation is the same, Mersenne is different

```

For every prime p up to N{
    successor = p + 1;
    while(successor > 1){
        if(successor % 2 == 1){
            break;
        }
        successor /= 2;
    }
    if(successor == 1)
        p is a mersenne prime
}

```

Pre_Lab 2)

1)

```

BitVector *bv_create ( uint32_t bit_len ){
    BitVector *fresh = (BitVector* ) malloc(sizeof(struct BitVector));
    if(!fresh){
        return NULL;
    }
    fresh->length = bit_len;
    uint32_t bytes = bit_len / 8;
    if(bit_len % 8 != 0){
        bytes++;
    }
    fresh->vector = (uint8_t *) malloc(bytes);
    if(!fresh->vector){
        return NULL;
    }
    return fresh;
}

```

```
}
```

```
void bv_delete ( BitVector *v){  
    if(v){  
        if(v->vector){  
            free(v->vector);  
        }  
        free(v);  
    }  
}
```

```
uint32_t bv_get_len ( BitVector *v){  
    if(v){  
        return v->length;  
    }  
    return 0;  
}
```

```
void bv_set_bit ( BitVector *v, uint32_t i){  
    if(v && v->vector && i < v->length){  
        v->vector[i/8] |= 1 << (i%8);  
    }  
}
```

```
void bv_clr_bit ( BitVector *v, uint32_t i){  
    if(v && v->vector && i < v->length){  
        v->vector[i/8] &= ~(1 << (i%8));  
    }  
}
```

```
uint8_t bv_get_bit ( BitVector *v, uint32_t i){  
    if(v && v->vector && i < v->length){  
        uint8_t bit = v->vector[i/8] >> (i%8);  
        return bit%2;  
    }  
    return 2;  
}
```

```
void bv_set_all_bits ( BitVector *v){  
    if(v && v->vector && v->length > 0){  
        uint32_t bytes = ((v->length - 1)>>3) + 1;  
        for(int i = 0;i<bytes;i++){  
            v->vector[i] = 0xFF;  
        }  
    }  
}
```

```

    }
}
}

```

2) avoid memory leaks by deleting every created bitvector

3) Before the for loop, one can clear all even numbers larger than two with a different for loop. Then, in the main loop, replace $k++$ with $k+=2$. This is because $(\text{odd} * \text{odd} + \text{odd})$ is even, so we are doing twice as many bit clears as we should be.

Design of program

The program will have a Bit Vector struct implementation, the functions and their implementations can be found in Pre-Lab 2.1

The program will have a prime sieve up to a specified number N, This will be implemented as a sieve of eratosthenes

```

mark all numbers up to N
unmark 0,1
for every integer 2 to N, L
    if L is marked{
        unmark  $L * L + k * L$  where  $k = \{0,1,2,3..\}$  and  $L * L + k * L < N$ 
    }

```

By the end of this sieve all the marked numbers will be prime

The main function of this program will receive three flags through getopt()

```

-s
-p
-n <value>

```

-s means the program will print out all the primes up to N and if they are a fibonacci, Lucas, or Mersenne prime it will state so.

-p means the program will print the primes that are palindromic in base 2, 10, 14, 11

-n <value> make $N = \text{<value>}$, if this flag is absent then $N=100$;

In the main function, A bit vector is created with a length of N

The bit vector is passed to the sieve, which sets only the prime indexed elements

For each of the prime numbers left by the sieve, it is printed.

if -s is present, the primes are tested to see if they are Fibonacci, Lucas, or Mersenne primes, the pseudo code for this is found in Pre_Lab 1.1

if -p is present, the primes are tested to see if they are palindromes in base 2, 10, 14, 11, and then printed

The pseudo code to determine if a number is a palindrome in arbitrary bases is as follows

```

boolean Palindrome(int n, int base){
    int digits[(int)(ln(n)/ln(base))];
    for(int i = 0; i < digits.length; i++){ // fills array with digits
        digits[i] = n%base;
        n/=base;
    }
    for(int i = 0; i < digits.length/2; i++){ //tests if it is a palindrome
        if(digits[i] != digits[n-i-1])
            return false;
    }
    return true;
}

```

Design changes

After implementation, the only change to the design was to make a separate function that fills a bit vector with fibonacci numbers, one that fills a bit vector with lucas numbers, and a function that tests if a number is a predecessor to a power of two.