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Pre-Lab 1)

- 1) 5 rounds, the number of swaps it takes to bring the 5 to the beginning
- 2) $O(N^2)$, if the smallest element is at the end of the list

Pre-Lab 2)

- 1) Worst time complexity is $O(N^2)$, if gap is simply 1 then it is identical to bubble sort
- 2) By choosing a sequence of gaps which has either been proven to have a good time complexity, or has been empirically determined to be fast.

Pre-Lab 3)

- 1) Behavior depends on the pivot choice, if the chosen pivot partitions the array by about a half every time then the complexity is $O(N\log(N))$. For randomized input arrays, the pivot is expected to partition the arrays pretty evenly. If the pivot is chosen to be the midway element of the array, then inputting a sorted array will produce best case, rather than worst case, behavior. If the pivot is randomly chosen in the array, then the time complexity is almost always $O(N\log(N))$ for all inputs.

Pre-Lab 4)

- 1) Binary search has a time complexity of $O(\log(N))$, repeating this for every element means repeating it N times. This makes the complexity $O(N\log(N))$

Pre-Lab 5)

- 1) Make each sorting algorithm return an array of size 2 (it will really return a pointer) which holds the number of comparisons it made and the number of moves it made

Design of program

There will be a main function that accepts 8 different options, which may appear in any combination, or it may have no options at all. The options are

- b, employ bubble sort on an array
 sets bubble_flag to true;
- s, employ shell sort on an array
 sets shell_flag to true;
- q, employ quicksort on an array
 sets quick_flag to true;
- i, employ binary insertion sort on an array
 sets insertion_flag to true;
- A, the program will employ every sort
 sets bubble_flag to true;
 sets shell_flag to true;
 sets quick_flag to true;

sets insertion_flag to true;
 -p <value>, sets the number of elements to print to <value>, default is 100
 sets n to <value>, n is 100 initially
 -r <value>, sets the random seed to <value>, default is 8222022
 sets seed to <value>, seed is 8222022 initially
 -n <value>, sets the number of elements to <value>, default is 100
 sets c to <value>, c is 100 initially

An array of size c is initialized using

```
(uint32_t *)calloc(c,sizeof(uint32_t))
```

The random number generator from stdlib.h has its seed set using
 srand(seed)

The array is filled, each value is set to
 rand() & 0x3FFFFFFF

Then, for each sort with a true flag, the array is copied and passed to them to be sorted.

For each sort, it must return a pointer to an array of 2 integers where the first number is the number of comparisons, and the second number is the number of moves.

Those numbers will be printed, as well as the first n (set by -p flag) elements of the sorted array

The sorts are implemented in their own .c files and header files, the pseudo code for each is as follows

```

bubble_sort(int[] arr){
    int a = length(arr) -1;
    while(a>0){
        int b = a;
        a = 0;
        for(int i = 0;i<b;i++){
            if(arr[i] > arr[i +1]){
                swap arr[i], arr[i+1] //using xor swap
                a = i;
            }
        }
    }
}
  
```

```

shell_short(int[] arr){
    for(int gap = floor(5*length(arr)/11); gap>0;gap = floor(5*gap/11) ){
        for(int r = 0; r < gap; r ++){
            int a = length(arr) - gap + r;
  
```

```

        while(a>0){
            int b = a;
            a = 0;
            for(int i = r; i<b; i += gap){
                if(arr[i] > arr[i + gap]){
                    swap arr[i], arr[i+1] //using xor swap
                    a = i;
                }
            }
        }
    }
}

```

```

quick_sort(int[] arr){
    if(length(arr) < 2){
        return;
    }
    int left = 0;
    int right = length(arr) - 1;
    int[length(arr)] new;
    for(int i = 1; i<length(arr); i++){ //0th element is index
        if(arr[i] < arr[0]){
            new[left] = arr[i];
            left++;
        }else{
            new[right] = arr[i];
            right--;
        }
    }
    new[left] = arr[0]
    arr = new; //copy array, do not simply change direction of pointer arr
    if(left>1){
        leftarray = pointer to (0 to left) elements of arr;
        quick_sort(leftarray);
    }
    if(right < length(arr) - 2){
        rightarray = pointer to (right to length(arr)-1) elements of arr;
        quick_sort(rightarray);
    }
}

```

```

binary_insertion_sort(int[] arr){
    for(int i = 1; i < length(arr); i++){
        int left = 0;
        int right = i;
        while(left<right){
            mid = (left+right)/2
            if(arr[i]>=arr[mid])
                left = mid +1;
            else
                right= mid;
        }
        for(int j = i; j>left; j++)
            swap( arr[j], arr[j-1])
    }
}

```

```

merge_sort(int[] arr){
    leftarr = first half of arr
    rightarr = second half of arr
    merge_sort(leftarr);
    merge_sort(rightarr);

    int a = 0;//index for left arr
    int b = 0;//index for right arr
    int i = 0;//index for main array
    while(a<length(leftarr) && b<length(rightarr)){
        if(leftarr[a] < rightarr[b]){
            arr[i] = leftarr[a];
            a++;
        }else{
            arr[i] = rightarr[b];
            b++;
        }
        i++;
    }
    if(b == length(rightarr){ // we reached the end of the second array first
        while(i<length(arr){
            arr[i] = leftarr[a];
            i++;
            a++;
        }
    }
    //if we reached the end of the first array first, then nothing needs to be done
}

```

```
} //because the second array is already where it should be
```