



# InSAR training 2024

InSAR time series analysis: applications,  
background and theory



The background of the slide is a map of the San Francisco Bay Area. It is overlaid with a dense distribution of small, colored dots representing InSAR data points. The dots are color-coded, likely by phase or deformation magnitude, with a palette including red, orange, yellow, green, cyan, blue, and purple. Black lines on the map represent major geological features, such as the San Andreas Fault and other tectonic boundaries. The map shows the coastline of the bay and surrounding landmasses.

# Outline

Examples: time series InSAR of slow deformation in the San Francisco Bay Area and elsewhere

Persistent scatterer InSAR (PSI)

The small baseline subset (SBAS) method

# InSAR time series methods

These methods make use of multiple interferograms in order to constrain:

- Slow deformation processes (i.e. processes that are at or below the noise level in an individual interferogram)
- Time-variable processes

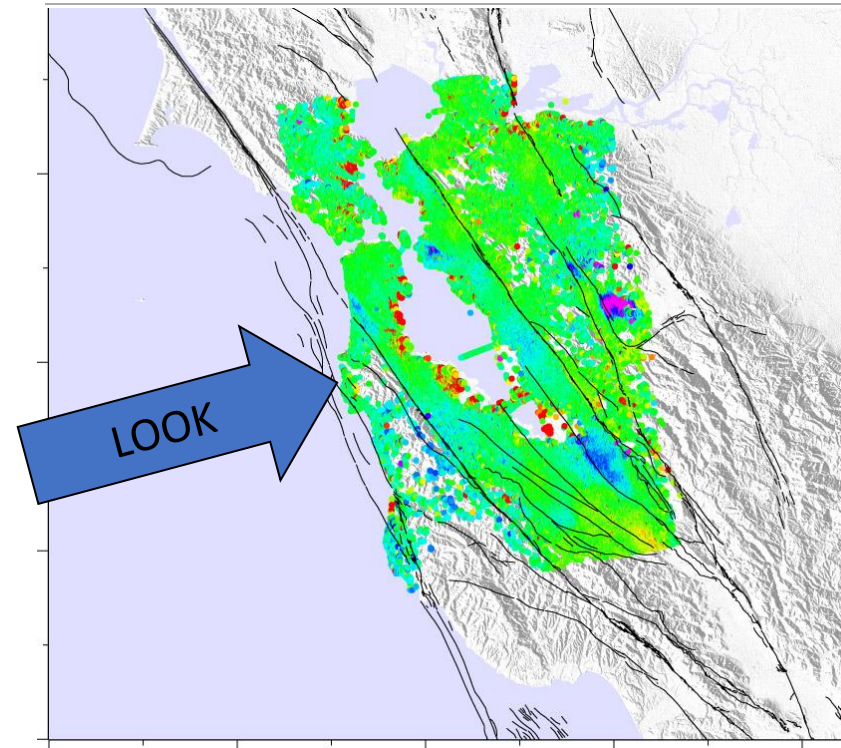
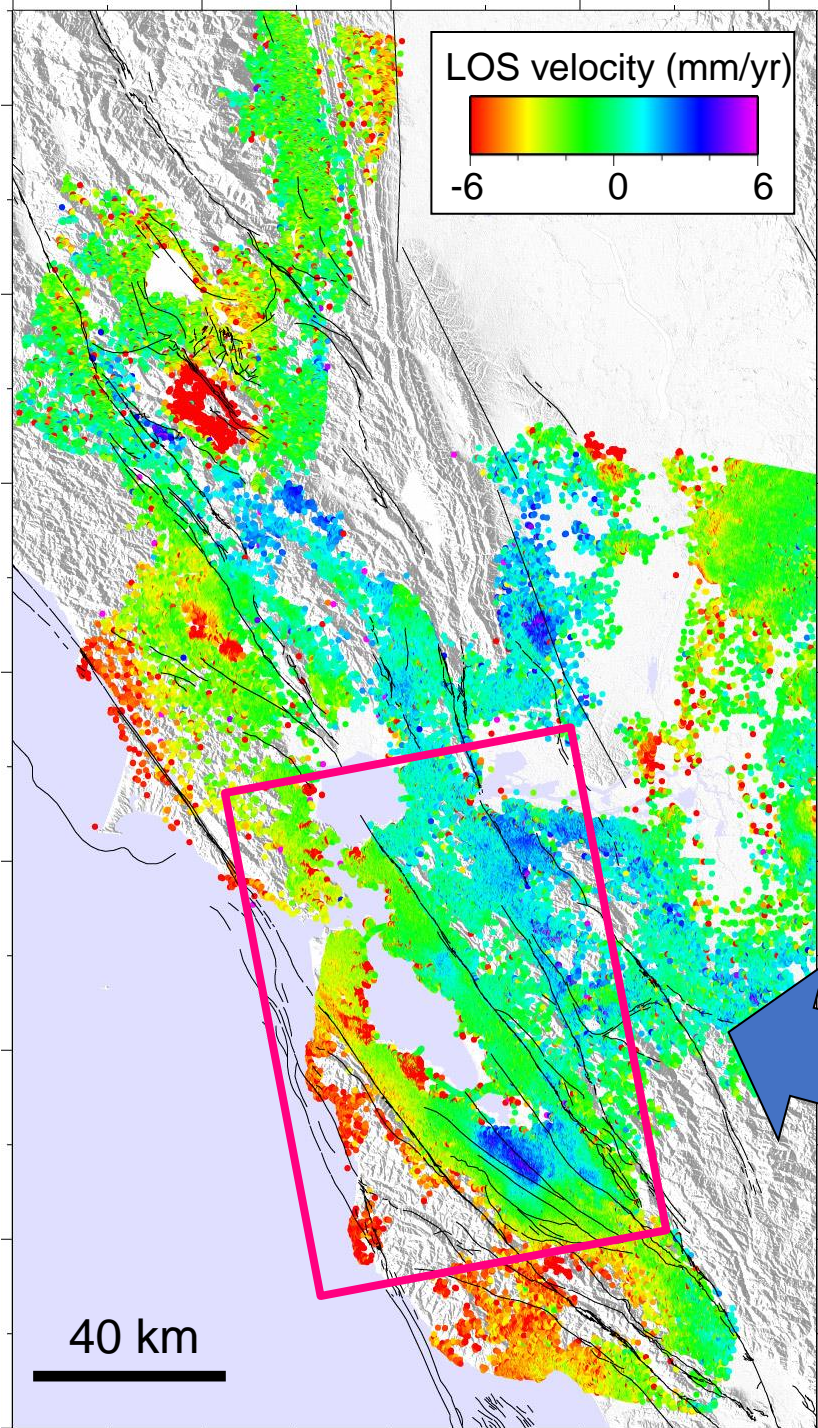
Time series methods typically make use of redundancy and/or temporal correlations in the data to maximize coherent pixels, extract deformation signals and mitigate noise



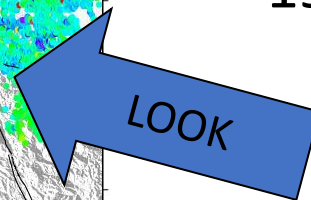
# Example: the San Francisco Bay Area





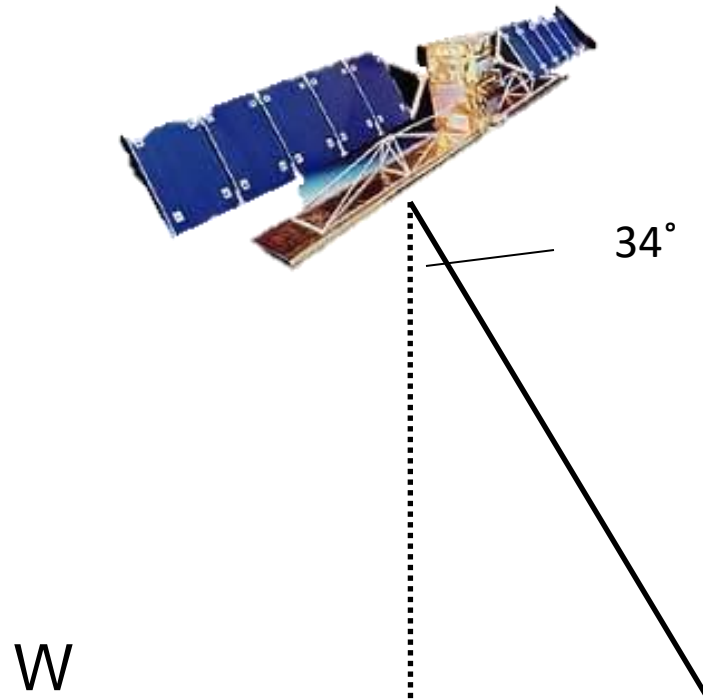


RADARSAT, track 38, beam S3  
1998–2006

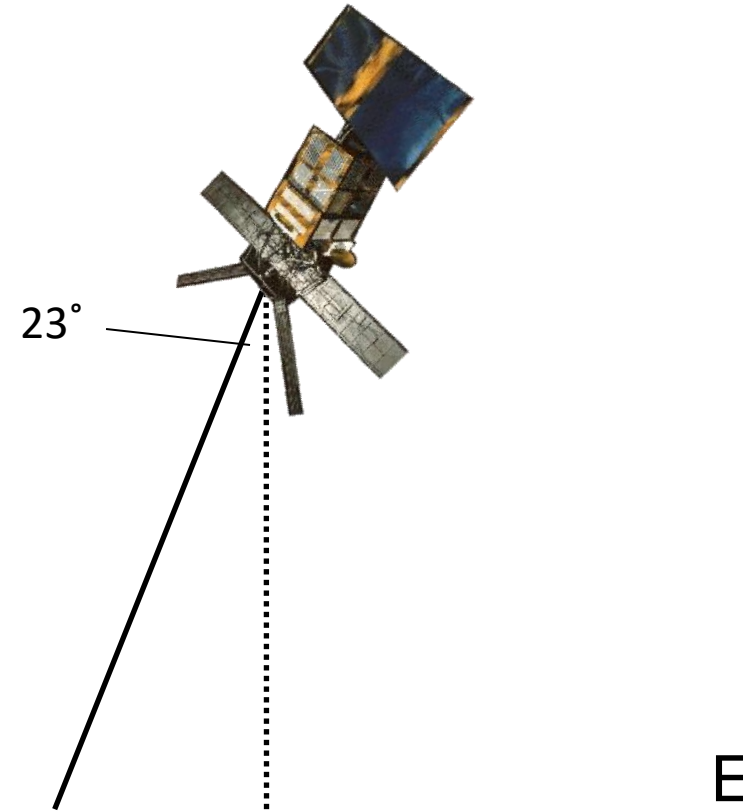


ERS, tracks 113, 342, 070  
1992–2000

RADARSAT ascending



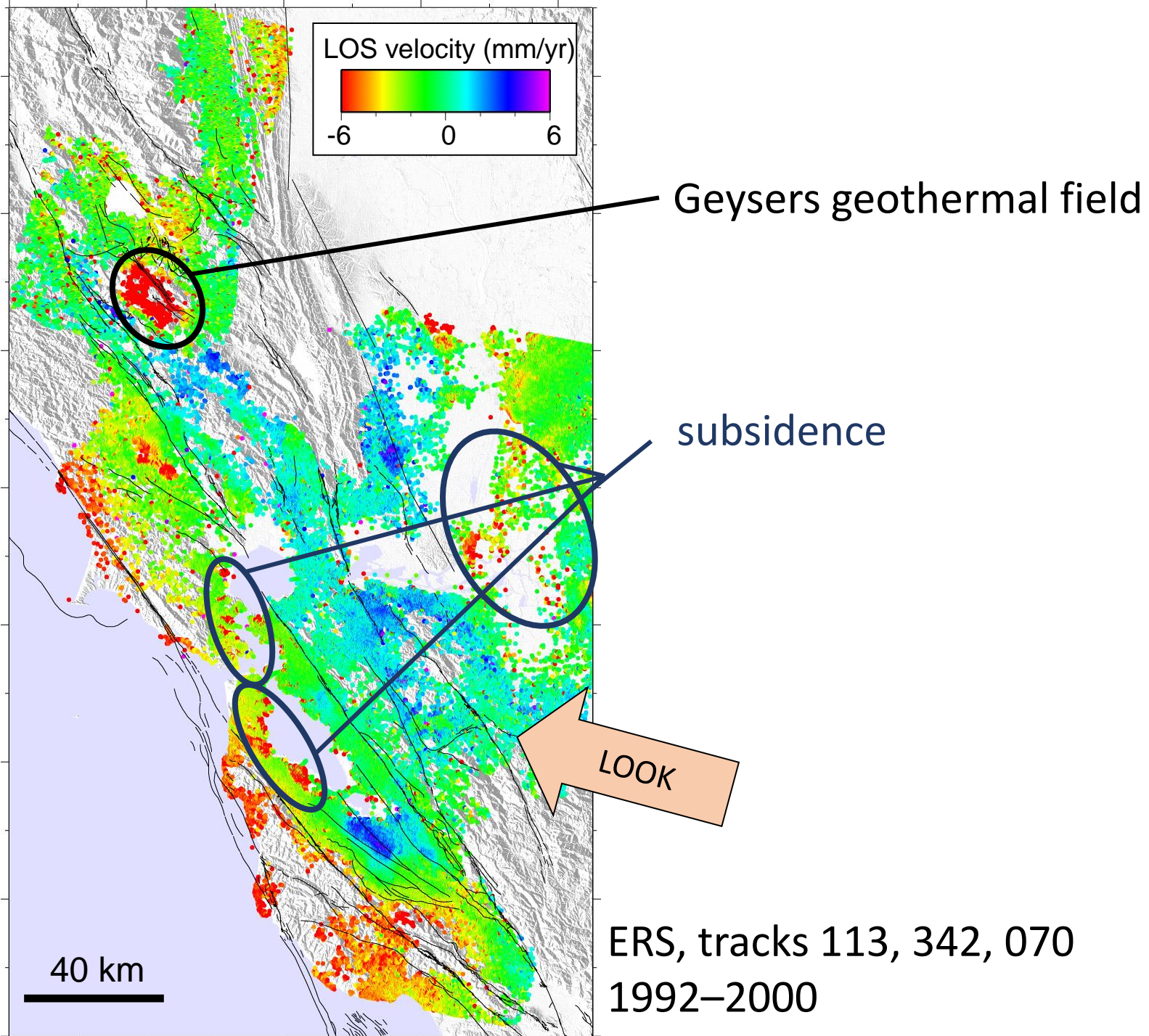
ERS descending



Deformation signals have same sign – vertical motion

Deformation signals have different signs – horizontal motion





# Subsidence at Treasure Island

Treasure Island is a man-made island, built in 1936/7



<http://walrus.wr.usgs.gov/geotech/treasureposter/treasure.html>



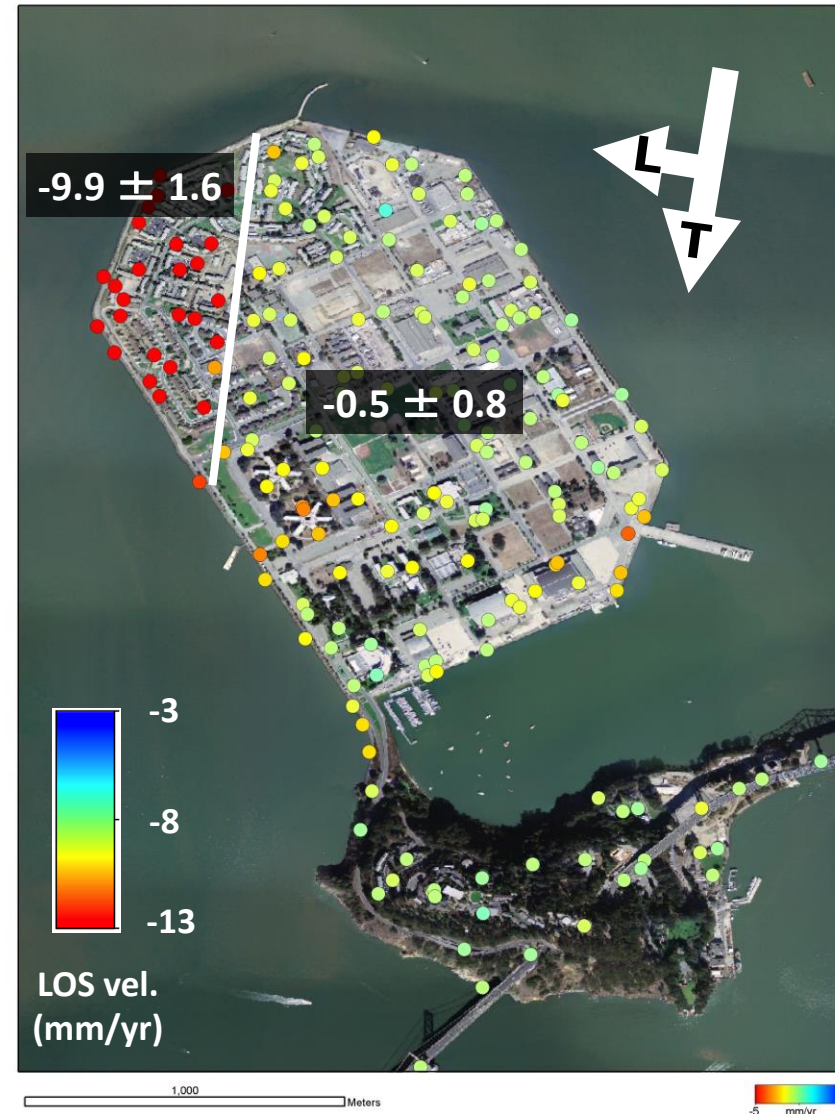
# Subsidence at Treasure Island

Calculate velocities of NW  
and central Treasure Island  
with respect to Yerba Buena

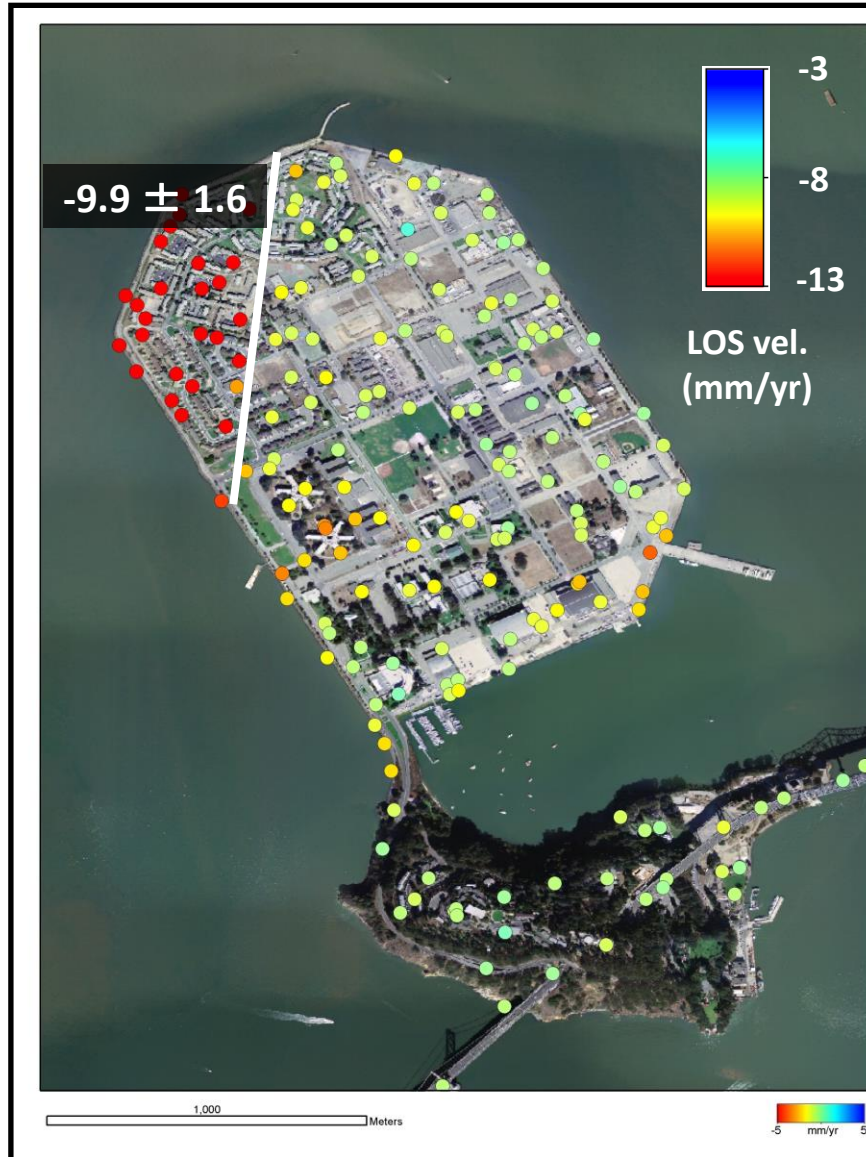
NW Treasure Island –  
significant high velocity

Central Treasure  
Island – stationary  
within error

ERS track 070 (1992-2000) velocities  
overlaid on 2004 airphoto



# Subsidence at Treasure Island

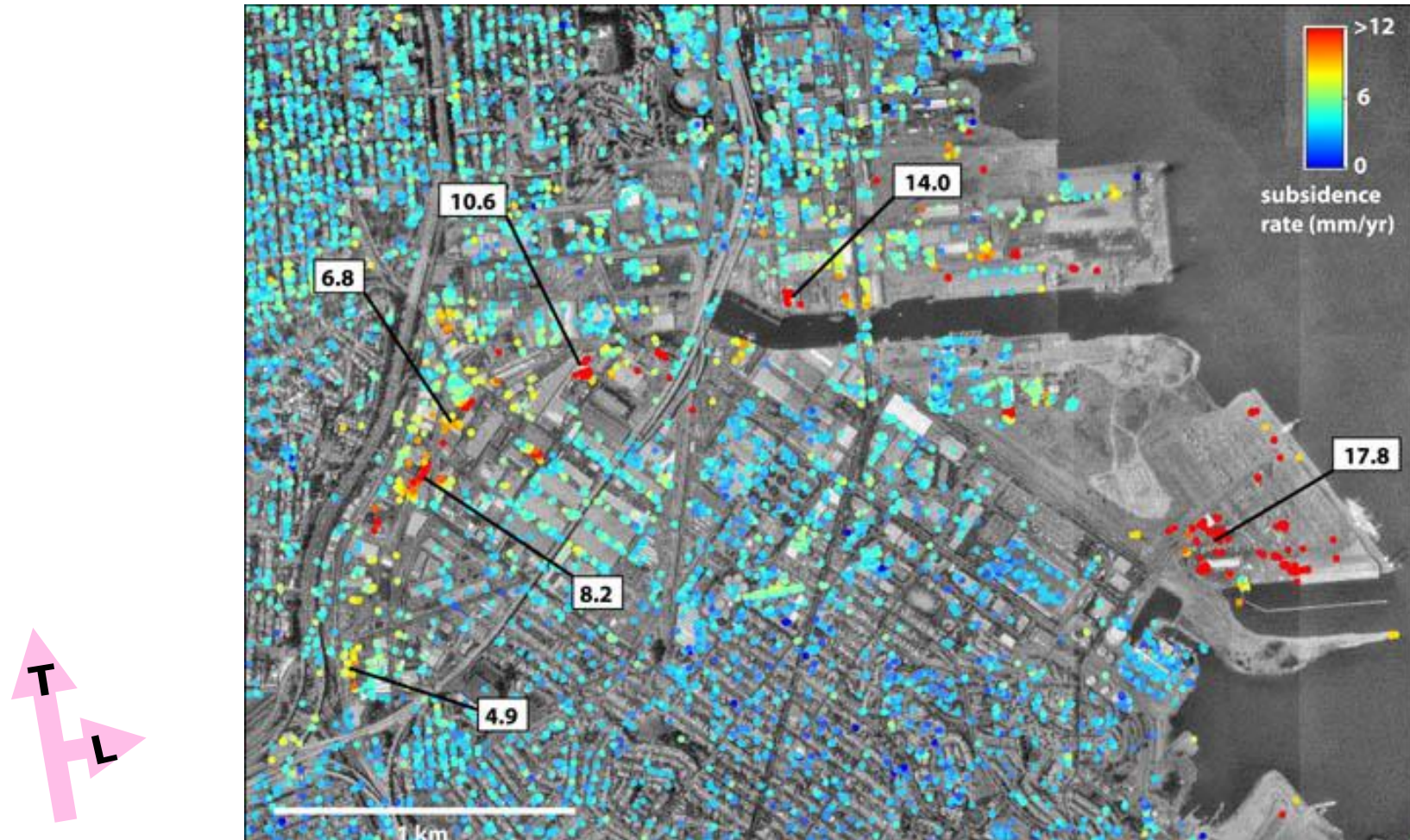


Region of greatest velocities  
correlates with thickest Bay  
mud on island (> 20 m)



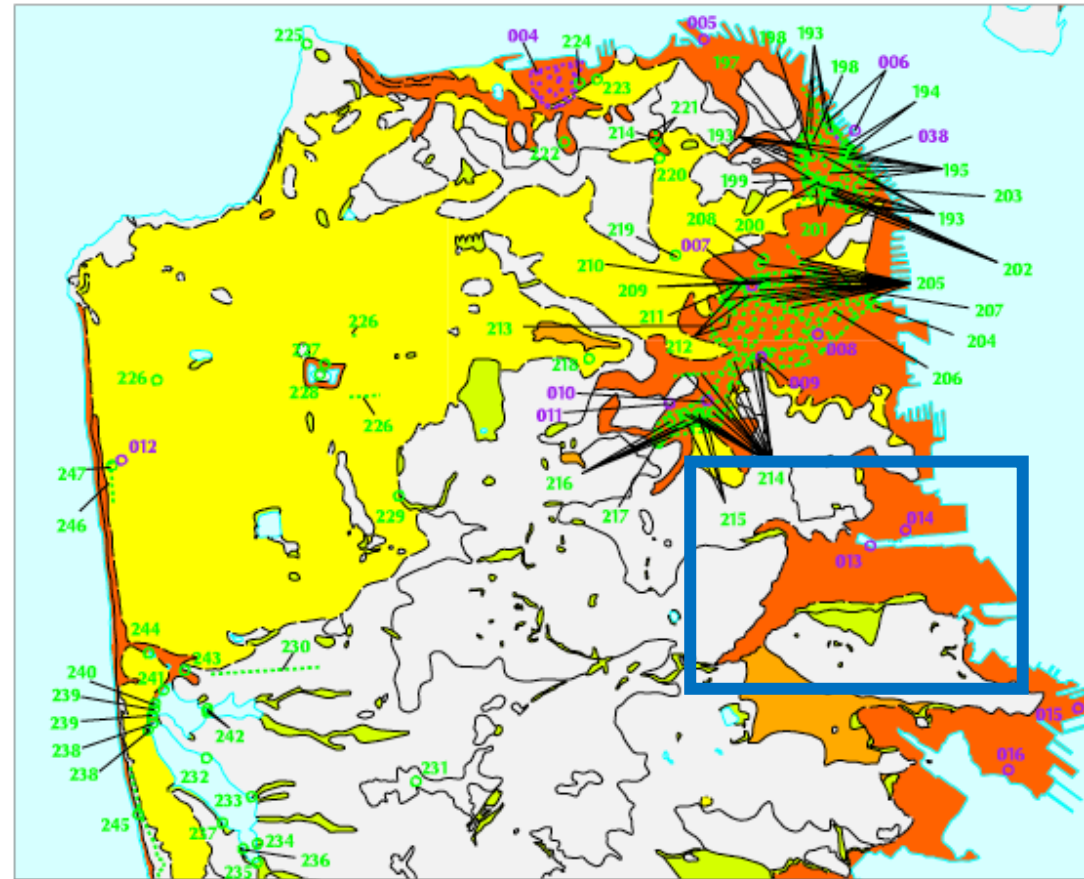
# Subsidence in San Francisco

High subsidence rates at the location of an old stream channel



# Subsidence in San Francisco

There is an excellent correlation between liquefaction risk and subsidence

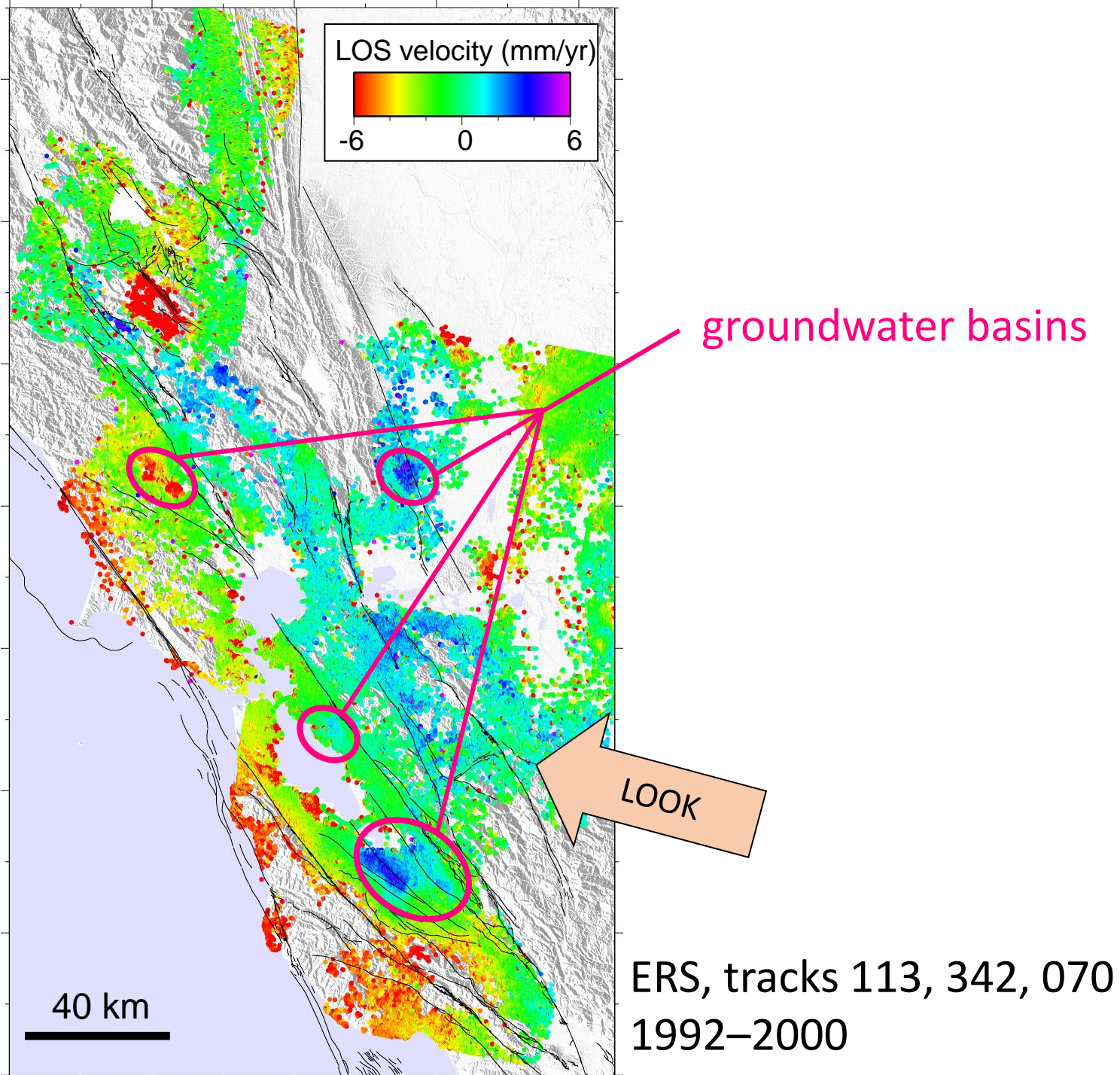


DETAIL OF SAN FRANCISCO AREA

MAP SCALE 1:100,000

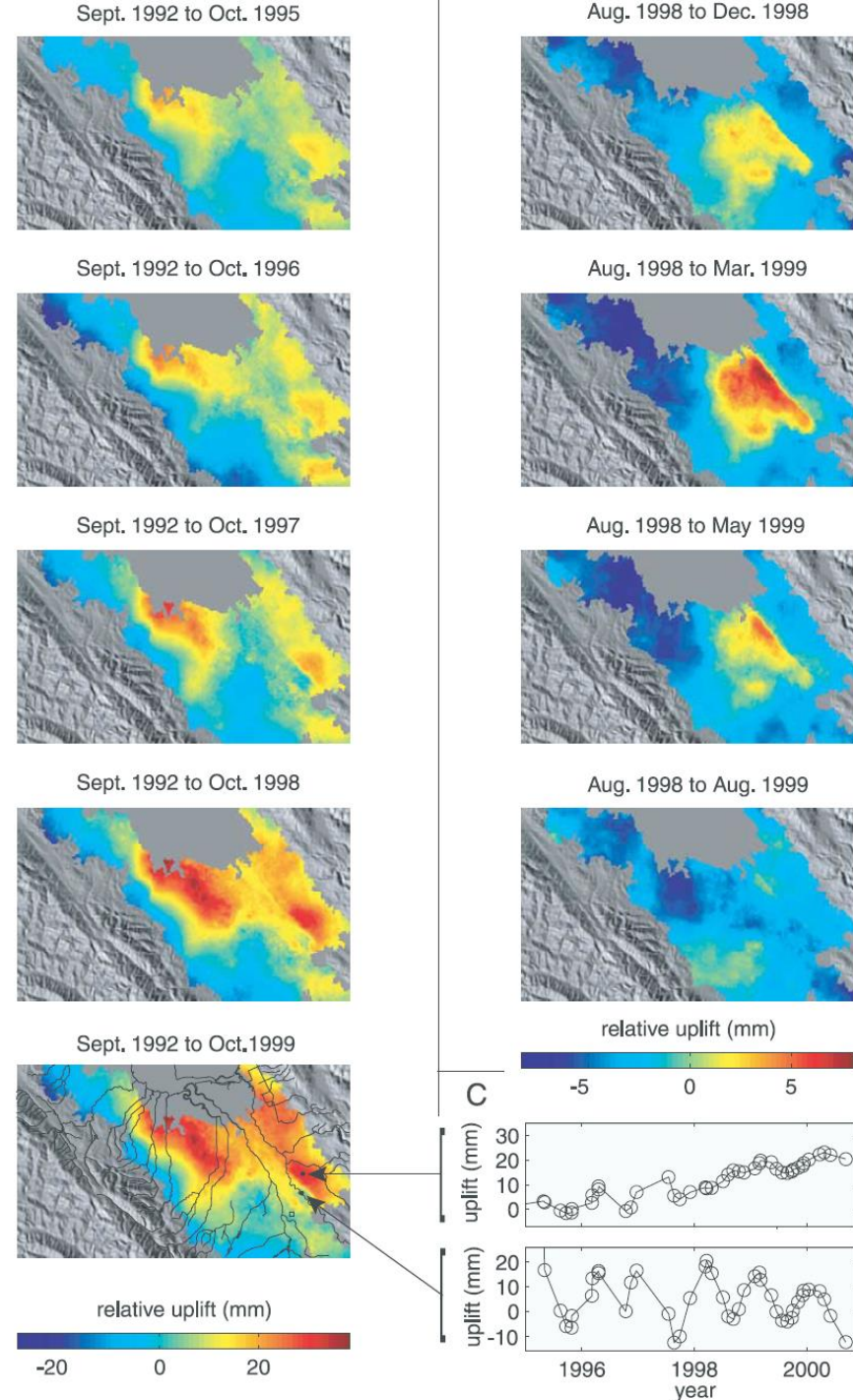






# The Santa Clara aquifer

Overall a pattern of increasing uplift,  
but there are large seasonal  
fluctuations (up in winter, down in  
summer)

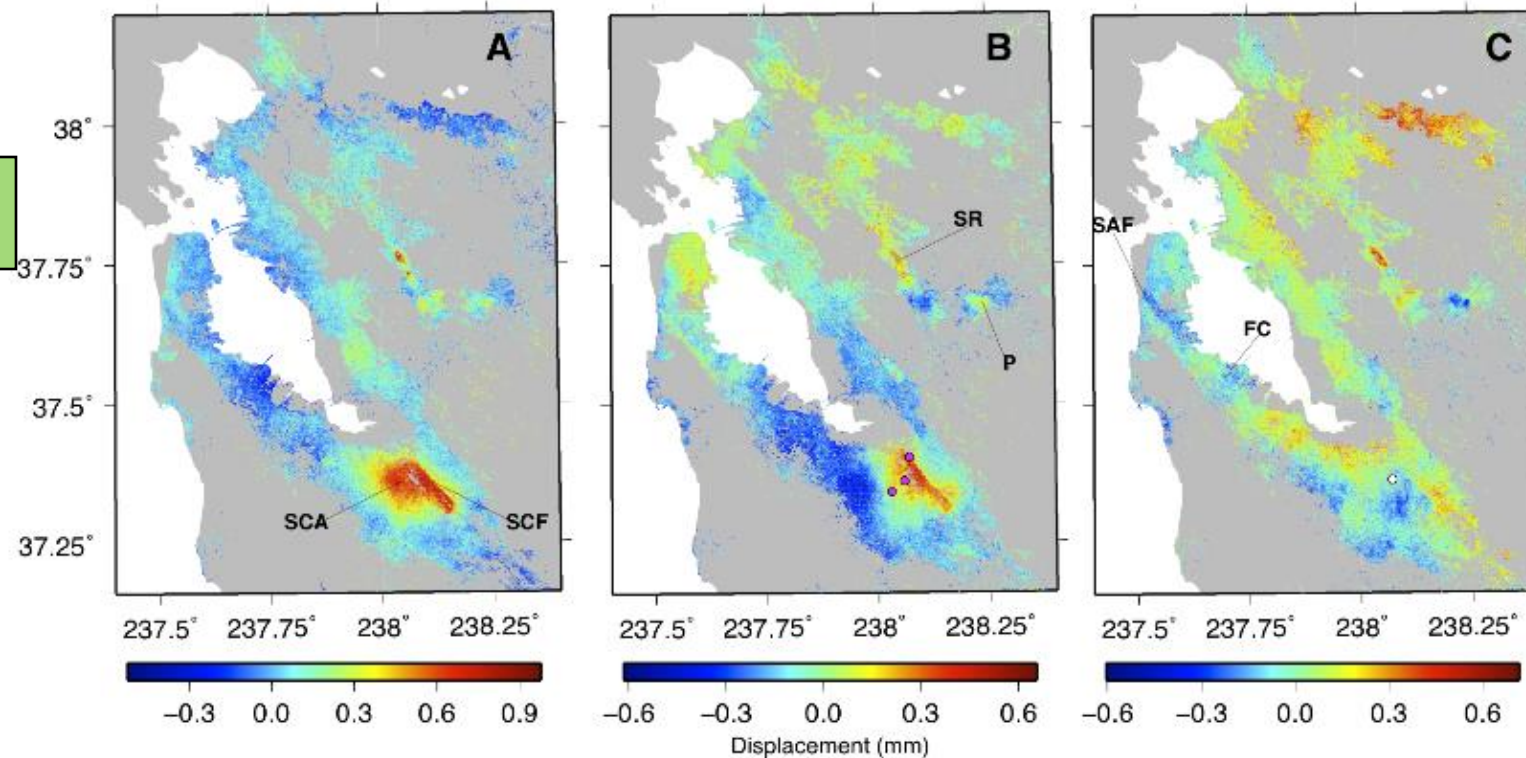




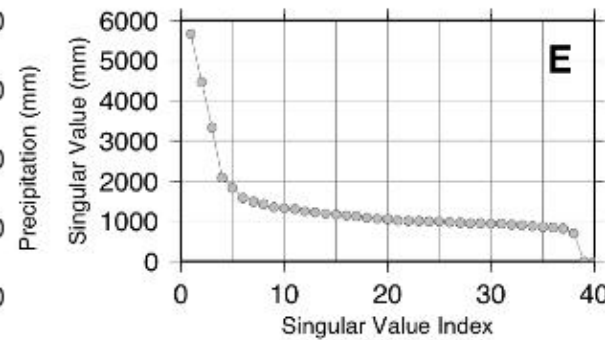
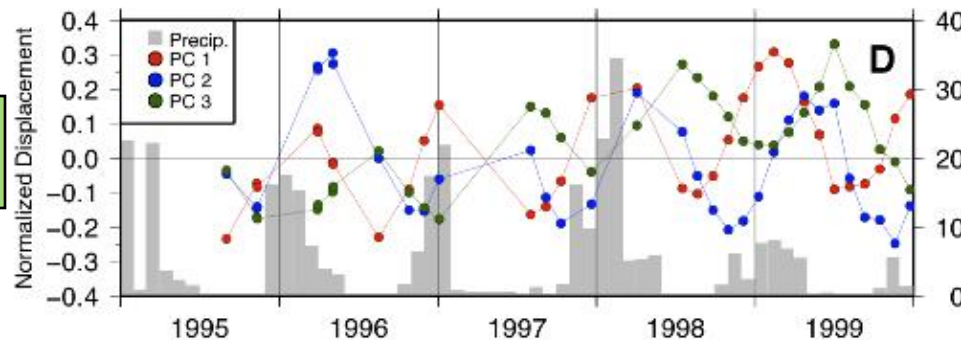
# Principal component analysis of InSAR time series

$$D = U(t) S V(x)^T$$

$V(x)$

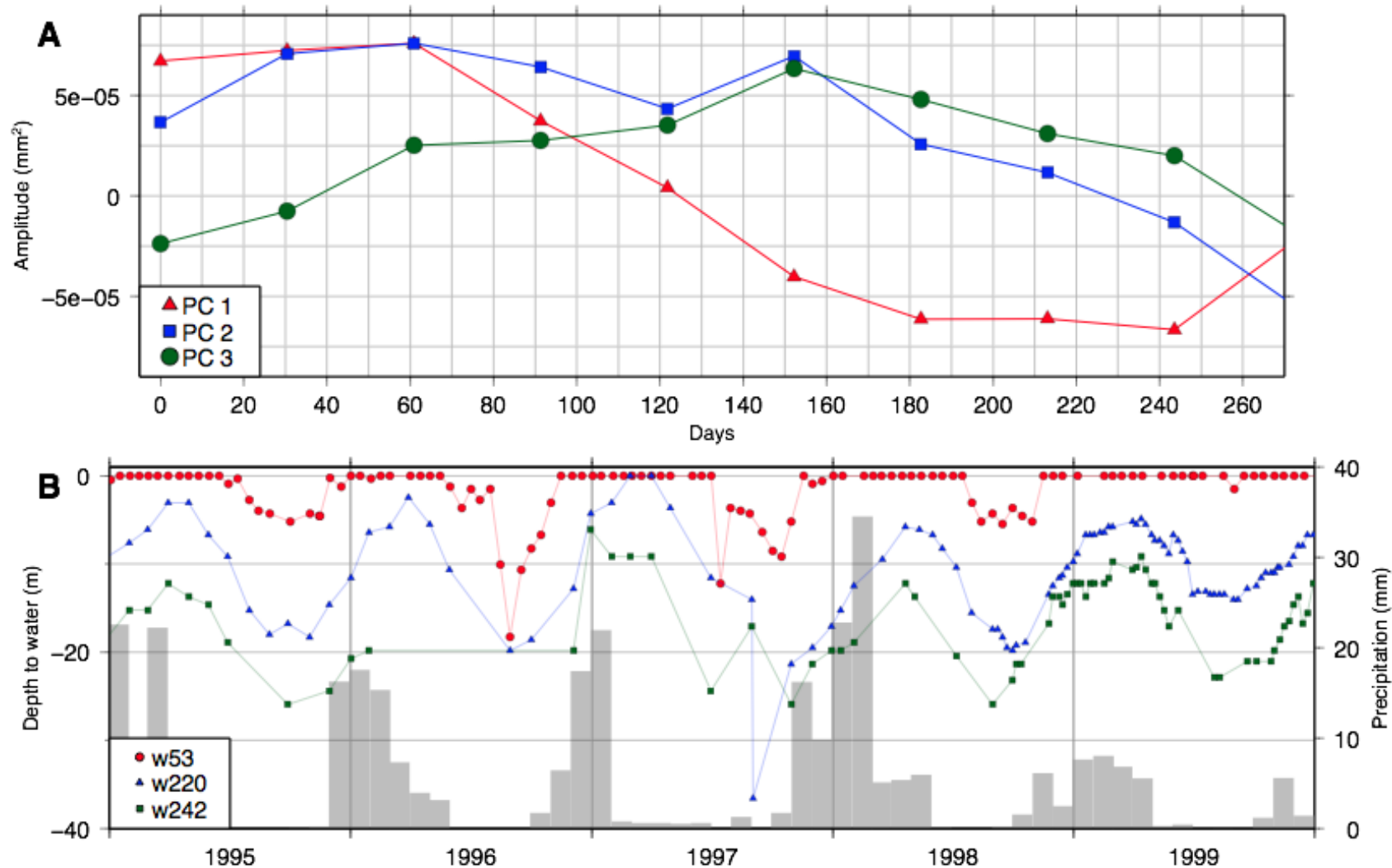


$U(t)$



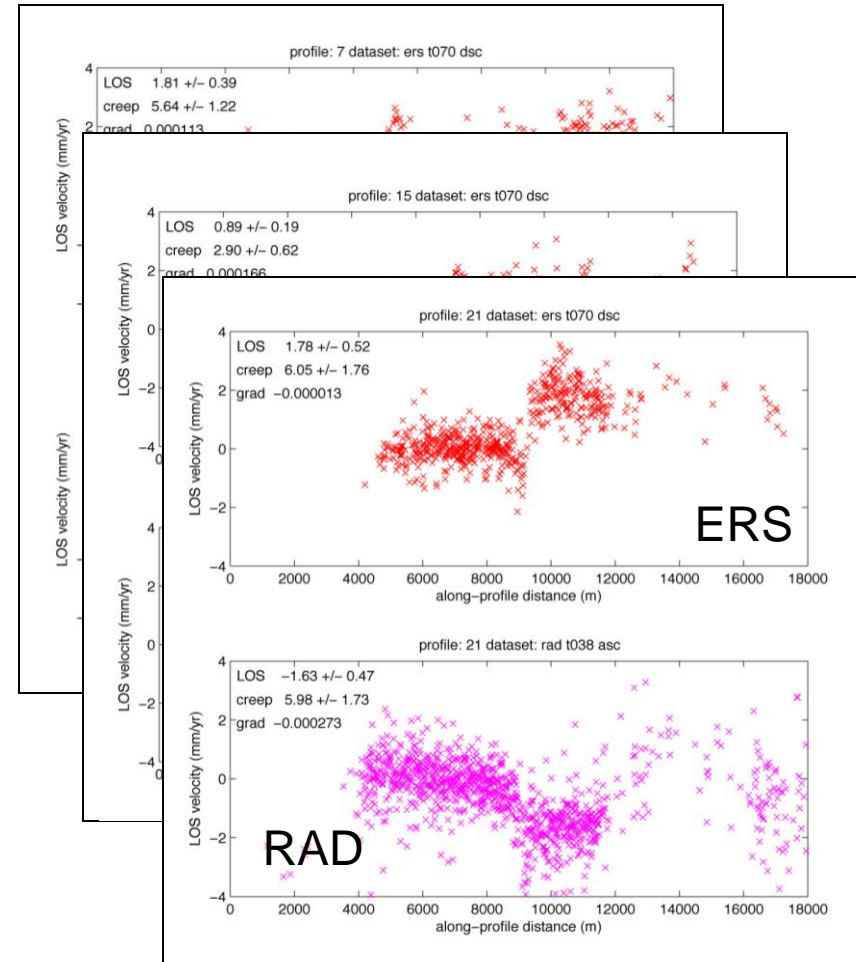
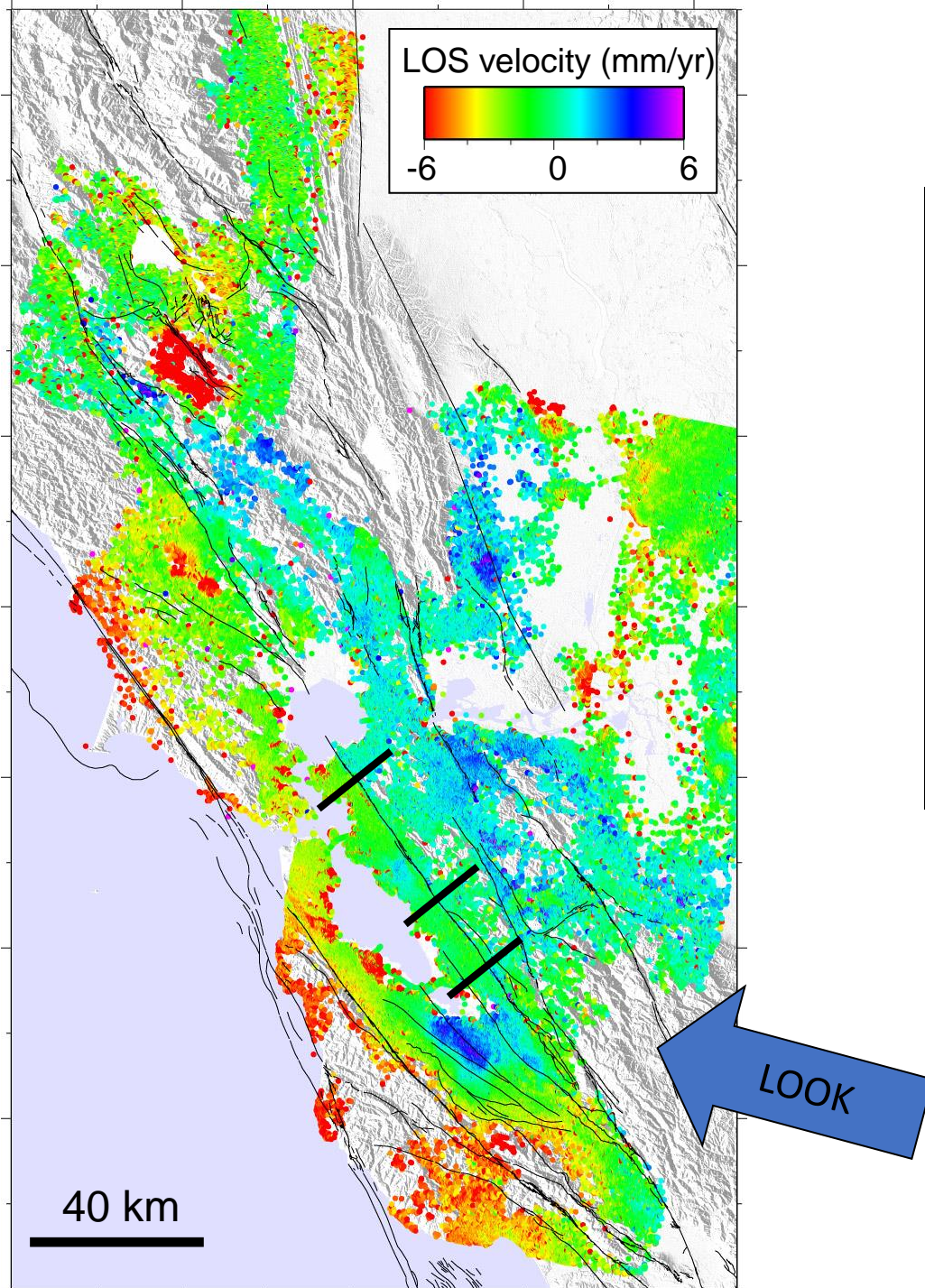
$S$

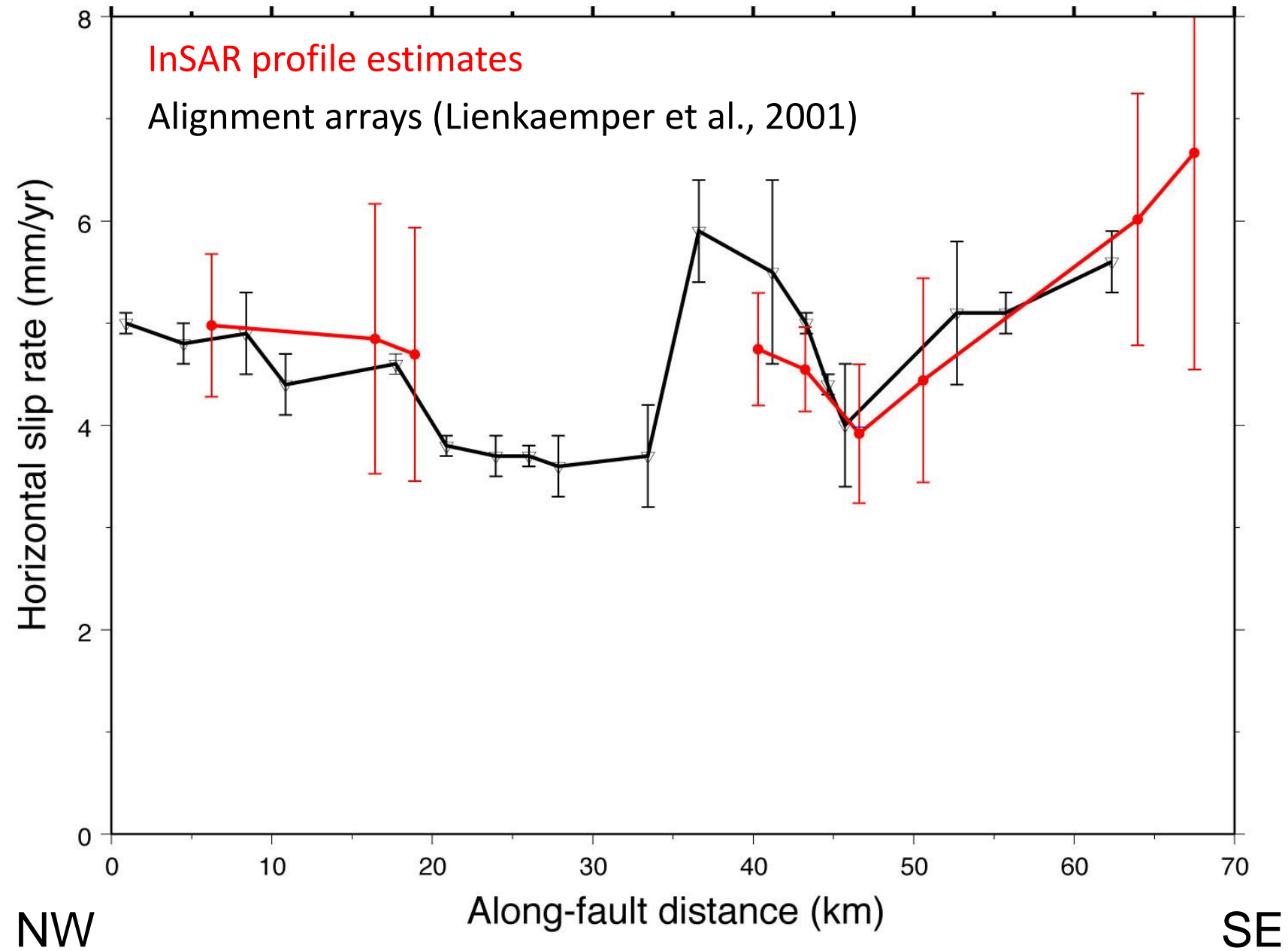
# Principal components can be tied to well and precipitation data





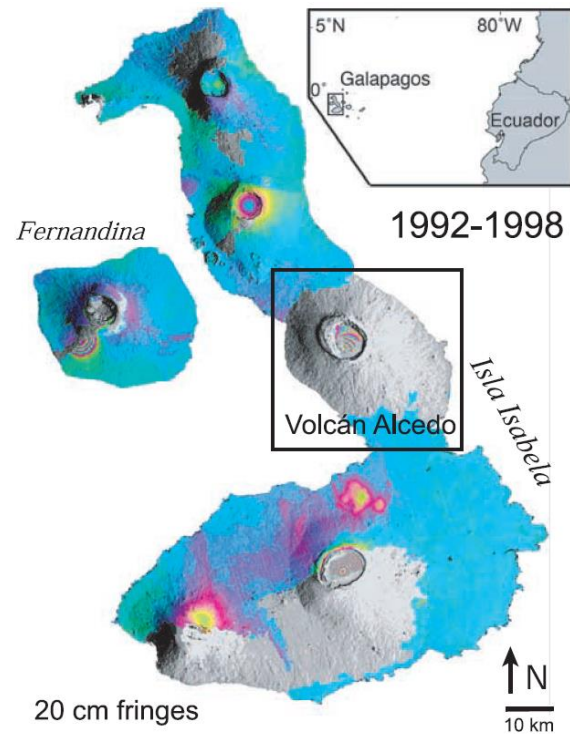
# Hayward fault creep



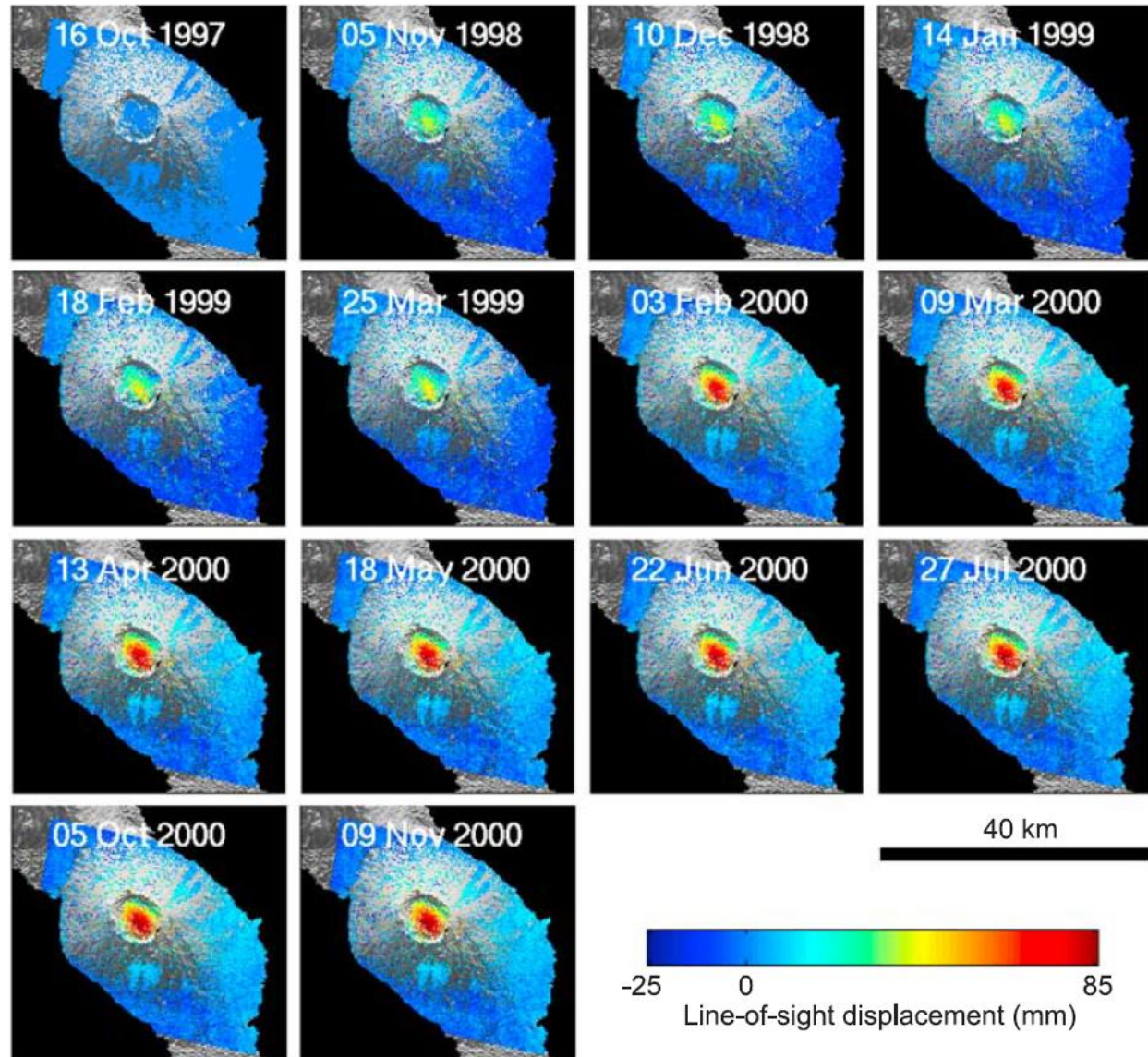




# Volcan Alcedo, Galapagos



Deflation/contraction  
in the caldera over  
three year period



# Persistent Scatterer InSAR

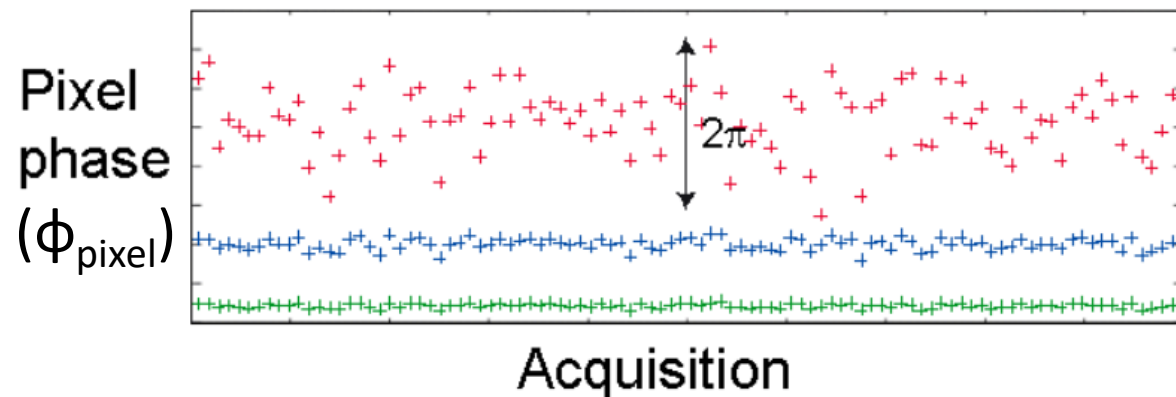
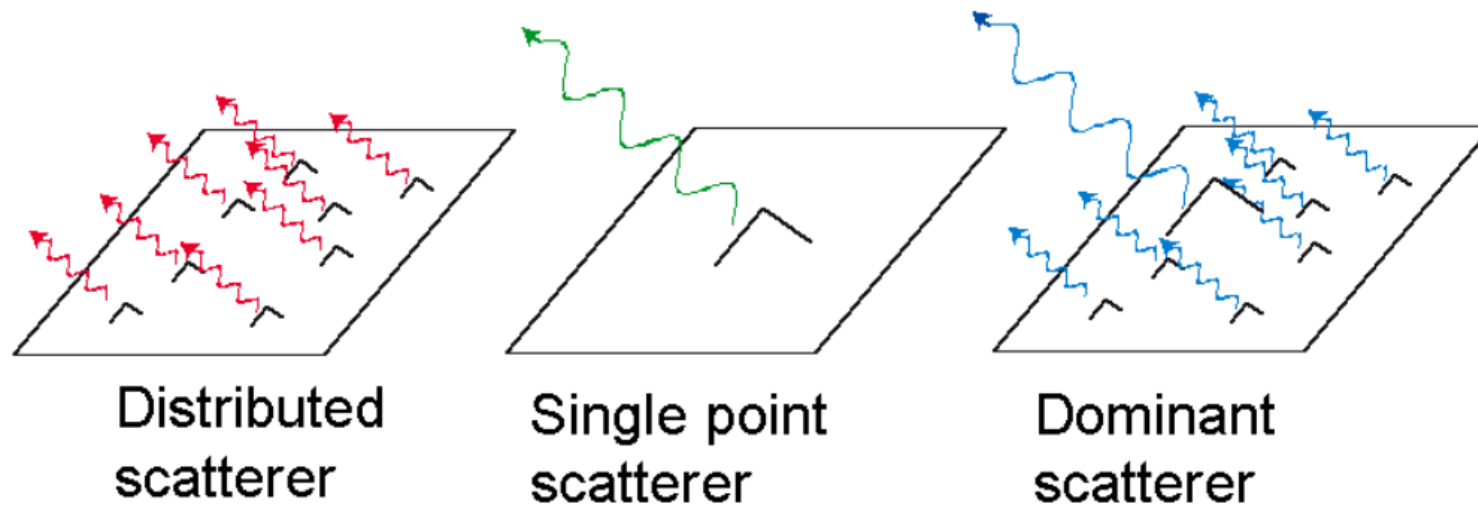
Persistent/Permanent Scatterer InSAR (PSI) offers a means to overcome these problems

- It relies on pixels that maintain coherence (hence the term 'persistent scatterer') and thus maximizes the number of observations
- It uses the idea that deformation signals are correlated over time...
- ...and that atmospheric signals are correlated in space, but uncorrelated in time, as a means of separating the two



# Characteristics of PS

PS are pixels with a single or dominant radar scatterer



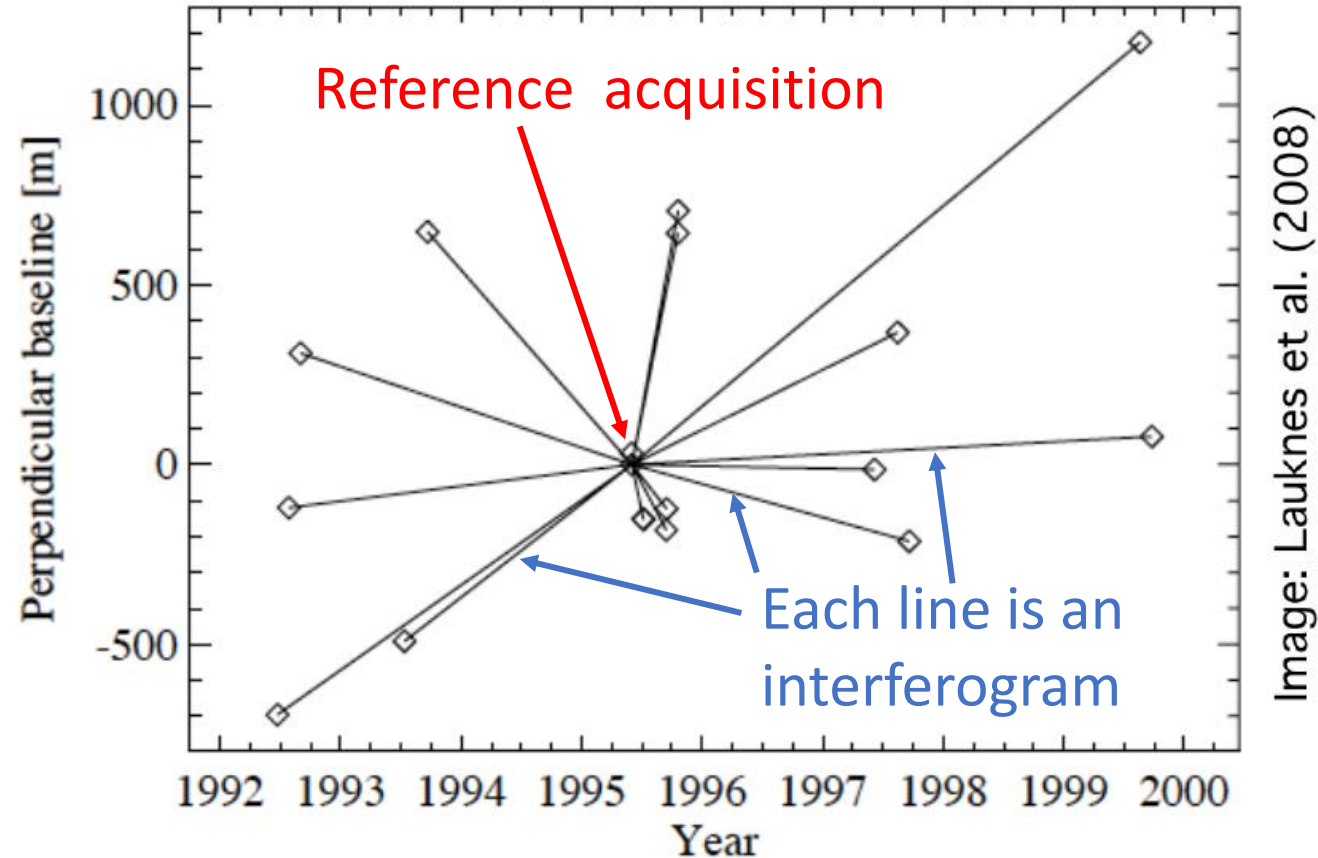
# PSI: the basics

- Typically need a minimum of 25 SAR images
- All images are coregistered; a multi-image amplitude map is made
- Interferograms are made with respect to a common reference (in the center of baseline/time space)
- PS candidates are selected on the basis of high, stable amplitude
- Phase of the PS candidates is used to estimate a best pixel height/velocity, considering pairs of points
- Atmospheric 'phase screen' estimated from residuals



# PSI: the basics

First, coregister every SAR image (SLC) to a common reference image (optimize for baseline and time span)

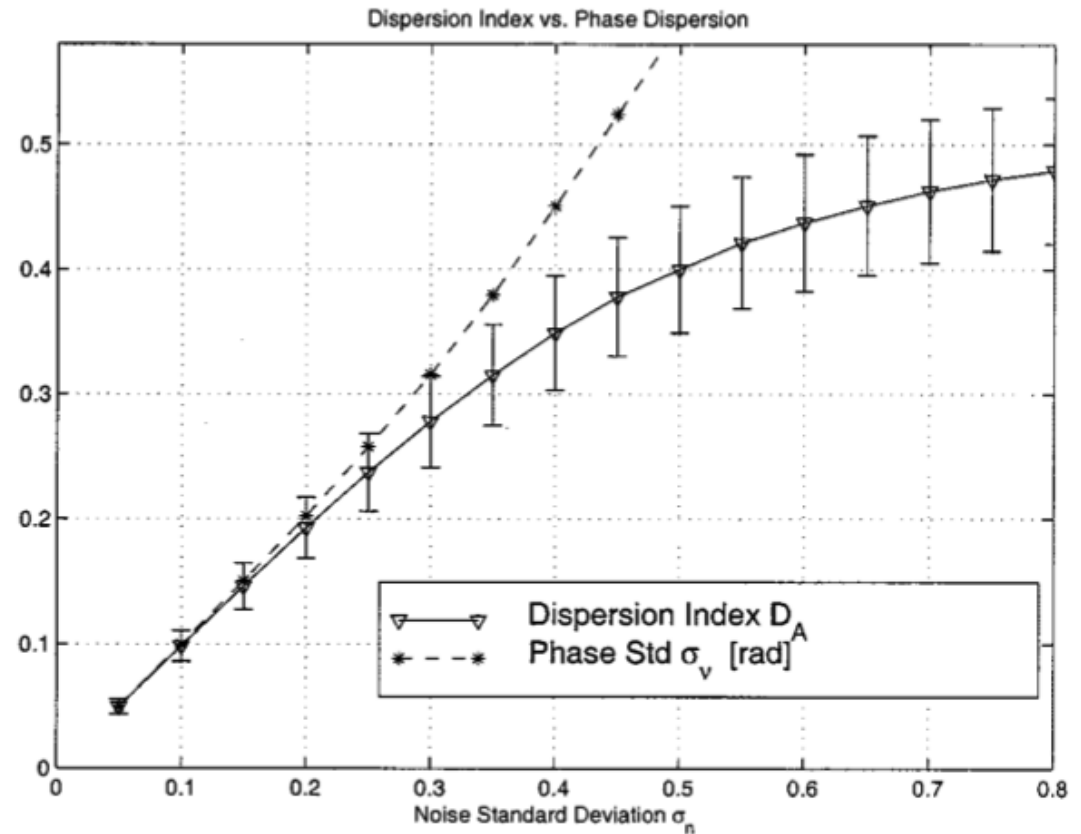


# PSI: the basics

Ferretti et al. (2001) showed that bright radar scatterers had consistent pixel phase over time

Amplitude dispersion,  $D$ , is a measure of amplitude variation

Phase std. dev. is a measure of phase variation

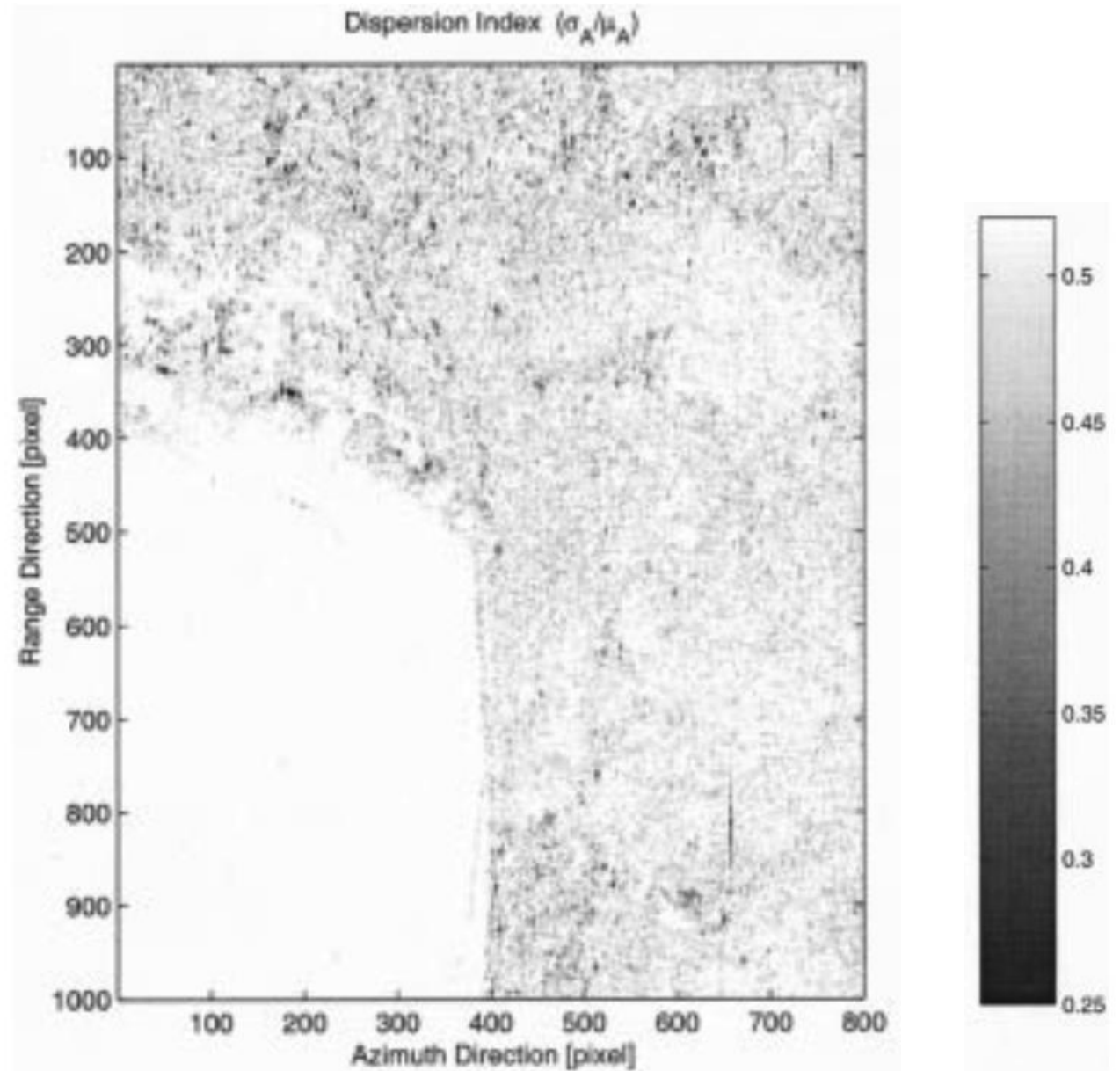




# PS candidates

Thus, the search for 'good' pixels is reduced to a (easier) search for consistently radar-bright (low dispersion) pixels

These are referred to as 'PS candidates'



# Phase-stable targets

Examples of the most common phase stable targets:



Roof

Dihedral  
(wall+ground)

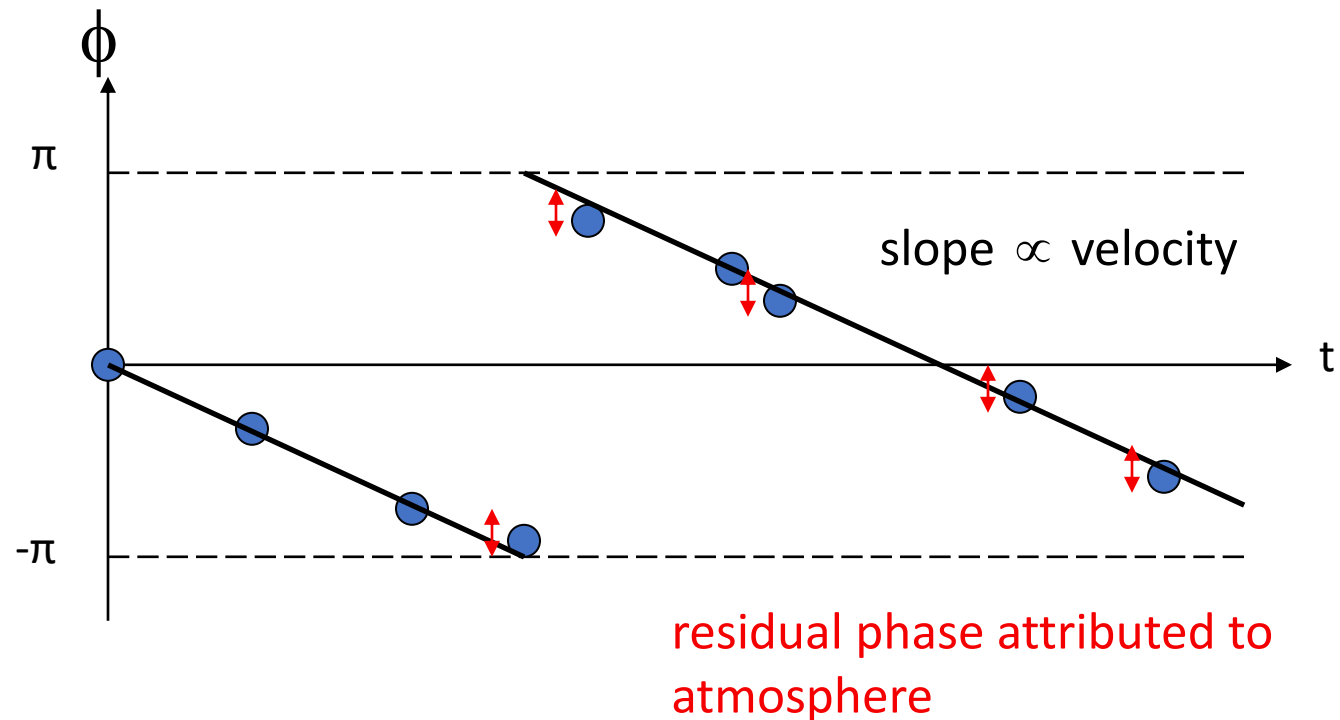
Pole

Trihedral (2  
walls+ground)



# Unwrapping in time

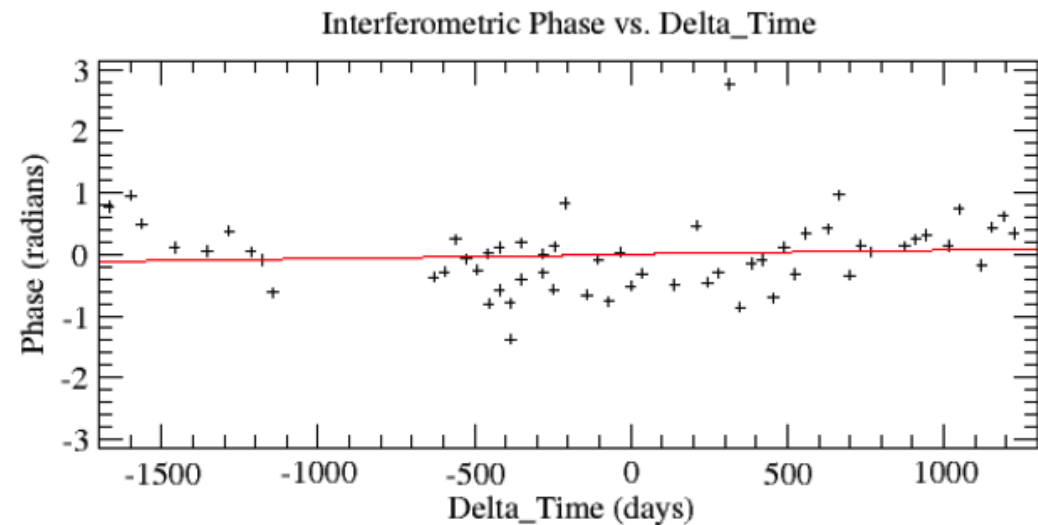
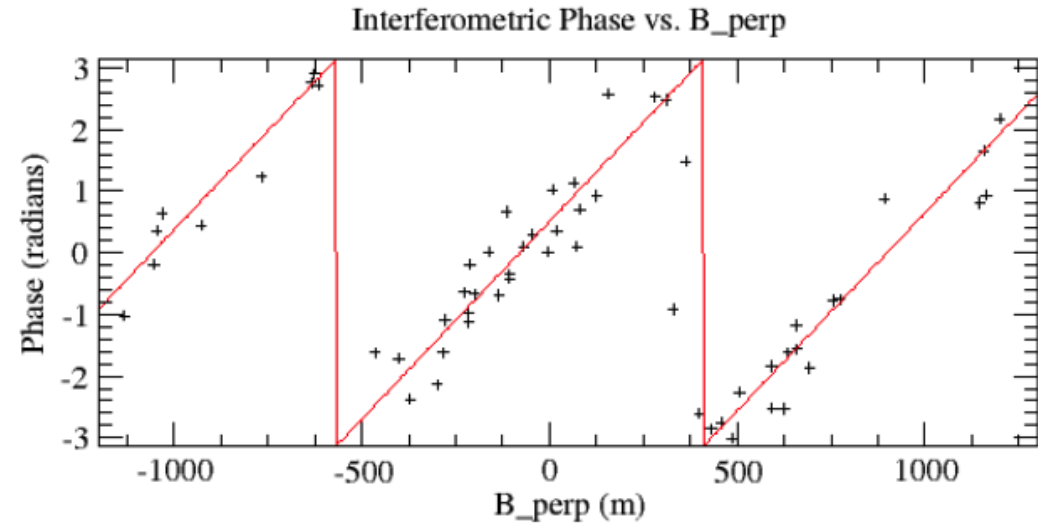
If we expect a particular behavior with time, we can unwrap the phase (and estimate the noise as whatever is left)



# Unwrapping the phase

In the Ferretti PS analysis,  
phase is unwrapped in time

The relative phase for a pair of points is unwrapped by finding the combination of scatterer height and velocity that best fits the wrapped time/baseline series

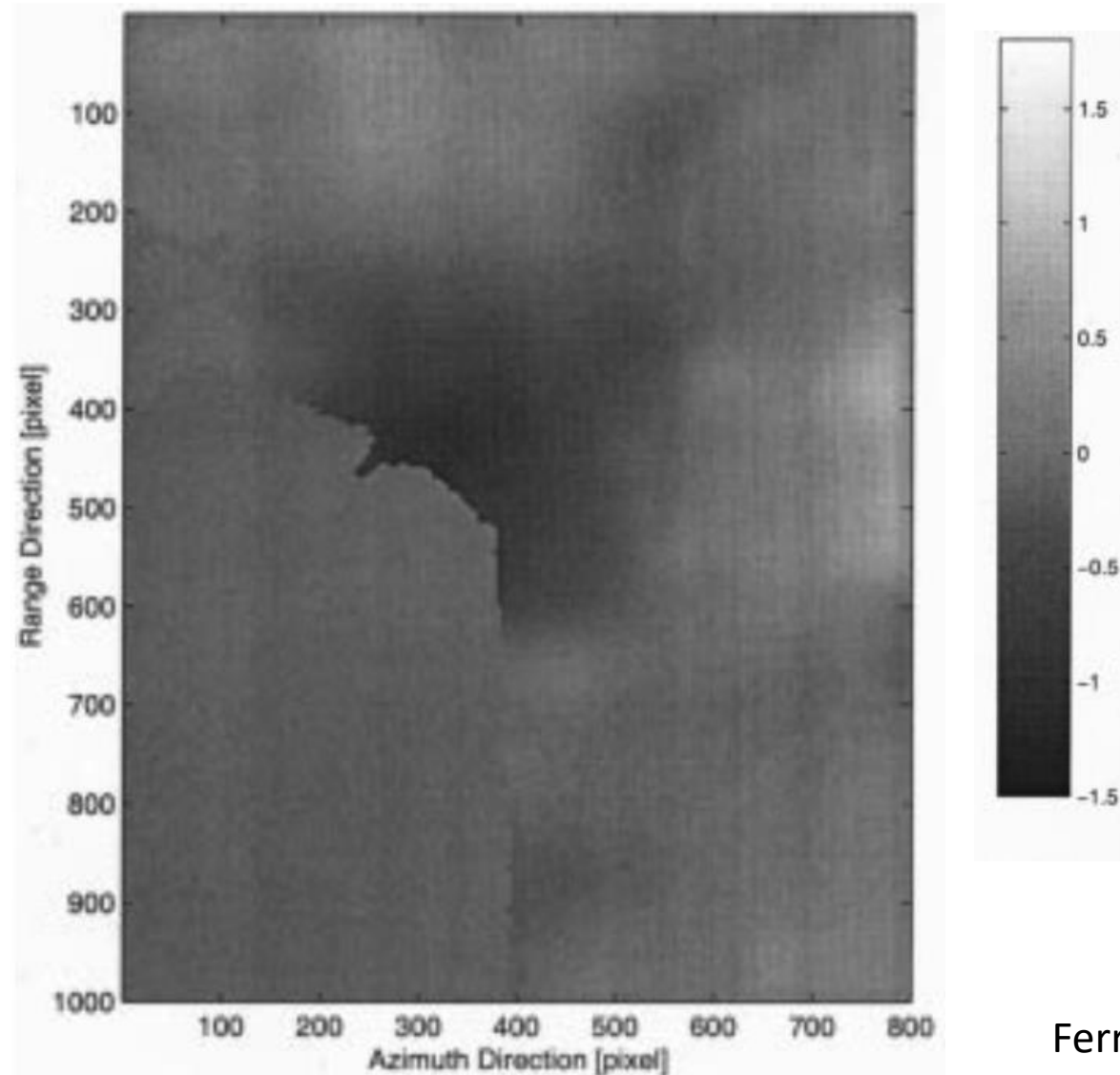


# The atmospheric phase screen

The APS is made by kriging (interpolating) the residuals to the velocity/height fit for each epoch

It is a prediction of the atmospheric phase in a given interferogram

Such estimates can be subtracted from all interferograms

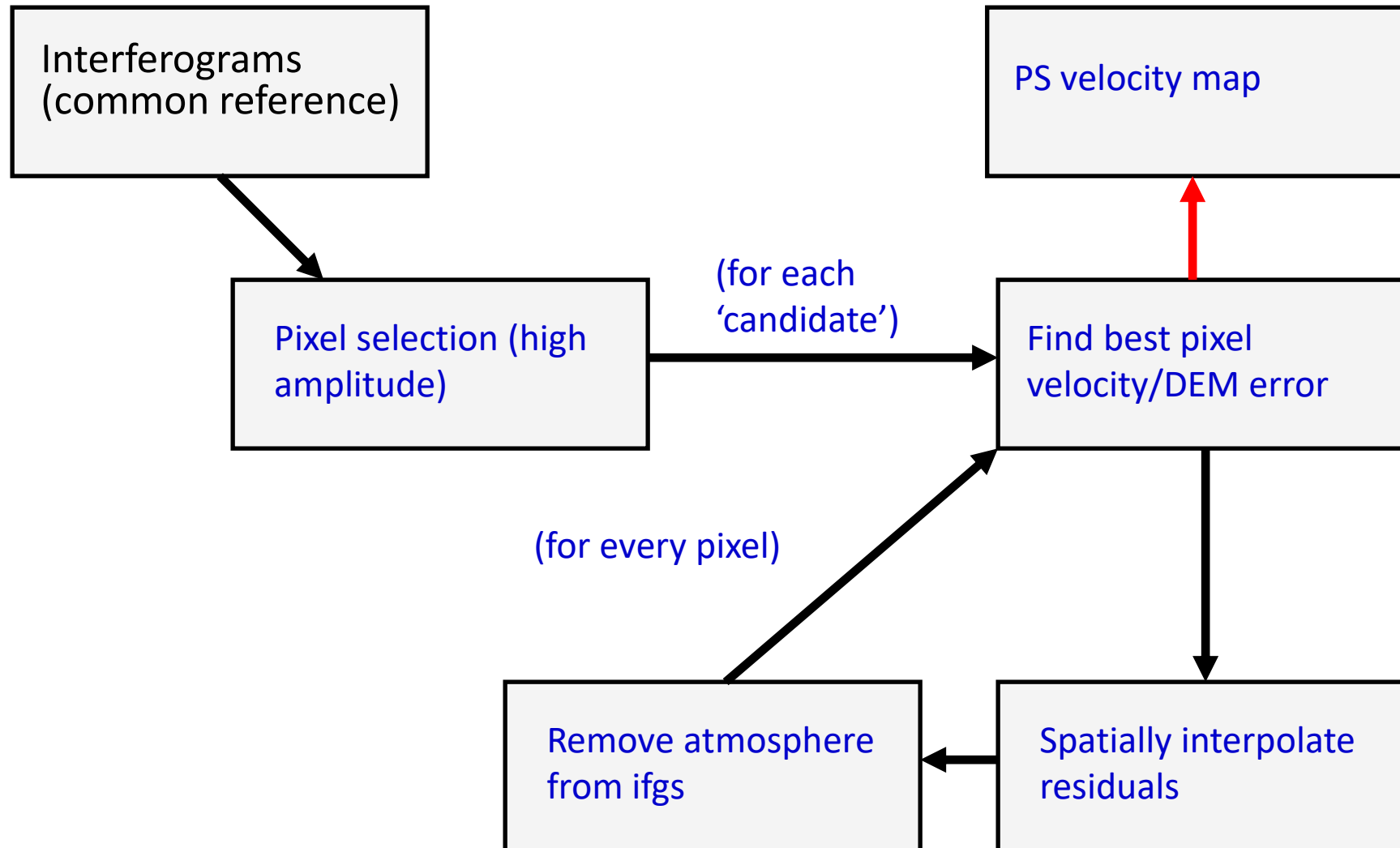




# PSI: step two

- Atmospheric phase screens subtracted from all interferograms
- Velocity/scatterer height estimation repeated for every single pixel (not just the high amplitude ones)
- Pixels with phase stability within a specified threshold are considered permanent scatterers (PS)
- Typically get 100-1000x more PS than PS candidates

# PSI methodology



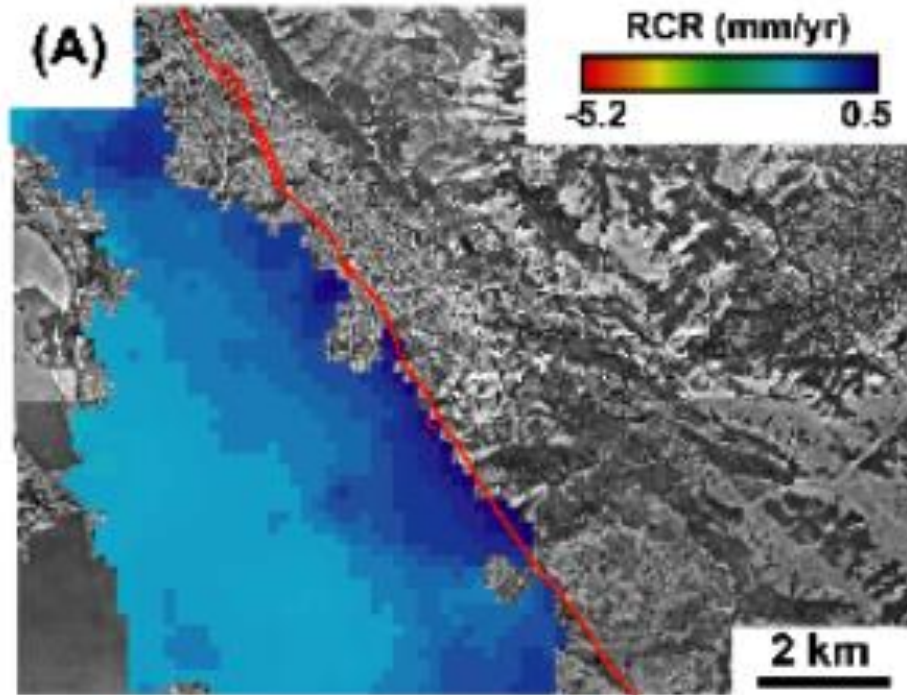
# Advantages of PSI

- Mitigates effect of atmospheric noise on data  
=> High precision in velocity estimates
- Maximizes number of observations with time
- As a scatterer is often smaller than a full SAR pixel, can increase the range of useable baselines (important for legacy satellites, not so important now)
- Does not require stable pixels to be adjacent to each other – each pixel can be identified independently

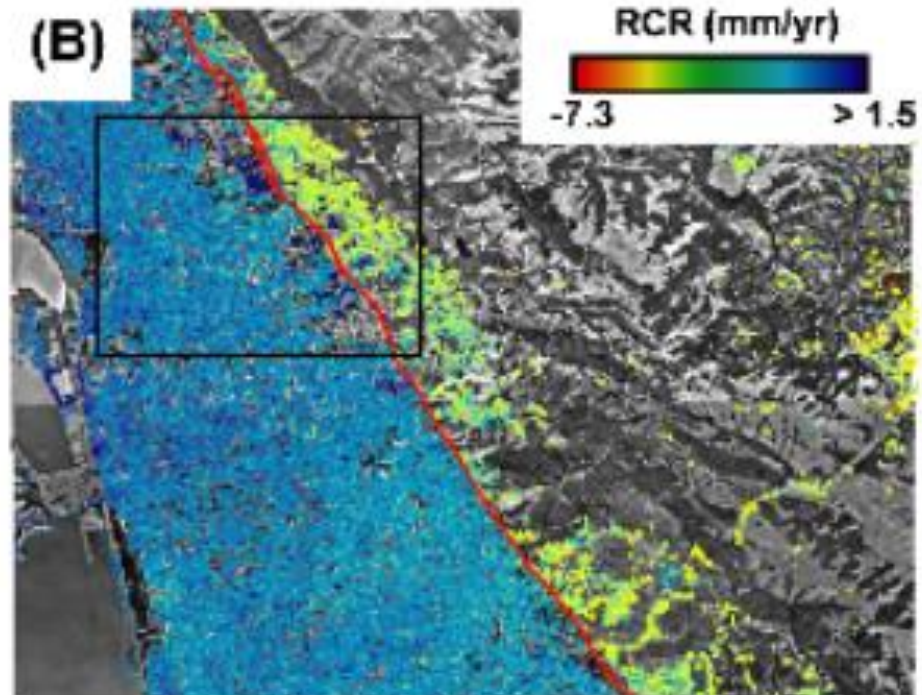


# More coverage in vegetated areas

Interferogram stack  
(Schmidt et al., 2005)



PSI



PSI gives better coverage in the heavily vegetated East Bay Hills

# But is it overkill?

PSI is very successful at recovering detailed information, especially in areas where InSAR is marginal, but it is very computationally expensive

- It assumes that each pixel is independent, but we know that most signals of interest are correlated spatially
- It does not make use of spatial unwrapping

# SBAS

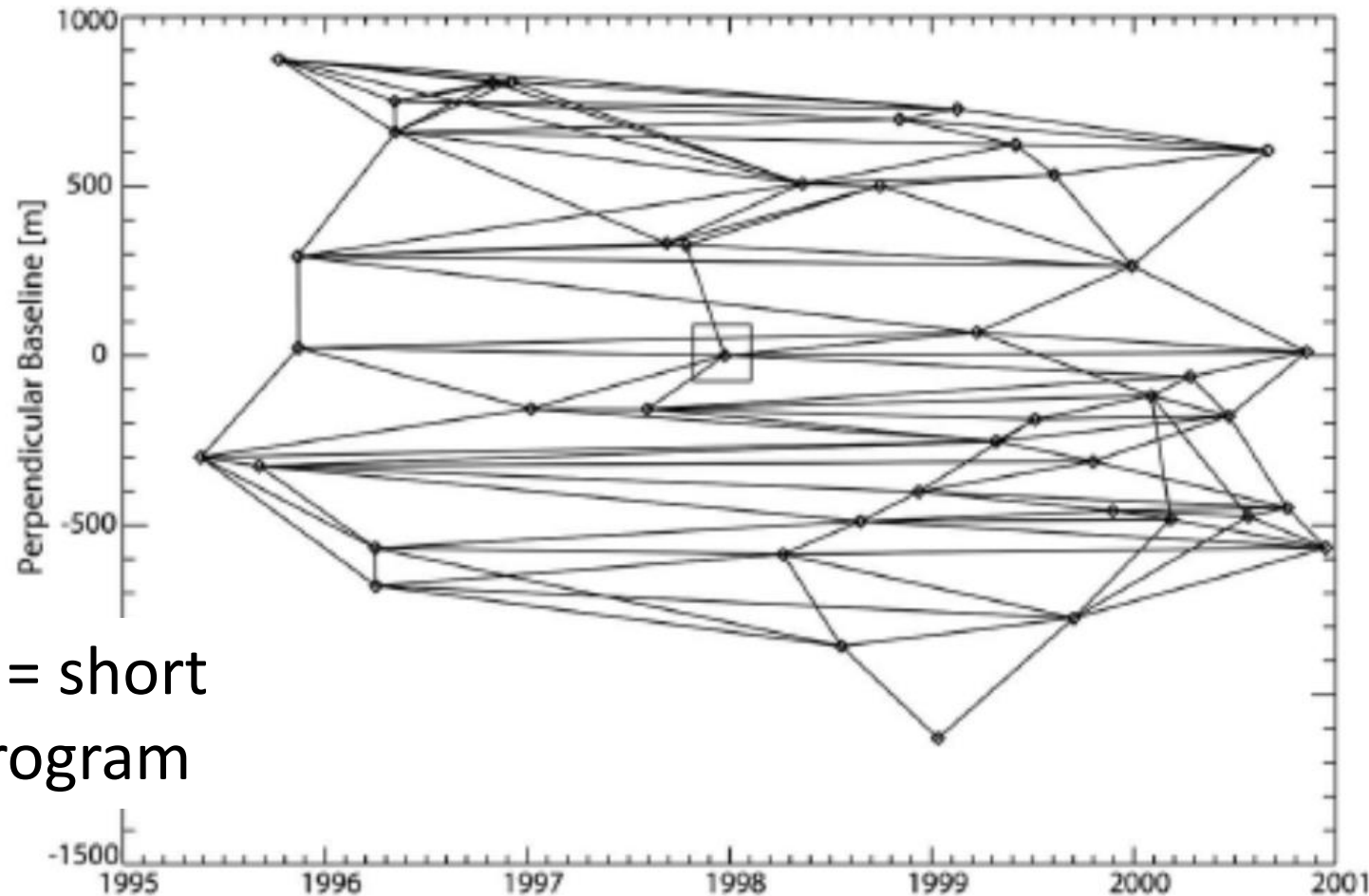
The **S**mall **B**aseline **S**ubset algorithm (SBAS) was proposed by Berardino et al. (2002) and Schmidt & Burgmann (2003) as a means of making use of spatially correlated data in a time series approach

- Only pairs of images with short spatial baselines are used
- Interferograms are unwrapped in space first
- Pixel phase time series are estimated by a least squares inversion (usually smoothed)



# SBAS basics

Maximize correlation by forming short baseline interferograms

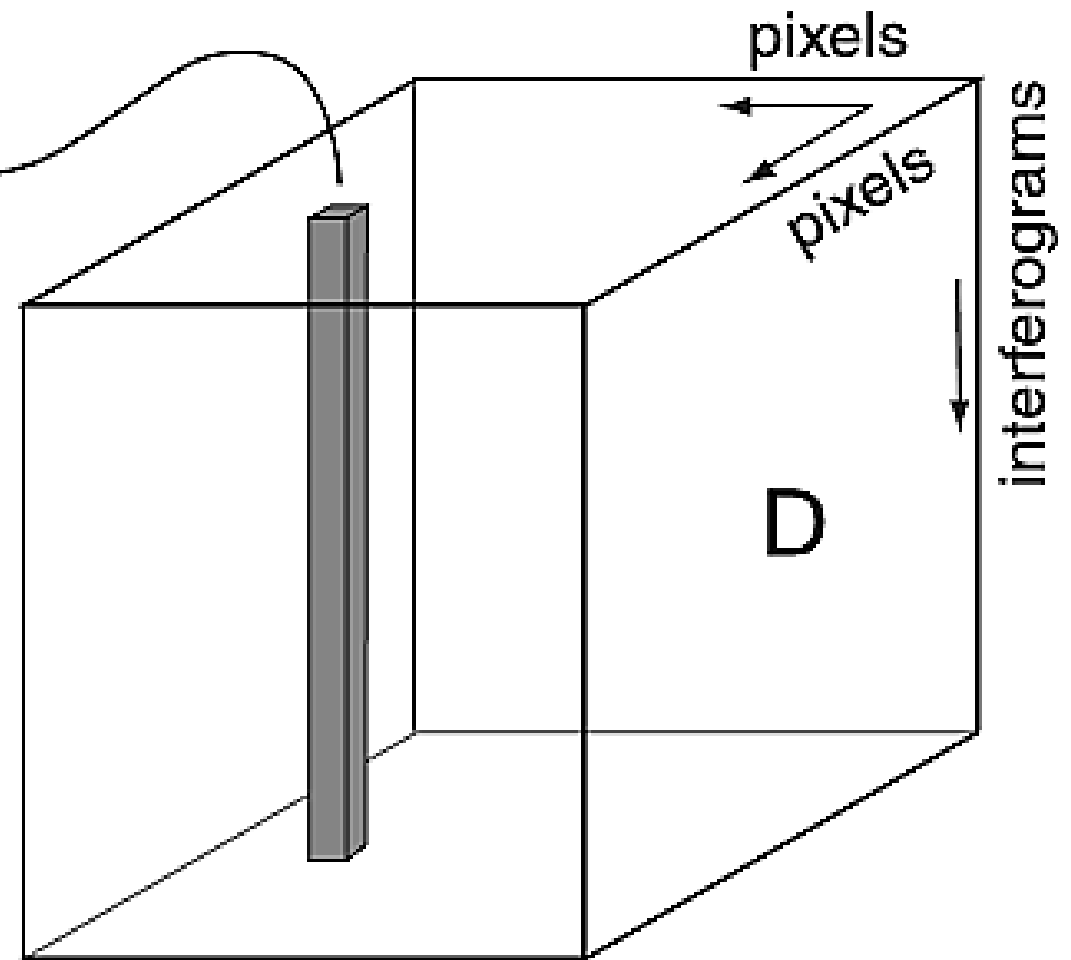


~Horizontal line = short  
baseline interferogram

$$Gm = d$$

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 1 \\ \vdots & & & & \ddots \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ \vdots \end{bmatrix} = \begin{bmatrix} d_1 \\ d_2 \\ \vdots \end{bmatrix}$$

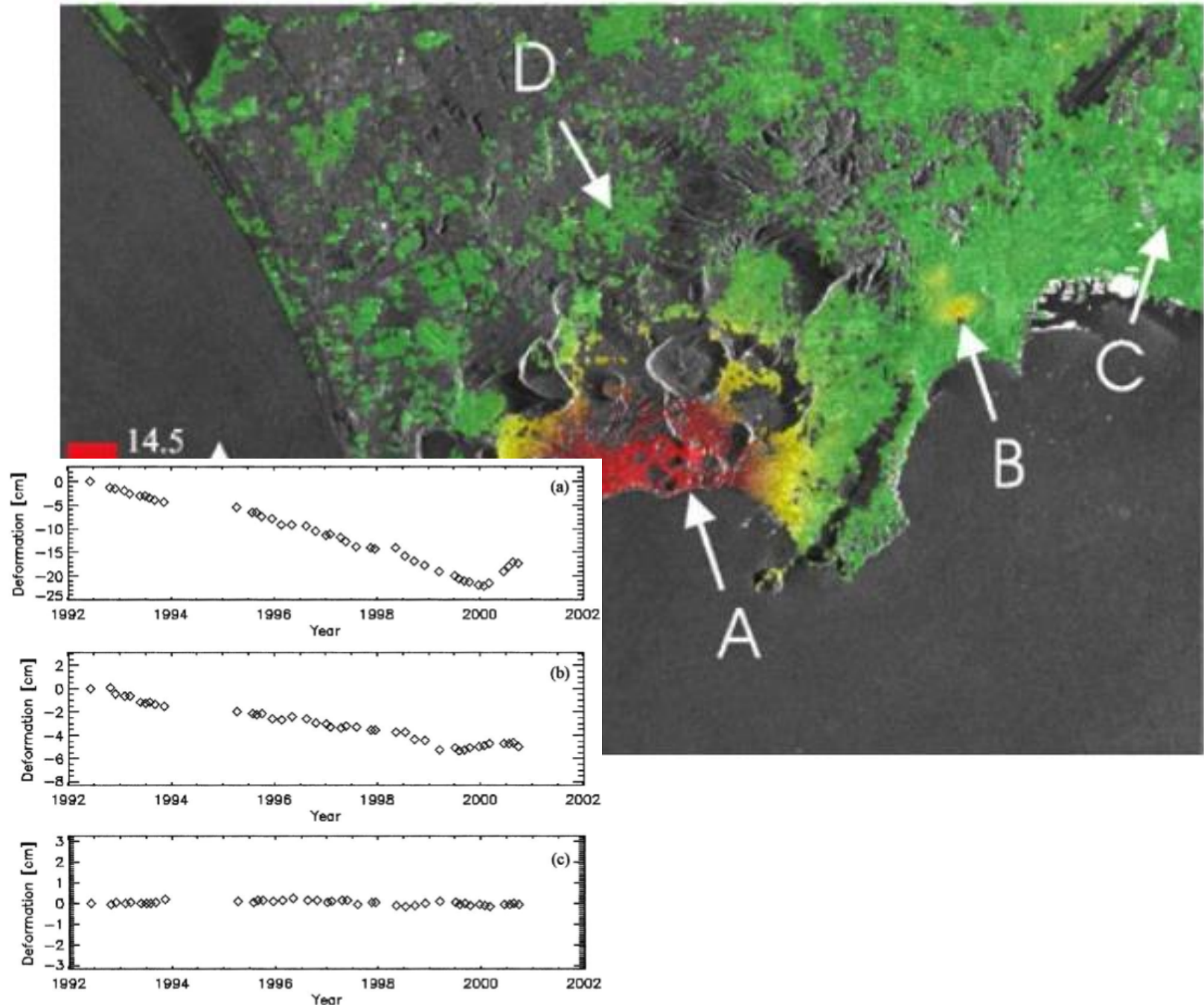
$$C = \begin{bmatrix} m_1 \\ m_1 + m_2 \\ m_1 + m_2 + m_3 \\ m_1 + m_2 + m_3 + m_4 \\ \vdots \end{bmatrix}$$



# Deformation in Naples

The deformation need not be linear in velocity, or have a prescribed form

Here negative displacement is away from the satellite – the major signal here is subsidence of Campi Flegrei volcano (A)





# Improvements to SBAS

More recent versions of SBAS codes have included features that improve the workflows and outputs

- Troposphere corrections from weather models
- 'Phase closure' tests for unwrapping errors (and in some cases, corrections)
- The ability to fit more complex functions to data (i.e. not just a best-fitting linear velocity)

# So, which should I use?

## PSI

- Good for monitoring of infrastructure and buildings (where high pixel resolution is necessary)
- Areas with isolated targets surrounded by vegetation
- Small spatial scales
- Usually requires processing interferograms yourself
- Computationally very expensive

## SBAS

- Good for geophysical/tectonic applications (large spatial coverage needed, high resolution less important)
- Can use processed, unwrapped interferograms
- Computation is less expensive

# Freely-available codes

A number of groups have implemented versions of the PSI and SBAS algorithms (or both). All of the following are freely available and open-source:

- MintPy (Miami InSAR method for Timeseries in Python) is a mature Python-based SBAS code that uses unwrapped interferograms
- StaMPS (Stanford Method for Persistent Scatterers) incorporates both PSI and SBAS, but it is MATLAB-based and is no longer actively supported
- FRINGE (Fine Resolution InSAR With Generalized Eigenvectors) is a PSI and SBAS code that is potentially very powerful, but support is limited
- MiAPIPy (MIAMI Phase Linking in Python) is a PSI and SBAS code built on top of MintPy that is relatively new, and has not been widely tested