

$$(1) \quad E_D = \frac{m^*}{m_0 \epsilon^2}$$

$$E_i = \frac{0.615 \times 13.6}{18^2} = 6.3 \times 10^{-4} \text{ eV}$$

$$(2) \quad r = \frac{4\pi \hbar^2 \epsilon_0 \epsilon}{m^* e^2} = \frac{m_0 \epsilon}{m^*} a_0 = 636 \text{ \AA}$$

$$(3) \quad N_D \geq \frac{1}{(2r)^3} = 4.86 \times 10^{20} \text{ m}^{-3}$$