

1. 解: $T = 300 \text{ K}$, $u = 1 \text{ eV} = 1.602 \times 10^{-19} \text{ eV}$

$$\therefore \frac{n}{N} = e^{-\frac{u}{k_B T}} = 1.61 \times 10^{-17}$$

2. N 个正离子对应 n 个空位 $\Omega_+ = C_N^n = \frac{N!}{n!(N-n)!}$

N 个负离子对应 n 个空位 $\Omega_- = C_N^n = \frac{N!}{n!(N-n)!}$

熵增: $\Delta S = k_B \ln \Omega = 2k_B [N \ln N - n \ln n - (N-n) \ln (N-n)]$

由 $F = F_0 + nE - T\Delta S$ T, P -定自由能最低, 无空位时 F_0 平衡位置

$$\therefore \frac{\partial F}{\partial n} = 0$$

$$\therefore E - 2k_B T \frac{\partial}{\partial n} [N \ln N - n \ln n - (N-n) \ln (N-n)] = 0$$

$$n = N e^{-\frac{E}{2k_B T}}$$