# POL212 TA Session

# Gento Kato April 11, 2019

```
## Clear Workspace
rm(list = ls())

## Set Working Directory to the File location
## (If using RStudio, can be set automatically)
setwd(dirname(rstudioapi::getActiveDocumentContext()$path))
getwd()

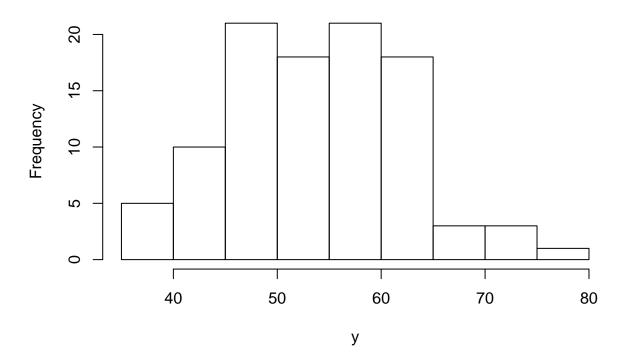
## [1] "C:/GoogleDrive/Lectures/2019_04to06_UCD/POL213_TA/POL213_TA_resource"
## Required packages
library(readr) # Reading csv file
library(ggplot2) # Plotting
library(faraway) # for ilogit function
```

#### Coarse Grid Search

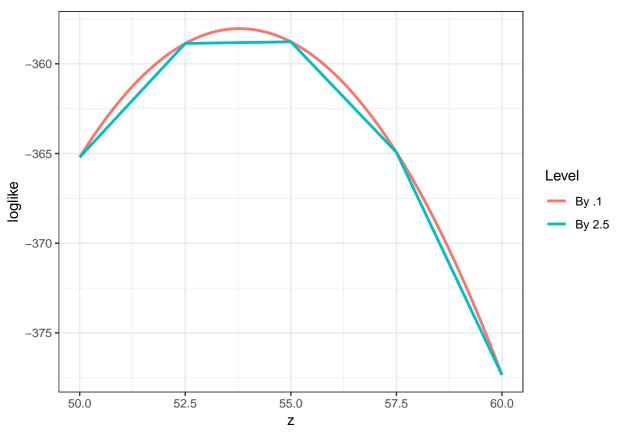
Think about the voter turnout of counties within a state, follows a normal distribution with mean 53.2 and standard deviation 8

```
set.seed(780)
y <- rnorm(100, mean = 53.2, sd = 8)
hist(y)</pre>
```

# Histogram of y



Assuming that standard deviation is 10, conduct a coarse grid search of theta parameter.



```
# Find Max
z1[which.max(loglike1)]
## [1] 55
z2[which.max(loglike2)] # More fine grained
## [1] 53.8
```

# Fitting Logit

The following data contains county level presidential election results 2000-2016. (Check codebook at <a href="https://github.com/gentok/POL213\_TA\_Resource/blob/master/data/County%2BPresidential%2BReturns%2B2000-2016.md">https://github.com/gentok/POL213\_TA\_Resource/blob/master/data/County%2BPresidential%2BReturns%2B2000-2016.md</a>)

d <- read\_csv("https://raw.githubusercontent.com/gentok/POL213\_TA\_Resource/master/data/countypres\_2000-

```
## Parsed with column specification:
## cols(
##
     year = col_integer(),
     state = col_character(),
##
     state_po = col_character(),
##
##
     county = col_character(),
##
     FIPS = col_integer(),
     office = col_character(),
##
     candidate = col_character(),
##
     party = col_character(),
##
```

```
## candidatevotes = col_integer(),
## totalvotes = col_integer(),
## version = col_integer()
## )
d <- na.omit(d)</pre>
```

Let's subset the data and extract county-level votes for Gore (2000), Bush (2000), Obama (2008), and McCain (2008) in Texas.

```
# Gore Vote Share in TX
TX_gore <- d[d$year==2000 & d$party == "democrat" & d$state_po == "TX",]
# Bush Vote Share in TX
TX_bush <- d[d$year==2000 & d$party == "republican" & d$state_po == "TX",]
# Obama Vote Share in TX
TX_obama <- d[d$year==2008 & d$party == "democrat" & d$state_po == "TX",]
# McCain Vote Share in TX
TX_mccain <- d[d$year==2008 & d$party == "republican" & d$state_po == "TX",]
# Check if county rows match
all(TX_obama$FIPS == TX_mccain$FIPS)</pre>
```

```
## [1] TRUE
```

```
all(TX_obama$FIPS == TX_bush$FIPS)
```

```
## [1] TRUE
```

```
all(TX_obama$FIPS == TX_gore$FIPS)
```

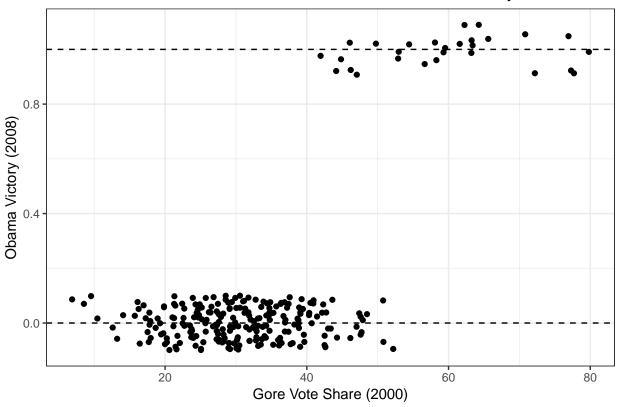
## [1] TRUE

Calculate 2008 Obama win-lose and 2000 Gore Vote Share

Estimate Logistic Regression predicting Obama win-lose by Gore vote share.

```
# Plot Obama win-lose by Gore Vote Share
p <- ggplot(TX_data, aes(x=goreshare,y=obamawin)) +
    geom_jitter(height=0.1) + # Jittered points
    geom_hline(aes(yintercept=1), linetype=2) + # Horizontal dashed line @ 1
    geom_hline(aes(yintercept=0), linetype=2) + # Horizontal dashed line @ 0
    xlab("Gore Vote Share (2000)") +
    ylab("Obama Victory (2008)") +
    ggtitle("TX Counties 2000 Gore Vote Share and 2008 Obama Victory") +
    theme_bw()</pre>
```

## TX Counties 2000 Gore Vote Share and 2008 Obama Victory



```
# Estimate Logistic regression
logit.TX_obamawin <- glm(obamawin ~ goreshare, TX_data, family = binomial)
summary(logit.TX_obamawin)</pre>
```

```
##
## Call:
## glm(formula = obamawin ~ goreshare, family = binomial, data = TX_data)
##
## Deviance Residuals:
       Min
                  1Q
                        Median
                                               Max
## -1.59085 -0.09826 -0.03393 -0.00881
                                           2.37681
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
                           3.59583 -4.977 6.44e-07 ***
## (Intercept) -17.89819
                0.36081
                           0.07651
                                     4.716 2.41e-06 ***
## goreshare
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 176.281 on 253 degrees of freedom
## Residual deviance: 41.618 on 252 degrees of freedom
## AIC: 45.618
## Number of Fisher Scoring iterations: 8
```

```
# Log-likelihood of the estimates
logLik(logit.TX_obamawin)

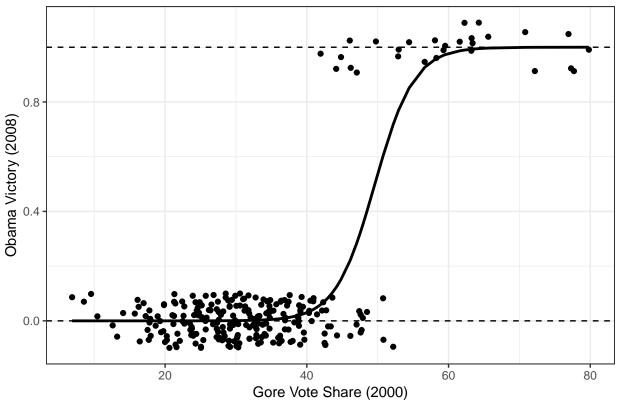
## 'log Lik.' -20.80918 (df=2)

# Calculate Logit prediction
prediction <- ilogit(-17.8919 + 0.36081*TX_data$goreshare)

# OR
prediction <- predict(logit.TX_obamawin, type="response")

# Add prediction to the plot
p + geom_line(aes(y=prediction), size=1)</pre>
```

# TX Counties 2000 Gore Vote Share and 2008 Obama Victory



# Manually Fitting Logit

## Prepare Variables & functions

```
# DV
y <- cbind(TX_data$obamawin)
# IV
x <- cbind(TX_data$goreshare)
# Constant
cons <- rep(1, length(x[,1]))
# Matrix of Constant and IV(s)
xmat<-cbind(cons, x)</pre>
```

```
# Function to calculate Log Likelihood
llk.logit <- function(param,y,x) {</pre>
  # prepare constant
  cons <- rep(1, length(x[,1]))
  # matrix of constant and IV(s)
 x <- cbind(cons, x)
  # assigned beta parameters
 b <- param[1 : ncol(x)]</pre>
  # calculate fitted values
 xb<-x%*%b
  # calculate log-likelihood
  sum(y*log(1 + exp(-xb)) + (1-y)*log(1 + exp(xb)))
# Set starting values taken from OLS.
ols.result <- lm(y~x); ols.result
##
## Call:
## lm(formula = y \sim x)
##
## Coefficients:
## (Intercept)
      -0.48227
                     0.01768
stval <- ols.result$coeff</pre>
```

#### First iteration

```
# Optimize by log-likelihood
logit.result <- optim(stval, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
## (Intercept)
## -0.48226639 0.01767522
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
                (Intercept)
## (Intercept) 0.130804583 -0.0034583735
               -0.003458373 0.0001041678
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## (Intercept)
## 0.36166916 0.01020626
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -176.0126
```

```
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 352.0252
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes</pre>
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
         parm_est
## cons -105.843
        -2993.912
##
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector</pre>
##
                  parm_est
## (Intercept) -3.49069077
## x
                0.05417553
# updated starting value
update <- cbind(stval) + direction.vector; update</pre>
##
                      stval
## (Intercept) -3.97295716
## x
                0.07185075
Second iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
##
                      stval
## (Intercept) -3.97295716
                0.07185075
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
                 [,1]
                                [,2]
## [1,] 0.286700820 -0.0067955146
## [2,] -0.006795515 0.0001791048
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 0.5354445 0.0133830
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -57.34766
```

```
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 114.6953
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes</pre>
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
##
             stval
## cons -23.60246
        -562.53390
##
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
##
              stval
## [1,] -2.94413702
## [2,] 0.05963834
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
##
                     stval
## (Intercept) -6.9170942
## x
                0.1314891
Third iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
##
                     stval
## (Intercept) -6.9170942
                0.1314891
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
               [,1]
                              [,2]
## [1,] 0.76343913 -0.0171157210
## [2,] -0.01711572  0.0004112217
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 0.8737500 0.0202786
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
```

## [1] -34.51776

```
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 69.03552
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes</pre>
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
##
             stval
## cons -8.44227
        -190.09565
##
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
##
              stval
## [1,] -3.19153532
## [2,] 0.06632409
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
##
                      stval
## (Intercept) -10.1086295
## x
                 0.1978132
Fourth iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
##
                      stval
## (Intercept) -10.1086295
                 0.1978132
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
               [,1]
                             [,2]
## [1,] 2.03563428 -0.044260128
## [2,] -0.04426013 0.001002926
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 1.426757 0.031669
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
```

## [1] -25.3888

```
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 50.77759
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes</pre>
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
##
             stval
## cons -3.085691
        -67.003799
##
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
##
              stval
## [1,] -3.31574124
## [2,] 0.06937323
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
##
                      stval
## (Intercept) -13.4243707
## x
                 0.2671864
Fifth iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
##
                      stval
## (Intercept) -13.4243707
                 0.2671864
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
               [,1]
                           [,2]
## [1,] 4.8897988 -0.10460130
## [2,] -0.1046013 0.00229326
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 2.211289 0.047888
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
```

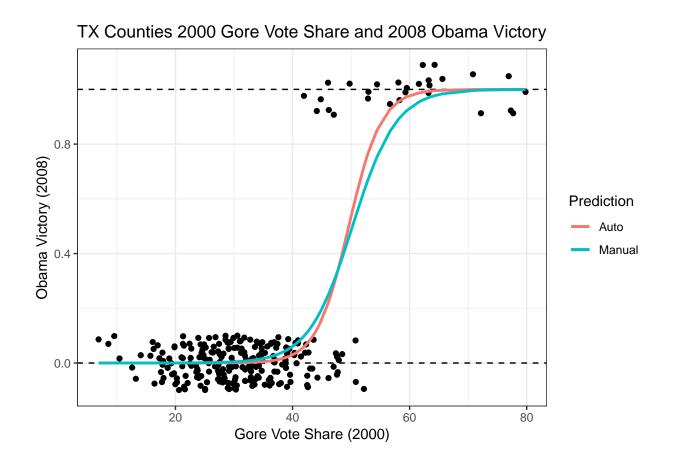
## [1] -21.90023

```
# Deviance
dev \leftarrow -2*(log_like - 0); dev
## [1] 43.80046
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes</pre>
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
##
              stval
## cons -1.056987
        -22.679856
##
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector</pre>
##
               stval
## [1,] -2.79610904
## [2,] 0.05855136
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
##
                      stval
## (Intercept) -16.2204798
## x
                  0.3257378
```

#### Compare manual and automatic results

```
# Fit Prediction
prediction_manual <- ilogit(parm_est[1] + parm_est[2]*x)

# Compare predictions
p + geom_line(aes(y=prediction, color="Auto"), size=1) +
geom_line(aes(y=prediction_manual, color="Manual"), size=1) +
scale_color_discrete(name="Prediction")</pre>
```



## Workshop question

## [1] TRUE

Fit logistic regression that predicts Trump victory by 2008 McCain vote share in California. Optimize by both automatic and manual methods and compare results.

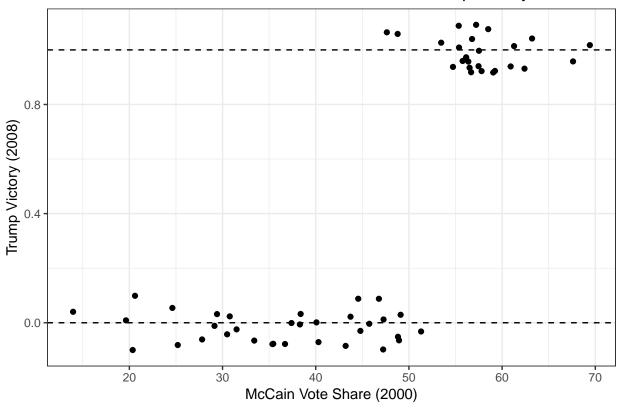
```
# Obama Vote Share in CA
CA_obama <- d[d$year==2008 & d$party == "democrat" & d$state_po == "CA",]
# McCain Vote Share in CA
CA_mccain <- d[d$year==2008 & d$party == "republican" & d$state_po == "CA",]
# Obama Vote Share in CA
CA_obama12 <- d[d$year==2012 & d$party == "democrat" & d$state_po == "CA",]
# Romney Vote Share in CA
CA_romney <- d[d$year==2012 & d$party == "republican" & d$state_po == "CA",]
# Clinton Vote Share in CA
CA_clinton <- d[d$year==2016 & d$party == "democrat" & d$state_po == "CA",]
# Trump Vote Share in CA
CA_trump <- d[d$year==2016 & d$party == "republican" & d$state_po == "CA",]
# Check if county rows match
all(CA_obama$FIPS == CA_mccain$FIPS)
## [1] TRUE
all(CA_obama$FIPS == CA_obama12$FIPS)
```

```
all(CA_obama$FIPS == CA_romney$FIPS)
## [1] TRUE
all(CA_obama$FIPS == CA_clinton$FIPS)
## [1] TRUE
all(CA_obama$FIPS == CA_trump$FIPS)
## [1] TRUE
Calculate 2016 Trump win-lose, 2012 Romney Vote Share, and 2008 McCain Vote Share
# Create Data
CA_data <- data.frame(FIPS = CA_obama$FIPS)</pre>
# McCain Vote Share
CA_data$mccainshare <- CA_mccain$candidatevotes/(CA_mccain$candidatevotes +
                                                CA_obama$candidatevotes) * 100
# Romney Vote Share
CA_data$romney$hare <- CA_romney$candidatevotes/(CA_romney$candidatevotes +
                                                    CA obama12$candidatevotes) * 100
# Trump Win-Lose in County
CA_data$trumpwin <- (CA_trump$candidatevotes >= CA_clinton$candidatevotes) * 1
Estimate Logistic Regression predicting Trump win-lose by McCain vote share.
# Plot Trump win-lose by McCain Vote Share
p <- ggplot(CA_data, aes(x=mccainshare,y=trumpwin)) +</pre>
  geom_jitter(height=0.1) + # Jittered points
  geom_hline(aes(yintercept=1), linetype=2) + # Horizontal dashed line @ 1
  geom_hline(aes(yintercept=0), linetype=2) + # Horizontal dashed line @ 0
  xlab("McCain Vote Share (2000)") +
  ylab("Trump Victory (2008)") +
```

ggtitle("CA Counties 2008 McCain Vote Share and 2016 Trump Victory") +

theme bw()

## CA Counties 2008 McCain Vote Share and 2016 Trump Victory



```
# Estimate Logistic regression
logit.CA_trumpwin <- glm(trumpwin ~ mccainshare, CA_data, family = binomial)
summary(logit.CA_trumpwin)</pre>
```

```
##
## Call:
## glm(formula = trumpwin ~ mccainshare, family = binomial, data = CA_data)
##
## Deviance Residuals:
       Min
                   1Q
                        Median
                                      3Q
                                               Max
  -1.49685 -0.02136 -0.00010
                                 0.10753
                                           2.00501
##
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -35.4037
                          12.6471 -2.799 0.00512 **
## mccainshare
                0.7042
                           0.2541
                                    2.772 0.00558 **
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 79.298 on 57 degrees of freedom
## Residual deviance: 12.396 on 56 degrees of freedom
## AIC: 16.396
## Number of Fisher Scoring iterations: 9
```

```
# Log-likelihood of the estimates
logLik(logit.CA_trumpwin)

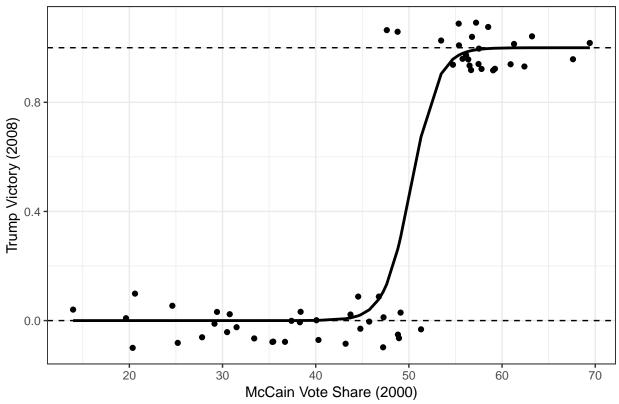
## 'log Lik.' -6.198203 (df=2)

# Calculate Logit prediction
prediction <- ilogit(-35.4037 + 0.7042*CA_data$mccainshare)

# OR
prediction <- predict(logit.CA_trumpwin, type="response")

# Add prediction to the plot
p + geom_line(aes(y=prediction), size=1)</pre>
```

# CA Counties 2008 McCain Vote Share and 2016 Trump Victory



#### Manually Fitting Logit

## Prepare Variables & functions

```
# DV
y <- cbind(CA_data$trumpwin)
# IV
x <- cbind(CA_data$mccainshare)
# Constant
cons <- rep(1, length(x[,1]))
# Matrix of Constant and IV(s)
xmat<-cbind(cons, x)</pre>
```

```
# Set starting values taken from OLS.
ols.result <- lm(y~x); ols.result</pre>
##
## Call:
## lm(formula = y \sim x)
## Coefficients:
## (Intercept)
      -0.91726
                      0.02956
##
stval <- ols.result$coeff</pre>
```

#### First iteration

```
# Optimize by log-likelihood
logit.result <- optim(stval, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
## (Intercept)
## -0.91725834 0.02955904
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
                (Intercept)
## (Intercept) 0.92811028 -0.0190658760
               -0.01906588 0.0004259653
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## (Intercept)
## 0.96338480 0.02063893
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -35.32679
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 70.65359
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes</pre>
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
           parm_est
## cons -9.964655
        -221.873945
```

```
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
                  parm_est
## (Intercept) -5.01807718
                0.09547427
# updated starting value
update <- cbind(stval) + direction.vector; update</pre>
                     stval
## (Intercept) -5.9353355
## x
                0.1250333
Second iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
                     stval
## (Intercept) -5.9353355
## x
                0.1250333
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
                             [,2]
                [,1]
## [1,] 2.69396919 -0.053778516
## [2,] -0.05377852 0.001117596
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 1.64133153 0.03343046
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -17.84337
# Deviance
dev \leftarrow -2*(log_like - 0); dev
## [1] 35.68674
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
             stval
## cons -2.815983
##
        -47.559500
```

```
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
              stval
## [1,] -5.02849230
## [2,] 0.09828709
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
                      stval
## (Intercept) -10.9638278
## x
                 0.2233204
Third iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
                      stval
## (Intercept) -10.9638278
## x
                 0.2233204
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
                           [,2]
               [,1]
## [1,] 8.3858365 -0.16487194
## [2,] -0.1648719 0.00330384
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 2.89583089 0.05747904
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -11.62362
# Deviance
dev \leftarrow -2*(log_like - 0); dev
## [1] 23.24724
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
            stval
## cons -1.27642
##
        -24.68247
```

```
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
             stval
## [1,] -6.6344028
## [2,] 0.1288989
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
                      stval
## (Intercept) -17.5982307
## x
                 0.3522193
Fourth iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
                      stval
## (Intercept) -17.5982307
## x
                 0.3522193
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
              [,1]
                            [,2]
## [1,] 23.9037084 -0.469013742
## [2,] -0.4690137 0.009295903
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 4.88914188 0.09641526
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -8.189548
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 16.3791
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
             stval
## cons -0.4713255
##
        -7.7532848
```

```
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector
             stval
## [1,] -7.6300300
## [2,] 0.1489844
# updated starting value
update <- cbind(update) + direction.vector; update</pre>
                      stval
## (Intercept) -25.2282607
## x
                 0.5012037
Fifth iteration
# Optimize by log-likelihood
logit.result <- optim(update, llk.logit, method="BFGS",</pre>
                       control=list(maxit=0, trace=1), hessian=TRUE, y=y, x=x)
# Printing Optimization results #
# beta paramter estimates
parm_est <- logit.result$par; parm_est</pre>
                      stval
## (Intercept) -25.2282607
## x
                 0.5012037
# variance covariance matrix
var_cov <- solve(logit.result$hessian); var_cov</pre>
##
             [,1]
                          [,2]
## [1,] 57.102240 -1.12755659
## [2,] -1.127557 0.02240716
# Standard error of beta estimates
std_err <- sqrt(diag(var_cov)); std_err</pre>
## [1] 7.5566024 0.1496902
# Log-likelihood
log_like <- -logit.result$value; log_like</pre>
## [1] -6.664625
# Deviance
dev <- -2*(log_like - 0); dev
## [1] 13.32925
# Find new starting value
beta <- cbind(parm_est) # Store paramete estiamtes
plgtb <- 1/(1 + exp(-xmat%*%beta))
# score vector
score.vector <- t(xmat)%*%(y - plgtb); score.vector</pre>
              stval
## cons -0.06222855
##
         2.42088232
```

```
# direction vector
direction.vector <- var_cov%*%score.vector; direction.vector

## stval
## [1,] -6.2830717
## [2,] 0.1244113

# updated starting value
update <- cbind(update) + direction.vector; update

## stval
## (Intercept) -31.511332
## x 0.625615</pre>
```

### Compare manual and automatic results

```
# Fit Prediction
prediction_manual <- ilogit(parm_est[1] + parm_est[2]*x)

# Compare predictions
p + geom_line(aes(y=prediction, color="Auto"), size=1) +
geom_line(aes(y=prediction_manual, color="Manual"), size=1) +
scale_color_discrete(name="Prediction")</pre>
```

## CA Counties 2008 McCain Vote Share and 2016 Trump Victory

