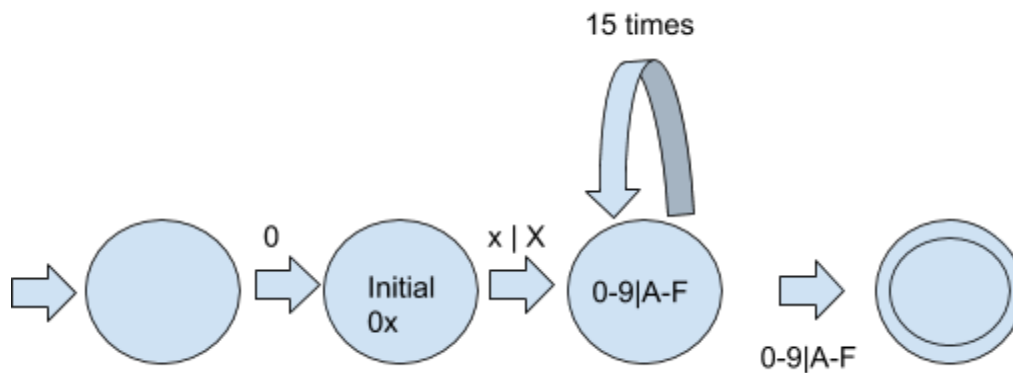


1) Write a regular expression to capture Java's long literals in base 16 and then construct a finite-state automation for it.

$0[xX][0-9|A-F]\{16, 16\}$



2) Consider the following grammar:

$\langle E \rangle ::= a \langle B \rangle \mid b \langle A \rangle \mid \epsilon$
 $\langle A \rangle ::= a \langle E \rangle \mid b \langle A \rangle \langle A \rangle$
 $\langle B \rangle ::= b \langle E \rangle \mid a \langle B \rangle \langle B \rangle$

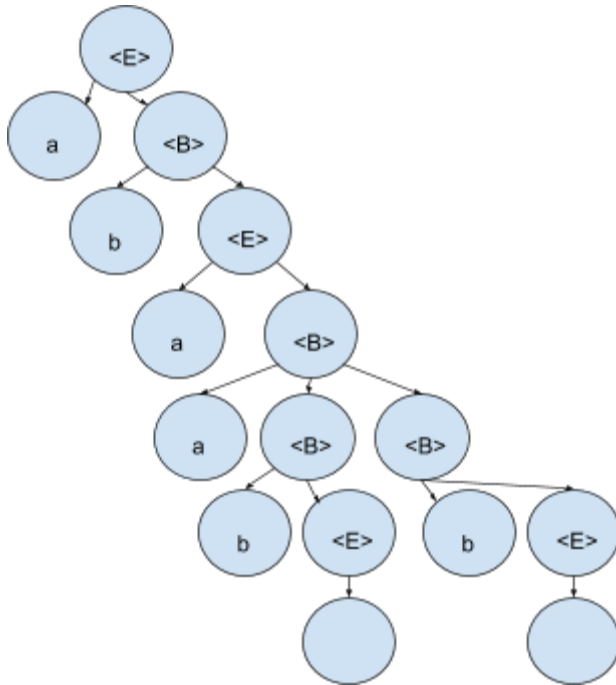
1. Write a leftmost derivation for the string a b a a b b.

$\langle E \rangle$
 $a \langle B \rangle$
 $ab \langle E \rangle$
 $aba \langle B \rangle$
 $abaa \langle B \rangle \langle B \rangle$
 $abaab \langle E \rangle \langle B \rangle$
 $abaab \epsilon \langle B \rangle$
 $abaabb \langle E \rangle$

abaabbε

abaabb

2. Show the parse tree for the string a b a a b b.



3. Describe in English the language that the grammar generates.

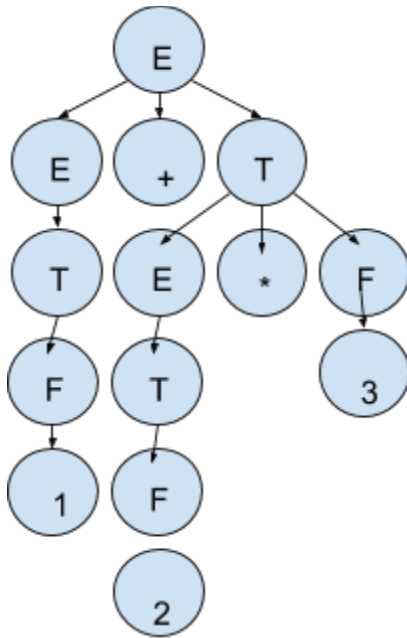
String of any length containing only a's and b's with a balanced number of a's and b's.

- 3) Consider the following grammar for expressions:

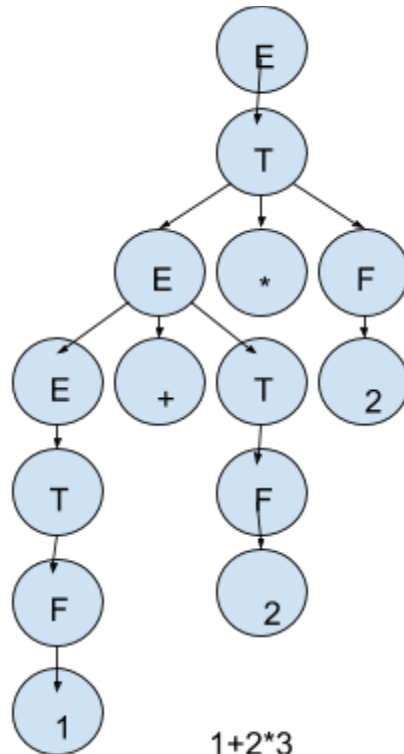
$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$
 $\langle \text{term} \rangle ::= \langle \text{expr} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle$
 $\langle \text{factor} \rangle ::= \text{id}$

1. Show that the grammar is ambiguous.

Two parse trees exist for the expression $1 + 2 * 3$, so the language must be ambiguous.



1+2*3



1+2*3

2. Provide an alternate unambiguous grammar that defines the same set of expressions.

```

<expr> ::= <expr> + <term> | <term>
<term> ::= <term> * <factor> | <factor>
<factor> ::= (<expr>) | id
  
```

4) Consider the grammar

S -> (L) | a

L -> L, S | S

1. Re-write the grammar in the EBNF notation.

S -> (L) | a

L -> [L,] {S,}* S

2. Write a recursive-descent parser based on the EBNF notation.

void S() {

```

    if (lookahead == a)
        nexttoken();
    else if (lookahead == ()
        nexttoken();
        L();
        nexttoken();
}

void L() {
    if nexttoken == L
        L();
        nexttoken();
    else while (nexttoken == S)
        S();
        if lookahead == ,
            nexttoken();
}

```

5)

(a) A number consists of digits from 0 to 9. For example, 1234 is a number. Give two different grammars to define a number, one using a left-recursive rule and the other using a right-recursive rule.

Left: <digit> -> <digit>id | id

Right: <digit> -> id<digit> | id

(b) A decimal number can be defined as a number followed by a decimal point (.) and another number. For example, 123.045 is a decimal number. Define attributes and write an attribute grammar to compute the value of any decimal number.

`<number> -> <left>.<right>`

`value = leftValue + rightValue`

`leftPower = 1, rightPower = 0.1`

`<left> -> id<left> | id`

`leftValue += id * leftPower`

`leftPower = leftPower * 10`

`<right> -> <right>id | id`

`rightValue += id * rightPower`

`rightPower *= 0.1`