

A Few Hidden Features in Q-CHEM for Geometry Optimization, Wavefunction Analysis, and QM/MM Calculations

Yihan Shao

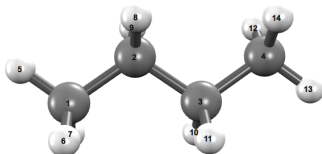
University of Oklahoma

Feb. 27, 2018

- 1 Potential Energy Scan
- 2 Electrostatic-Potential-Derived (ESP) Charges
- 3 Decomposition of TDDFT excitation energies
- 4 Multiple-Environment Single-System QM/MM
- 5 General Research Interest

Relaxed Potential Energy Scan

- A series of constrained geom opt



- Initial angle: -180°
- Final angle: 180°
- Increment: 15°
- constraints: bond lengths, bond angles, torsional angles
- Initial value can be larger than the final value
- 2-d scan is allowed

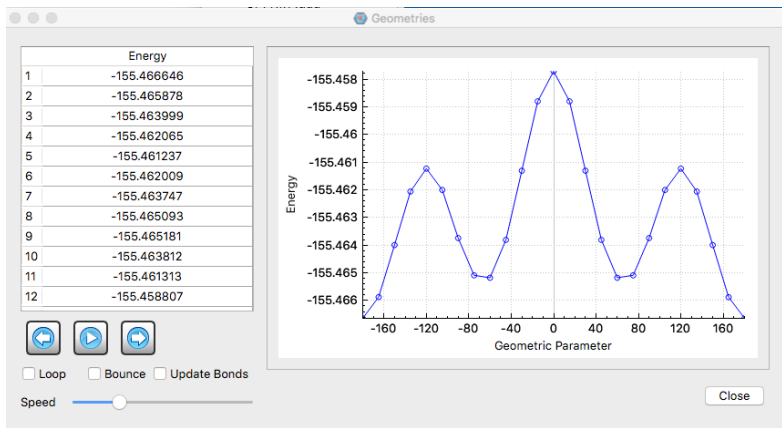
```
$molecule
0 1
C      1.934574      -0.128781      -0.000151
C      0.556601       0.526657       0.000200
C     -0.556627     -0.526735       0.000173
C     -1.934557      0.128837     -0.000138
H      2.720125      0.655980     -0.000236
H      2.061880     -0.759501     -0.905731
H      2.062283     -0.759765       0.905211
H      0.464285      1.168064     -0.903444
H      0.464481      1.167909       0.903924
H     -0.464539     -1.167976       0.903964
H     -0.464346     -1.168166     -0.903402
H     -2.062154      0.759848       0.905185
H     -2.720189     -0.655832     -0.000229
H     -2.061778      0.759577     -0.905748
$end
```

```
$rem
jobtype pes_scan
method hf
basis sto-3g
$end
```

```
$scan
tors 1 2 3 4 -180 180 15
$end
```

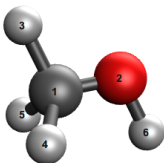
Relaxed Potential Energy Scan Results

- IQmol visualization of 1-d scan results



Frozen Potential Energy Scan

- A series of single-point energy calculations



- Initial bond length: 1.0 Å
- Final bond length: 2.0 Å
- Increment: 0.5 Å
- No geometry optimization
- Input geometry must be z-matrix

```
$molecule
0 1
C
O C RCO
H1 C RCH1 O H1CO
X C 1.0 O XCO H1 180.0
H2 C RCH2 X H2CX H1 90.0
H3 C RCH2 X H2CX H1 -90.0
H4 O ROH C HOC H1 180.0
```

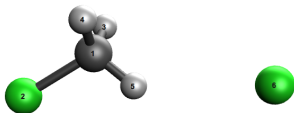
```
RCO = 1.421
RCH1 = 1.094
RCH2 = 1.094
ROH = 0.963
H1CO = 107.2
XCO = 129.9
H2CX = 54.25
HOC = 108.0
$end
```

```
$rem
JOBTYPES pes_scan
FROZEN_SCAN TRUE
EXCHANGE S
CORRELATION VWN
BASIS 3-21G
$end
```

```
$scan
stre 1 2 1.0 2.0 0.5
$end
```

Restrained Potential Energy Scan

- A series of **restrained** geom opt



- Geometry restraints

$$k (R_{12} - R_{16} - R)^2$$

- R_{min} : -2.0Å
- R_{max} : 2.0 Å
- Increment: 0.2 Å
- Force constant (k): 1000.0
- 1-d scan only
- Can also use "r12pr34"

```
$molecule
-1 1
  C      0.418808      -1.240869      0.249048
  Cl     -0.775224     -1.495584      1.586668
  H       1.408172     -1.490565      0.631227
  H       0.147593     -1.907736     -0.568952
  H       0.413296     -0.199000     -0.092071
  Cl      1.947359      1.619163     -1.747832
```

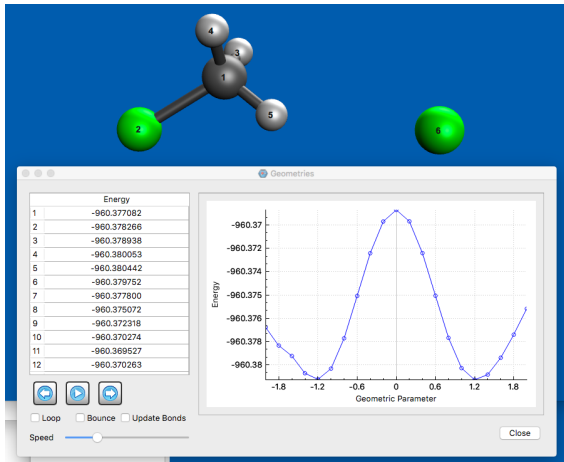
```
$end
```

```
$rem
jobtype pes_scan
exchange b3lyp
basis 6-31G*
$end
```

```
$scan
r12mr34 1 2 1 6 -2.0 2.0 0.2 1000.0
$end
```

Restrained Potential Energy Scan Results

- IQmol visualization of 1-d scan results



Restrained Geometry Optimization

```
$molecule
```

```
-1 1
  C      0.4188082876    -1.2408695705    0.2490483370
 Cl     -0.7752244258    -1.4955845511    1.5866685479
  H      1.4081726568    -1.4905651530    0.6312274608
  H      0.1475935065    -1.9077368904   -0.5689527615
  H      0.4132963138    -0.1990006891   -0.0920715962
 Cl      1.9473593327     1.6191631608   -1.7478328574
```

```
$end
```

```
$rem
```

```
jobtype opt
```

```
exchange b3lyp
```

```
basis 6-31G*
```

```
$end
```

```
$opt2
```

```
r12mr34 1 2 1 6 0.0 1000.0
```

```
$end
```


- 1 Potential Energy Scan
- 2 Electrostatic-Potential-Derived (ESP) Charges**
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Charge Populations in Q-CHEM

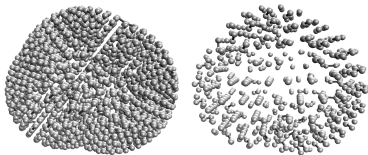
- Mulliken charges
 - Can be **non-physical** with larger basis sets
- NBO charges
- CHELPG charges (CHELPG = TRUE)
 - Well reproduce the dipole moment
- Hirshfeld charges (HIRSHFELD = TRUE)
 - Usually **too small**
- CM5 charges (CM5 = TRUE)
 - Improvement by Don Truhlar
- Iterative Hirshfeld charges (HIRSHITER = TRUE)
 - Much better than Hirshfeld charges

J. Phys. Chem. A, 119, 5865 (2015).

ESP/RESP charge calculations

- ESP Grid Options:

- 1: Spherical harmonics
- 2: Lebedev



- RESP_CHARGES = TRUE

```

$molecule
0 1
  C      1.22227    -0.2466    0.0178
  H      2.09272     0.3971   -0.0423
  H      1.27594    -0.9548   -0.8023
  H      1.26663    -0.7997    0.9461
  C     -0.07041     0.5616   -0.0459
  H     -0.12063     1.1336   -0.9663
  H     -0.12012     1.2567    0.7739
  O     -1.24418    -0.2540    0.1065
  H     -1.35216    -0.8912   -0.5924
$end

$rem
BASIS      = 6-31G*
METHOD     = B3LYP
JOBTYPE    = SP
RESP_CHARGES = 1    # or 2
$end

```

ESP charges with different grids

● Dipole moment: X 1.0606; Y -0.2250; Z -1.2090; Tot 1.6239

● ESP_Charges = 1

Merz-Kollman ESP Net Atomic Charges

Atom	Charge (a.u.)
-----	-----
1 C	-0.359692
2 H	0.075218
3 H	0.088502
4 H	0.105036
5 C	0.356774
6 H	-0.035130
7 H	0.032457
8 O	-0.673003
9 H	0.409839
-----	-----
Sum of atomic charges =	0.000000

Related Dipole Moment = 1.6305
(X 1.0669 Y -0.2059 Z -1.2157)

● ESP_Charges = 2

Merz-Kollman ESP Net Atomic Charges

Atom	Charge (a.u.)
-----	-----
1 C	-0.362941
2 H	0.076361
3 H	0.090774
4 H	0.107454
5 C	0.338283
6 H	-0.028913
7 H	0.038096
8 O	-0.669108
9 H	0.409994
-----	-----
Sum of atomic charges =	0.000000

Related Dipole Moment = 1.6285
(X 1.0631 Y -0.2069 Z -1.2162)

ESP and RESP charges

• Dipole moment: X 1.0606; Y -0.2250; Z -1.2090; Tot 1.6239

• ESP_Charges = 1

Merz-Kollman **ESP** Net Atomic Charges

Atom	Charge (a.u.)
1 C	-0.359692
2 H	0.075218
3 H	0.088502
4 H	0.105036
5 C	0.356774
6 H	-0.035130
7 H	0.032457
8 O	-0.673003
9 H	0.409839

Sum of atomic charges =	0.000000

Related Dipole Moment = 1.6305
(X 1.0669 Y -0.2059 Z -1.2157)

• RESP_Charges = 1

Merz-Kollman **RESP** Net Atomic Charges

Atom	Charge (a.u.)
1 C	-0.272946
2 H	0.067338
3 H	0.067338
4 H	0.067338
5 C	0.346165
6 H	-0.015626
7 H	-0.015626
8 O	-0.608147
9 H	0.364167

Sum of atomic charges =	0.000000

Related Dipole Moment = 1.7694
(X 1.0670 Y -0.1781 Z -1.4002)

ESP charges for TDDFT excited states

```
$molecule
```

```
0 1
```

O	-0.00000	0.00000	0.7625
C	0.00000	0.00000	-0.6375
H	0.86602	-0.00000	-1.1375
H	-0.86602	0.00000	-1.1375

```
$end
```

```
$rem
```

```

BASIS          = 6-31G*
METHOD         = B3LYP
JOBTYPE        = SP
CIS_N_ROOTS    = 3
SET_TRIP       = FALSE
RPA            = 2          # No TDA
POP_MULLIKEN   = -1        # Mulliken charges for all states
ESP_CHARGES    = 1          # ESP charges for all states
CIS_RLX_DNS    = 1          # We should use the relaxed density

```

```
$end
```

ESP and RESP charges

● CIS_RLX_DNS = 0

Merz-Kollman ESP Net Atomic Charges

Atom	Charge (a.u.)
-----	-----
1 O	-0.365648
2 C	0.185380
3 H	0.090134
4 H	0.090134
-----	-----
Sum of atomic charges =	0.000000

Related Dipole Moment = 2.8917
(X 0.0000 Y 0.0000 Z -2.8917)

ESP charges for excited states

	1	2	3
1	0.2938661	0.2277436	-0.0598282
2	-0.8473374	-0.8761796	0.0035142
3	0.2767357	0.3242180	0.0281570
4	0.2767357	0.3242180	0.0281570

● CIS_RLX_DNS = 1

Merz-Kollman ESP Net Atomic Charges

Atom	Charge (a.u.)
-----	-----
1 O	-0.365648
2 C	0.185380
3 H	0.090134
4 H	0.090134
-----	-----
Sum of atomic charges =	0.000000

Related Dipole Moment = 2.8917
(X 0.0000 Y 0.0000 Z -2.8917)

ESP charges for excited states

	1	2	3
1	-0.0914159	-0.0518477	-0.3150189
2	-0.3737757	-0.5369765	0.2755906
3	0.2325958	0.2944121	0.0197142
4	0.2325958	0.2944121	0.0197141

- 1 Potential Energy Scan
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TDDFT excitation energies

- TDDFT working equation is

$$\begin{pmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{B} & \mathbf{A} \end{pmatrix} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix} = \Delta E \begin{pmatrix} \mathbf{X} \\ -\mathbf{Y} \end{pmatrix}$$

Hirata and Head-Gordon, Chem. Phys. Lett. 302, 375 (1999);

TDDFT excitation energies

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$$\begin{pmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{B} & \mathbf{A} \end{pmatrix} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix} = \Delta E \begin{pmatrix} \mathbf{X} \\ -\mathbf{Y} \end{pmatrix}$$

- We can write the vertical excitation energy (VEE) as

$$\begin{aligned} \Delta E &= \Delta E_1 + \Delta E_2 \\ \Delta E_1 &= \sum_{ai} (X_{ai}^2 + Y_{ai}^2) (\varepsilon_a - \varepsilon_i) \\ \Delta E_2 &= \Delta E_{2,J} + \Delta E_{2,K} + \Delta E_{2,XC} \end{aligned}$$

Hirata and Head-Gordon, Chem. Phys. Lett. 302, 375 (1999);
Mol. Phys. 108, 2791 (2010).

TDDFT excitation energies

- TDDFT working equation is

$$\begin{pmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{B} & \mathbf{A} \end{pmatrix} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix} = \Delta E \begin{pmatrix} \mathbf{X} \\ -\mathbf{Y} \end{pmatrix}$$

- We can write the vertical excitation energy (VEE) as

$$\begin{aligned} \Delta E &= \Delta E_1 + \Delta E_2 \\ \Delta E_1 &= \sum_{ai} (X_{ai}^2 + Y_{ai}^2) (\varepsilon_a - \varepsilon_i) \\ \Delta E_2 &= \Delta E_{2,J} + \Delta E_{2,K} + \Delta E_{2,XC} \end{aligned}$$

- VEE can be decomposed for
 - pure and hybrid functionals
 - two range-separated functionals: ω B97X-D and LRC- ω PBEh
 - Results are slightly off for pure basis sets

Hirata and Head-Gordon, Chem. Phys. Lett. 302, 375 (1999);
Mol. Phys. 108, 2791 (2010).

Sample Input: H₂CO

```
$molecule
0 1
O
C,1,R1
H,2,R2,1,A
H,2,R2,1,A,3,180.
```

```
R1=1.4
R2=1.0
A=120.
$end
```

```
$rem
method                wB97X-D
basis                 6-31++G**
cis_n_roots           5
rpa                   2
cis_dynamic_mem       false      #use old TDDFT implementation
excit_energy_components true
$end
```

- HOMO: -0.369; LUMO: -0.028; **Gap: 9.279 eV**

- Output file:

```
Excited state 1: excitation energy (eV) = 2.1475
Total energy for state 1: -114.33552540 au
Multiplicity: Triplet
Trans. Mom.: 0.0000 X 0.0000 Y 0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9968
Details -- H: 26.7523 J1: -28.3251 K1: 8.1581 XC1: 3.0430
           J2: 0.0000 K2: -7.1299 XC2: -0.3510 Total: 2.1475
```

dE1 = 9.6283 eV; dE2 = -7.4809 eV #not shown in output

```
Excited state 3: excitation energy (eV) = 2.8774
Total energy for state 3: -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X -0.0000 Y -0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9963
Details -- H: 28.4549 J1: -30.3332 K1: 8.1053 XC1: 3.2048
           J2: 0.6325 K2: -6.9064 XC2: -0.2806 Total: 2.8774
```

dE1 = 9.4318 eV; dE2 = -6.5545 eV #not shown in output

● HOMO: -0.369; LUMO: -0.028; **Gap: 9.279 eV**

● Output file:

```
Excited state 1: excitation energy (eV) = 2.1475
Total energy for state 1: -114.33552540 au
Multiplicity: Triplet
Trans. Mom.: 0.0000 X 0.0000 Y 0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9968
Details -- H: 26.7523 J1: -28.3251 K1: 8.1581 XC1: 3.0430
           J2: 0.0000 K2: -7.1299 XC2: -0.3510 Total: 2.1475
```

dE1 = 9.6283 eV; dE2 = -7.4809 eV #not shown in output

```
Excited state 3: excitation energy (eV) = 2.8774
Total energy for state 3: -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X -0.0000 Y -0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9963
Details -- H: 28.4549 J1: -30.3332 K1: 8.1053 XC1: 3.2048
           J2: 0.6325 K2: -6.9064 XC2: -0.2806 Total: 2.8774
```

dE1 = 9.4318 eV; dE2 = -6.5545 eV #not shown in output

● HOMO-LUMO gap >> lowest singlet/triplet excitation energies

● Why is the triplet state lower in energy?

```
Excited state 1: excitation energy (eV) = 2.1475
Total energy for state 1: -114.33552540 au
Multiplicity: Triplet
Trans. Mom.: 0.0000 X 0.0000 Y 0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9968
Details -- H: 26.7523 J1: -28.3251 K1: 8.1581 XC1: 3.0430
J2: 0.0000 K2: -7.1299 XC2: -0.3510 Total: 2.1475
dE1 = 9.6283 eV; dE2 = -7.4809 eV #not shown in output
```

```
Excited state 3: excitation energy (eV) = 2.8774
Total energy for state 3: -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X -0.0000 Y -0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9963
Details -- H: 28.4549 J1: -30.3332 K1: 8.1053 XC1: 3.2048
J2: 0.6325 K2: -6.9064 XC2: -0.2806 Total: 2.8774
dE1 = 9.4318 eV; dE2 = -6.5545 eV #not shown in output
```

● Why is the triplet state lower in energy?

```
Excited state 1: excitation energy (eV) = 2.1475
Total energy for state 1: -114.33552540 au
Multiplicity: Triplet
Trans. Mom.: 0.0000 X 0.0000 Y 0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9968
Details -- H: 26.7523 J1: -28.3251 K1: 8.1581 XC1: 3.0430
J2: 0.0000 K2: -7.1299 XC2: -0.3510 Total: 2.1475
dE1 = 9.6283 eV; dE2 = -7.4809 eV #not shown in output
```

```
Excited state 3: excitation energy (eV) = 2.8774
Total energy for state 3: -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X -0.0000 Y -0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9963
Details -- H: 28.4549 J1: -30.3332 K1: 8.1053 XC1: 3.2048
J2: 0.6325 K2: -6.9064 XC2: -0.2806 Total: 2.8774
dE1 = 9.4318 eV; dE2 = -6.5545 eV #not shown in output
```

● The J2 tem is

$$\Delta E_{2,J} = \iint \rho_{\text{trans}}(\mathbf{r}_1) \frac{1}{r_{12}} \rho_{\text{trans}}(\mathbf{r}_2) d\mathbf{r}_1 d\mathbf{r}_2$$

● Why is the triplet state lower in energy?

```
Excited state 1: excitation energy (eV) = 2.1475
Total energy for state 1: -114.33552540 au
Multiplicity: Triplet
Trans. Mom.: 0.0000 X 0.0000 Y 0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9968
Details -- H: 26.7523 J1: -28.3251 K1: 8.1581 XC1: 3.0430
J2: 0.0000 K2: -7.1299 XC2: -0.3510 Total: 2.1475
dE1 = 9.6283 eV; dE2 = -7.4809 eV #not shown in output
```

```
Excited state 3: excitation energy (eV) = 2.8774
Total energy for state 3: -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X -0.0000 Y -0.0000 Z
Strength : 0.0000000000
X: D( 8) --> V( 1) amplitude = 0.9963
Details -- H: 28.4549 J1: -30.3332 K1: 8.1053 XC1: 3.2048
J2: 0.6325 K2: -6.9064 XC2: -0.2806 Total: 2.8774
dE1 = 9.4318 eV; dE2 = -6.5545 eV #not shown in output
```

● The J2 tem is

$$\Delta E_{2,J} = \iint \rho_{\text{trans}}(\mathbf{r}_1) \frac{1}{r_{12}} \rho_{\text{trans}}(\mathbf{r}_2) d\mathbf{r}_1 d\mathbf{r}_2$$

● The transition density, $\rho_{\text{trans}}(\mathbf{r})$, is zero for triplet excitations.

● TDDFT with B3LYP functional:

```

Excited state   3: excitation energy (eV) =    2.8422
Total energy for state   3:                -114.21958212 au
Multiplicity: Singlet
Trans. Mom.:  0.0000 X  -0.0000 Y  -0.0000 Z
Strength      :      0.0000000000
X: D( 8) --> V( 1) amplitude =  0.9998
Details -- H:   28.8102 J1:  -30.6356 K1:    4.2395   XC1:    3.0889
              J2:   0.6445 K2:   -3.0329   XC2:   -0.2723 Total:    2.8422
dE1 = 5.5030 eV;    dE2 = -2.6607 eV      #not shown in output
HOMO: -0.297; LUMO: -0.098; Gap: 5.415 eV  #not shown in output

```

● TDDFT with ω B97X-D functional:

```

Excited state   3: excitation energy (eV) =    2.8774
Total energy for state   3:                -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X  -0.0000 Y  -0.0000 Z
Strength      :      0.0000000000
X: D( 8) --> V( 1) amplitude =  0.9963
Details -- H:   28.4549 J1:  -30.3332 K1:    8.1053   XC1:    3.2048
              J2:   0.6325 K2:   -6.9064   XC2:   -0.2806 Total:    2.8774
dE1 = 9.4318 eV;    dE2 = -6.5545 eV      #not shown in output
HOMO: -0.369; LUMO: -0.028; Gap: 9.279 eV  #not shown in output

```

● TDDFT with B3LYP functional:

```

Excited state   3: excitation energy (eV) =    2.8422
Total energy for state   3:                -114.21958212 au
Multiplicity: Singlet
Trans. Mom.:  0.0000 X  -0.0000 Y  -0.0000 Z
Strength      :      0.0000000000
X: D( 8) --> V( 1) amplitude =  0.9998
Details -- H:   28.8102 J1:  -30.6356 K1:    4.2395   XC1:    3.0889
              J2:    0.6445 K2:   -3.0329   XC2:   -0.2723 Total:    2.8422
dE1 = 5.5030 eV;    dE2 = -2.6607 eV      #not shown in output
HOMO: -0.297; LUMO: -0.098; Gap: 5.415 eV  #not shown in output

```

● TDDFT with ω B97X-D functional:

```

Excited state   3: excitation energy (eV) =    2.8774
Total energy for state   3:                -114.30870220 au
Multiplicity: Singlet
Trans. Mom.: -0.0000 X  -0.0000 Y  -0.0000 Z
Strength      :      0.0000000000
X: D( 8) --> V( 1) amplitude =  0.9963
Details -- H:   28.4549 J1:  -30.3332 K1:    8.1053   XC1:    3.2048
              J2:    0.6325 K2:   -6.9064   XC2:   -0.2806 Total:    2.8774
dE1 = 9.4318 eV;    dE2 = -6.5545 eV      #not shown in output
HOMO: -0.369; LUMO: -0.028; Gap: 9.279 eV  #not shown in output

```

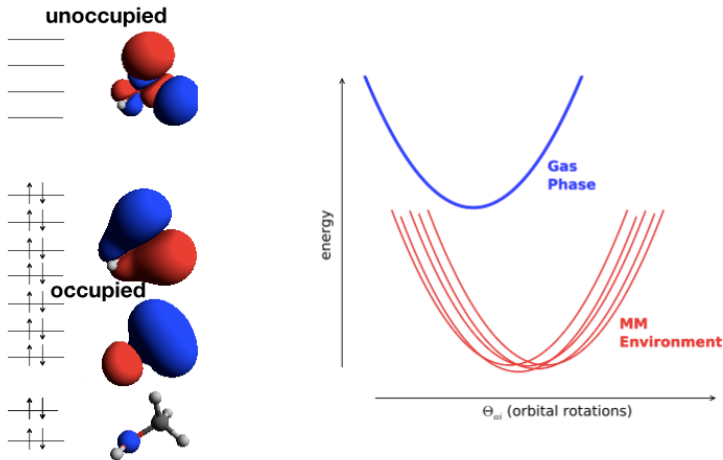
● The **K2** term is

$$\Delta E_{2,K}(\text{PBE0}) = - \int \int \rho_{\text{detach}}(\mathbf{r}_1) \frac{0.25}{r_{12}} \rho_{\text{attach}}(\mathbf{r}_2) d\mathbf{r}_1 d\mathbf{r}_2$$

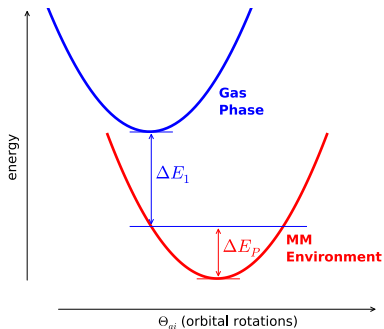
$$\Delta E_{2,K}(\omega\text{B97X} - \text{D}) = - \int \int \rho_{\text{detach}}(\mathbf{r}_1) \frac{0.22 \operatorname{erfc}(\omega r_{12}) + \operatorname{erf}(\omega r_{12})}{r_{12}} \rho_{\text{attach}}(\mathbf{r}_2) d\mathbf{r}_1 d\mathbf{r}_2$$

- 1 Potential Energy Scan
- 2 Electrostatic-Potential-Derived (ESP) Charges
- 3 Decomposition of TDDFT excitation energies
- 4 Multiple-Environment Single-System QM/MM**
- 5 General Research Interest

Multiple-Environment Single-System QM/MM (MESS-QM/MM): QM/MM Calculations with a Fixed-Geometry QM Region



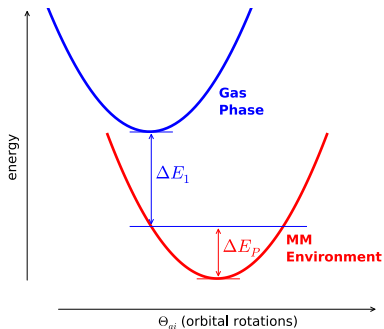
MESS-QM/MM: Fast Estimation of QM/MM Energy



J. Phys. Chem. A, 119, 1511 (2015); J. Chem. Theory Comput., 12, 332 (2016); 13, 679 (2017).

MESS-QM/MM: Fast Estimation of QM/MM Energy

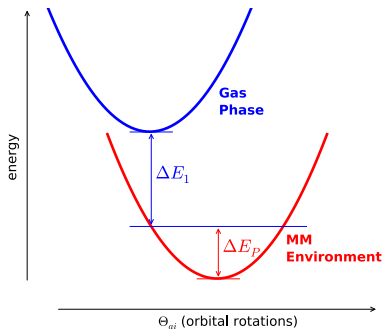
- Assume a quadratic surface



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MESS-QM/MM: Fast Estimation of QM/MM Energy

- Assume a quadratic surface
- Compute the Hessian for a reference environment

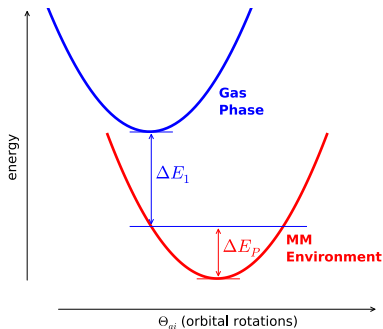


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MESS-QM/MM: Fast Estimation of QM/MM Energy

- Assume a quadratic surface
- Compute the Hessian for a reference environment
- For each MM environment
 - Compute the gradient (g)
 - Take a Newton step

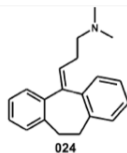
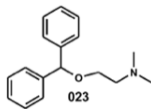
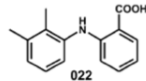
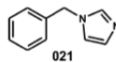
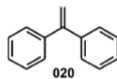
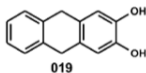
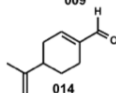
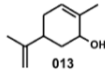
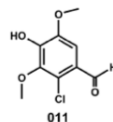
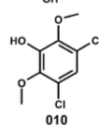
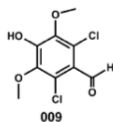
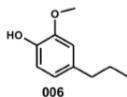
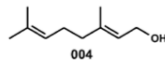
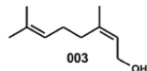
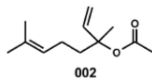
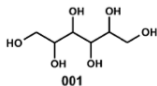
$$\Delta\Theta = \mathbf{H}^{-1} \cdot g$$



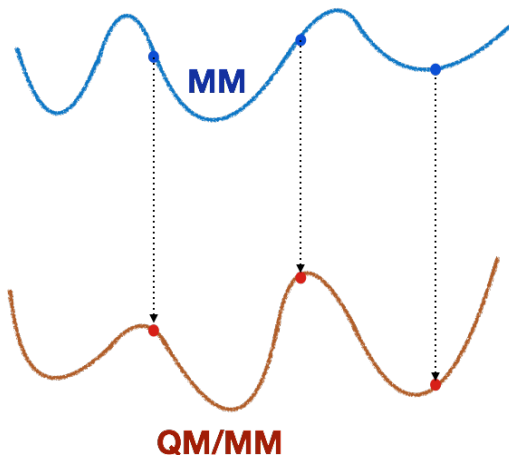
- Potential applications:
 - solvation free energies
 - enzymatic reaction free energy profiles
 - polarizable force-field development

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Hydration Free Energy Calculations



Computational Strategy



Step 1: Compute hydration free energy using MM energy functions.
Solvent: >1500 TIP3P water

Step 2: Compute QM/MM energy on some MM configurations. Obtain QM/MM correction to the hydration free energy.
QM region: solute

QM/MM Hydration Free Energy Calculations

- Computational Efficiency
 - MM: 100 CPU Hours
 - QM/MM correction: 400-2700 CPU Hours

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QM/MM Hydration Free Energy Calculations

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 - MM: 100 CPU Hours
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 - Our accelerated QM/MM correction: 7-12 CPU Hours
 - Assumes a fixed geometry for the solute (QM region)
 - Difference in hydration free energy predictions: <0.2 kcal/mol

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- Computational Accuracy

Error (kcal/mol)	MM	After QM/MM correction
		BLYP
MSE	-1.15	-0.63
RMSE	1.80	1.07

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Error (kcal/mol)	MM	After QM/MM correction				
		BLYP	B3LYP	PBE0	M06-2X	ω B97X-D
MSE	-1.15	-0.63	-1.42	-1.95	-1.97	-2.13
RMSE	1.80	1.07	1.70	2.18	2.22	2.37

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- More sophisticated functionals yielded worse results.

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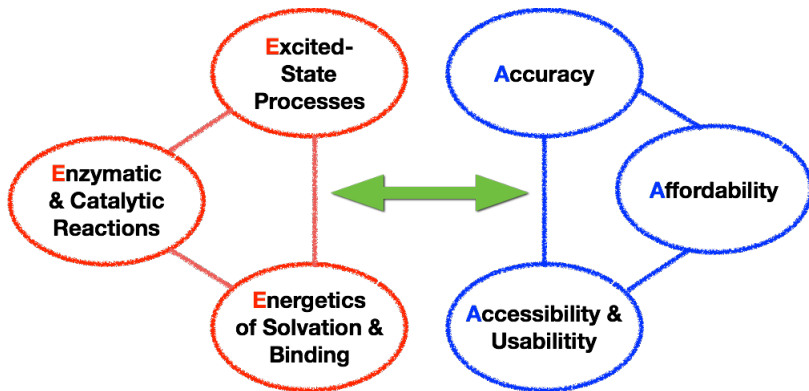
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- More sophisticated functionals yielded worse results.
- We also need to improve QM/MM vdW interactions.

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- 3 Decomposition of TDDFT excitation energies
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- 5 General Research Interest**

Computational Chemistry: Applications, Theory and Software



Main Topics

- Fluorescence/bioluminescence, reaction rates, binding affinity
- Chemical, solvent, macromolecular, methodological perturbations

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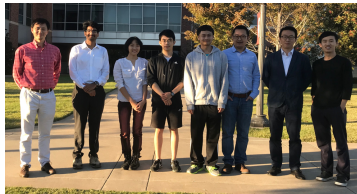
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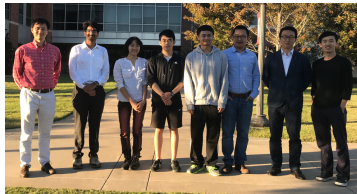
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