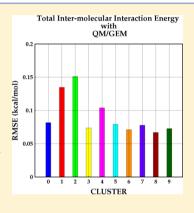


# OM/MM Simulations with the Gaussian Electrostatic Model: A **Density-based Polarizable Potential**

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Supporting Information

ABSTRACT: The use of advanced polarizable potentials in quantum mechanical/molecular mechanical (QM/MM) simulations has been shown to improve the overall accuracy of the calculation. We have developed a density-based potential called the Gaussian electrostatic model (GEM), which has been shown to provide very accurate environments for QM wave functions in QM/MM. In this contribution we present a new implementation of QM/GEM that extends our implementation to include all components (Coulomb, exchange-repulsion, polarization, and dispersion) for the total intermolecular interaction energy in QM/MM calculations, except for the charge-transfer term. The accuracy of the method is tested using a subset of water dimers from the water dimer potential energy surface reported by Babin et al. (J. Chem. Theory Comput. 2013 9, 5395-5403). Additionally, results of the new implementation are contrasted with results obtained with the classical AMOEBA potential. Our results indicate that GEM provides an accurate MM environment with average rootmean-square error <0.15 kcal/mol for every intermolecular interaction energy component compared with SAPT2+3/aug-cc-pVTZ reference calculations.



he accurate and reliable study of large systems, such as biomolecules, remains a challenge for the quantum

Table 1. Clusters Obtained with the k-Means Clustering Approach, Their Populations and the O-O Distances of the Centroids

cluster	population	$r_{ m O-O}^{ m centroid}$ (Å)
0	347	5.332
1	464	4.882
2	894	4.381
3	321	5.402
4	378	5.312
5	323	5.383
6	447	5.429
7	267	5.351
8	264	5.353
9	369	5.423

chemistry community. Hybrid QM/MM simulations have become one of the standard methods for the study of reaction mechanisms in biochemical and condensed-phase chemical systems. 1-3 The accuracy of these simulations depends on two factors, the level of theory/basis set employed for the QM subsystem<sup>4-10</sup> and the classical potential for the MM subsystem. 11-14 The former has received a significant amount of attention, whereas the latter has lagged behind. Most classical force fields approximate the energy of the system by summing bonded and nonbonded interactions. Conventional nonpolarizable potentials generally use atom-centered point charges to approximate the Coulomb interactions and a Lennard-Jones function for van der Waals (vdW) interactions. The use of point charges in close proximity to the QM wave function can result in the overpolarization of the QM subsystem. 15,16 This problem can be addressed by using delocalized charges or by using molecular density-based potentials. 11,17-20 Several methods that reproduce the electronic charge density have been proposed to improve the accuracy of electrostatic interactions. <sup>21–24</sup> New force fields have been introduced to prevent the loss of anisotropy by employing distributed multipoles<sup>25–27</sup> yet have failed to provide correct charge penetration effects at close range.<sup>28,29</sup> However, this shortcoming can be avoided by employing damping functions

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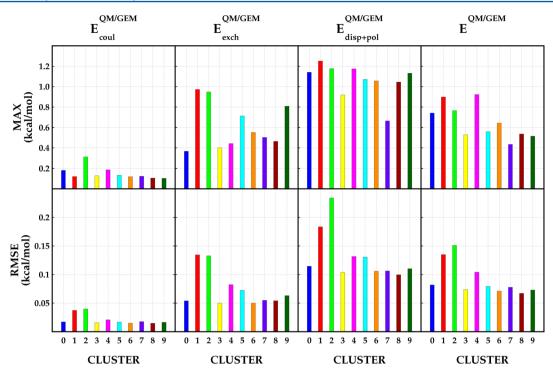
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**Figure 1.** Errors per cluster with respect to SAPT. The errors corresponding to the Coulomb interaction energy are depicted on the first column, and the errors corresponding to the exchange interaction energy are given on the second column. The computed errors for the sum of dispersion and polarization energies are depicted on the third, while the error for total energy is given on the fourth column.

or by a continuous description of the molecular charge density.  $^{11,13}$ 

The Gaussian electrostatic model (GEM), has been developed to provide an accurate potential based on molecular electronic densities.<sup>30-33</sup> GEM uses the density fitting formalism to expand the molecular density with Hermite Gaussian functions. In this method, the molecular electronic density fitting is performed by the minimization of the error of the Coulomb self-interaction energy, <sup>30,34–37</sup> where the approximate density  $\tilde{\rho}(r)$  is expanded with the use of auxiliary Hermite Gaussian basis functions (ABS). After the calculation of the Hermite coefficients with the density fitting procedure, distributed multipoles can also be obtained. <sup>31,38,39</sup> The fitted densities are then employed to calculate each term in the QM energy decomposition analysis (EDA), that is, Coulomb, exchange, polarization, charge transfer, and dispersion.<sup>3</sup> GEM has been shown to produce accurate energies and forces for a range of systems. The present method is similar in spirit to the polarizable density embedding (PDE). 40,41 Recently, an approximate version of GEM, termed GEM\*, has been developed to enable the use of the GEM densities in molecular dynamics (MD) simulations.<sup>42</sup> This new force field has been implemented in a modified version of pmemd, pmemd.gem, in the AMBER suite of programs. The functional form for GEM\* combines frozen core contributions (Coulomb and exchange-repulsion) from GEM, with the polarization, (modified) vdW, and bonded terms from AMOEBA. It has also been previously shown that the use of GEM in a QM/MM implementation can provide a significantly more accurate electrostatic environment. 11 However, that work focused exclusively on the electrostatic interactions between the QM and MM subsystems.

In this work, we present the first implementation of GEM for QM/MM calculations, QM/GEM, which involves all of the

components of the total intermolecular interaction energy, except for the charge-transfer term. To our knowledge, this is the first implementation of a QM/MM program where the MM environment is explicitly represented by molecular electron density used to calculate separate Coulomb, exchange, polarization, and dispersion contributions.

The total energy of the system in QM/GEM calculations can be written as

$$E_{\rm Tot} = E^{\rm QM} + E^{\rm GEM} + E^{\rm QM/GEM} \tag{1}$$

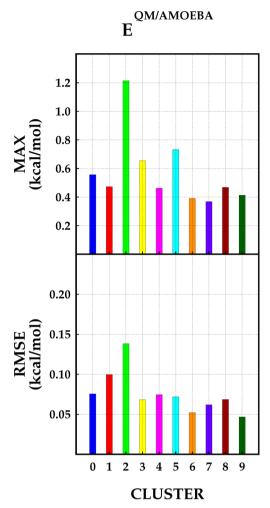
The last term in eq 1 corresponds to the intermolecular interactions between the QM and MM subsystems, which can be separated as

$$E^{\rm QM/GEM} = E^{\rm QM/GEM}_{\rm Coul} + E^{\rm QM/GEM}_{\rm exch} + E^{\rm QM/GEM}_{\rm pol} + E^{\rm QM/GEM}_{\rm disp}$$
 (2)

where  $E_{\mathrm{Coul}}^{\mathrm{QM/GEM}}$  is the Coulomb interaction,  $E_{\mathrm{exch}}^{\mathrm{QM/GEM}}$  corresponds to the exchange—repulsion between the GEM densities and the QM wave function, and  $E_{\mathrm{pol}}^{\mathrm{QM/GEM}}$  and  $E_{\mathrm{disp}}^{\mathrm{QM/GEM}}$  represent the polarization and dispersion between the two subsystems. In this implementation the exchange—repulsion component can be computed after a successful SCF cycle

$$E_{\text{exch}}^{\text{QM/GEM}} = K_{\text{exch}} \int \rho^{\text{A}}(r_{\text{A}}) \tilde{\rho}^{\text{B}}(r_{\text{B}}) dr_{\text{A}} dr_{\text{B}}$$
(3)

where  $K_{\rm exch}$  is the proportionality parameter,  $\rho^{\rm A}(r_{\rm A})$  denotes the electronic density of molecule A corresponding to the QM subsystem, and  $\tilde{\rho}^{\rm B}(r_{\rm B})$  is the GEM density for molecule B in the MM subsystem. Alternatively, the exchange–repulsion term can be explicitly included in the effective Hamiltonian,  $H_{\rm eff}$  similar to recent work by Giovannini et al. In our implementation, the modified external potential includes both



**Figure 2.** Total intermolecular interaction energy errors per cluster for QM/AMOEBA with respect to SAPT.

the GEM Coulomb and exchange fields (see the Supporting Information)

$$\hat{H}_{\rm eff} = \hat{H}_{\rm core} + \hat{V}_{\rm GEM} \tag{4}$$

$$\hat{V}_{\text{GEM}} = \sum_{l} x_{l} \sum_{\mu\nu} \langle \mu\nu | l \rangle + K'_{\text{exch}} \sum_{l} x_{l} \sum_{\mu\nu} \langle \mu\nu | l \rangle_{S}$$
 (5)

This implementation of QM/GEM uses LICHEM<sup>12</sup> to interface a modified version of Psi4 to calculate the required three center Coulomb and overlap integrals, with TINKER to calculate the polarization and dispersion terms (see the Supporting Information). 44-46 In this initial implementation, the GEM densities for each MM subsystem are fitted individually (at the  $\omega$ B97XD/aug-cc-pVTZ level) for each dimer instead of using the same fitted density for every MM subsystem as in our previous implementation. <sup>11</sup> Consequently, two different scenarios are taken into account for each dimer within the subset, first monomer under the field of the second monomer and vice versa. These fitted densities are used for the evaluation of the Coulomb and overlap integrals needed for the calculation of  $E_{\text{Coul}}^{\text{QM/GEM}}$  and  $E_{\text{exch}}^{\text{QM/GEM}}$ . The fitting is performed using either Cholesky decomposition (Chol) or Tychonov regularization (Tych).<sup>47</sup> For the latter, a total molecular charge constraint (via Lagrange multipliers) is applied to ensure that the density integrates to the correct number of electrons.<sup>11</sup> Furthermore, the accuracy of the fitting with the Tychonov

regularization is tuned by optimizing the eigenvalue cutoff,  $\lambda$ .<sup>11</sup> We have previously shown that the optimal fitting for Coulomb may not provide the best reproduction of the density for the exchange—repulsion interaction.<sup>11</sup> Thus a case is also considered where sets of fitting coefficients are obtained for each term ( $\lambda_1$  for Coulomb and  $\lambda_2$  for exchange—repulsion).

The exchange-repulsion term is calculated by means of the Wheatley-Price overlap model via the two implemented methods described above (see eqs 3-5 and the Supporting Information). 48,49 The proportionality parameter for the exchange term after SCF (eq 3),  $K_{\text{exch}}$ , is calculated via leastsquares fitting and is fitted to reproduce the corresponding EDA components obtained from SAPT2+3 for a fitting set that correspond to the 10 water dimers, as reported by Tschumper et al. (see the Supporting Information). 50 The proportionality parameter  $K'_{\text{exch}}$  for the combined Coulomb and exchangerepulsion embedding (eqs 4 and 5) has been fitted by an iterative process. Here the exchange-repulsion embedding included in  $\hat{H}_{\mathrm{eff}}$  affects the QM density and thus results in a different response depending on the value of  $K'_{\text{exch}}$ . Therefore,  $K'_{\text{exch}}$  is fitted iteratively using least-squares fitting to the SAPT2+3 reference for the same 10 water dimer set (see the Supporting Information). The calculated proportionality parameters are similar to previously reported parameters for GEM\* and GEM.11,42

The QM/MM polarization component is computed based on the AMOEBA model by approximating the QM wave function using the procedure employed in LICHEM including Tholé damping. This method has been show to account for >80% of the total QM/MM polarization component. 12 The dispersion component is calculated by employing three terms of the dispersion expansion and fitting the required  $C_n$  (n = 6, 8, 10) coefficients to the same 10 dimer reference set as for the exchange-repulsion term. The results for the total intermolecular interactions calculated with QM/GEM are compared with the total intermolecular energy obtained from the SAPT2+3 reference and with QM/AMOEBA. 12,27,51-53 Therefore, this implementation comprises direct embedding from the two first-order terms ( $E_{\rm Coul}^{\rm QM/GEM}$  and  $E_{\rm exch}^{\rm QM/GEM}$ ) and two responses from the MM environment ( $E_{\rm pol}^{\rm QM/GEM}$  and  $E_{\rm disp}^{\rm QM/GEM}$ ) calculated after the SCF cycle. All QM/GEM calculations have been performed using the  $\omega$ B97XD/aug-cc-pVTZ level for the QM subsystem. <sup>44,54–56</sup> The GEM density has been fitted using two auxiliary basis sets. 11 Results for the A2DG auxiliary basis set are discussed below (results with A2 are provided in the Supporting Information).

The capability of this initial QM/GEM implementation is assessed by comparing total and component-wise intermolecular interactions for a subset of the water dimer potential energy surface (PES) reported by Paesani and coworkers. A QM EDA has been performed on the full data set at the SAPT2+3/aug-cc-pVTZ level, as implemented in Psi4 (see the Supporting Information). The population of the Paesani data set has been reduced to the subset of water dimers that involve monomers with internal structures similar to the AMOEBA equilibrium geometry (see the Supporting Information). 59 The distances and angles that are taken into account and their nomenclature are depicted in Figure S.2. The final subset corresponds to dimers with AMOEBA angle and bond energies  $\leq$ 10 kcal/mol, H-O-H angles of 98.0 <  $\theta$  <  $118.0^{\circ}$ , H-O bond distances of 0.87 < r < 1.07 Å, and O-O intermonomer distances >3.2 Å (see Figure S.3 and Table S.1). The resulting subset contains 4074 dimers, 2356(1718) of which have attractive(repulsive) total intermolecular interaction energy. The resulting subset of water dimers is further subdivided into 10 different clusters using the k-means clustering method, as implemented in the Scikit-learn<sup>60</sup> package to facilitate the error analysis. The centroids for the clusters are defined by using the same geometrical criteria that are used to form the subset (see the Supporting Information). The nomenclature of the clusters, their population, and the intermolecular O–O distance of the centroids  $(r_{\rm O-O}^{\rm centroid})$  are depicted in Table 1.

Figure 1 shows the calculated maximum unsigned error (MAX) and root-mean-square error (RMSE) obtained with Tychonov regularization using  $\lambda_1 = 0.00003$  for Coulomb interactions and  $\lambda_2 = 0.001$  for exchange-repulsion interactions. The component-by-component comparison is presented for the Coulomb ( $E_{\rm Coul}^{\rm QM/GEM}$ ) and exchange—repulsion  $(E_{
m exch}^{
m QM/GEM})$  terms. The errors for the polarization and dispersion terms  $(E_{
m disp+pol}^{
m QM/GEM})$  are presented together to enable their comparison with the induction and dispersion terms from the SAPT2+3 reference calculations (see the Supporting Information for detailed decomposition results). The error analysis for results obtained via Cholesky decomposition and Tychonov regularization using only  $\lambda_1$  and exchange—repulsion terms computed after SCF cycle are provided in the Supporting Information. The calculated RMSE (MAX) for the Coulomb term is below 0.05 kcal/mol (0.2 kcal/mol), with the exception of MAX = 0.3 kcal/mol for cluster 2, compared with the Cholesky decomposition, where three clusters are observed to have MAX > 0.2 kcal/mol (1, 2, and 4). About 92% of all 4074 water dimers exhibit unsigned error (UE) for  $E_{\text{Coul}}^{\text{QM/GEM}} \leq 0.05$ kcal/mol when the fitting is performed with the Tychonov regularization compared with 87% of dimers fitted using the Cholesky decomposition.

As expected, the exchange-repulsion results are found to be more accurate with the Tychonov regularization using  $\lambda_1$  and  $\lambda_2$ , with calculated MAX(RMSE) for all dimers below 1.0(0.15) kcal/mol (Figure 1). Conversely, when only one set of Hermite coefficients (optimized for Coulomb) or when the Cholesky decomposition is used for exchange-repulsion, the MAX-(RMSE) is observed to increase above 1.0(0.2) kcal/mol for almost half of the clusters (Figures S.4 and S.5). About 86% of the water dimers have UE  $\leq 0.1$  kcal/mol using the Tychonov method with individual fitting for Coulomb and exchangerepulsion ( $\lambda_1$  and  $\lambda_2$ ), while 83 and 82% of the water dimers have UE ≤ 0.1 kcal/mol without individual fitting using the Tychonov regularization or Cholesky decomposition, respectively. Computing the exchange-repulsion term after SCF cycle results in higher errors, where ~80% of the water dimers have UE ≤ 0.1 kcal/mol for both Tychonov method without individual fitting and Cholesky decomposition (see the Supporting Information).

The errors for the polarization+dispersion term are larger than for the frozen core (Coulomb and exchange-repulsion) terms for all of the fitting schemes, with RMSE values below 0.15 kcal/mol for most clusters and MAX > 1.0 kcal/mol for almost every cluster, regardless of the fitting method. The decrease in accuracy for these two components is mainly due to the approximations used for the calculation of these two terms and the lack of the charge transfer term. Nevertheless,  $\sim$ 78% of the water dimers have UE  $\leq$  0.1 kcal/mol irrespective of the fitting method.

For the total intermolecular interaction, the RMSE(MAX) for almost all clusters is observed to be <0.1(0.8) kcal/mol

except for clusters 1 and 2 (1 and 4) (RMSE  $\leq$  0.15; MAX < 1.0 kcal/mol) with Tychonov regularization using  $\lambda_1$  and  $\lambda_2$ . Similar errors are observed with the other two fitting schemes (Cholesky and Tychonov with only one  $\lambda$ ), although the maximum and RMS errors are increased to 1.2 kcal/mol for three clusters.

Figure 2 shows the MAX and RMSE values for the dimers subset, calculated at the same QM level of theory ( $\omega$ B97XD/ aug-cc-pVTZ) using the AMOEBA potential to represent the MM environment. The overall RMSE with AMOEBA is similar to those observed with GEM. Both methods result in UE  $\leq 0.4$ kcal/mol for ~99% of the water dimers. However, three dimers have UE > 1.0 kcal/mol with AMOEBA compared with GEM. This is mostly due to the penetration error because the high UE dimers in AMOEBA, which have intermolecular distances <2.0 Å, are well within the region of intermolecular density overlap. In the case of GEM, only one dimer has 1.0 kcal/mol > UE > 0.9 kcal/mol. This dimer has intramolecular angles of 98.9 and 105.3°, indicating that the error is likely arising due to the intramolecular strain of the monomers. It should be noted that in our current implementation the computational cost of the QM/GEM calculation is roughly five times more expensive than for QM/AMOEBA. This is due to the fact that the density of the molecule in the MM subsystem is fitted explicitly each time (as described above). However, as we have previously reported, prefitted densities can be employed,<sup>32</sup> which will significantly improve the computational efficiency in subsequent implementations.

Overall, it is observed that the use of AMOEBA provides an accurate representation for the total intermolecular interaction. However, the comparison of the Coulomb intermolecular interaction reveals that the term-by-term interactions have reduced accuracy (see the Supporting Information). Thus the accuracy of the total intermolecular interaction with AMOEBA is mostly due to error cancellation between the Coulomb, polarization and buffered Halgren terms. Similar results for AMOEBA as an embedding environment in close proximity of a QM wave function have been previously reported. <sup>19</sup>

In summary, we have presented an initial implementation of QM/GEM involving four energy components for the GEM subsystem. The results indicate that GEM provides a very accurate environment in a QM/MM setting with the additional advantage of a physically intuitive decomposition of the intermolecular interaction terms. The average RMSE is <0.2 kcal/mol for every term as well as for the total energy, with MAX below 1.0 kcal/mol for second-order and total interactions and 0.2 kcal/mol for the frozen-core terms. The introduction of a total molecular charge constraint to ensure that the density integrates to the correct number of electrons, coupled to the individual optimization of eigenvalue cutoffs for Coulomb and exchange-repulsion, is shown to improve the accuracy of the GEM environment. It is noteworthy that even with a small fitting set consisting only 10 water dimers, the accuracy of the total intermolecular interaction energy with GEM is very similar to AMOEBA, yet unlike AMOEBA, GEM does not result in MAXs over 1.0 kcal/mol. Because all of the energy components are computed individually with GEM, further improvements can be achieved by the introduction of an explicit charge-transfer term, improvement of the auxiliary basis set, or a better description for the dispersion energy term. This proof of principle constitutes an incentive toward the future application of this technology for full hybrid polarizable QM/ MD using PDE.<sup>61</sup>

## ASSOCIATED CONTENT

# **S** Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpclett.8b01412.

Scheme for subset selection, clustering details, fitting details for exchange and dispersion parameters, QM/GEM errors for subset, QM/AMOEBA errors for subset, QM/GEM results separated by monomers included in the QM subsystem, and SAPT2+3/aug-cc-pVTZ results for full Paesani PES (PDF)

Term-by-term and total intermolecular interaction energy components (XLSX)

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#### **Notes**

The authors declare no competing financial interest.

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