

# Classification and regression approaches

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**Reinforcement learning:** Developing and refining models as data arrive.

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**Clustering:** An unsupervised learning approach where data are grouped together.

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**Variance:** Change in your model's performance as different training data are used.

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Terms that will come up repeatedly: **loss** and **cost** (e.g., “minimize your loss function”). **Loss** tells us how far one prediction is from some target value; **cost** describes loss across a dataset.

**Okay, let us consider your projects — what sort of problem are you solving?**

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- Polynomial regression: A non linear regression.

# Classification algorithms

Likewise, there are many classification algorithms. You have probably heard of a few, including:

- K nearest neighbors (kNN)
- Decision trees
- Support vector machines
- Linear Discriminant Analysis (LDA)
- Naive Bayes (NB)

## On to some classification examples

Chapters 3.3 and 3.4 in the notebook

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Your predictions of  $P$  and  $N$  are made up of  $TP + FP$  and  $TN + FN$ , respectively.

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- **Accuracy**: the fraction of the data that was correctly classified:

$$acc = \frac{TP+TN}{N} = 1 - err \rightarrow 1$$

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This ratio is also the **recall** value or **sensitivity**.

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- **TN-rate:** the ratio of samples predicted in the *negative* class that are correctly classified:

$$TNR = \frac{TN}{TN+FP} \rightarrow 1$$

This ratio is also the **specificity**.

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- **Precision:** the ratio of samples predicted in the *positive* class that were indeed *positive* to the total number of samples predicted as *positive*.

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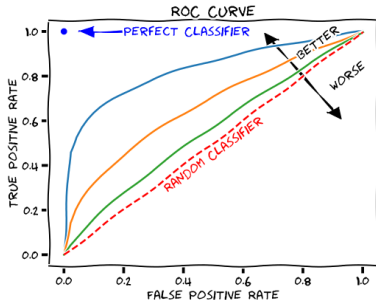
Note that, as precision increases, recall decreases.

- **F1 score:**

$$F_1 = \frac{2}{(1/precision + 1/recall)} = \frac{2TP}{2TP + (FN + FP)} \rightarrow 1.$$

## Visualizing rates

Since the classifier uses some *threshold* value to determine which label to give a datum, we can plot the true positive rate vs. the false positive rate for different thresholds. This plot is known as the *Receiver Operating Characteristics*.



**Figure 1:** An ROC plot.