

## Question 1:

```

function [ABDmatrix,distances,Qbars,Sbars] =
laminatedStiffnessMatrix(thicknesses,thetas,E1s,E2s,G12s,v12s)
    A=zeros(3);
    B=zeros(3);
    D=zeros(3);
    N=length(thicknesses);
    thickness=sum(thicknesses);
    distances=zeros(1,length(thicknesses)+1);
    distances(1)=-thickness/2;
    distances(end)=thickness/2;
    for i=2:N
        distances(i)=distances(i-1)+thicknesses(i-1);
    end
    Qbars{1}=[];
    Sbars{1}=[];
    for k=1:N
        Qbar =
transReducedStiffnessMatrix(E1s(k),E2s(k),G12s(k),v12s(k),thetas(k));
        Qbars{k}=Qbar;
    end

    for i=1:3
        for j=1:3
            for k=1:N
                A(i,j)=A(i,j)+(Qbars{k}(i,j)*(distances(k+1)-distances(k)));
                B(i,j)=B(i,j)+(Qbars{k}(i,j)*(1/2)*(distances(k+1)^2-
distances(k)^2));
                D(i,j)=D(i,j)+(Qbars{k}(i,j)*(1/3)*(distances(k+1)^3-
distances(k)^3));
            end
        end
    end
    ABDmatrix=[A,B;B,D];
end

```

## MAIN:

```

clc;clear;
E1s=[140e9,140e9,140e9,140e9,140e9,140e9];
E2s=[10e9,10e9,10e9,10e9,10e9,10e9];
G12s=[7e9,7e9,7e9,7e9,7e9,7e9];
v12s=[0.3,0.3,0.3,0.3,0.3,0.3];
thicknesses=[0.0002,0.0002,0.0002,0.0002,0.0002,0.0002];
thetas=[0,30,-30,-30,30,0];

ABDmatrix1 = laminatedStiffnessMatrix(thicknesses,thetas,E1s,E2s,G12s,v12s);

E1s=[140e9,140e9,140e9,140e9,140e9,140e9];
E2s=[10e9,10e9,10e9,10e9,10e9,10e9];
G12s=[7e9,7e9,7e9,7e9,7e9,7e9];
v12s=[0.3,0.3,0.3,0.3,0.3,0.3];
thicknesses=[0.0002,0.0002,0.0002,0.0002,0.0002,0.0002];
thetas=[30,-15,-75,20,-60,-30];

```

```
ABDmatrix2 = laminateStiffnessMatrix(thicknesses,thetas,E1s,E2s,G12s,v12s);
```

OUTPUT:

Part a:

|   | 1           | 2           | 3           | 4           | 5           | 6           |
|---|-------------|-------------|-------------|-------------|-------------|-------------|
| 1 | 1.2538e+08  | 2.1163e+07  | 0           | 3.6380e-12  | -7.3896e-13 | 4.5475e-13  |
| 2 | 2.1163e+07  | 2.0706e+07  | 0           | -7.3896e-13 | -5.6843e-13 | 2.2737e-13  |
| 3 | 0           | 0           | 2.5940e+07  | 4.5475e-13  | 2.2737e-13  | -9.0949e-13 |
| 4 | 3.6380e-12  | -7.3896e-13 | 4.5475e-13  | 17.9593     | 1.3702      | 1.3116      |
| 5 | -7.3896e-13 | -5.6843e-13 | 2.2737e-13  | 1.3702      | 1.9095      | 0.5014      |
| 6 | 4.5475e-13  | 2.2737e-13  | -9.0949e-13 | 1.3116      | 0.5014      | 1.9435      |

Part b:

|   | 1           | 2           | 3           | 4           | 5           | 6           |
|---|-------------|-------------|-------------|-------------|-------------|-------------|
| 1 | 8.8654e+07  | 2.2117e+07  | -2.5920e+06 | -4.1989e+03 | 972.3900    | -6.6143e+03 |
| 2 | 2.2117e+07  | 5.5523e+07  | -1.3413e+07 | 972.3900    | 2.2542e+03  | -4.6584e+03 |
| 3 | -2.5920e+06 | -1.3413e+07 | 2.6894e+07  | -6.6143e+03 | -4.6584e+03 | 972.3900    |
| 4 | -4.1989e+03 | 972.3900    | -6.6143e+03 | 11.7950     | 3.2539      | -0.7495     |
| 5 | 972.3900    | 2.2542e+03  | -4.6584e+03 | 3.2539      | 4.3066      | -0.8938     |
| 6 | -6.6143e+03 | -4.6584e+03 | 972.3900    | -0.7495     | -0.8938     | 3.8271      |

Problem 2:

```
function [ABDmatrixINV,distances,Qbars,Sbars] =
laminateStiffnessMatrixINV(thicknesses,thetas,E1s,E2s,G12s,v12s)

    [ABDmatrix,distances,Qbars,Sbars] =
laminateStiffnessMatrix(thicknesses,thetas,E1s,E2s,G12s,v12s);

    ABDmatrixINV=ABDmatrix^-1;
end
```

Part a:

|   | 1           | 2           | 3           | 4           | 5           | 6           |
|---|-------------|-------------|-------------|-------------|-------------|-------------|
| 1 | 9.6387e-09  | -9.8514e-09 | 1.9443e-41  | -2.5553e-21 | 2.6473e-21  | -6.1321e-23 |
| 2 | -9.8514e-09 | 5.8364e-08  | -5.6887e-40 | 4.1621e-21  | 1.3409e-20  | -1.0792e-20 |
| 3 | 1.9443e-41  | -5.6887e-40 | 3.8551e-08  | -1.8735e-21 | -8.9199e-21 | 2.1607e-20  |
| 4 | -2.5553e-21 | 4.1621e-21  | -1.8735e-21 | 0.0607      | -0.0352     | -0.0319     |
| 5 | 2.6473e-21  | 1.3409e-20  | -8.9199e-21 | -0.0352     | 0.5822      | -0.1265     |
| 6 | -6.1321e-23 | -1.0792e-20 | 2.1607e-20  | -0.0319     | -0.1265     | 0.5687      |

Part b:

|   | 1           | 2           | 3          | 4          | 5           | 6          |
|---|-------------|-------------|------------|------------|-------------|------------|
| 1 | 1.4174e-08  | -3.9382e-09 | 5.8764e-11 | 7.3647e-06 | -2.3694e-06 | 2.0577e-05 |
| 2 | -3.9382e-09 | 2.4143e-08  | 1.2420e-08 | 4.0915e-06 | 2.9358e-06  | 2.0912e-05 |
| 3 | 5.8764e-11  | 1.2420e-08  | 5.4721e-08 | 1.9257e-05 | 4.1178e-05  | 1.4704e-05 |
| 4 | 7.3647e-06  | 4.0915e-06  | 1.9257e-05 | 0.1179     | -0.0679     | 0.0200     |
| 5 | -2.3694e-06 | 2.9358e-06  | 4.1178e-05 | -0.0679    | 0.3384      | 0.0547     |
| 6 | 2.0577e-05  | 2.0912e-05  | 1.4704e-05 | 0.0200     | 0.0547      | 0.3353     |