

Assessed Exercises 1:

Exercise 1: Tennis

Part 1 – Writing the Tennis Class:

Created a class called TennisMatch, which stores the variables of a game and has a game loop function. It is interacted with via the console asking for the winning player of each round.

```
1  ✓ #include <iostream>
2  #include <string>
3  #include <iomanip> //setw
4
5  ✓ class TennisMatch{
6
7      private:
8
9          // Private Variables
10     int score1= 0; int score2 = 0; int games1 = 0; int games2 = 0; //points and games
11     int server = 1; //This keeps track of server (either 1 or 2)
12     std::string player1, player2;
13     bool running = true;
14     int gameWinner = 0;
15
16     // Functions
17     void addScoreToWinner(){ //Takes and input and adds the points to the round winner.
18         int lastWinner;
19         std::cout << "\n";
20         std::cout << "Input winner: ";
21         std::cin >> lastWinner;
22         std::cout << "\n" << std::endl;
23
24         if (lastWinner==1){
25             score1++;
26         }
27         if (lastWinner==2){
28             score2++;
29         }
30     }
31 }
```

```

33 void announcement(){ // Umpire Announces in "english" rather than scores.
34
35     std::cout << "===== " << std::endl;
36     if (gameWinner == 1){
37         std::cout << "Umpire : game, " << player1 <<std::endl;
38         gameWinner = 0;
39     }
40     if (gameWinner==2){
41         std::cout << "Umpire : game, " << player2 <<std::endl;
42         gameWinner = 0;
43     }

```

```

44
45     //Non server reliant annoucments
46     if (score1==0 && score2==0){
47         std::cout << "Umpire: " << "love-all" << std::endl;
48     }
49     if (score1==1 && score2==1){
50         std::cout << "Umpire: " << "fifteen-all" << std::endl;
51     }
52     if (score1==2 && score2==2){
53         std::cout << "Umpire: " << "thirty-all" << std::endl;
54     }
55     if ((score1>=3 && score2>=3) && (score1 == score2)){
56         std::cout << "Umpire: " << "deuce" << std::endl;
57     }
58

```

```

58
59     //Server reliant announcements
60     if (((score1 < 4 && score2 < 3) && (score1 != score2)) || ((score1 < 3 && score2 < 4) && (score1 != score2)) ){//Both less than 40
61         if (server==1){
62             std::cout << "Umpire: " << intToSpeech(score1, 1) << " - " << intToSpeech(score2, 2) << std::endl;
63         }
64         if (server==2){
65             std::cout << "Umpire: " << intToSpeech(score2, 2) << " - " << intToSpeech(score1, 1) << std::endl;
66         }
67     }
68
69     if (score1>=3 && score2>=3){
70         if ((score1 == score2 + 1)){
71             std::cout << "Umpire: " << "Advantage " << player1 << std::endl;
72         }
73
74         if ((score2 == score1 + 1)){
75             std::cout << "Umpire: " << "Advantage " << player2 << std::endl;
76         }
77     }
78
79     std::cout << std::endl;
80 }
81

```

```

82
83
84 void scoreReading(){ //Prints out the scoreboard.
85     std::cout << std::setw(19) << player1 << serving(1) << " | " << serving(2) << player2; //Server
86     std::cout << std::endl << std::setw(10) << "points | " << std::setw(10) << intToScore(score1, 1) << " | " << intToScore(score2, 2);
87     std::cout << std::endl << std::setw(10) << "games | " << std::setw(10) << games1 << " | " << games2 << std::endl; //Games
88 }
89
90
91 std::string serving(int player){ //Is used to print the asterix next to the server.
92     if (player == server){
93         return "*";
94     }
95     return " ";
96 }
97
98

```

```

98
99 int scoreTranslation(int score, int player){ //The scoring logic. Returns a number so can't return "AD"
100
101     if (score1<=3 && score2<=3){
102         if (score==0){
103             return 0;
104         }
105         if (score==1){
106             return 15;
107         }
108         if (score==2){
109             return 30;
110         }
111         if (score==3){
112             return 40;
113         }
114     }
115
116     if ((score1==3 && score2==2) || (score1==2 && score2==3)){
117         if ((score1 > score2) && player==1){
118             return 40;
119         }
120         if ((score2 > score1) && player==2){
121             return 40;
122         }
123         return 30;
124     }

```

```

125
126     if (score1==3 && score2 == 3){
127         return 40;
128     }
129
130     if (score1>=3 && score2>=3){
131         if ((score1 == score2 + 1)){
132             if (player==1){
133                 return -10; // -10 = Advantage
134             }
135         }
136         if ((score2 == score1 + 1)){
137             if (player==2){
138                 return -10; // -10 = Advantage
139             }
140         }
141         return 40; // Watched a game of tennis and it goes back to 40 from "AD-40"
142     }
143
144     return -5;
145
146 }

```

```

148
149     std::string intToScore(int score, int player){ //Takes the result of the logic, and returns a string. (Implemented to get "AD")
150         int value = scoreTranslation(score, player);
151
152         switch (value){
153             case 0: return "0";
154             case 15: return "15";
155             case 30: return "30";
156             case 40: return "40";
157             case -10: return "AD";
158         }
159         return "Error";
160     }
161
162
163     std::string intToSpeech(int score, int player){ //Returns what umpire should say.
164         int value = scoreTranslation(score, player);
165
166         switch (value){
167             case 0: return "love";
168             case 15: return "fifteen";
169             case 30: return "thirty";
170             case 40: return "fourty";
171             case -10: return "advantage";
172         }
173         return "Error";
174     }

```

```

175
176
177     int checkGameWon(){ //Checking if someone has won the game, uses the reset function.
178         if (score1 >3 && score1 >= score2 + 2){
179             games1++;
180             reset();
181             gameWinner = 1;
182             return 1;
183         }
184         if (score2 >3 && score2 >= score1 + 2){
185             games2++;
186             reset();
187             gameWinner = 2;
188             return 2;
189         }
190         return 0;
191     }
192
193
194     void reset(){ //Resets the scores and swaps the player serving.
195         score1 = 0;
196         score2 = 0;
197
198         if (server==1){
199             server=2;
200             return;
201         }
202         if (server==2){
203             server=1;

```

```

202         if (server==2){
203             server=1;
204             return;
205         }
206     }
207 }
208
209
210 void checkMatchWon(){ //Checks if someone has 3 games. If they do, the game loop ends.
211     if (games1>=3 || games2>=3){
212         if (games1 > games2){
213             std::cout << player1 << " Wins the Series!" << std::endl;
214         }
215     }
216     else{
217         std::cout << player2 << " Wins the Series!" << std::endl;
218     }
219 }
220     running = false;
221 }
222
223 }

```

And now for the public functions:

```

225     public:
226
227     //Constructor
228     TennisMatch(std::string _player1, std::string _player2){
229         player1 = _player1;
230         player2 = _player2;
231     }
232
233     //Functions
234     void play(){ // function that runs everything when called.
235
236         announcement();
237         scoreReading();
238
239         while (running){
240
241             addScoreToWinner();
242             checkGameWon();
243             announcement();
244             scoreReading();
245             checkMatchWon();
246
247             //announcement();
248
249         }
250     }
251 };

```

And the main where the class instance is set up with two names input by the software user.

The game loop function is then used.

```

254  int main(){
255
256  //Gets the inputs for the names of the people playing.
257  std::string string1; std::string string2;
258  std::cout << "Enter the names of the players: " << std::endl << "Player 1 : ";
259  std::cin >> string1;
260  std::cout << "Player 2 : ";
261  std::cin >> string2;
262  std::cout << std::endl;
263
264  //Initializes class
265  TennisMatch match(string1, string2);
266
267  //Starts game loop
268  match.play();
269
270  return 0;
271
272  }

```

Part 2 - Testing of the tennis loop:

For the testing, the program was run, and I entered in the names and the winners of each point.

Test 1:

Winning a game: Player 1 "George" wins all the points. Once he goes over 40, He gains a game, the points reset and the server swaps.

```

$ ./playTennis.exe
Enter the names of the players:
Player 1 : George
Player 2 : Alan

=====
Umpire: love-all

      George* |  Alan
points|      0 |  0
games |      0 |  0

Input winner: 1

=====
Umpire: fifteen - love

      George* |  Alan
points|     15 |  0
games |      0 |  0

Input winner: 1

=====
Umpire: thirty - love

      George* |  Alan
points|     30 |  0
games |      0 |  0

Input winner: 1

=====
Umpire: fourty - love

      George* |  Alan
points|     40 |  0
games |      0 |  0

Input winner: 1

=====
Umpire : game, George
Umpire: love-all

      George | *Alan
points|      0 |  0
games |      1 |  0

Input winner: |

```

Test 2: Checking the announcements. Such as deuce at 40-40 and advantage.

Here it shows that when someone scores into advantage, the Umpire calls "Advantage 'player'".

Then if the other player scores, the advantage is gone, and it returns to deuce as it does in professional tennis games.

It also shows player 2 getting a game, and the server switching back to the other player.

```

Input winner: 1
=====
Umpire: love - fifteen
=====
      George | *Alan
points|    15 |  0
games |     1 |  0
Input winner: 1
=====
Umpire: deuce
=====
      George | *Alan
points|    40 | 40
games |     1 |  0
Input winner: 1
=====
Umpire: Advantage George
=====
      George | *Alan
points|    AD | 40
games |     1 |  0
Input winner: 2
=====
Umpire: deuce
=====
      George | *Alan
points|    40 | 40
games |     1 |  0
Input winner: 2
=====
Umpire: Advantage Alan
=====
      George | *Alan
points|    40 | AD
games |     1 |  0
Input winner: 1
=====
Umpire: deuce
=====
      George | *Alan
points|    40 | 40
games |     1 |  0
Input winner: 2
=====
Umpire: Advantage Alan
=====
      George | *Alan
points|    40 | AD
games |     1 |  0
Input winner: 2
=====
Umpire: deuce
=====
      George | *Alan
points|    40 | 40
games |     1 |  0
Input winner: 2
=====
Umpire : game, Alan
Umpire: love-all
=====
      George* | Alan
points|     0 |  0
games |     1 |  1

```

Test 3: Checking the end of the game loop

The winner is the first player to get to three games:

Player 1 “Georges” gets to three games. The umpire says “game, George” and then the program prints “George wins the series” and then it ends.


```

=====
Umpire: love - fourty

      George | *Alan
points|      40 | 0
games |       2 | 1

Input winner: 1

=====
Umpire : game, George
Umpire: love-all

      George* | Alan
points|       0 | 0
games |       3 | 1
George Wins the Series!

```

Exercise 2: Rational number class

Part 1 – Writing the class:

Made a class which holds a numerator and a denominator of a fraction. Overloaded lots of operators so that this class can be easily used in other methods, such as a regular Falsi method.

```

1  #include <iostream>
2
3  class Fraction{
4
5      private:
6
7          // Variables
8          long long numerator; long long denominator; //Long ints to get larger range of fractions.
9
10     public:
11
12         //Constructor
13         constexpr Fraction(long long _numerator, long long _denominator):
14             numerator(_numerator),
15             denominator(_denominator){
16             if (_denominator==0){//Check to make sure not dividing by zero.
17                 throw std::logic_error("Divided by 0. You cannot have a denominator of 0.");
18             }
19             simplify(); // Simplify the fraction on initialisation.
20         };

```

Constructor checks whether the denominator is 0. If it is, an error is thrown.

The fractions are simplified in the initialization so that $2/4 == \frac{1}{2}$.

```

22 //Functions
23
24 friend std::ostream& operator<<(std::ostream& os, const Fraction& fraction){ //Print to console (cout)
25     std::cout << fraction.numerator << "/" << fraction.denominator << std::endl;
26     return os;
27 }
28
29 long long gcf(const long long &a,const long long &b){ //Get common factor
30     long long c = a % b;
31     if (c == 0){
32         return b;
33     }
34
35     return gcf(b,c);
36 }
37
38 void simplify(){//Simplifies to fraction as much as possible
39     long long bcf = gcf(numerator, denominator);
40
41     numerator /= bcf;
42     denominator /= bcf;
43
44     if (denominator < 0){
45         numerator *= -1;
46         denominator *= -1;
47     }
48 }

```

Now for all the operators:

```

50 Fraction operator +(Fraction const &other){ //Addition
51     long long newNum = numerator*other.denominator + other.numerator*denominator;
52     long long newDen = denominator*other.denominator;
53
54     Fraction sum(newNum,newDen);
55
56     return sum;
57 }
58
59 Fraction operator -(Fraction const &other){ // Subtraction
60     long long newNum = numerator*other.denominator - other.numerator*denominator;
61     long long newDen = denominator*other.denominator;
62
63     Fraction sum(newNum,newDen);
64
65     return sum;
66 }
67
68 Fraction operator *(Fraction const &other){ // Multiplication
69     long long newNum = numerator*other.numerator;
70     long long newDen = denominator*other.denominator;
71
72     Fraction product(newNum,newDen);
73
74     return product;
75 }

```

```

77     Fraction operator /(Fraction const &other){ // Division
78         long long newNum = numerator*other.denominator;
79         long long newDen = denominator*other.numerator;
80
81         Fraction product(newNum,newDen);
82
83         return product;
84     }
85
86     Fraction& operator +=(Fraction const &other){
87         *this = *this + other;
88         return *this;
89     }
90
91     Fraction& operator -=(Fraction const &other){
92         *this = *this - other;
93         return *this;
94     }
95
96     Fraction& operator /=(Fraction const &other){
97         *this = *this / other;
98         return *this;
99     }
100
101     Fraction& operator *=(Fraction const &other){
102         *this = *this * other;
103         return *this;
104     }

```

```

106     constexpr Fraction& operator++(){ //Prefix ++
107         numerator = numerator + denominator;
108
109         return *this;
110     }
111
112     constexpr Fraction operator++(int){ //Postfix ++
113         Fraction holder = *this;
114         ++(*this);
115         return holder;
116     }
117
118     constexpr Fraction& operator--(){ //Prefix --
119         numerator = numerator - denominator;
120         return *this;
121     }
122
123     constexpr Fraction operator--(int){ //Postfix ++
124         Fraction holder = *this;
125         --(*this);
126         return holder;
127     }

```

```

129     bool operator==(const Fraction &other){
130         if (numerator == other.numerator && denominator == other.denominator){
131             return true;
132         }
133         return false;
134     }
135
136     bool operator!=(const Fraction &other){
137
138         if (numerator != other.numerator || denominator != other.denominator){
139             return true;
140         }
141         return false;
142     }
143
144     bool operator>(const Fraction &other){
145         double forigin = (long double)numerator/(long double)denominator;
146         double fother  = (long double)other.numerator/(long double)other.denominator;
147
148         if (forigin > fother){
149             return true;
150         }
151         return false;
152     }
153 }

```

```

155     bool operator<(const Fraction &other){
156         double forigin = (long double)numerator/(long double)denominator;
157         double fother  = (long double)other.numerator/(long double)other.denominator;
158
159         if (forigin < fother){
160             return true;
161         }
162         return false;
163     }
164
165     bool operator>=(const Fraction &other){
166         double forigin = (long double)numerator/(long double)denominator;
167         double fother  = (long double)other.numerator/(long double)other.denominator;
168
169         if (forigin >= fother){
170             return true;
171         }
172         return false;
173     }
174
175     bool operator<=(const Fraction &other){
176         double forigin = (long double)numerator/(long double)denominator;
177         double fother  = (long double)other.numerator/(long double)other.denominator;
178
179         if (forigin <= fother){
180             return true;
181         }
182         return false;
183     }

```

Some other useful functions:

```

185     Fraction abs(){//Absolute of the fraction
186         simplify();
187         long long store = numerator;
188         if (store < 0){
189             store *=-1;
190         }
191         Fraction absolute(store, denominator);
192         return absolute;
193     };
194
195     constexpr Fraction pow(int x){ //To the power of
196         Fraction result(1,1);
197
198         for (unsigned i = 0; i < x; ++i){
199             result *= *this;
200         }
201
202         return result;
203     }
204 };
205

```

The class is now finished. All the methods are defined inside the class due to personal preference.

Testing the class:

```

238 int main(){
239     Fraction first(7,15);
240     Fraction second(6,29);
241
242     std::cout << "\n+ : " << first + second << std::endl; //expected : 293/435
243     std::cout << "- : " << first - second << std::endl; //expected : 113/435
244     std::cout << "* : " << first * second << std::endl; //expected : 14/145
245     std::cout << "/ : " << first / second << std::endl; //expected : 203/90
246
247     first += Fraction(1,1);
248     std::cout << "+= : " << first << std::endl; //expected : 22/15
249
250     first++;
251     std::cout << "++ : " << first; //expected : 37/15
252
253     return 0;
254 }

```

Provides an overview of the basic operators and gives the output:

```

$ ./a.exe
+ : 293/435
- : 113/435
* : 14/145
/ : 203/90
+= : 22/15
++ : 37/15

```

This time with a negative number: Note that it does not matter if the minus sign is included in the numerator or denominator as the simplify function will correct it.

```

238 int main(){
239     Fraction first(-7,15);
240     Fraction second(6,29);
241
242     std::cout << "\n+ : " << first + second << std::endl; //expected : -113/435
243     std::cout << "- : " << first - second << std::endl; //expected : -293/435
244     std::cout << "* : " << first * second << std::endl; //expected : -14/145
245     std::cout << "/ : " << first / second << std::endl; //expected : -203/90
246
247     first += Fraction(1,1);
248     std::cout << "+= : " << first << std::endl; //expected : 8/15
249
250     first++;
251     std::cout << "++ : " << first; //expected : 23/15
252
253     return 0;
254 }

```

Testing the pow and abs functions

```

236 int main(){
237     Fraction first(-7,15);
238     Fraction second(6,5);
239
240     std::cout << first << "Squared is : " << first.pow(2) << std::endl;
241     std::cout << second << "Cubed is : " << second.pow(3) << std::endl;
242
243     std::cout << first << "The absolute is : " << first.abs() << std::endl;
244
245
246     return 0;
247 }

```

Returns:

```

-7/15
Squared is : 49/225

6/5
Cubed is : 216/125

-7/15
The absolute is : 7/15

```

Now using a few to combine into something slightly more complicated:

```

236 int main(){
237     Fraction half(1,2);
238     Fraction six(6,1);
239     Fraction third(1,3);
240     Fraction nine(9,1);
241     std::cout << "((6 * 0.5)/(1/3))*9. Would expect 81:" << std::endl;
242     std::cout << "we get: " << (six * half)/third * nine << std::endl;
243
244
245     return 0;
246 }

```

```

((6 * 0.5)/(1/3))*9. Would expect 81:
we get: 81/1

```

Part 2 – Implementing Regula Falsi:

Now that the class has the mathematical operators, we can start to use it to build more complex programs.

Using the class to find a root using the regular Falsi method.

Here a function for the Regular Falsi is defined as well as the equation $x^2 - 2$ which we want to find the route for.

```
210 Fraction findRootFalsi(Fraction (*f)(Fraction), Fraction x1, Fraction x2){
211     Fraction tolerance(111,1000000011); //Tolerance of 10^-8
212     Fraction zero(011,111);           // Just a 0 fraction 0/1
213
214     Fraction middle = (x1*(*f)(x2) - x2*(*f)(x1)) / ((*f)(x2) - (*f)(x1));
215
216     while( ((*f)(middle)).abs() > tolerance){ // While the absolute value at middle is greater than the tolerance away from 0.
217
218         if ( (*f)(middle) <= zero){ //If the value at middle is below 0. Set x1 to middle.
219             x1 = middle;
220         }
221         else{ //If the value at middle is above 0. Set x2 to middle.
222             x2 = middle;
223         }
224         middle = (x1 * (*f)(x2) - x2*(*f)(x1)) / ((*f)(x2) - (*f)(x1));
225         std::cout << (middle) << std::endl;
226     }
227     //}
228     return middle;
229 }
```

The regular falsi can be used to find a root of an equation (provided it has a root):

The assessment asked for the root of the function $x^2 - 2$, between 0 and 2.

Running the main function:

```
236 int main(){
237     |
238     Fraction root = findRootFalsi(myQuadratic, Fraction(0,1), Fraction(2,1));
239     std::cout << "\n Root of x^2 -2 : " << root << std::endl;
240
241     return 0;
242 }
```

Where myFunction is :

```
Fraction myQuadratic(Fraction x){ // Simple quadratic to show off regular falsi y = x^2 - 2
    return (x * x) -Fraction(2,1);
}
```

Returns:

```
4/3
7/5
24/17
41/29
140/99
239/169
816/577
1393/985
4756/3363
8119/5741
27720/19601
Root of x^2 -2 : 27720/19601
```

Which when put into a calculator gives the value: 1.414213561.

And the actual root is at 1.414213562....

The answer is extremely close as expected with the low tolerance.

Part 3 – Arising problems and limitations to a rational number class:

One limitation is the amount of memory each object consumes. If you want a precise number, the numerator and denominator need to be sufficiently big enough to accommodate for that accuracy. An extremely small number requires a huge denominator, as well as a numerator. If you are using these fraction classes on a grand scale, it would be more memory efficient to use doubles or long doubles. Limiting the effectiveness of using this class for high performance programs.

Overflows could become a problem since some numbers require exceptionally large numerators and/or denominators. Therefore, when using this rational number class to do some arithmetic, overflow errors can pop up due to the size of the answer's object's value holders being too small to hold the new number. For example, 0.124349729340 requires large values for its numerator and denominator. Multiplying this number by some other number, say, 22.13457903 which also includes large values for the numerator and denominator, then a completely wrong answer could arise due to an overflow error resulting from the extremely large values that do not fit into the memory allocated for the numerator and denominator in the class. This limits the usefulness of the class for uses where high accuracy is required.

An arising problem would be the usefulness of displaying the fractions. When the number gets exceptionally large, printing out the numerator and the denominator becomes difficult to read, and to get an understanding of the actual number it represents requires the use of a calculator. For example, getting an output of 134797495902/2425793992 is difficult for a human to comprehend, whereas if it is displayed in a different form such as a double, it is simply 55.56840208.