

# Vesicle Simulation Framework

## Overview

This project simulates two-phase vesicle shapes governed by curvature elasticity and volume/area constraints.

Each solution is obtained by solving a coupled two-region boundary-value problem (BVP) in the Laplace–Beltrami form using MATLAB's bvp6c solver.

The simulation framework explores a 2-D parameter space in spontaneous curvatures ( $H_0^{(1)}, H_0^{(2)}$ ) while keeping global physical parameters fixed for each run (area ratio, moduli, etc.).

Solutions are stored in a content-addressed database (SimResults/) and organized through a persistent catalog (catalog.mat).

## High-Level Design Components

### User script (driver)

Defines a simulation configuration and launches a task driver.

Key Files: `run_initial_sweep.m`

### Simulation configuration

Specifies physical parameters (`sim.MP`), thresholds (`sim.TH`), and solver settings (`sim.SP`).

Key Files: `sim_config()`

### Task driver

Performs adaptive quadtree exploration in  $H_0$  space, coordinating catalog I/O and solver calls.

Key Files: `src/sim_explore_H0_quad_tree.m`

### Bootstrap & cleanup

Initialize and teardown environment, import seeds, manage paths.

Key Files: `bootstrap.m`, `cleanup.m`

### Solver

Computes a solution at a single parameter point. Performs warm-starts, continuation, and quality gating.

Key Files: `src/utils/solveAtParams.m`

### Continuation

Smoothly walks a prior solution toward a new target  $H_0$ .

Key Files: `src/utils/continuation_towards_H0.m`

### Scheduler (quadtree)

Chooses which cell and parameter point to solve next.

Key Files: `src/utils/processQuadtree.m`

### Catalog utilities

Manage a persistent MAT-based catalog of all results.

Key Files: `catalog_load.m`, `catalog_append.m`, `catalog_save.m`, `catalog_view_wide.m`

### Seed importer

Registers initial shape files from `InitialShapes/` as seeds for warm starts.

Key Files: `bootstrap.m` → `import_initial_shapes_into_catalog()`

### Warm-start selector

Finds nearest solved or seeded shape to initialize new solves.

Key Files: `src/utils/pickWarmStart.m`

## Execution Flow

### 1. Environment setup

Running:

```
bootstrap();
```

- Resets MATLAB's path, adds `src/`, `bvp6c-solver/`, and `InitialShapes/`.
- Ensures `SimResults/` exists.
- Imports any new `InitialShapes/SIM_Node_*.mat` files into the catalog as seed entries.

### 2. Simulation configuration

The user config function (`sim_config`) defines three nested structures:

SP: Simulation parameters  
`MaxIter`, `ModelVersion`, `LogFile`

TH: Thresholds & solver knobs  
`BCmax`, `DEmaxHard`, `rMin`, `delta`, `opts`

MP: Physical parameters  
`A`, `V`, `KA`, `KB`, `KG`, ( $\rightarrow$  `aS`, `bS` via `computePhaseScales`)

Each simulation run keeps MP fixed while exploring  $(H_0^{(1)}, H_0^{(2)})$ .

### 3. Task driver

`sim_explore_H0_quad_tree` orchestrates the run:

Initialize or resume from previous cache (`cache.mat`) and catalog (`catalog.mat`).

#### Quadtree scheduling:

- `processQuadtree` proposes the next  $(H_0^{(1)}, H_0^{(2)})$  to solve based on solved corners.

## Hash generation:

- A SHA-256 hash computed from
- {ModelVersion, H0\_1, H0\_2, A, V, KA, KB, KG}
- defines a unique key and file name in SimResults[hashed\_results]/.

## Solve or skip:

- If <hash>.mat exists → skip (already solved).
- Otherwise → call solveAtParams.

## Save result:

- Save to hashed\_results/<hash>.mat.
- Append to catalog.mat.
- Update cache.mat to track quadtree progress.
- Repeat until all cells are solved or MaxIters reached.

## 4. Solver stage

solveAtParams(params, sim, warm):

- Builds the parameter bundle:

```
Par = {H0, A, V, KA, KB, KG, aS, bS, delta}
```

- Uses warm start from pickWarmStart if available.
- Optionally applies continuation\_towards\_H0 to precondition the solution.
- Executes an attempt ladder of increasing tolerance looseness and delta scaling: Baseline → δ/2 → δ/4 → looser tolerances.
- Accepts a solution if all gates pass:

```
BCmax ≤ TH.BCmax  
DEmax ≤ TH.DEmaxHard  
rMin ≥ TH.rMin
```

- Records metadata {label, E, P, BCmax, DEmax, mesh} and returns to the driver.

## 5. Catalog management

All solved data is tracked in SimResults/catalog.mat (MAT-only):

Column	Type	Description
hash	string	SHA-256 key
timestamp	datetime(UTC)	Creation/update time
entry	cell → struct	Contains: <ul style="list-style-type: none"><li>• params: full parameter set (H0 + physics)</li><li>• meta: metrics &amp; provenance</li></ul>

Seeds added by bootstrap have entry.meta.type = "seed".

All later solves have numerical results and metrics.

## Warm-Start Hierarchy

When solving at a new  $H_0$  point, pickWarmStart searches:

1. **Nearest solved neighbor** with identical physics in the catalog. Loads its .mat file and returns its BVP structure as warm.result.sol.
2. **Seed entry** from InitialShapes/ matching ( $A, V, KA, KB, KG$ ). Loads its Version(1).Solution for use as the starting state.
3. **Fallback analytic/legacy seed** via initialGuessFromFile.

If the warm-start's  $H_0$  differs significantly from the target (>0.15 units), solveAtParams calls continuation\_towards\_H0 to bridge the gap in small steps.

## Content-Addressed Storage Layout

```
SimResults/
├── hashed_results/
│   ├── <hash>.mat           % result, meta structs
│   ├── cache.mat             % quadtree & scheduler state
│   ├── catalog.mat           % persistent catalog table
│   └── OPfile.txt            % optional run log
```

All results are immutable: rerunning the solver with identical parameters produces the same hash and simply updates the catalog timestamp.

## Adaptive Quadtree Exploration

The quadtree scheduler partitions the  $H_0$  plane into cells.

Each cell stores corner solutions (if solved) and tests uniformity based on energy and pressure:

1. Pop a cell from the queue.
2. For each corner, check if its parameters exist in the catalog (using lookup\_in\_catalog).
3. If a corner is unsolved → return it as a new task.
4. Once all corners are solved, run uniformTest:
  - \* If the solution is uniform → finalize cell.
  - \* Otherwise → subdivide into four children and enqueue.

This process continues until the target resolution or MaxIters is reached.

## Physics Summary

Symbol	Meaning	Appears in
$A$	area ratio ( $\alpha/\beta$ phases)	computePhaseScales, sim.MP
$V$	volume fraction	BendV_Lag_EIGp_BC_Impl
$K^{(1)}, K^{(2)}, K_G$	elastic moduli	DE/BC implementation
$(H_0^{(1)}, H_0^{(2)})$	spontaneous curvatures	exploration plane
$a_S, b_S$	arc-length scalings (from A)	DE equations
$\delta$	small buffer near poles for Taylor expansion	DE equations
opts	solver tolerances	numerical controls only

## Catalog Entry Example

```

entry.params =
    struct with fields:
        H0_1: 0.5
        H0_2: -0.3
        A: 0.75
        V: 0.72
        KA: 1
        KB: 1
        KG: 0
        aS: 0.75/pi
        bS: (0.75 - 1)*pi

entry.meta =
    struct with fields:
        label: 2
        E: 3.147
        P: 0.061
        BCmax: 2.8e-7
        DEmax: 1.9e-2
        mesh: 167
        version: "BVP-v3.1"
        hash: "<SHA256>"

```

## Run Lifecycle

### Initialize environment

```
bootstrap();
```

### Run simulation

```

sim = sim_config();
sim_explore_H0_quad_tree(sim);

```

### Cleanup

```
cleanup();
```

## Inspect results

```
T = catalog_load('SimResults');
W = catalog_view_wide('SimResults');
```

## Key Advantages of the Refactor

- **Single Source of Truth:** All results in one unified MAT catalog; no CSV duplicates.
- **Idempotent Execution:** Content-hashing prevents re-solving existing parameter points.
- **Flexible Configuration:** Physics and numerical settings are cleanly separated.
- **Warm-Start Intelligence:** Automatic reuse of nearest solved or seed shapes; continuation ensures stability far from seeds.
- **Adaptive Refinement:** Quadtree exploration automatically concentrates computation in regions of high variation.
- **Modular Design:** Each major function is standalone and easily testable.

## File Dependency Diagram

```
run_initial_sweep.m
└── bootstrap.m
    └── import_initial_shapes_into_catalog.m
sim_config()
sim_explore_H0_quad_tree.m
└── processQuadtree.m
    └── lookup_in_catalog() ...
pickWarmStart.m
solveAtParams.m
    ├── continuation_towards_H0.m
    ├── BendV_Lag_EIGp_DE_impl.m
    ├── BendV_Lag_EIGp_BC_impl.m
    ├── bc_diagnostics.m
    ├── de_residual.m
    └── labelFromSolution.m
catalog_append.m / catalog_load.m / catalog_save.m
computePhaseScales.m
cleanup.m
```

## Extensibility

Future enhancements can include:

- **Parallel scheduling** for independent cells.
- **Phase-aware continuation** (bias by label).
- **Result-based pruning** (stop refining when energy variation  $< \epsilon$ ).
- **JSON/CSV export** for external analysis.
- **Visualization tools** for the quadtree and phase diagram.