

Precision measurements with polar molecules: the role of the black body radiation

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In the perspective of the outstanding developments of high-precision measurements of fundamental constants using polar molecules related to ultimate checks of fundamental theories, we investigate the possibly counterproductive role of black-body radiation on a series of diatomic molecules which would be trapped and observed for long durations. We show that the absorption of black-body radiation at room temperature may indeed limit the lifetime of trapped molecules prepared in a well-defined quantum state. Several examples are treated, corresponding to pure rotational absorption, pure vibrational absorption or both. We also investigate the role of a black-body radiation-induced energy shift on molecular levels and how it could affect high-precision frequency measurements.

Keywords: Black-body radiation; Precision measurements; Absorption rate; Light shift; Cold polar molecules

1. Introduction

Over the last few decades, more and more effort has been put into searching experimentally for 'new physics' breaking the fundamental C, P, T symmetries. High-energy experiments initiated this quest for physics beyond the Standard Model more than 40 years ago with the discovery of the CP violation [1]. Since then not only high-energy experiments have been searching for parity violations, but also low-energy experiments based on high-precision measurements, as initially proposed for atomic systems [2]. For instance, recent results on the P parity violation have been obtained probing the highly dipole-forbidden $6S-7S$ transition in caesium [3, 4].

This kind of precision measurement is especially eager to take advantage of the most sensitive tools to gain in precision and to reduce systematic errors. In that respect, cold atoms have brought huge improvements in several high-precision investigations, and nowadays cold molecules hold even greater promise. In such experiments, interferometers and quantum beats with atoms and molecules are often used and very long interrogation times (up to a few seconds) are needed to allow the phase to accumulate in the interferometer. The search for time dependence of the

fundamental constants needs particularly high-precision measurements since it is looking for small relative drifts. In the search for a time dependence of the fine structure constant, which would imply the violation of both Lorentz invariance and CPT symmetry, the best measurement to date has been achieved through comparisons of atomic frequency standards [5]. The recent high-resolution spectroscopy of cold OH radicals in a Stark-decelerated beam combined with astrophysical measurements of OH megamasers gives hope for yielding an even better determination of the time variation of the fine structure constant [6]. The time dependence of the proton–electron mass ratio is planned to be investigated by measuring extremely precisely the inversion splitting in the ammonia molecule in a molecular fountain [7]. A tremendously exciting search for a possible permanent electric dipole moment (EDM) of atoms, nucleons and elementary particles, such as the electron and the muon, is being carried out [8–12], since its existence would reveal a violation of the time-reversal invariance. To date, the lowest limit on the value of a possible electron EDM has been established using the thallium atom [11]. Molecules are expected to open the way to even more precise measurements and much effort nowadays is put into setting up experiments with cold beams of heavy polar molecules, such as YbF, PbO or PbF [13, 14]. Cold-slowed or trapped molecules offer even better prospects, allowing very long interrogation times on the order of several seconds.

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The accuracy of such high-precision measurements has become so amazingly high that every possible small disturbance has to be considered very carefully, including black-body radiation (BBR), always present in an experimental environment. Atoms in the ground state are normally immune to the absorption of black-body photons at room temperature, since such photons do not carry enough energy to induce a dipole-allowed transition. This is not the case in Rydberg species, as has been known for a long time [15]. A distribution of molecular ions has also been shown to evolve toward a thermal equilibrium at the environment temperature through exchange of black-body photons [16]. It has been proposed to use BBR to cool down internal states of molecular ions [17] and very recently laser-trapping of radium took advantage of BBR as repumping light [9]. Recently BBR absorption rates have been experimentally measured in trapped clouds of cold OH and OD radicals [18]. The presence of BBR also induces a shift of the atomic resonances, which is a well-known effect on frequency measurements in atomic clocks. Such a light shift is now one of the biggest uncertainties in high-precision measurements of frequencies [19–21]. So far it has not been observed in molecular systems.

In this paper, we investigate the possible limitations induced by BBR on experiments aiming at interrogating molecular systems over long time intervals. Such experiments often require heavy molecules with large permanent dipole moments which make them very sensitive to the presence of any external electric field, like the BBR electric field. We first recall in section 2 the different transitions which can be induced by BBR in molecules, emphasizing through a simple model the crucial role of both the *magnitude* and the *variation* of the permanent electric dipole moment of the molecule with the internuclear distance. Then we explore several classes of molecules of relevance for running, planned or possible high-precision measurements: heavy fluoride radicals (section 3), strongly polar alkali dimers, alkali hydrides as well as sulphur oxide (section 4). We investigate in section 5 the role of the BBR-induced energy shift in two molecular systems of relevance now in the context of high-precision measurements: the YbF radical and the ammonia molecule.

2. Absorption of black-body radiation by diatomic molecules

The spectral energy density of BBR at a frequency ν and a temperature T is given the Planck radiation law:

$$\rho(\nu) = \frac{8\pi h \nu^3}{c^3} \frac{1}{\exp(h\nu/k_B T) - 1}. \quad (1)$$

spectral energy density: energy per volume per spectral unit
peaks at 2.821 kT

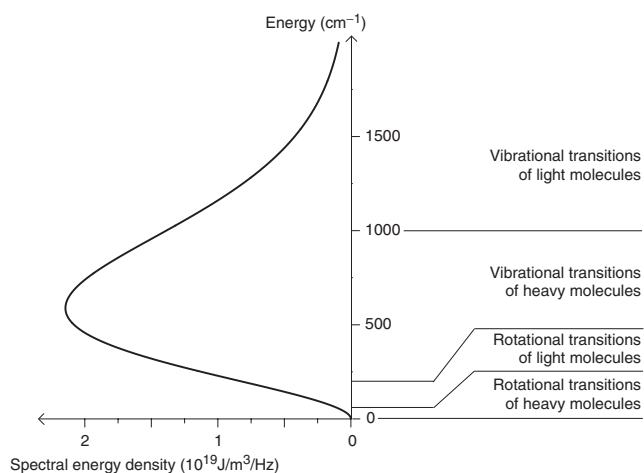


Figure 1. Spectral energy density of the BBR at room temperature (300 K). On the right side are schematically depicted the typical energy ranges for vibrational and rotational transitions in heavy and light molecules.

Figure 1 shows the BBR spectral energy density at room temperature. The BBR absorption rate of a quantum system in the initial state i reads:

$$\Gamma_i^{\text{BBRabs}} = \sum_f \frac{\mu_{fi}^2}{6\epsilon_0 \hbar^2} \rho(\nu_{fi}) \equiv \frac{8\pi^2}{3\epsilon_0 \hbar c^3} \sum_f \frac{\nu_{fi}^3 \mu_{fi}^2}{\exp(h\nu_{fi}/k_B T) - 1}, \quad (2)$$

where the summation is performed over all final states f accessible from the initial state i via an electric dipole transition at frequency ν_{fi} . The details of the rovibronic structure of the quantum system are involved through the matrix elements $\mu_{fi} = \langle f | \mu | i \rangle$ of the dipole moment operator μ between the initial state i and the final state f . We restrict ourselves to the study of heteronuclear (i.e. polar) diatomic molecules, assuming that both i and f states can properly be described within the Born–Oppenheimer (BO) approximation with total wave functions Ψ_i^{BO} and Ψ_f^{BO} . The BO wave functions are written as products of electronic (ψ), vibrational (χ) and rotational wave functions (Θ):

$$\Psi_{i,f}^{\text{BO}} = \psi_{\alpha_{i,f}}(R; \{\mathbf{r}\}) \chi_{v_{i,f}}(R) \Theta_{J_{i,f}}(\Omega). \quad (3)$$

In equation (3), the $\alpha_{i,f}$, $v_{i,f}$ and $J_{i,f}$ labels refer respectively to the electronic, vibrational and rotational quantum numbers of the initial and final states. The electronic part depends on all electronic coordinates $\{\mathbf{r}\}$, and the rotational part on the angular coordinates Ω of the molecular axis in the space-fixed frame. We assumed that there is no coupling between vibrational and rotational degrees of freedom. The transition dipole

moment μ_{fi} can be reformulated as the integral over the interatomic separation \mathbf{R} :

$$\mu_{fi} = \int \chi_{vj}(R) \Theta_{J_j}(\Omega) \mu_{fi}^{\text{BO}}(\mathbf{R}) \cdot \boldsymbol{\varepsilon} \chi_{vi}(R) \Theta_{J_i}(\Omega) dR d\Omega, \quad (4)$$

which accounts for the orientation of the instantaneous dipole moment for all electrons relative to the polarization $\boldsymbol{\varepsilon}$ of the black-body photon. The R -dependent transition dipole moment function $\mu_{fi}^{\text{BO}}(\mathbf{R})$ is obtained after integration of the product $\psi_{\alpha_j} \mu \psi_{\alpha_i}$ on the electronic coordinates.

The energy distribution of the BBR spectrum peaks around 600 cm^{-1} at room temperature, which is not sufficient to induce any electronic transition starting from the ground state or from a low metastable state in diatomic molecules. Therefore we can safely ignore them, and restrict our attention to transitions between rotational or vibrational levels of a single electronic state α . The transition dipole moment function now reduces to the permanent dipole moment function $\mu_\alpha(R)$ of the state α so that equation (4) becomes

$$\mu_{v'J'vJ} \propto \int_0^\infty \chi_{v'}(R) \mu_\alpha(R) \chi_v(R) dR \equiv \mu_{v'v}, \quad (5)$$

where v and v' (resp. J and J') are the initial and final vibrational (resp. rotational) levels of the transition within the state α . The proportionality factor in equation (5) is the Hönl–London factor between the initial and the final state, which accounts for the initial and final rotational levels J and J' and for the relative orientation of the molecular axis and of the polarization of the BBR electric field. We will see from equation (5) that depending on the type of transition, the magnitude of $\mu_{v'J'vJ}$ is determined either by the magnitude or by the R -dependence of the dipole moment function. The knowledge of molecular dipole moment functions generally require quantum chemistry calculations which are available over a wide R range only for a few molecules of interest here. The value of this function at the equilibrium distance R_e of the molecule and its first derivative around R_e are also sometimes given in the literature. This information is actually sufficient to evaluate the BBR absorption rate, as in all cases considered here the vibrational ground state wave function—which peaks at R_e —is of relevance. Indeed, the function $\mu_\alpha(R)$ can be expanded to the first order around R_e and reads

$$\mu_\alpha(R) = \mu_\alpha(R_e) + \left[\frac{d\mu_\alpha}{dR} \right]_{R=R_e} (R - R_e), \quad (6)$$

where $[d\mu_\alpha/dR]_{R=R_e}$ is the first derivative of the electric dipole moment function evaluated at R_e . The scheme displayed in figure 1 illustrates the various situations treated here. For light molecules, with a mass smaller than ten atomic mass units say, the typical energy for vibrational transitions often exceeds the peak of the BBR energy distribution, so that pure rotational transitions are dominant, the molecule remaining in its lowest vibrational level ($v=0$). The constant term $\mu_\alpha(R_e)$ in equation (6), i.e. the magnitude of the dipole moment, brings the main contribution to $\mu_{v'J'vJ}$ and the integral in equation (5) almost reduces to $\mu_\alpha(R_e)$. In contrast, for heavier molecules the energy of rotational transitions corresponds to the low energy part of the BBR distribution, so that vibrational transitions are favoured. Therefore, $\mu_{v'J'vJ}$ (with $v' \neq v$) mainly depends on the slope of the dipole moment function, and no longer on its magnitude, due to the mutual orthogonality of vibrational wave functions. A further simplification can be made if the vibrational (harmonic) constant ω_e of the relevant potential curve is known. The radial integral between two adjacent vibrational levels in equation (5) can be analytically evaluated for a harmonic potential:

$$\mu_{v+1,v} = \left(\frac{v+1}{2} \right)^{1/2} \left(\frac{\hbar}{m\omega_e} \right)^{1/2} \left[\frac{d\mu}{dR} \right]_{R=R_e}, \quad (7)$$

where m is the reduced mass of the molecule. These approximations break down if the potential well is strongly anharmonic, if the dipole moment function is notably nonlinear or too flat around R_e , or if couplings such as rovibrational couplings are not negligible.

3. BBR absorption rate for fluoride radicals: BaF, YbF, HgF and PbF

In heavy paramagnetic molecules such as BaF, YbF, HgF and PbF—of relevance for the search of the electron EDM—the vibrational wave function of low-lying vibrational levels extends typically over a small fraction of an atomic unit ($1 \text{ a.u.} \equiv a_0 = 0.0529177 \text{ nm}$), so that the dipole moment function of the electronic ground state can safely be considered linear over this extension. Therefore, the strength of the electric dipole transition between two consecutive vibrational states can be estimated following equation (7) as soon as the derivative of the electric dipole moment function at the equilibrium distance is known.

Diatomic lanthanide compounds possess partially filled $4f$ and $5d$ shells and involve strong inter-shell couplings, which generate very complicated spectra.

Table 1. Equilibrium distances, vibrational and rotational frequencies, values of the dipole moment function and of its first derivative at the equilibrium distance for the dimers discussed throughout the paper. The state considered here is always the rovibrational ground state, unless otherwise stated.

Species	Initial state	$R_e(a_0)$	$\omega_e(\text{cm}^{-1})$	$B_e(\text{cm}^{-1})$	$\mu_e(\text{D})$	$\mu'_e(\text{Da}_0^{-1})$	Ref.
YbF	$X^2\Sigma^+$	3.80	502	0.24	3.55	3.09	[22]
BaF	$X^2\Sigma^+$	4.09	469	0.21	3.51	4.52	[36]
HgF	$X^2\Sigma^+$	3.87	489		7.24	4.14	
PbF	$X^2\Sigma^+$	3.94	530		4.32	3.38	[24]
SrF	$X\Sigma$	3.92	509	0.2536	3.4963	3.17	[25] or John Barry thesis
LiRb	$X^1\Sigma^+$	6.50	185		4.15	0.14	[37]
LiCs	$X^1\Sigma^+$	6.82	164		5.44	0.45	[37]
NaRb	$X^1\Sigma^+$	6.84	107		3.30	0.20	[37]
NaCs	$X^1\Sigma^+$	7.20	98.0		4.61	0.34	[37]
KRb	$X^1\Sigma^+$	7.64	75.5		0.61	0.03	[37]
KCs	$X^1\Sigma^+$	8.01	66.2		1.90	0.11	[37]
RbCs	$X^1\Sigma^+$	8.28	49.4		1.23	0.07	[37]
LiH	$X^1\Sigma^+, J=1$	2.98	1405	7.5	5.88	0.96	[38]
CsH	$X^1\Sigma^+, J=1$	4.50	891	2.7	8.30	2.10	[38]
SO	$X^3\Sigma^-, N=0, J=1$	2.80	1150	0.72	1.51	0.94	[39]

Their study is therefore challenging for both theoretical and experimental investigations. Among the molecules mentioned above, YbF [22, 23] and PbF [24] have been studied from *ab initio* theory and dipole moment function of YbF and its value and first derivative for PbF at the equilibrium internuclear distance have been derived.

Extensive quantum chemistry studies on alkaline earth monohalides are available mainly for the lighter ones (involving Be, Mg, Ca, Sr linked with F or Cl), providing all necessary quantities for the present purpose, including the derivative of the permanent dipole moment [25]. Quantum chemistry calculations have also been devoted to BaF [26] and HgF [27] molecules, providing the main properties of the electronic ground state except the R variation of its permanent dipole moment function. Fortunately, alkaline earth monohalides (hereafter labelled as Me-Hal) have been extensively studied in the past, since their theoretical description is underlined by a simple picture: such molecules are ionic-bond molecules, in which the lone electron evolves in the field of two atomic ions, namely the closed-shell doubly-charged metal cation Me^{++} and the halogen anion Hal^- . The ligand approach [28, 29] assumes that the electronic structure of the system can be described with orbitals centred on the free Me^{++} ion while the electrostatic field of the ligand Hal^- ion is treated as a perturbation. The electrostatic model proposed by Rittner [30] accounts for the mutual polarization of the Me^+ and Hal^- ions through induced dipole moments which reduce the primary permanent dipole moment of the molecule. However, due to the

large polarizability of the Me^+ ion, higher order effects break this approximation down. The more elaborated electrostatic model of Törring *et al.* [31] accounts for the strong hybridization of the external electron of the Me^+ ion induced by Hal^- , which acts as a radial shift of the centre of charge of the electron wave function. The induced dipole moments are modified accordingly in the expression of the net dipole moment of the molecule, whose derivative can also be derived. Finally, as pointed out in [26, 31] an effective polarizability of the Hal^- ion should be introduced in such ionic molecules which accounts for the influence of the Me^+ ion on the somewhat floppy negative ion. The effective value of 4.7 a.u. is recommended in [26, 31] for F^- within the CaF and BaF molecules, indeed much smaller than the free ion polarizability (about 16 a.u. [32, 33]).

Using the value 81 a.u. of [31] for the Ba^+ polarizability, the ionic model yields for BaF at the equilibrium distance ($R_e = 4.09$ a.u.) of its $X^2\Sigma^+$ electronic ground state $\mu(R_e) = 1.38$ a.u. (close to the experimental value 1.24 a.u. [34]) and $[d\mu/dR]_{R=R_e} = 1.78$ a.u.. For HgF in its $X^2\Sigma^+$ electronic ground state ($R_e = 3.87$ a.u.) the same model leads to $\mu(R_e) = 2.85$ a.u. and $[d\mu/dR]_{R=R_e} = 1.63$ a.u., taking the Hg⁺ polarizability 19 a.u. from [35].

The structure parameters used for the BBR absorption rate calculations are collected in table 1. We found rates slightly smaller than 1 s^{-1} (see table 2), suggesting that the lifetime of a molecular sample in a well-defined initial state could be limited by BBR. In the near future, molecular interferometry for precision measurements will be performed in traps, which offer the opportunity

Table 2. BBR absorption rate at 300 K for selected heavy diamagnetic polar molecules used in various precision measurement experiments, for selected alkali dimers and for LiH, CsH and SO. For all calculated rates and lifetimes the initial state is the vibrational ground state ($v = 0$). Values for KRb (resp. RbCs) are in agreement with previous calculations of [40] (resp. [41]).

Species	Initial state	$\Gamma_{\text{rot}}(s^{-1})$	$\Gamma_{\text{vib}}(s^{-1})$	Lifetime(s)
YbF	$X^2\Sigma^+$	—	0.26	3.8
BaF	$X^2\Sigma^+$	—	0.60	1.7
HgF	$X^2\Sigma^+$	—	0.47	2.1
PbF	$X^2\Sigma^+$	—	0.29	3.4
LiRb	$X^1\Sigma^+, J = 0$	—	8.0×10^{-3}	125
LiCs	$X^1\Sigma^+, J = 0$	—	1.7×10^{-2}	59
NaRb	$X^1\Sigma^+, J = 0$	—	7.3×10^{-4}	1.4×10^3
NaCs	$X^1\Sigma^+, J = 0$	—	1.7×10^{-3}	600
KRb	$X^1\Sigma^+, J = 0$	—	7.5×10^{-6}	1.3×10^5
KCs	$X^1\Sigma^+, J = 0$	—	8.2×10^{-5}	1.2×10^4
RbCs	$X^1\Sigma^+, J = 0$	—	1.5×10^{-5}	6.7×10^4
LiH	$X^1\Sigma^+, J = 1$	1.52	6.0×10^{-2}	0.63
CsH	$X^1\Sigma^+, J = 1$	1.55	1.2	0.36
SO	$X^3\Sigma^-, N = 0, J = 1$	—	8.3×10^{-3}	120

to keep the molecules for seconds and hence in an interferometry experiment to let the phase being built for much longer times than in a beam experiment. Traps are therefore a very promising tool for measuring very small level energy differences with a molecular interferometer, as planned for instance with YbF and PbF. If seconds are needed to let the phase build up, cycles of absorption–emission are then induced by the BBR and limit the contrast of the interferometer by breaking its coherence.

As a check of such predictions, we also calculated the BBR absorption rate for YbF and PbF using the ionic model and found a good agreement with the calculation using the derivatives of the dipole moment function from [22, 23]. Moreover, the influence of the inaccuracy on the static polarizability of the ions, which determines the molecular dipole moment, is exemplified with HgF and BaF. Indeed, the F^- effective polarizability depends *a priori* on the accompanying positive ion. In particular, the dipole moment of HgF (2.85 a.u.) presently obtained using the Hg^+ polarizability from [35] (19 a.u.) is about 70% larger than the one given in [27]. If we use the ionic model to adjust the dipole moment of HgF to the experimental value, the F^- effective polarizability becomes close (14 a.u.) to the one of the free ion. The derivative of the HgF dipole moment around R_e increases with the F^- effective polarizability, increasing the BBR absorption rate only from 0.47 to $0.86 s^{-1}$. Note also that Angstrmann *et al.* [35] computed a value of 122 a.u. for the Ba^+ polarizability, significantly higher than in [31]. Introducing this value in the ionic model

then yields a F^- effective polarizability of 1.3 a.u. to recover the experimental dipole moment from [34]. We clearly reach here the limits of the validity of the ionic model but this does not significantly change the conclusions of our analysis.

4. BBR absorption rates for alkali dimers, alkali hydrides and sulphur oxide

Polar molecules are expected to exhibit long-range dipole–dipole interactions. One expects to be able to characterize the dipole–dipole interactions by studying collisions in a cold sample of polar molecules, just as the details of interactions between cold atoms in the late 1990s were investigated [42]. Cold (half-) collisions could also be studied by controlling the orientation of the molecules with external electric fields. Polar molecules are also promising candidates for quantum computing [43, 44].

Great experimental efforts are put on the production of ultracold heteronuclear alkali dimers, which possess rather large dipole moments [37]. They are formed experimentally from trapped ultracold atoms and are therefore obtained at very low temperatures, much lower than in experiments starting from a molecular beam. The disadvantage of this technique is that it has so far addressed only alkali dimers. Up to now densities of ultracold polar alkali dimers are still low, but several groups are heading toward accumulating and trapping these dimers in order to start investigating molecule–molecule collisions [45–47].

Many efforts are done nowadays on cold intense beams of alkali hydrides [48]. The lightest of them, LiH, could be stopped with a Stark decelerator in order to perform further sympathetic or evaporative cooling in a trap. However, in the samples of trapped molecules obtained up to now [49], densities are still too low, and temperature still too high to observe cold collisions.

Due to their large dipole moment, these molecules can undergo vibrational and rotational BBR induced electric dipole transitions within their electronic ground state. Nevertheless, for all alkali dimers, rotational constants are on the order of a fraction of a wavenumber, where the spectral energy density of the BBR is very small (see figure 1). Only vibrational transitions are therefore of relevance. The vibrational matrix elements of the dipole moment were evaluated using the Fourier grid Hamiltonian method [50] taking as input data electronic ground state potentials and dipole moment functions provided by [37]. We performed the calculations for several alkali dimers (see table 2). For most of them, the absorption of black-body photons cannot be noticeable at room temperature even for extremely long trapping times of several minutes which are reachable if special care is taken to reduce the background gas pressure. A noticeable exception to this is the case of LiCs. The black-body limited lifetime of LiCs in its ground state at room temperature is only on the order of one minute, which constitutes a limitation in the investigation of collisions in a trapped cloud of LiCs and further evaporative cooling [46].

The lowest level in which LiH is foreseen to be efficiently manipulated in an electrostatic deceleration and trapping process is the $v=0$, $J=1$ rovibrational level of its $X^1\Sigma^+$ electronic ground state. The pumping rate at room temperature due to vibrational transitions is rather small (0.06 s^{-1}) since the vibrational constant is quite high ($\approx 1400\text{ cm}^{-1}$). However, the black-body photons are quite efficient at pumping the $v=0$, $J=1$ level to the $v=0$, $J=2$ level at a rate of 1.26 s^{-1} and at depumping it down to the $v=0$, $J=0$ level at a rate of 0.163 s^{-1} . Moreover, the spontaneous emission depletes the $v=0$, $J=1$ level which decays to the $v=0$, $J=0$ level with a rate of 0.036 s^{-1} . Finally, this leads to an overall lifetime of LiH in the $v=0$, $J=1$ level of about 650 ms at room temperature. This harms long trapping of LiH in this state and therefore all cooling processes that could follow like evaporative, sympathetic or cavity-assisted cooling. Even at 77 K the lifetime increases only to about 3 s, still limited by the black-body assisted rotational transitions.

In order to investigate dipole–dipole interactions, the best alkali hydride is CsH (with a dipole moment of 8.3 D), for which one can expect strong interactions between CsH molecules through the

dipole–dipole interaction. However its dipole moment to mass ratio is not encouraging from the perspective of a Stark deceleration. Nevertheless, under the same conditions as for LiH above, we found that the contribution of the vibrational transition to $v=1$ levels amounts to 1.17 s^{-1} , since the vibrational frequency (891 cm^{-1}) is quite close to the peak of the black-body spectrum. The rotational transitions contribute to the depletion of the $v=0$, $J=1$ level with the following rates: 0.56 s^{-1} for $J=2 \leftarrow J=1$ and 0.071 s^{-1} for $J=0 \leftarrow J=1$, while the spontaneous emission rate is negligibly small (0.0056 s^{-1}). In total, at room temperature the $v=0$, $J=1$ level is depleted at a rate of 1.80 s^{-1} . At 77 K this rate drops down to 0.16 s^{-1} , essentially given by the $J=2 \leftarrow J=1$ black-body assisted transition.

Cold chemistry involving free radicals is a blooming field and is expected to bring new insight on reactive collision and dissociation. As an experiment aims at producing cold SO radicals and O atoms produced from near-threshold dissociation of trapped SO_2 [51], it is worth calculating also the BBR absorption rate of the SO radical in its ground state. The lowest electronic states have been studied and potential energy curves and dipole moments have been computed [39]. We estimate that the BBR absorption rate, solely due the first vibrational transition (1120 cm^{-1}), is $8.3 \cdot 10^{-3}\text{ s}^{-1}$, in agreement with [18]. This should not affect the trapping time of SO radicals in an electrostatic or in a magnetic trap.

5. The black-body radiation-induced shift in molecules

According to quantum electrodynamics theory, light cannot only be absorbed by a massive particle, but it also shifts the level energies of the particle [52]. The BBR has been known for a long time to be responsible for a shift of the atomic hyperfine splittings [53], which is of extreme relevance for atomic clocks [19–21]. For atoms in their ground state, all electric dipole allowed transitions require photons with much more energy than available in the BBR spectrum at room temperature. Therefore the BBR electric field acts on the atom through its static polarizability, exactly like a dc electric field does, and only the amplitude of the black-body electric field is then of importance. As shown in the previous sections, a molecule likely absorbs resonantly a black-body photon through an electric dipole transition. Therefore BBR does not act on the molecule simply like a dc electric field but the entire BBR spectrum has to be considered.

The black body is a very incoherent source of photons, with a coherence time of about $\hbar/4k_{\text{B}}T \approx 40\text{ fs}$ at room temperature [54], which is

much smaller than the typical absorption time of a black-body photon by the molecule (see rates of table 2 and [18]). Therefore, according to [52], the BBR-induced frequency shift of the level i reads:

$$\Delta_i = \frac{4\pi}{3\epsilon_0 \hbar c^3} \sum_{f \text{ states}} P \int dv \frac{v^3}{\exp(hv/k_B T) - 1} \frac{\mu_{fi}^2}{v - v_{fi}}, \quad (8)$$

with the same notations as in section 2, and where the symbol $P \int$ holds for the Cauchy principal part integral.

Molecular interferometers constitute excellent tools to quantify very small energy differences or measure very accurately transition frequencies. First, the experiments carried out on YbF in order to detect the electron EDM ultimately need to measure frequencies down to a precision of tens of μHz [13]. In that reference, the effect of BBR is not explicitly discussed. We found that the BBR-induced shift due to rotational electric dipole allowed transitions ($N = 1 \leftarrow N = 0$) is on the order of tens of mHz, while the contribution to the shift of vibrational transitions is on the order of a few mHz, much larger than the above needed precision. However, a careful analysis of the paper by Hudson *et al.* [13] shows that the ratio of the differences of phases measured under various external field conditions is insensitive to the first order of the induced light shifts. Indeed, each individual phase measured in the YbF interferometer depends on the difference between light shifts induced on two Zeeman sublevels, which is proportional (with an extremely small factor of about 10^{-13}) to their energy difference. This ensures that a BBR-induced correction to the electron EDM could be at maximum 10^{13} times smaller than its actual value, hence totally undetectable.

The discussion above suggests that a BBR-induced light shift could play a significant role if a frequency measurement aimed at a relative accuracy of 10^{-13} , which is typical of what is needed to investigate possible time variation of fundamental constants. For instance, a very sensitive probe for a possible time variation of the proton–electron mass ratio is the inversion frequency in ammonia. A new experiment is currently being set up, which aims at performing very high resolution spectroscopy in a Ramsey type interferometry experiment in an ammonia molecular fountain [7]. An accuracy of 10^{-13} – 10^{-14} is expected on the measurement of the inversion frequency (of about 23.8 GHz) in the state $J = 1, K = 1$. Note that the hyperfine structure of $^{15}\text{ND}_3$ molecules has been recently measured with an accuracy of a few 10^{-9} in spectroscopy experiments using cold decelerated ammonia molecules [55]. The use of a molecular interferometer is expected to increase further the accuracy by several orders of magnitude. Therefore, we evaluated

the BBR-induced energy shift on both inversion levels involved in this experiment, which might be of importance since the levels considered are of different symmetries, i.e. are coupled to different sets of levels by the electric dipole interaction.

Microwave transitions, which have led to the ammonia maser [56], have been studied for decades in NH_3 [57, 58], as well as its rotation–inversion structure. We denote the lowest level involved in the inversion transition by $0^-, J = 1, K = 1$, the upper one being $0^+, J = 1, K = 1$, with the opposite parity. Both levels are coupled by electric dipole allowed transitions to all other rovibrational levels. Let us examine first the rotational radiative coupling: each of these levels is coupled to an inversion level of the $J = 2, K = 1$ rotation manifold via an electric dipole allowed transition. Because of the inversion–rotation structure (see for instance [59]), these two allowed transitions, around 39.7 cm^{-1} , differ in frequency by the sum of the inversion splittings of the $J = 1, K = 1$ and $J = 2, K = 1$ states, i.e. by about 46.8 GHz. This implies that the levels $0^-, J = 1, K = 1$ and $0^+, J = 1, K = 1$ experience different BBR-induced shifts, given by equation (8). Both BBR-induced shifts, on the order of 80 mHz at room temperature, differ by about 5 mHz, which represents 2×10^{-13} times the inversion frequency between the $0^-, J = 1, K = 1$ and $0^+, J = 1, K = 1$ levels. Although not negligible in the absorption rate of BBR photons, the coupling to higher vibrational states via BBR photons only gives rise to light shifts lower than 10^{-14} times the inversion frequency (see for instance [60, 61] for electric dipole moment matrix elements). Note that the dipole moment matrix elements we used give an absorption rate compatible with the one calculated in [18].

In conclusion, at room temperature the measured inversion frequency between the $0^-, J = 1, K = 1$ and $0^+, J = 1, K = 1$ levels is lowered by about 2×10^{-13} by BBR-induced energy shifts. We have also calculated that a room-temperature variation of 5°C changes relatively the measured frequency by about 10^{-14} . We did the same type of calculation on $^{15}\text{ND}_3$ and we draw the same conclusion, i.e. that the inversion frequency is lowered by about 2×10^{-13} by BBR-induced shifts. This should be considered carefully in a high-precision interferometry experiment aiming at measuring the inversion frequency of ammonia at an accuracy of 10^{-13} – 10^{-14} and more generally in high-precision frequency measurements involving molecules.

6. Conclusion

We have performed calculations to evaluate the influence of the black-body radiation on molecular

systems in use in, or of relevance for high-precision measurements. Both absorption rates and induced energy shifts have been estimated. The BBR absorption could disturb the coherence of molecular interferometers if they are achieved in traps with heavy radicals like YbF, PbF or HgF, which hold promise in the search for the electron EDM. Alkali dimers should not suffer from the BBR absorption, except LiCs that survives in its ground state for one minute only, which might hamper further evaporative or sympathetic cooling. Much more critical is the case of LiH, which is predicted to be pumped out of the prepared initial state $v=0$, $J=1$ in less than one second at room temperature and only in 3 s at liquid nitrogen temperature. Finally, we have shown that the BBR-induced shift on molecular level energies should be considered carefully in high-precision frequency measurements, like in the case of a molecular fountain of ammonia, which is currently being built to investigate the time variation of the proton–electron mass ratio.

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