

# 2021 Workshop on Gravitational Waves and High-Performance Computing

Geoffrey Lovelace

August 16, 2021 – August 20, 2021

# Welcome to the workshop!

- Please make sure you create a **free** account at <https://cocalc.com>
- Please find a profile picture that is clear, friendly, and recognizable, such as:
  - A photo of you e.g.
  - An avatar from bitmoji.com, getavataars.com, hexatar.com, ...
- Workshop supported by the National Science Foundation
- Website with useful materials:  
<https://geoffrey-lovelace.com/Workshop/2021>



# Photos

- We would like to take some "photos" (zoom screenshots) during the workshop
- The photos would appear on the Cal State Fullerton website, in news stories about the workshop
- If you would prefer to not have your picture taken, please feel free to turn off your camera

# A commonly held **inaccurate** model of teaching and learning



Joe Reddish, 2001, AAPT, San Diego

Bill Watterson - Calvin and Hobbs

# Results from cognitive science and education research

- Learning requires **mental effort**.
- New information must link with what you **already know**.
- **Most people learn best when interacting with others.**

# Daily schedule

- Morning: 9:30 AM - 11:00 AM
- Afternoon I: 12:30 PM - 2:00 PM
- Afternoon II: 2:30 PM - 4:00 PM

# Tentative schedule

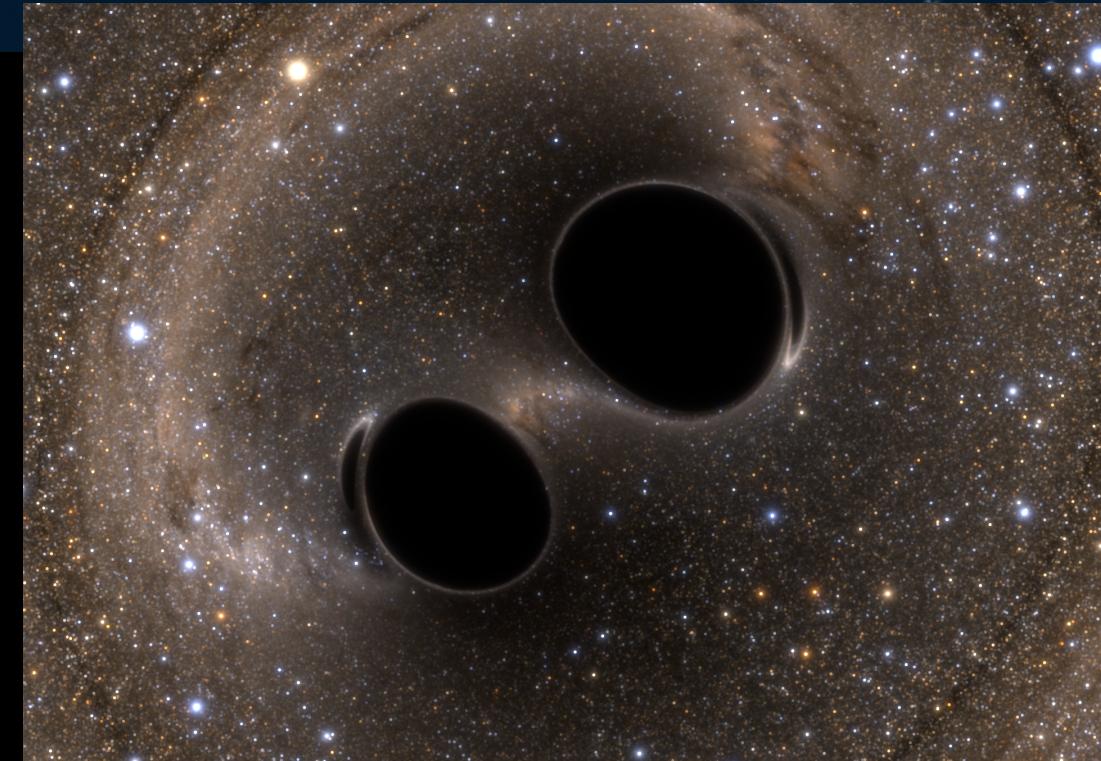
- **Monday:** Powers of 10 & computing, programming with Python
- **Tuesday:** Programming with Python, Unix Command Line, using a supercomputer
- **Wednesday:** Simulating colliding black holes, black holes, gravitational waves
- **Thursday:** Gravitational-wave research, panel discussion
- **Friday:** visualizing colliding black holes, exit survey

# About the pace...

- The pace is intense: you'll be learning a lot
- It's normal to feel confused...that's actually what learning feels like
- There is no such thing as a dumb question!!
- You will get the most out of this experience by participating! It's more like learning a sport or a musical instrument or a language or ...

# GW PAC

GRAVITATIONAL WAVE  
Physics and Astronomy Center



# Which brother am I?



C

Both

D

Neither

E

Not sure

# Icebreaker

- If you had to gain one superpower, which one would you choose?

A

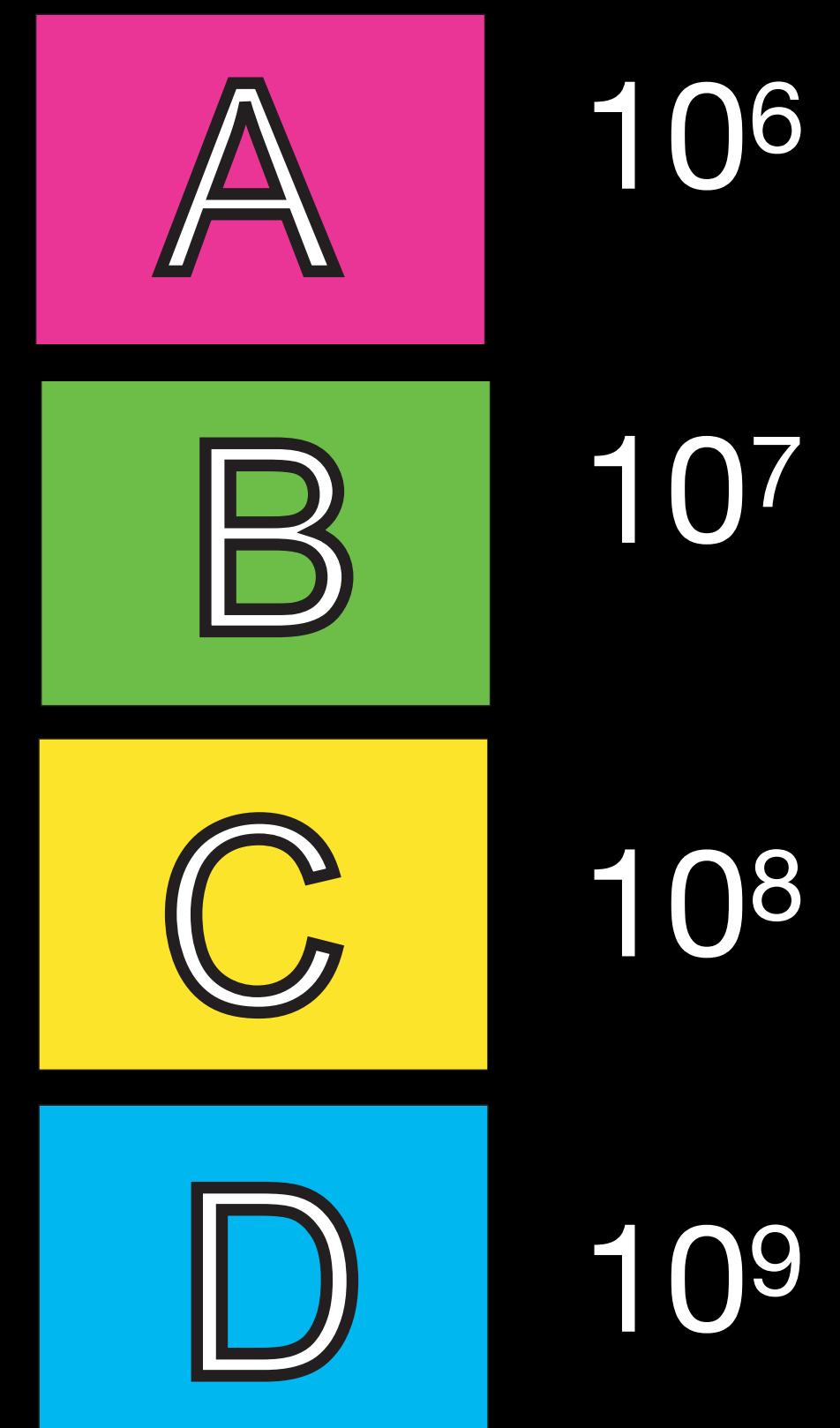
Ability to fly

B

Power to be invisible

# Powers of 10

- How many meters across is Earth?







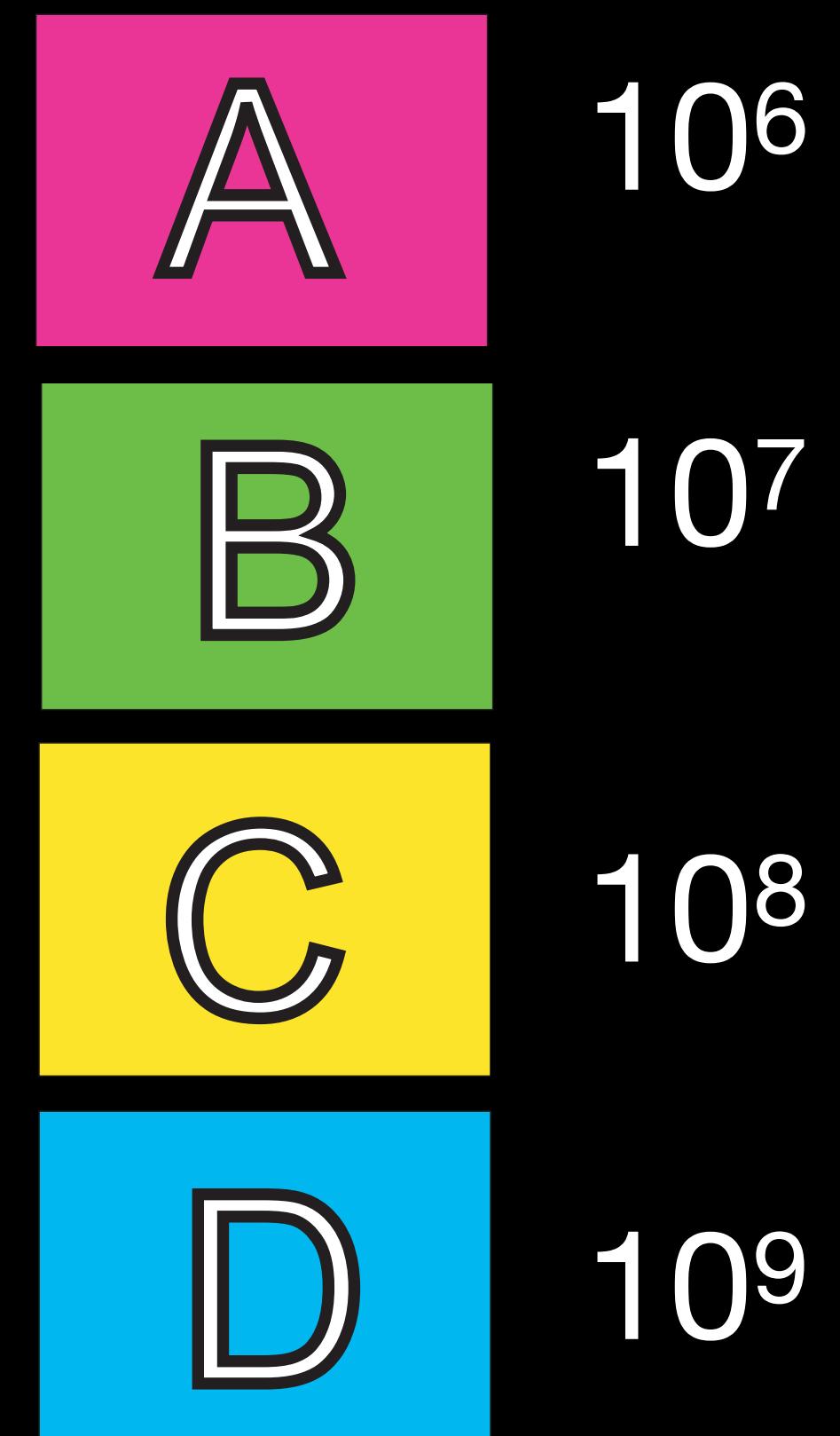
$10^{24}$   
meters



100 million light years

# Powers of 10

- How many meters across is Earth?



# Powers of 10

- How many meters is a light year?

A	$10^8$
B	$10^{12}$
C	$10^{16}$
D	$10^{20}$

# Powers of 10 & computers

# Humans

- First entities called “computers” were teams of people
- Divide up the work into operations done in parallel, by hand (perhaps with mechanical aid)
- Redundant calculations to check accuracy
- Since 1700s
- $10^{-1}$  to 1 FLOPS / human  
(decimal operations / second / human)



1949 NACA High Speed  
Flight Station “Computer Room”)

# Colossus (1942)

- First programmable, digital, electronic computer
- Break codes in World War II Britain
- $5 \times 10^5$  FLOPS

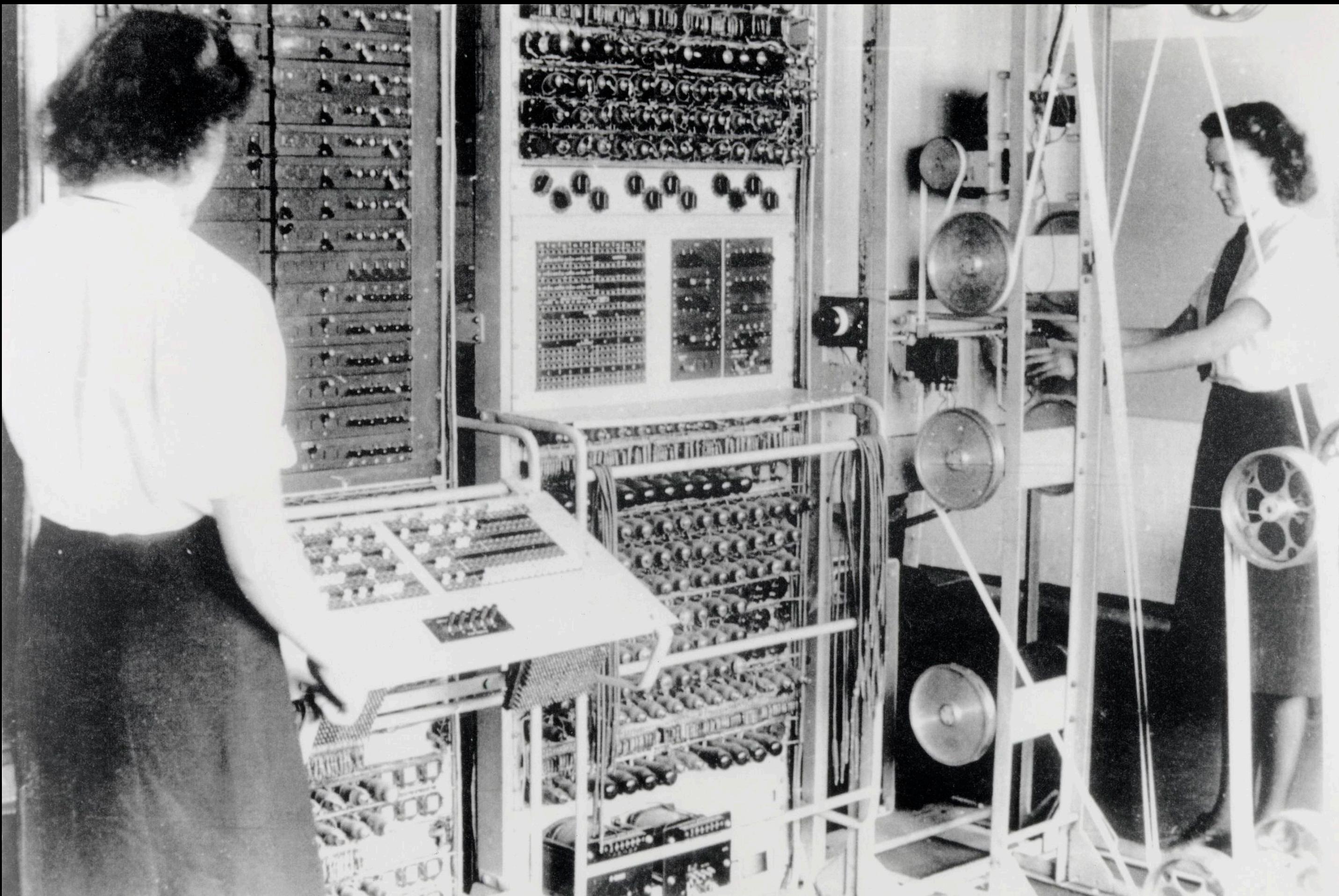


Image courtesy wikipedia

# My first Mac (1984)

- First Macintosh
- $1 \times 10^6$  FLOPS



Image courtesy wikipedia

# My Mac in 2003

- 2 cores
- $2 \times 10^9$  FLOPS



Image courtesy Apple

# My current Mac

- 4 cores
- $2 \times 10^{11}$  FLOPS



Image courtesy Apple

# My current iPhone

- 6 cores
- $2 \times 10^{11}$  FLOPS



Image courtesy Apple

# Clicker question #1.4

- In 1 second, today's high-end smart phones can perform \_\_\_\_\_ calculations per second (FLOPS).

A	$10^4$ (10 thousand)
B	$10^7$ (10 million)
C	$10^{10}$ (10 billion)
D	$10^{12}$ (1 trillion)

# Clicker question #1.5

- In 1 second, today's high-end smart phones can perform as many calculations as \_\_\_\_\_ humans?

A	$10^4$ (10 thousand)
B	$10^7$ (10 million)
C	$10^9$ (1 billion)
D	$10^{11}$ (100 billion)

*For comparison:*

*Humans alive in 2018:  $7.6 \times 10^9$*

*Total humans who ever lived:  $10^{11}$*

*Sources: [google.com](http://google.com), [pro.org](http://pro.org)*

# Clicker question #1.3

- Today's most powerful computers are \_\_\_\_\_ times more powerful than *today's high-end personal computers*.

- A 10 (ten)
- B  $10^3$  (a thousand)
- C  $10^6$  (a million)
- D  $10^9$  (a billion)

# Ocean supercomputer at Cal State Fullerton

- Supercomputer for Cal State Fullerton Gravitational-Wave Physics and Astronomy Center
- 824 cores
- $\approx 10^{12} - 10^{13}$  FLOPS



# Blue Waters

- Most powerful computer I have used
- 70,000 cores
- $1 \times 10^{16}$  FLOPS



Image courtesy Blue Waters

# Summit

- First exaflop computer (with graphics cards)
- 200,000 cores
- $2 \times 10^{17}$  FLOPS



Image courtesy Oak Ridge National Laboratory

# Supercomputer Fugaku



© R

- Current fastest computer in the world
- Kobe, Japan
- 7.6 million cores
- $1 \times 10^{18}$  FLOPS

Image courtesy Riken & Fujitsu

# High performance computing

- Computing beyond what personal devices can do
- Many cores work together in parallel

FLOPS	Example	Computing Type
$10^0$	<i>Addition by human with pen &amp; paper</i>	<i>Early</i>
$10^3$	<i>Room-sized computer in 1940s</i>	
$10^6$	1980s personal computers (1984)	Personal
$10^9$	Personal computers around year 2000	
$10^{10}$	High-end smartphone today	
$10^{11}$	High-end PC today	
$10^{12}$	<b>Small supercomputer today</b>	<b>High-Performance</b>
$10^{16}$	<b>Most powerful computer I've used</b>	
$10^{18}$	<b>Most powerful computer in the world</b>	

# Clicker question #1.3

- Today's most powerful computers are \_\_\_\_\_ times more powerful than *today's high-end personal computers*.

- A 10 (ten)
- B  $10^3$  (a thousand)
- C  $10^6$  (a million)
- D  $10^9$  (a billion)

# Clicker question #1.6

- In 1 second, the most powerful computer in the world can perform as many calculations as \_\_\_\_\_ humans?

A	$10^8$ (100 million)
B	$10^{11}$ (100 billion)
C	$10^{14}$ (100 trillion)
D	$10^{18}$ (1 quintillion)

*For comparison:*

*Humans alive in 2018:  $7.6 \times 10^9$*

*Total humans who ever lived:  $10^{11}$*

*Sources: [google.com](http://google.com), [pro.org](http://pro.org)*

# Clicker question #1.7

- In 1 second, a small supercomputer like Ocean can perform as many calculations as \_\_\_\_\_ humans?

A

$10^6$  (1 million)

B

$10^9$  (1 billion)

C

$10^{12}$  (1 trillion)

D

$10^{15}$  (1 quadrillion)

*For comparison:*

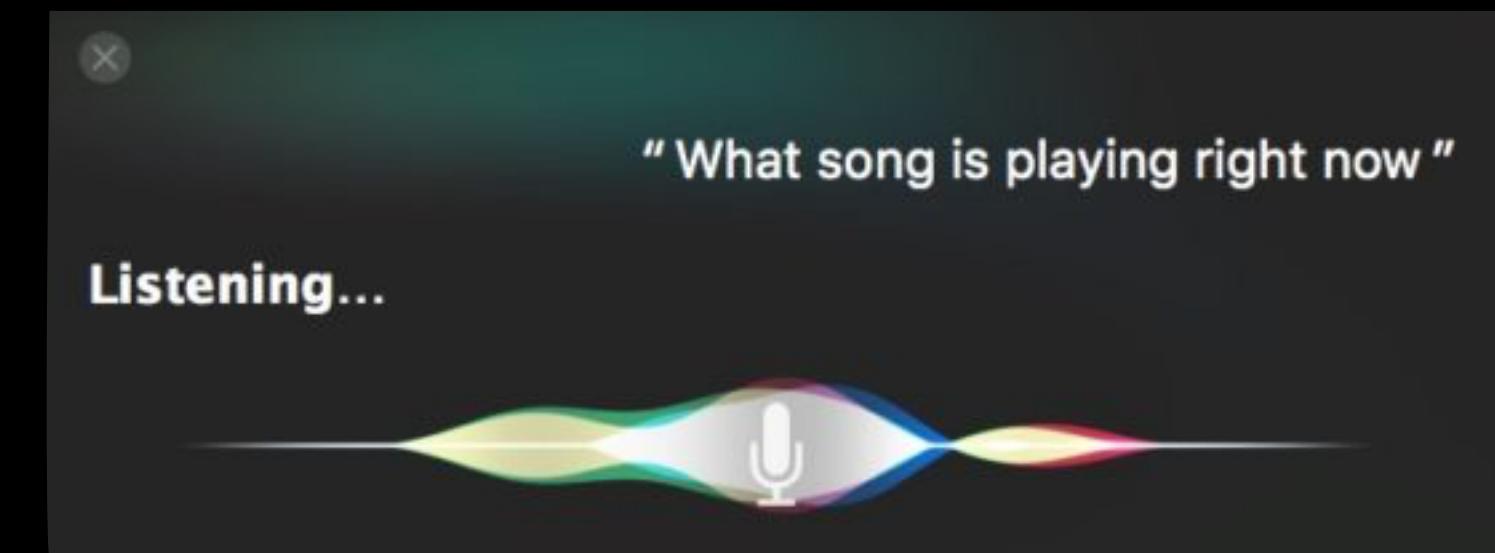
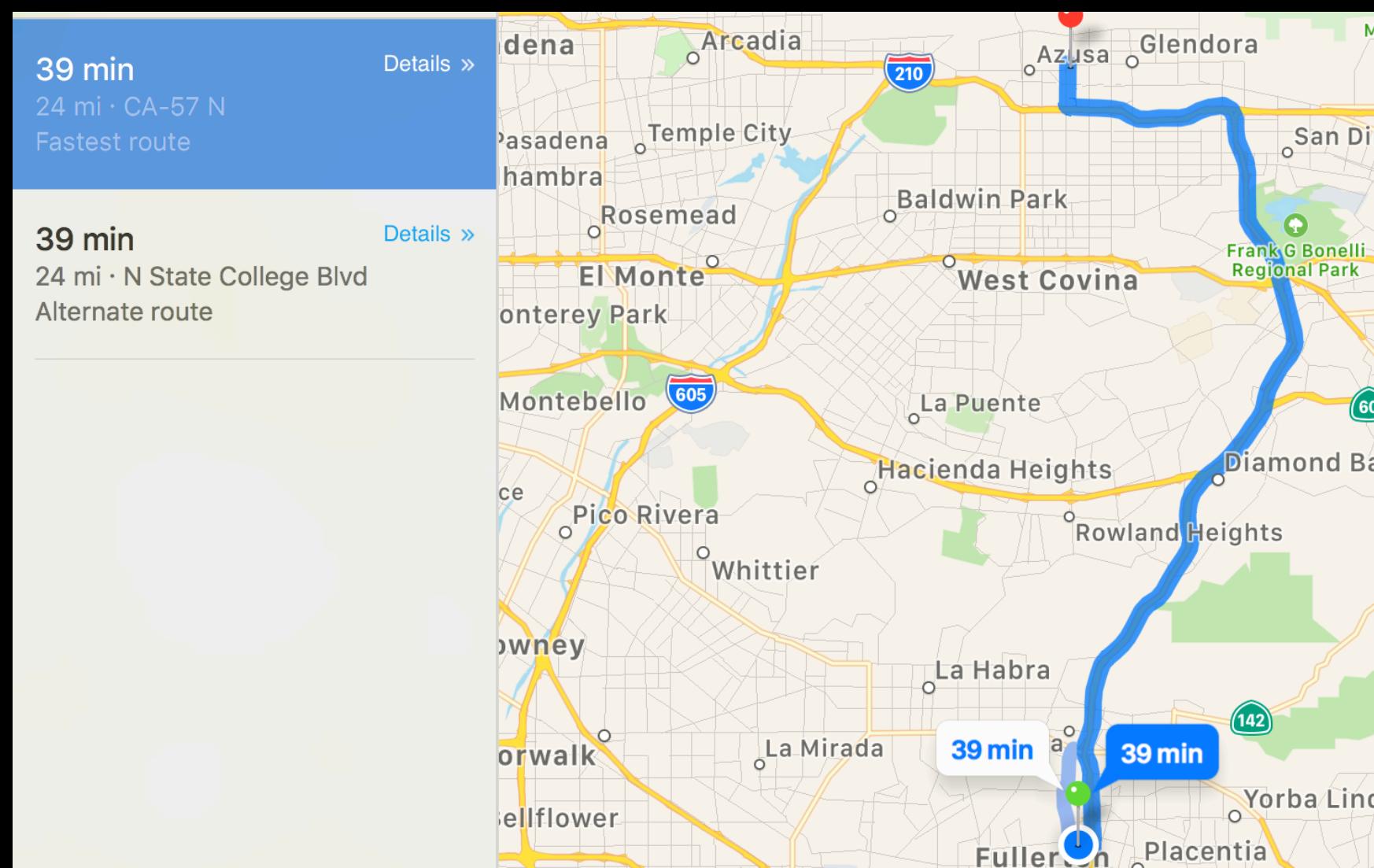
*Humans alive in 2018:  $7.6 \times 10^9$*

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*Sources: [google.com](http://google.com), [pro.org](http://pro.org)*

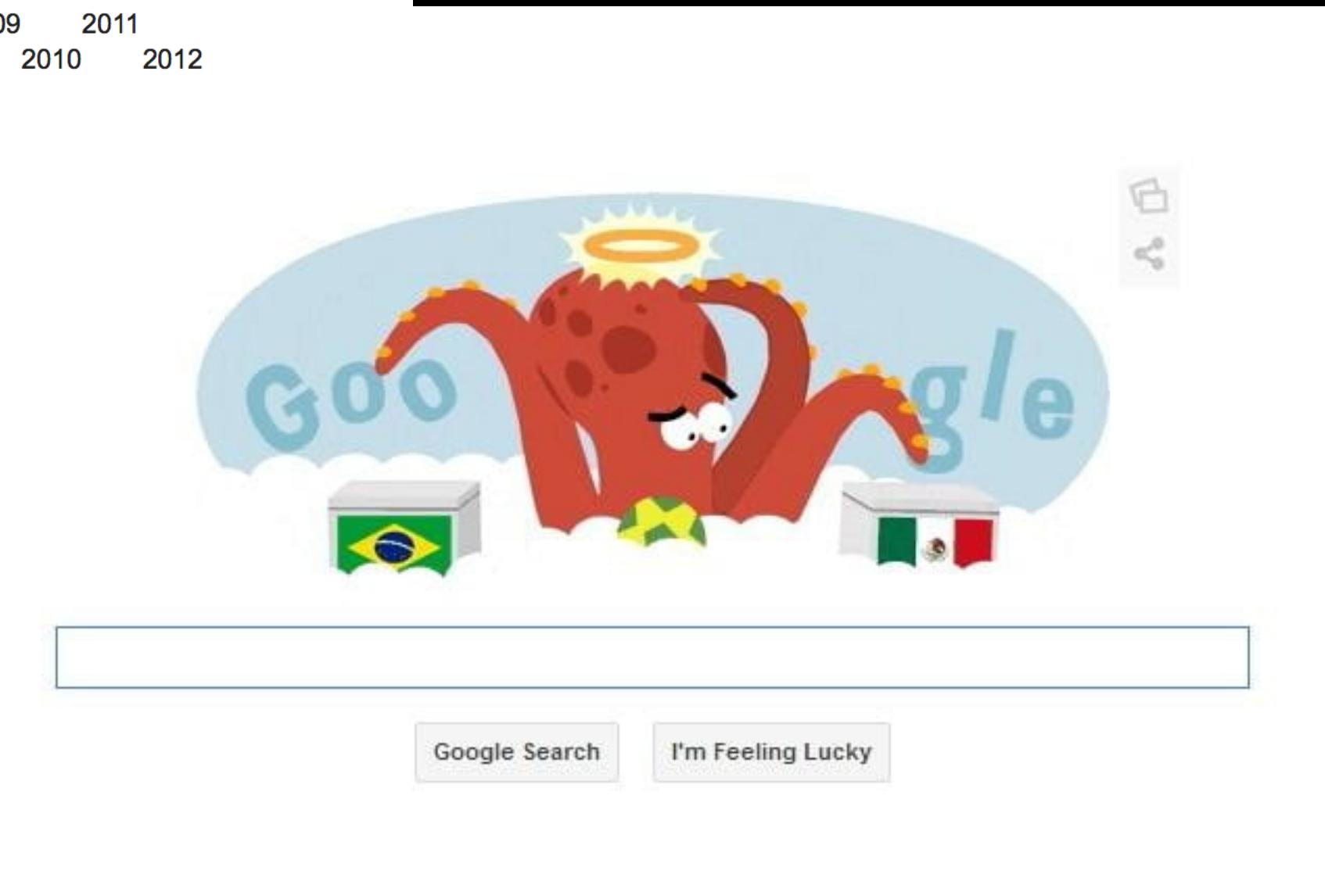
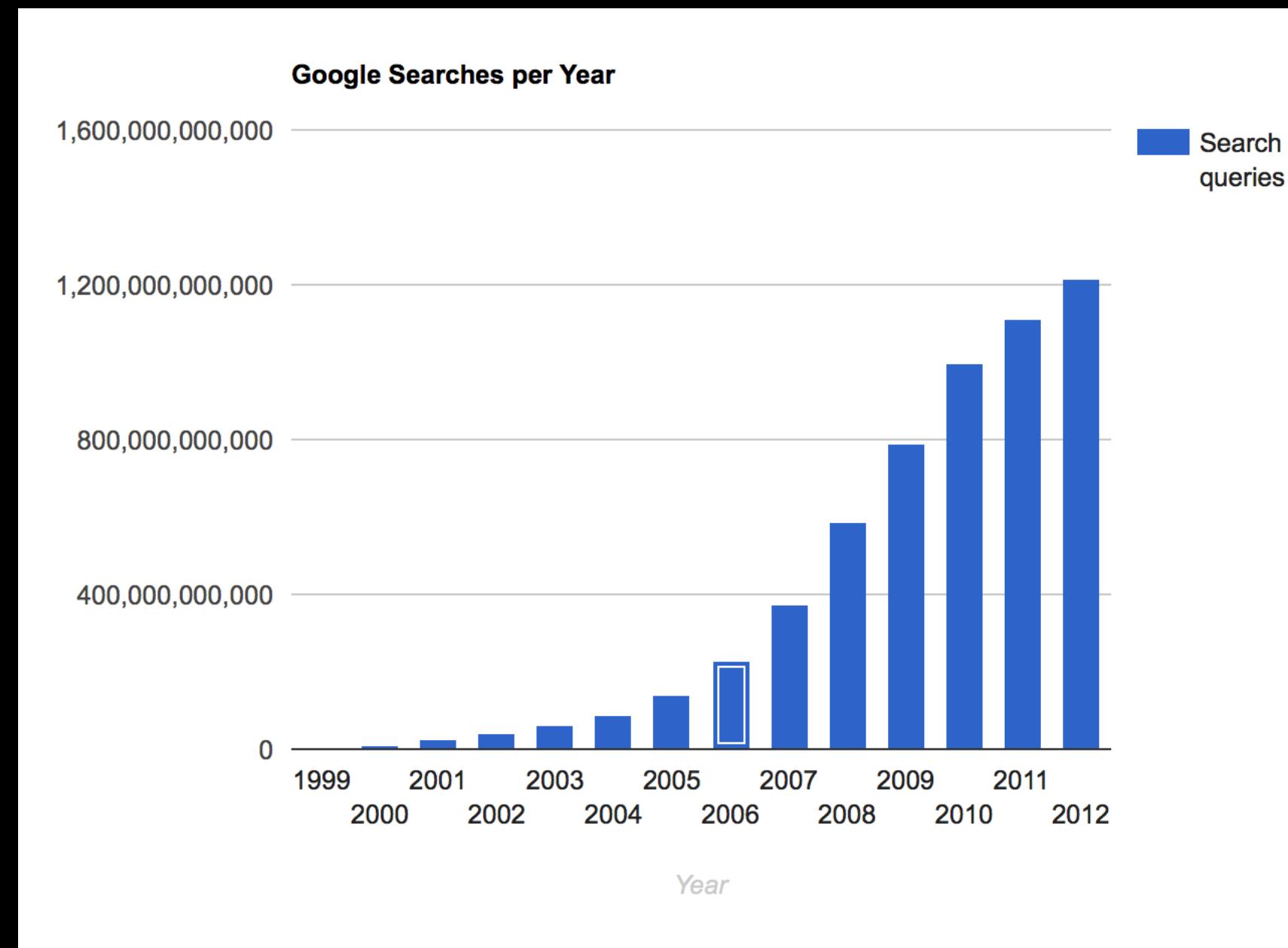
# High-performance computing in everyday life

- Cloud computing
- Search the web
- Identify a song
- Get directions
- Voice assistants
- Speech recognition



# Example: Google search

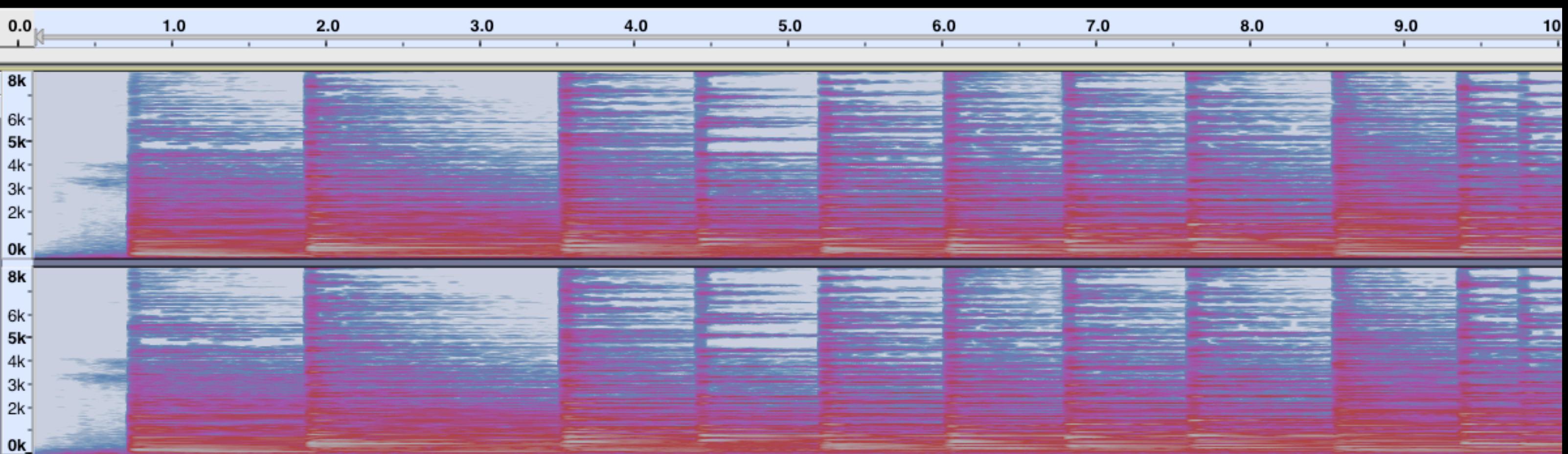
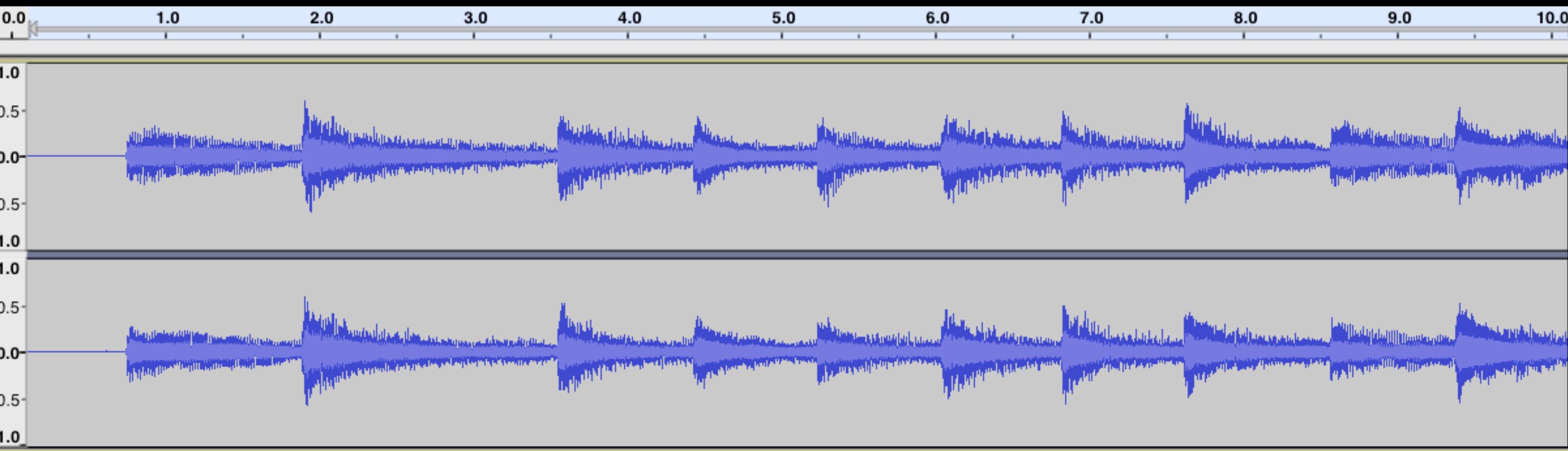
- Search  $\sim 10^{13}$  web pages
- $10^3$  “servers” per query
- Each query takes about 0.2 seconds
- $4 \times 10^4$  queries on average every second of every day
- If each server is “only”  $10^9$  FLOPS, Google search requires about  $10^{16}$  FLOPS



Images courtesy Google,  
internetlivestats.com

# Example: Shazam

- 200 queries on average every second of every day
  - Convert sound into time-frequency plots, filter to keep only the loudest notes
  - Compare to a large library
  - Similar to how LIFO searches data for gravitational waves!
  - One query is a PC-sized calculation, roughly





Amazon web services data center  
Courtesy [amazon.com](http://amazon.com)



Microsoft Azure data center  
(courtesy [sensorslab.co](http://sensorslab.co))

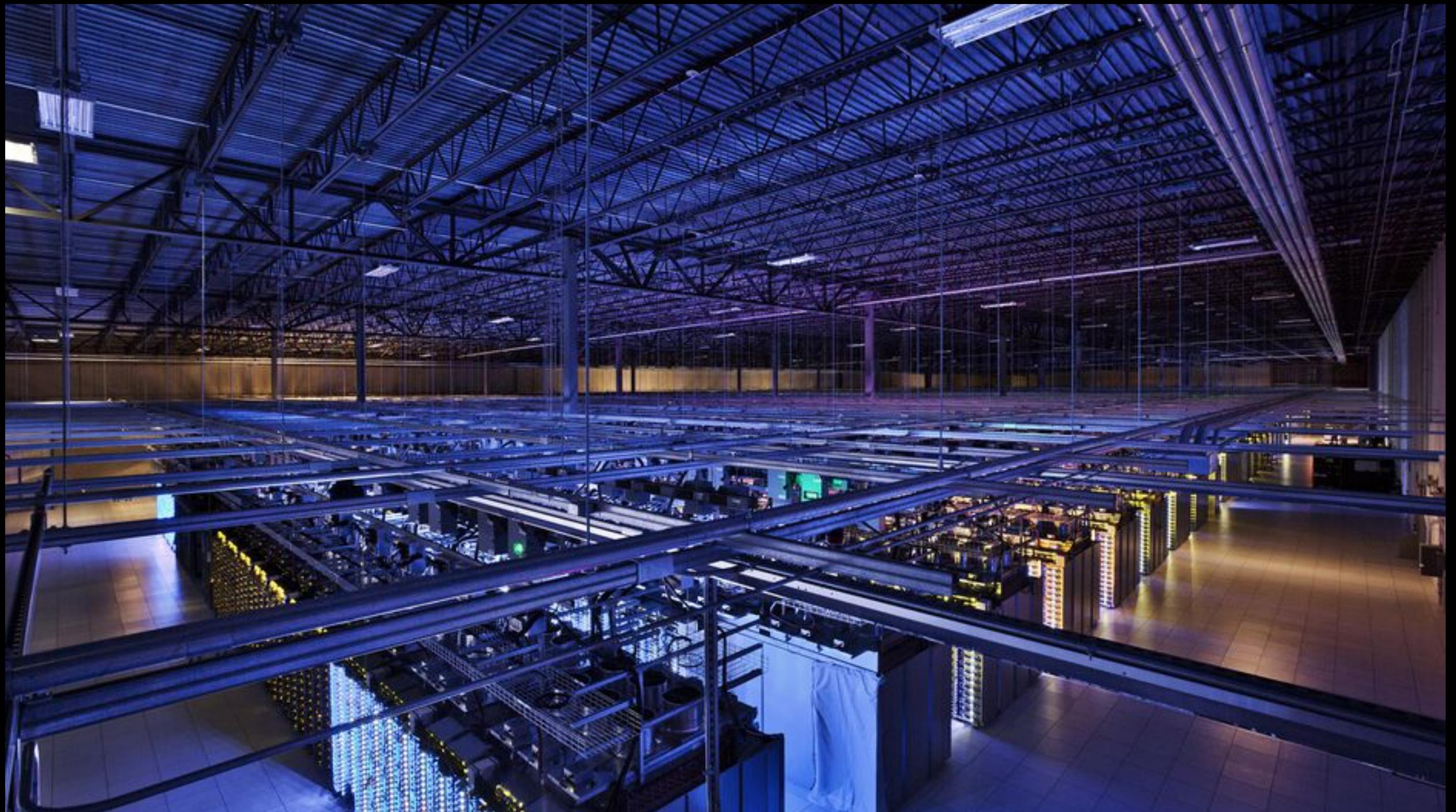
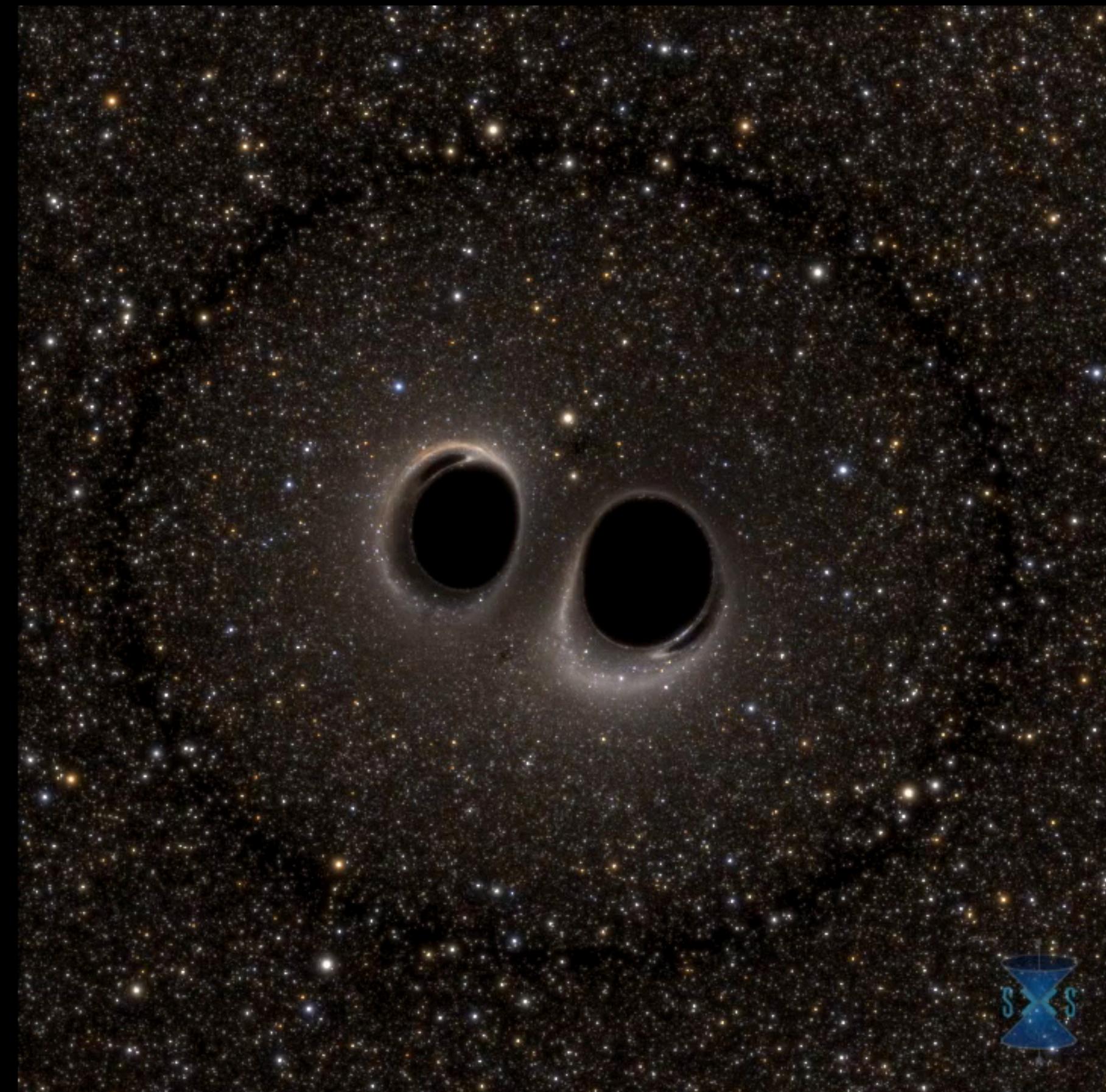


Image courtesy cnet: Google data center,  
Council Bluffs, Iowa  
Google: 60,000 searches/second

Provide many  $10^{15}$  FLOPS  
of performance to customers

# High-performance computing for science

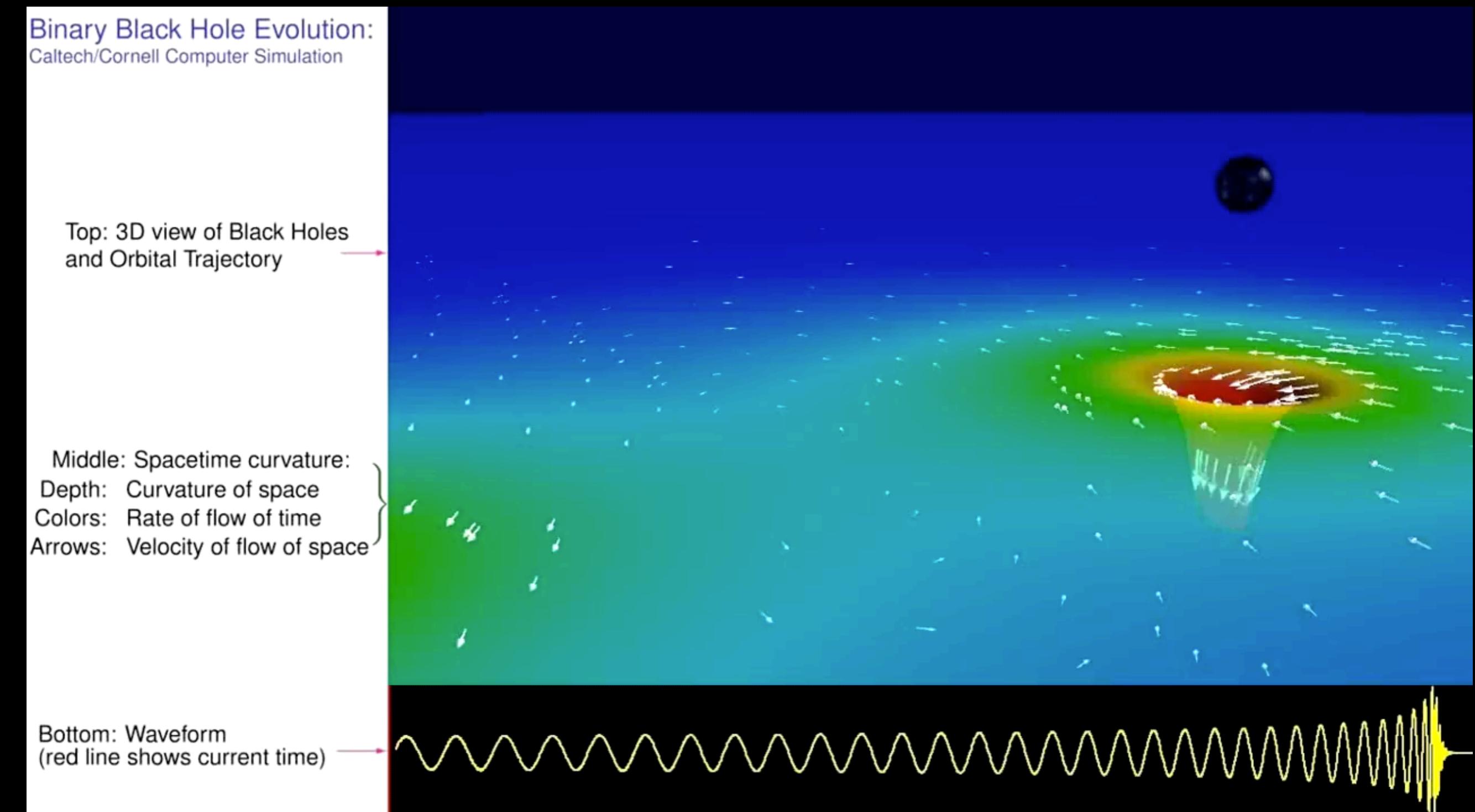
- Solve otherwise unsolvable problems
- Insight into scientific data & results
  - Experimental measurements
  - Results of calculations
  - Complicated pencil & paper results



Movie & calculation by undergraduate  
Haroon Khan, Nick Demos,  
Simulating eXtreme Spacetimes collaboration

# Example: Simulating colliding black holes

- Head-on collision example
  - About  $1.4 \times 10^{17}$  floating-point operations
  - 3 days (48 (slower) cores on ocean)
  - Several weeks on a typical laptop
- Inspiral, merger, ringdown example
  - About  $7.8 \times 10^{17}$  floating-point operations
  - 17 days (48 cores before merger, 36 cores after, on orca)
  - Months on a typical laptop



# Programming with Python

# Programming is like magic

- Say the right cryptic words and something cool happens
- Mess up a word and the spell fizzles



# Google collaborative

- [https://  
colab.research.google.com](https://colab.research.google.com)
- Google lets us program and run on their computers for free

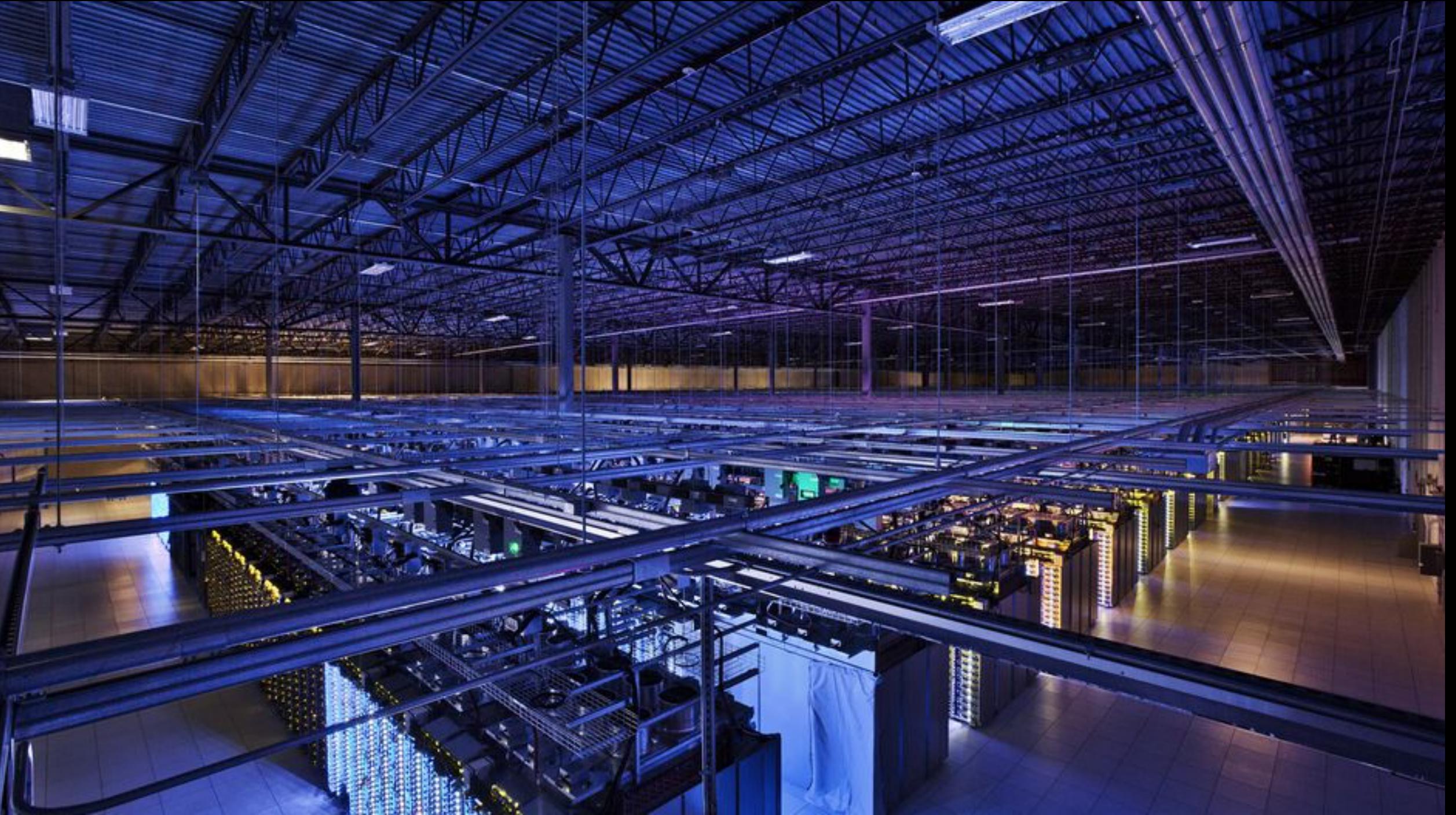


Image courtesy cnet: Google data center, Council Bluffs, Iowa

# Cocalc

- <https://cocalc.com>
- Hosted by Google
- Limited free service
  - This course: ~\$20/month paid plan (I paid, don't worry!)

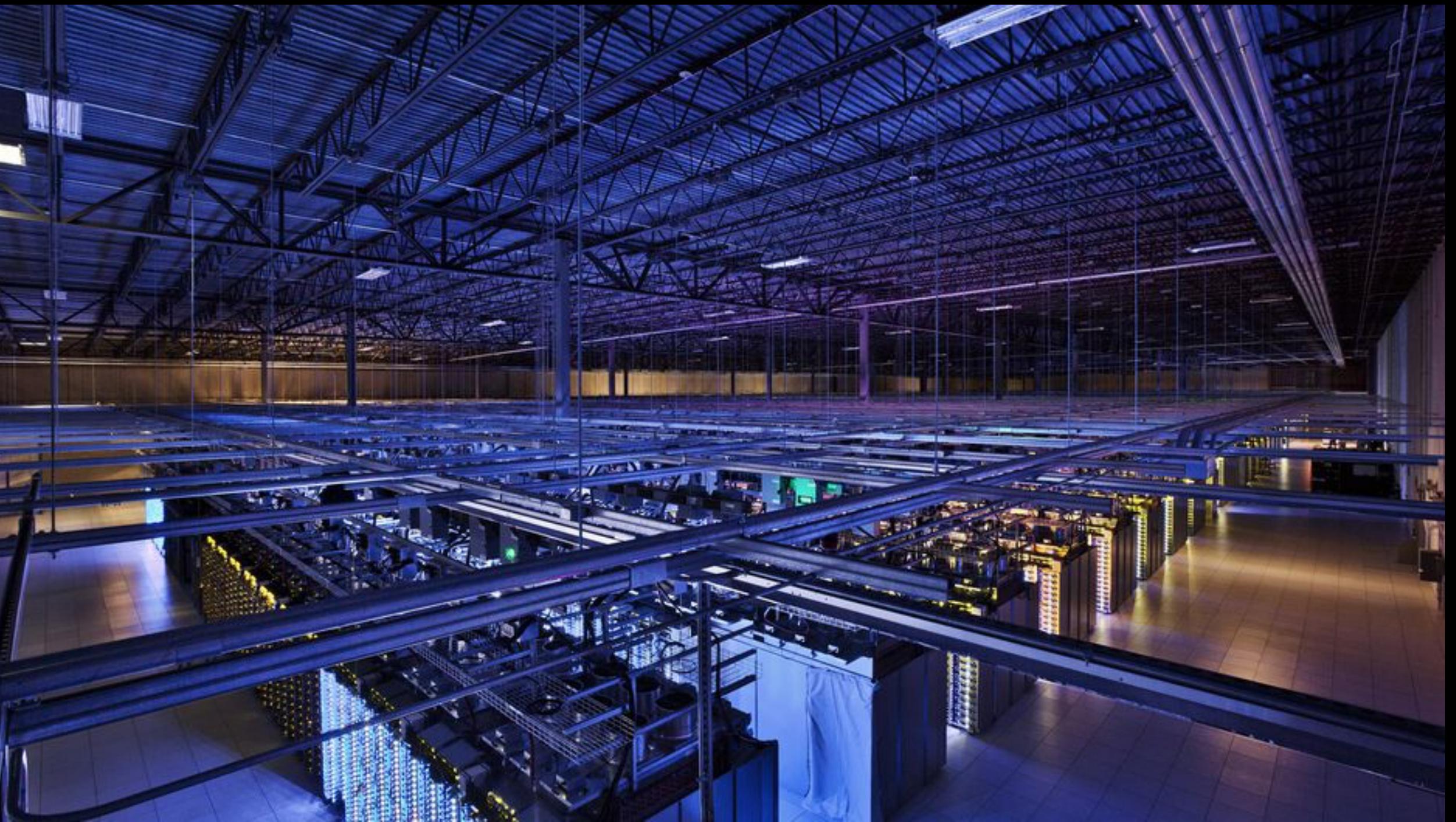
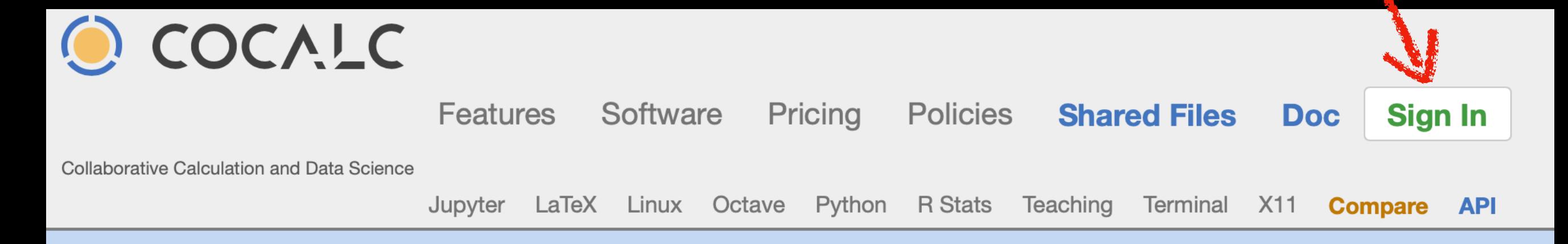
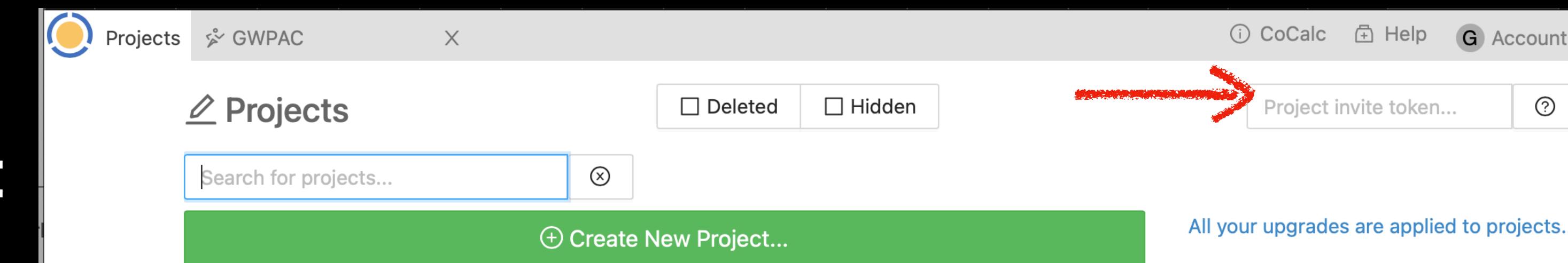


Image courtesy cnet: Google data center,  
Council Bluffs, Iowa

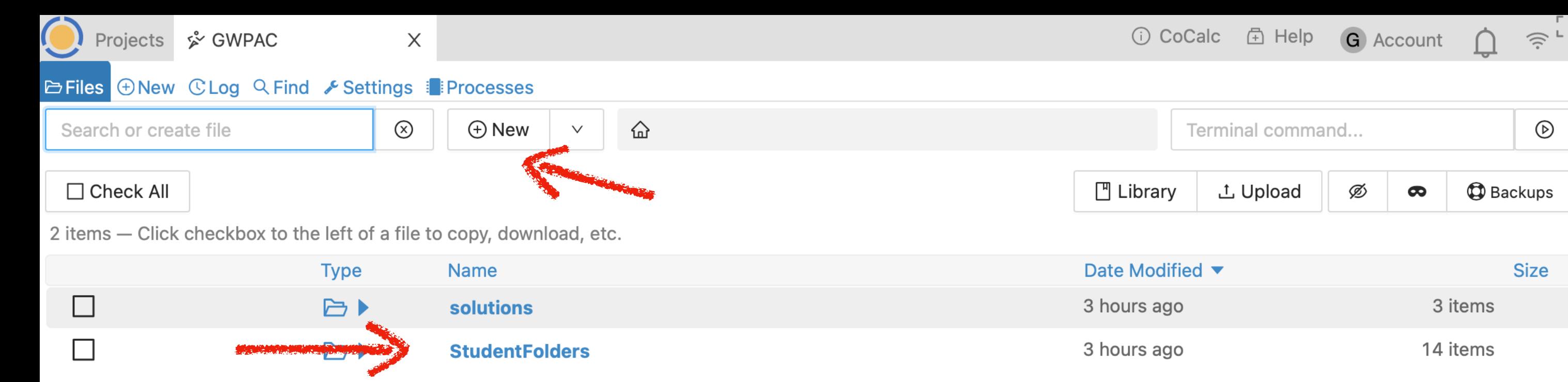
- Open <https://cocalc.com> and sign in



- See zoom chat for the "token": enter it in the "token" box and press enter



- Click "Welcome.ipynb"



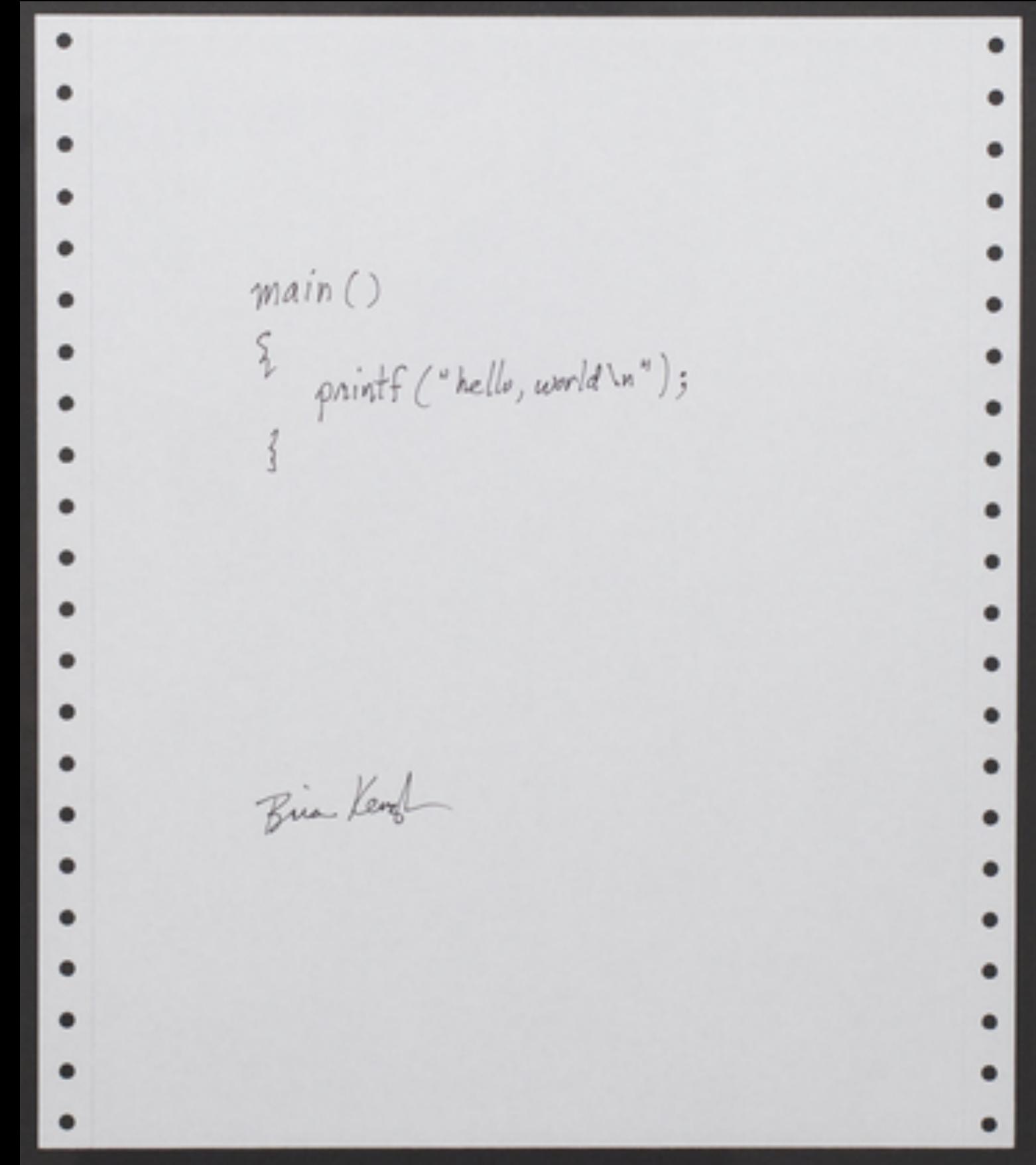
- Scroll to your name, and click in the blank box labeled "In [ ]:" below your name

# Output

- Your program needs to tell you the result
- Tradition since 1974: first program prints "Hello world"
- Python (language commonly used in scientific computing) makes this easy

Try:

```
print("Hello, world!")
```



Brian Kernighan  
(early UNIX developer), 1978

Try:

```
print(4*4+4-4)
```

# Libraries

- Don't reinvent the wheel when you want to hit the road
  - (But OK if you want to learn how to make wheels)
- Python has *many* libraries for numerical computing & everything else
- By "Libraries", I mean any pre-written code that you can use in your programs

Try in tutor:

```
import math  
print(math.pi)
```

# Math

Try in tutor (only type  
the left hand  
side of the ==):

- Arithmetic operations built in

```
(4 + 4) * 4 / 4 - 4
```

- Exponents with \*\*

```
4 ** 4 == 256
```

- Scientific notation

```
4e4 == 40000
```

- The rest in the math library

```
math.sin(4)  
math.sqrt(4)
```

# Expressions

- Value = piece of data of a particular type

4.444

"Hello world"

- Type = kind of data

float

string

- Operator = combine values  
to get a new value

+ - \* /

+

- Behavior depends on type

- Expression = group of  
values and operators

4.0 \* 3.0 - 2.0

"Hello" + " world"

- Python evaluates expressions,  
like a calculator

# Clicker question #2.0

- What does Python get when it evaluates this expression?

**4.0 \* 3.0 - 2.0**

- A 4.0
- B 10.0
- C Some other number
- D An error

# Try out some expressions

```
4.0 * 3.0 - 2.0
```

```
"Hello" + " world"
```

# Try out some expressions

```
print(4.0 * 3.0 - 2.0)
```

```
print("Hello" + " world")
```

*#make up your own*

# Some types we will need

- Float
- Int
- String
- Boolean

# Type: float

- **Values:** real numbers (“numbers with decimal points”)

- Examples

4.1234

4.0

4.4e2

-5.2e-3

- If you don't include a decimal point, it is an integer!

- Operators:

+ - \* / \*\*

## Try in tutor:

```
print(22.0 / 7.0)
```

```
print(8.0**2.0)
```

```
print(type(4))  
print(type(4.0))
```

```
print(-3.0e-3 * 10.0)
```

```
print(1.0/3.0)
```

# Type: int

- **Values:** integers (whole numbers, positive, negative, zero)

- Examples

-4

742352046

7

-33

- Don't use commas when typing an int or float

- Operators: + - \* \*\*

/

// %

## Try in tutor:

```
print(2**8)
```

```
print(4 * 3 - 2)
```

```
print(7 / 3) #float in Python3,  
           #int in Python2 (avoid! )
```

```
print(7 // 3) # quotient  
print(7 % 3) # remainder
```

# Clicker question #2.1

- In Python 3, what is the value of this expression?

```
10 // 3 + 1
```

A

4

B

4.3333333333

C

Some other number

D

An error

# Type: boolean

- **Values:** true or false

- Examples

True

False

- **Operators:** and or not

- a **and** b    is true if both are true, false otherwise

- a **or** b    is true if a is true, b is true, or both are true  
is false if both a and b are false

- **not** a    is true if a is false, false if a is true

# = and ==

- = stores results in a named object ("variable")

```
myNumber = 4  
print(myNumber * myNumber)
```

```
print(myNumber * myNumber == 16)  
True
```

- == tests whether two objects are equal

```
print(2 + 2 == 5)  
False
```

# Try some of these

```
a = True  
b = True  
c = False  
d = False
```

- = stores results in a named object ("variable")
- == tests whether two objects are equal

```
print(2 + 2 == 4 and 3 + 3 == 6)
```

```
print(2 + 2 == 4 and 3 + 3 == 7)
```

```
print(2 + 2 == 4 or 3 + 3 == 7)
```

```
print(not 3 + 3 == 7)
```

# Pick a few of these

```
print(a)
```

```
print(not c)
```

```
print(not a)
```

```
print(a or b)
```

```
print(a or c)
```

```
print(c or d)
```

```
print(a and b)
```

```
print(a and c)
```

```
print(c and d)
```

# Converting types

Try in tutor:

```
q = 4  
print("The number is "+q)
```

```
print(type(4))  
print(type(str(4)))  
print(type(float(4)))
```

```
q = 4  
print("The number is "+str(q))
```

# Clicker question #2.2

- What does this line print?

```
import math  
print("The value of pi is "+math.pi)
```

A

The value of pi is 3.141592653589793

B

The value of pi is math.pi

C

Something else but not an error

D

An error

# Clicker question #2.2

- What does this line print?

```
import math  
print("The value of pi is "+str(math.pi))
```

A

The value of pi is 3.141592653589793

B

The value of pi is math.pi

C

Something else but not an error

D

An error

# Comments

- Comments explain what you're doing
- Use comments to explain your code
- Use names that help explain, even without comments

```
# Say hello to someone by name
personName = "Geoffrey"
print("Hello " + personName)
```



**Go to cocalc Day2.ipynb**

# Functions

Try in cocalc (YOU -> your initials)!

```
def square_YOU(x):  
    return x*x
```

```
square_YOU(4)  
16
```

- Input(s) ("arguments")
- Returns output
- Functions can call other functions

# Activity

- Define a function that takes a decimal  $x$  and returns  $\cos(\cos(x))$
- Hint: use `math.cos()`
- Print the result for some test number

# Activity

- Define a function "cos2Times" that takes a decimal x and returns  $\cos(\cos(x))$
- Hint: use `math.cos()`
- Print the result

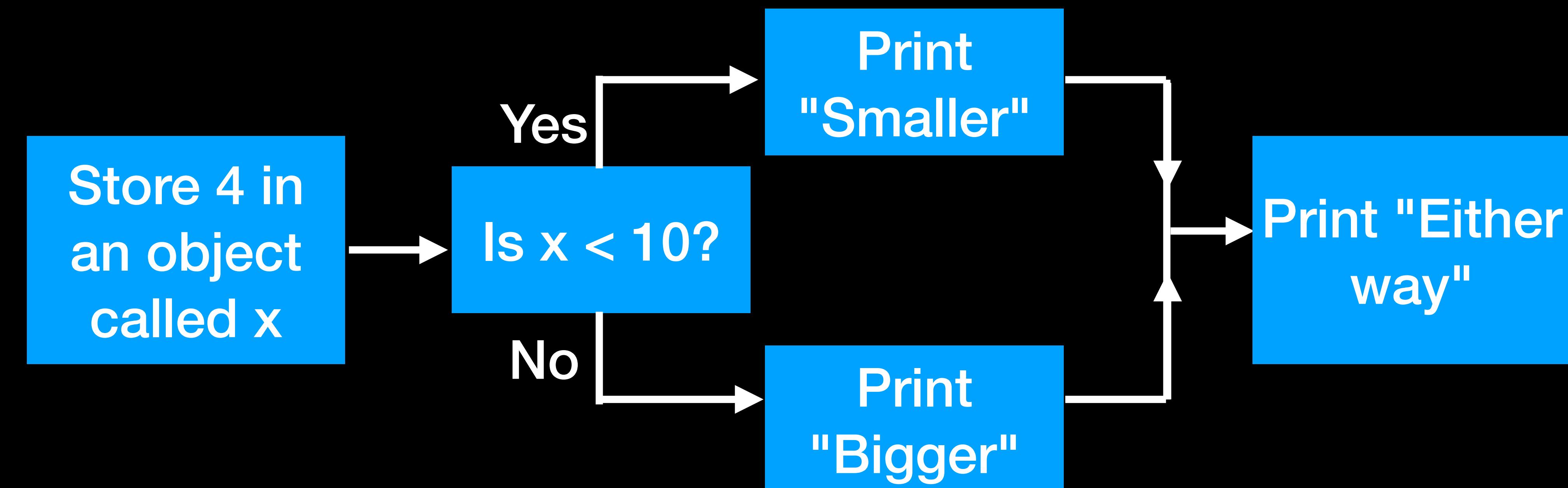
```
import math
def cos2Times(x):
    return math.cos(math.cos(x))
print(cos2Times(44.44))
print(cos2Times(0.0))
```

# If/else

- If does the first indented thing if the stuff in () is True
- Otherwise it does the indented stuff under "else"

```
x = 4
if(x < 10):
    print("Smaller")
else:
    print("Bigger")
print("Either way.")
```

Try in cocalc!

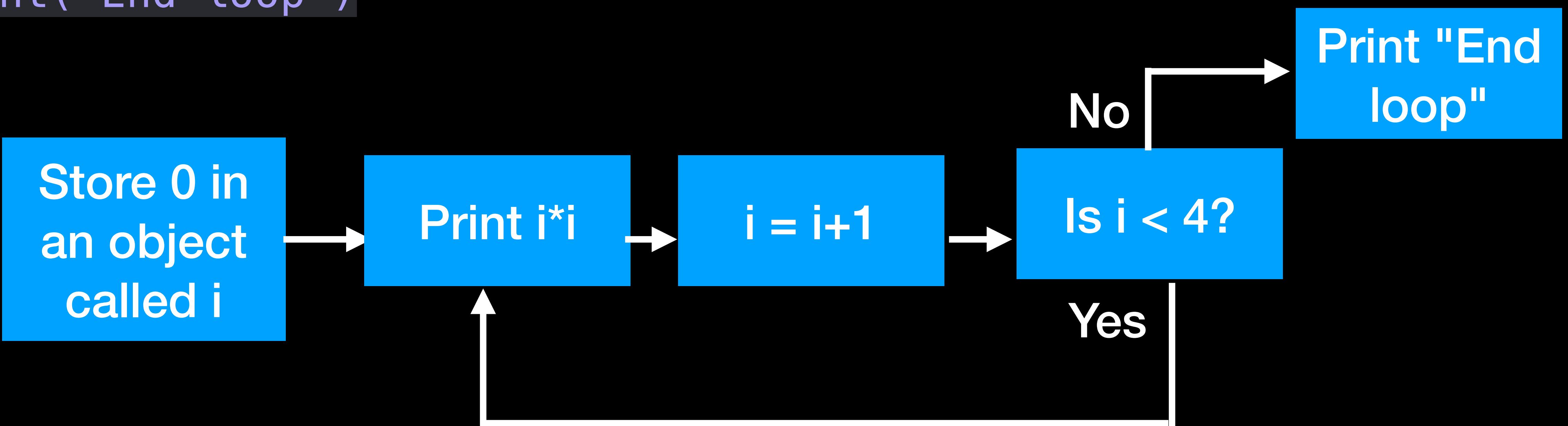


Try in tutor!

```
i = 0
while i < 4:
    print(i*i)
    i = i + 1
print("End loop")
```

0  
1  
4  
9

# Loops



# Loops

```
for i in [1,2,3,4]:  
    print(i*i)
```

```
0  
1  
4  
9
```

```
i = 0  
while i < 4:  
    print(i*i)  
    i = i + 1
```

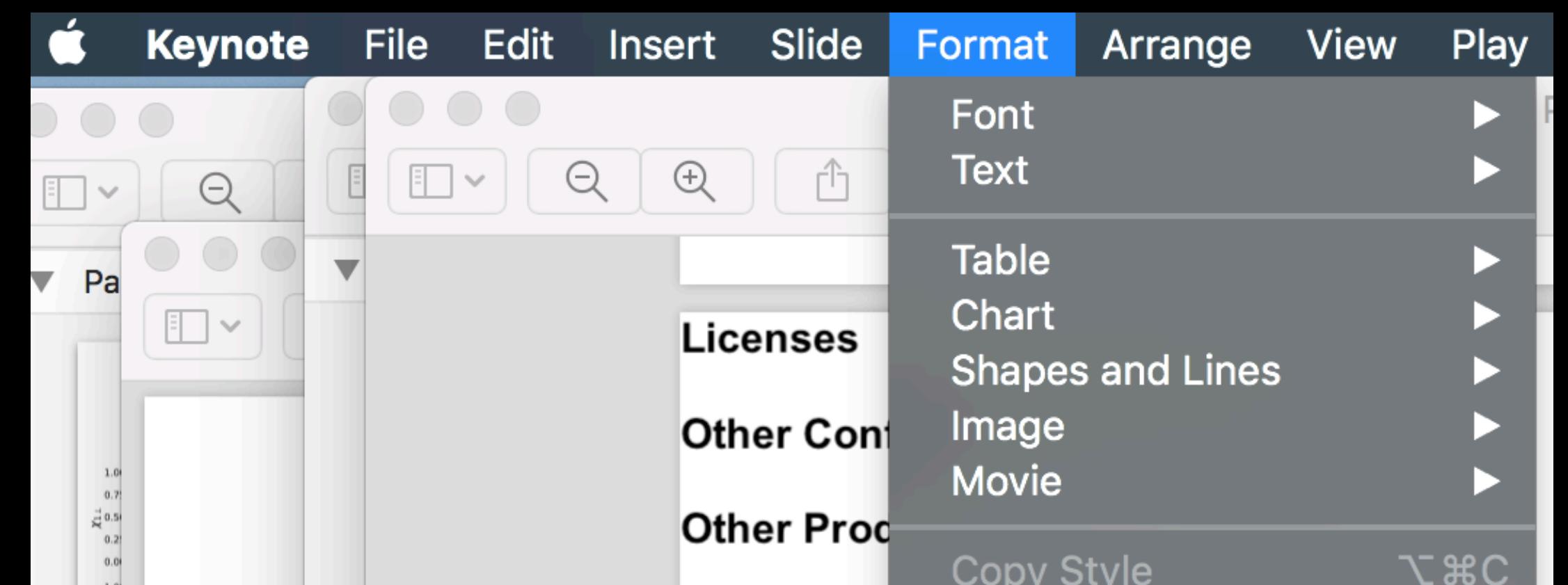
```
0  
1  
4  
9
```

So far, our programs just run & stop...  
How do programs with a user interface work?

# Loops

- Real life:  
event loop
- Event = key press,  
mouse/trackpad  
click,  
...

```
while message != quit:  
    message = get_next_message()  
    process_message(message)
```



# My first program

- Basic, 1987
- Python equivalent

```
10 PRINT "GEOFFREY"  
20 GOTO 10
```

```
done = False  
while not done:  
    print("Geoffrey")
```

# Clicker question #2.2b

- What does this program print?

```
x = 4
if x==10:
    print('yes')
else:
    print('no')
```

- A Yes
- B No
- C The code gives an error

# Clicker question #2.2b

- What does this program print?

```
x = 4
if x==10 or x==11:
    print('yes')
else:
    print('no')
```

- A Yes
- B No
- C The code gives an error

# Clicker question #2.2

- What does this program print?

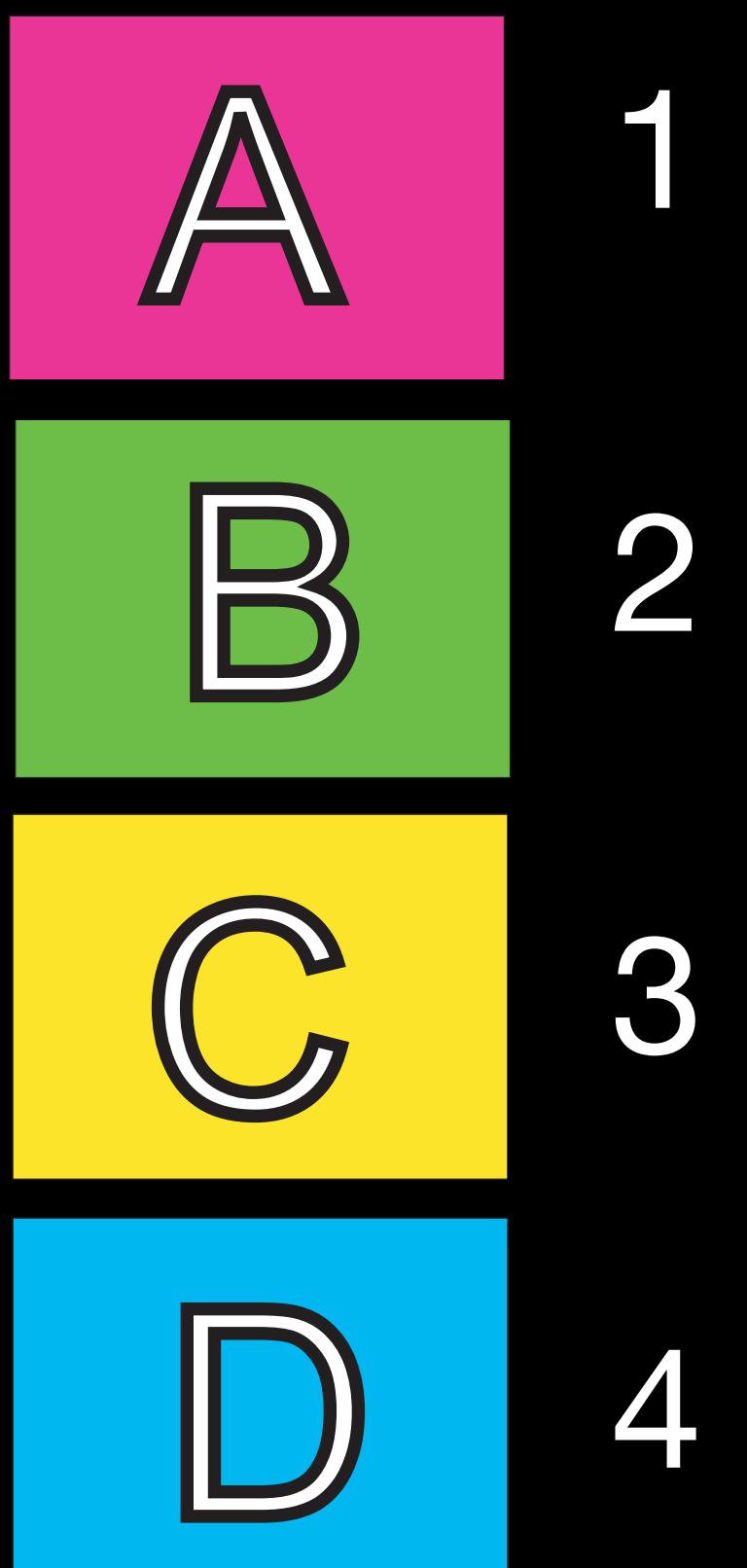
```
x = 4
if x==10 or 11:
    print('yes')
else:
    print('no')
```

- A Yes
- B No
- C The code gives an error

# Clicker question #2.3

- What does this program print?

```
j = 1  
while j < 3:  
    j = j + 1  
print(j)
```



# Clicker question #2.4

- What does this program print?

```
product = 1
j = 1
while j < 3:
    product = product * j
    j = j + 1
print(product)
```

- A 1
- B 2
- C 6
- D 24

# Clicker question #2.4b

- What does this program print?

```
product = 1
j = 1
while j < 4:
    product = product * j
    j = j + 1
print(product)
```

- A 1
- B 2
- C 6
- D 24

# Clicker question #2.4c

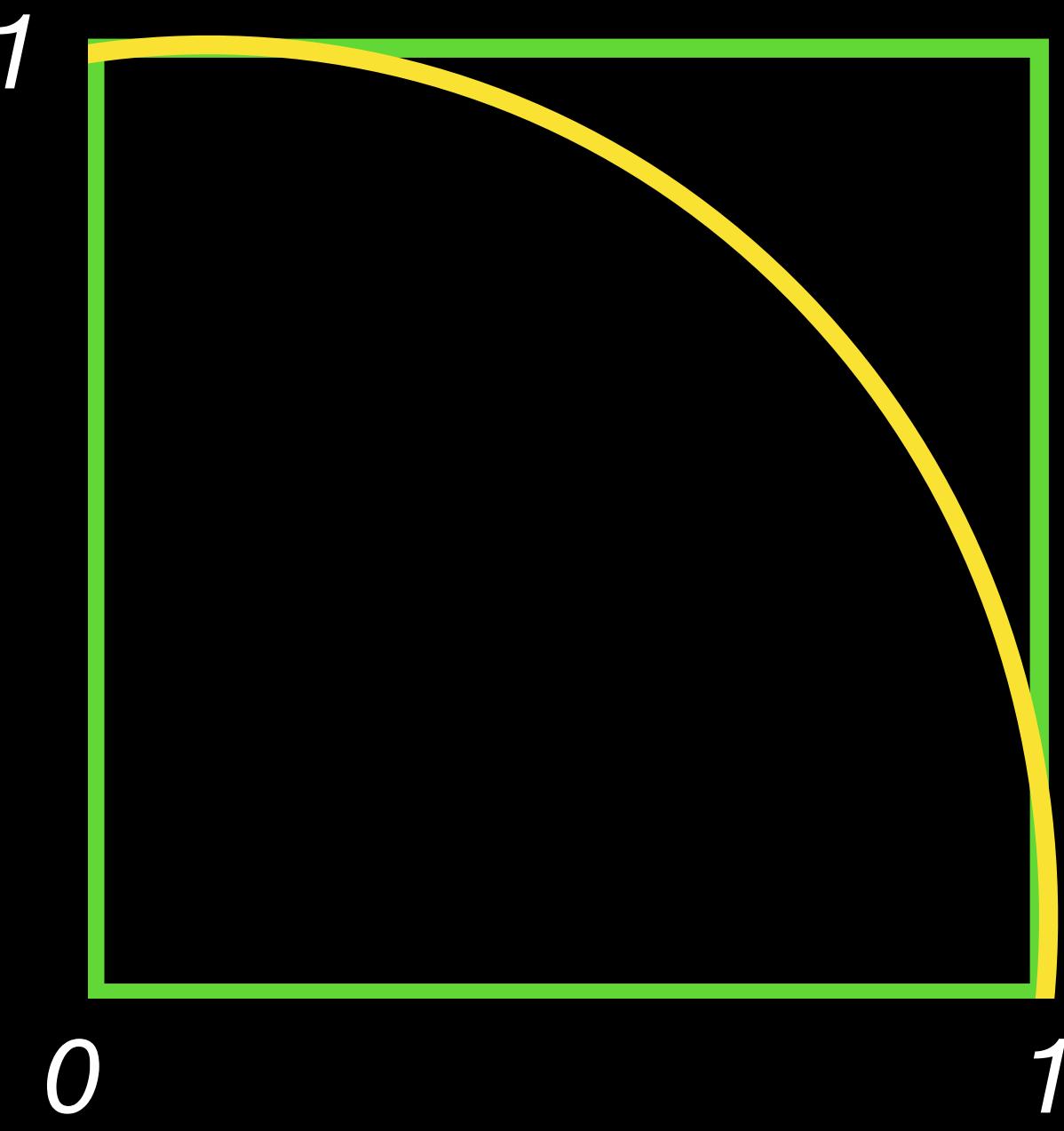
- What value of x makes the program print 24?

```
product = 1
j = 1
while j < x:
    product = product * j
    j = j + 1
print(product)
```

- A 3
- B 4
- C 5
- D 6

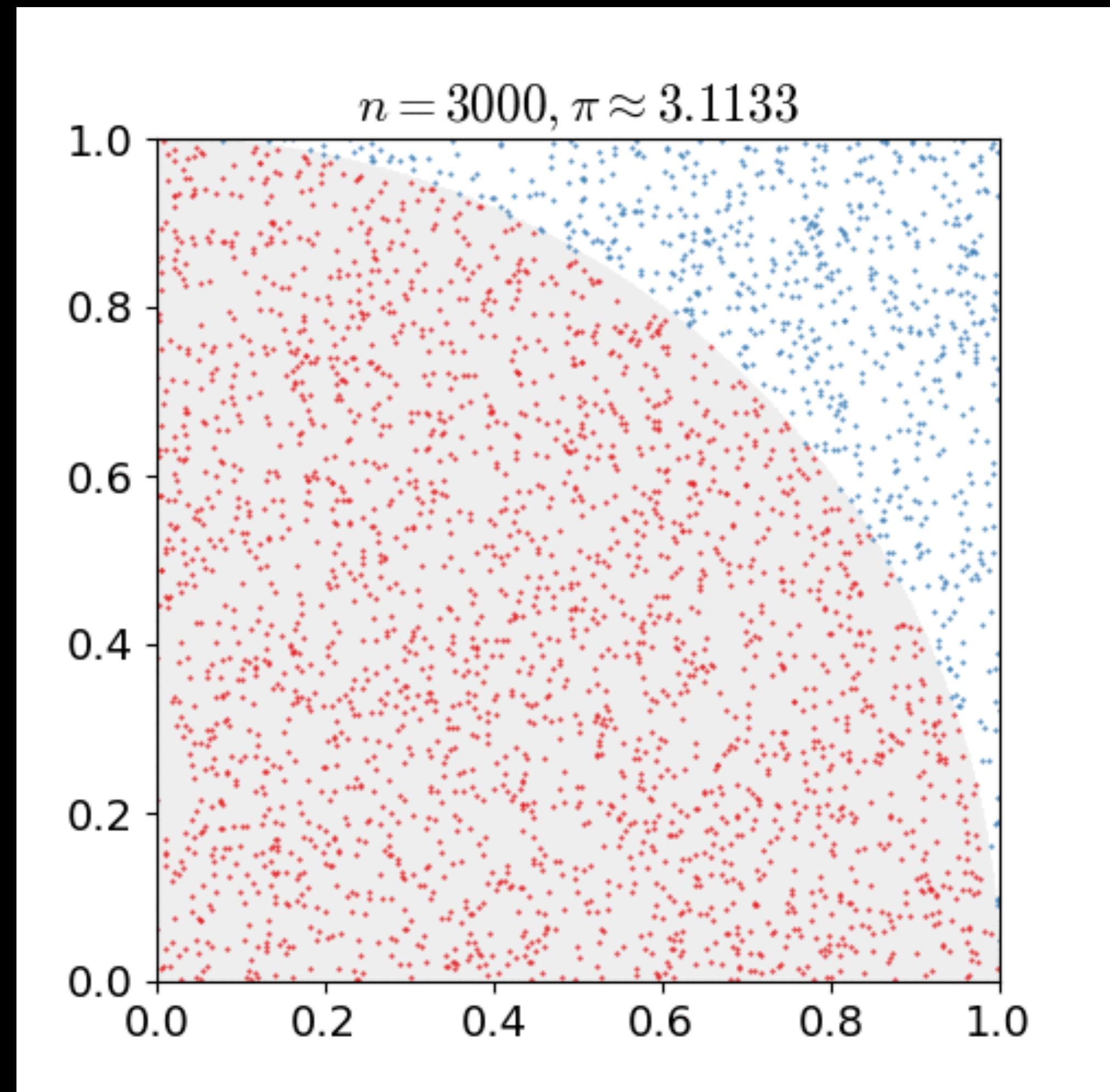
# A silly way to compute $\pi$

- Area of circle?
- Area of square?
- Idea: throw darts in square
  - $(\text{circle area}) \div (\text{square area}) \approx \text{darts in circle} \div \text{darts in square} = \text{"hits" / ("hits" + "misses")}$



# A silly way to compute $\pi$

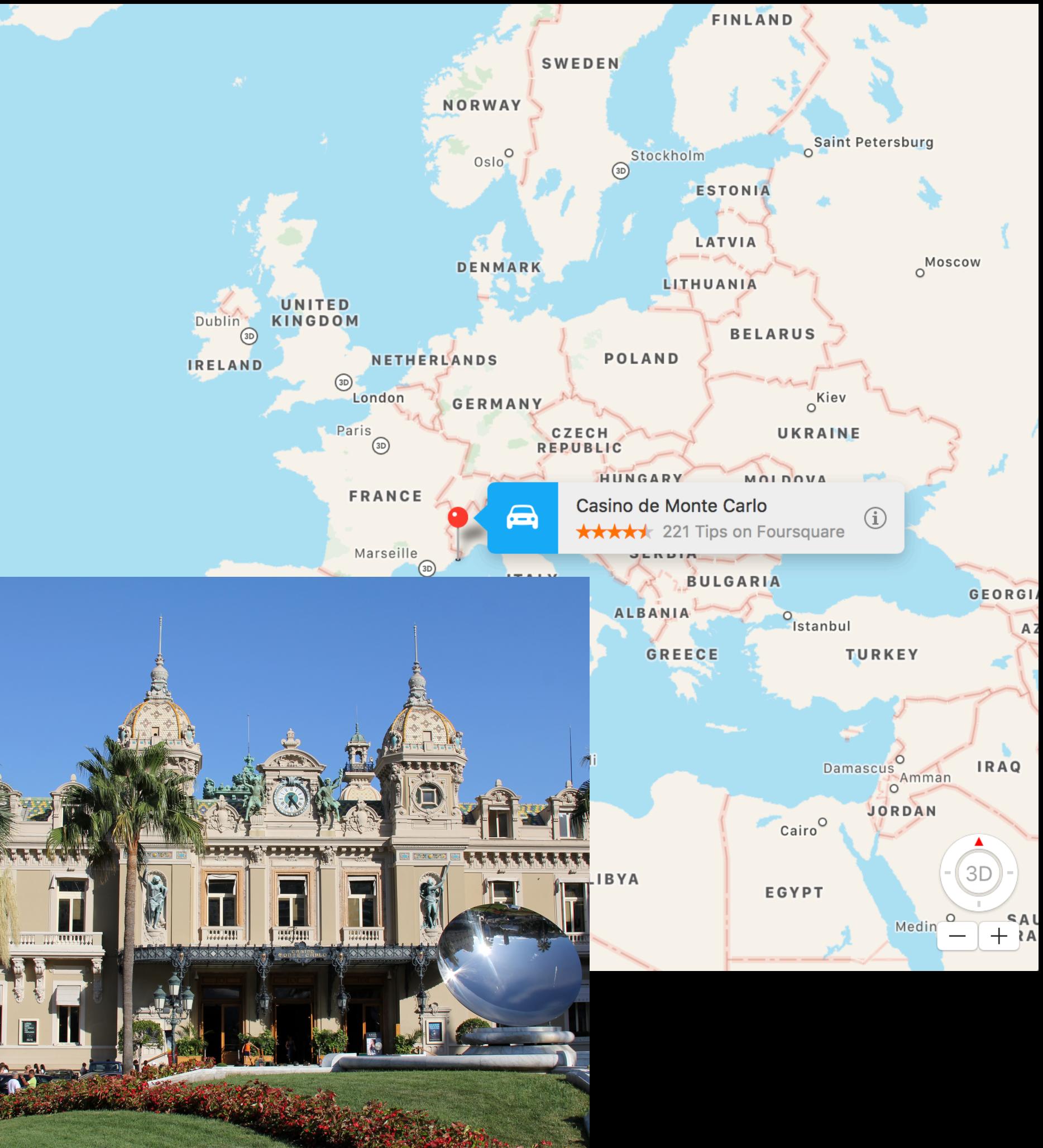
- Throw darts in square
  - $(\text{circle area}) \div (\text{square area}) \approx \text{darts in circle} \div \text{darts in square} = \pi/4$



Courtesy wikipedia

# Monte Carlo methods

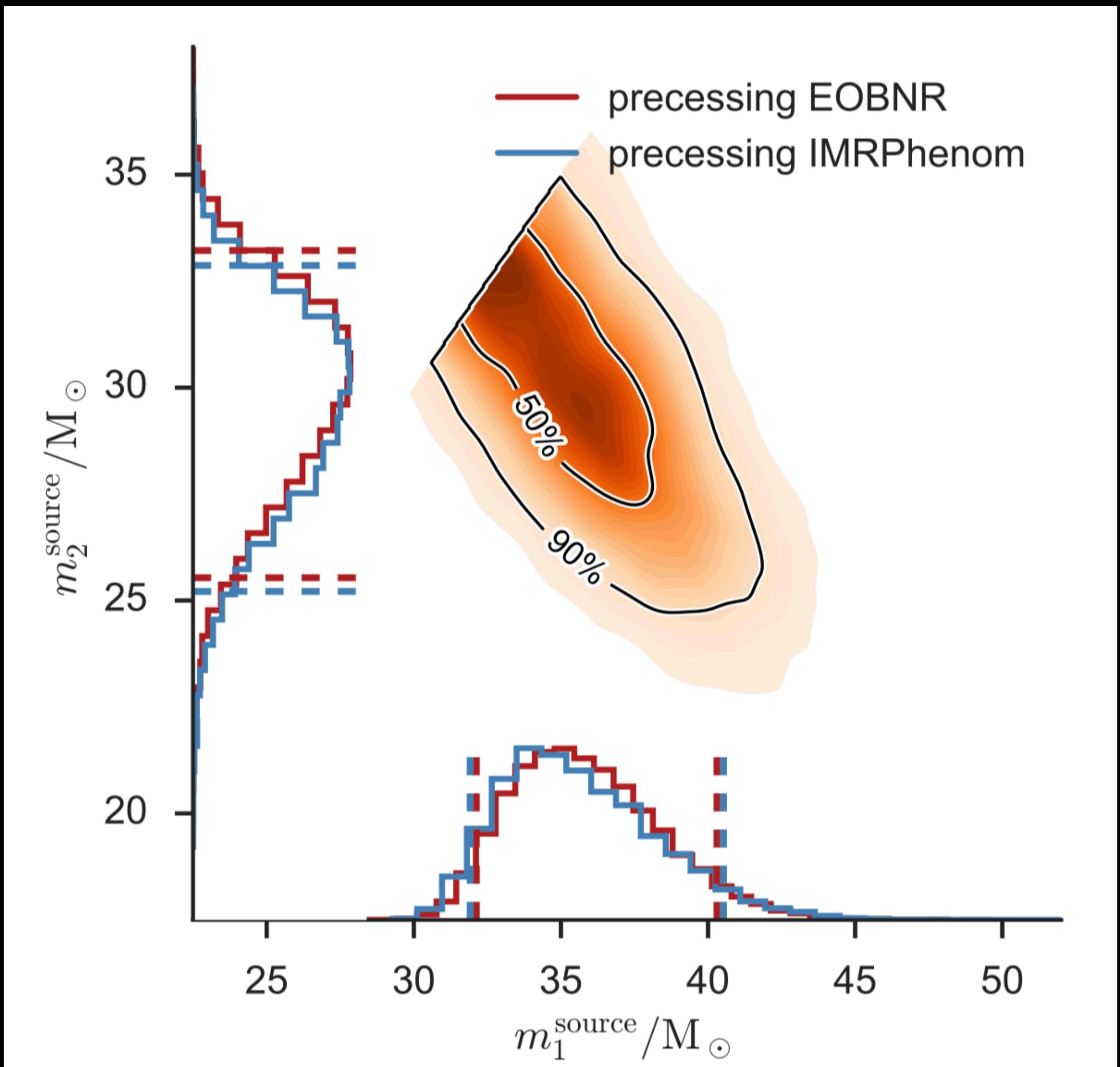
- This idea might seem silly, but it actually has a lot of uses in physics
- **Monte Carlo methods: use repeated random numbers to get results**
- Min/max of functions  
*especially functions of many variables*
- Integrals  
*especially high dimensional*
- Explore probability distributions



Images courtesy Wikipedia, Apple Maps

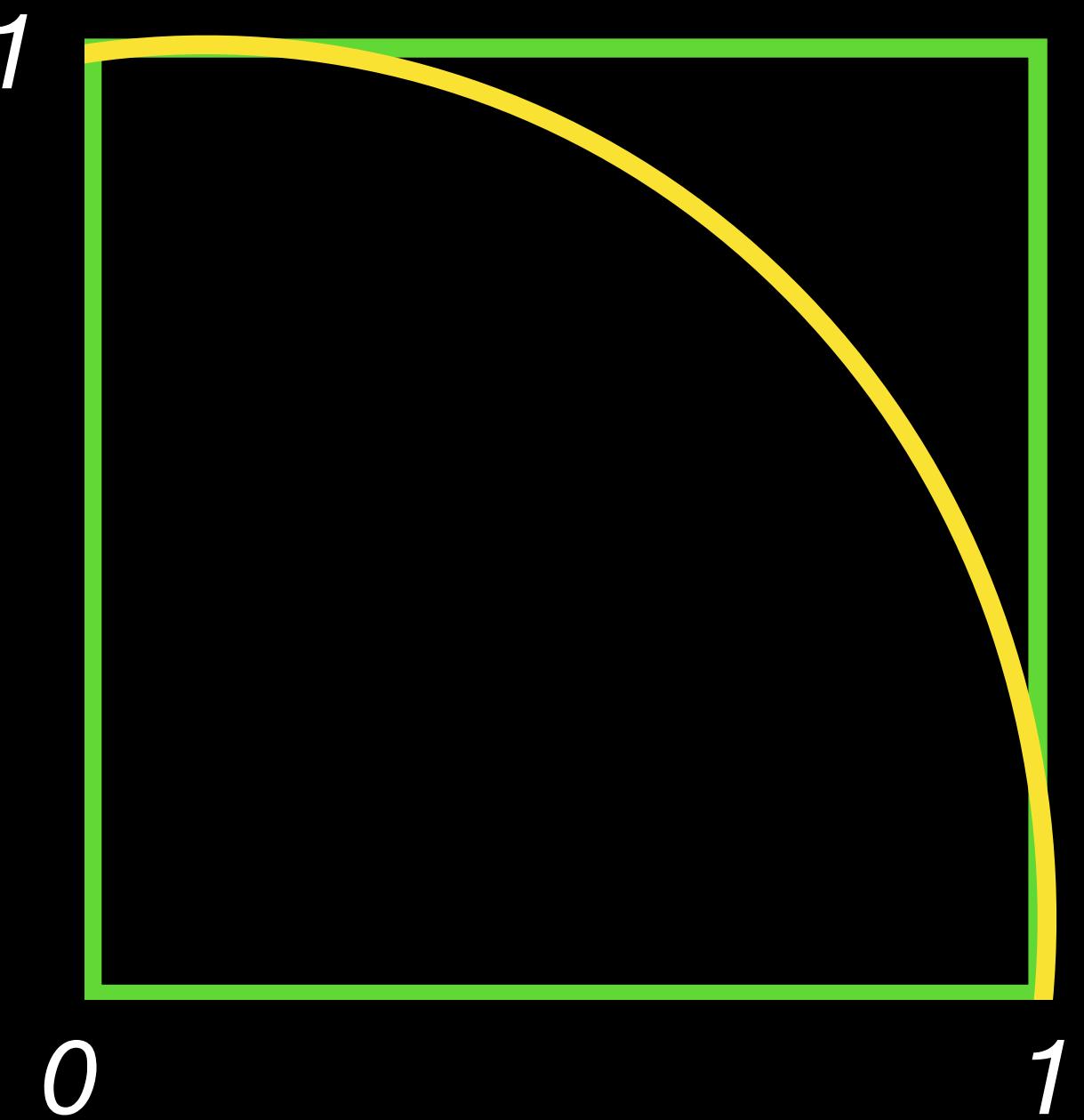
# Monte Carlo methods

- This idea might seem silly, but it actually has a lot of uses in physics
- When we observe a gravitational wave from merging black holes...
  - What kinds of black holes made the waves?
  - Choose random parameters (masses, spins, ...)
  - Compute the corresponding grav. wave
  - More likely to call the wave a “hit” the better it matches—vs. the last wave “hit”



GW150914: Abbott+ (2016)

# Pi Dartboard 1



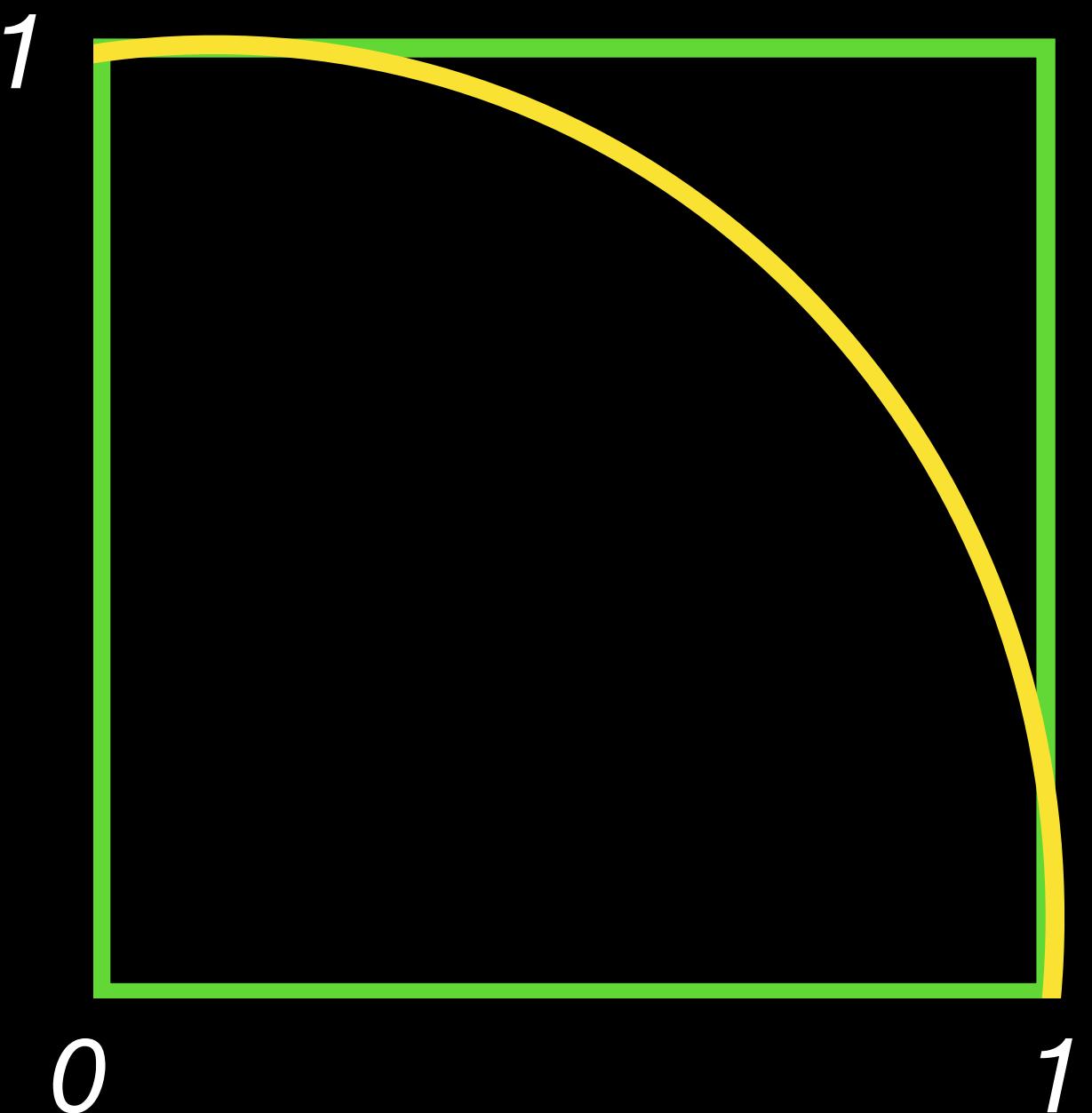
- Write a program that prints one random number between 0 and 1

```
import math  
import random  
print(random.random())
```

# Pi Dartboard 2

- **Challenge:** Modify your program
  - Store the random number in a variable x
  - Store a second random number in a variable y
  - Print x and y

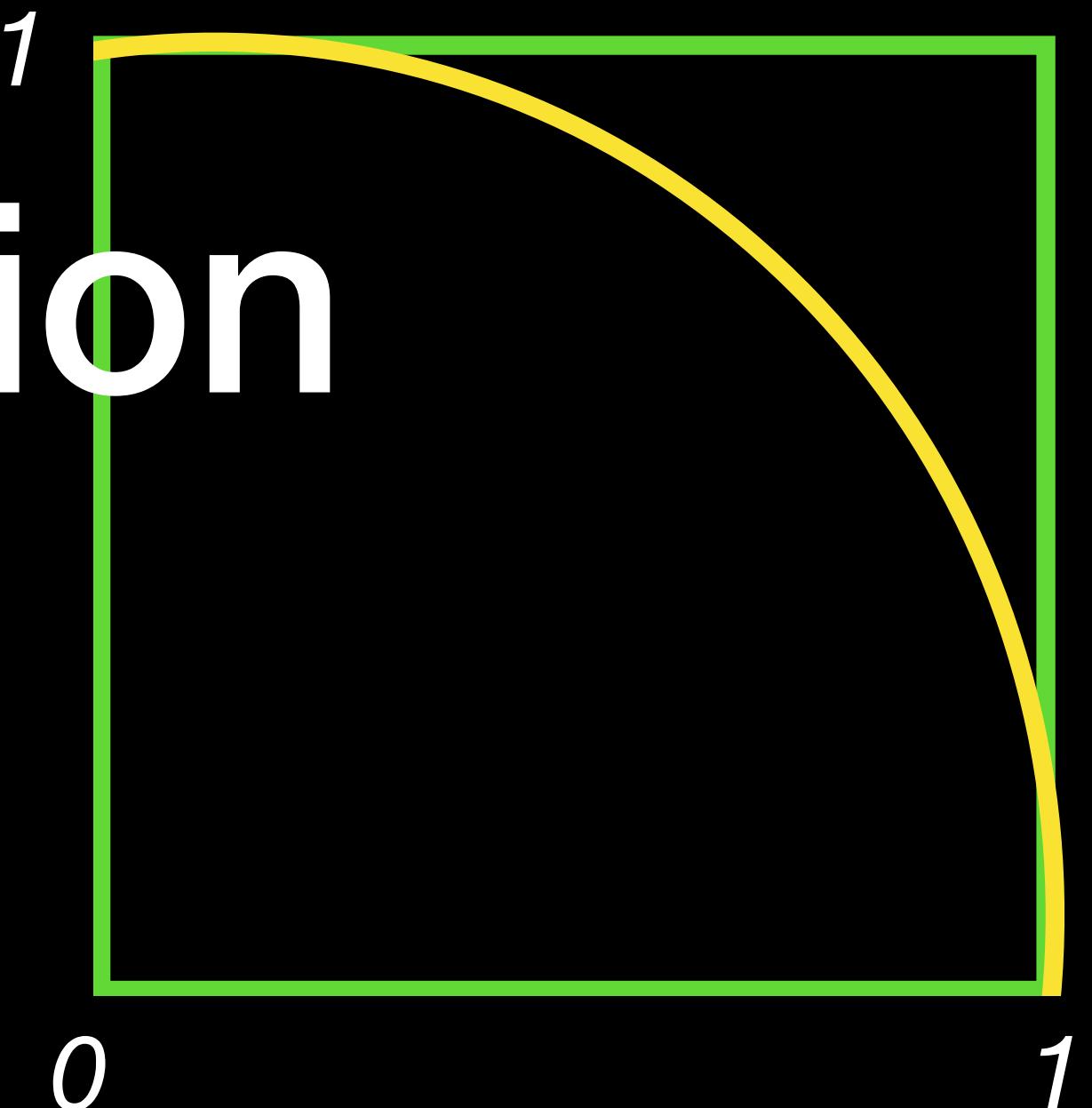
```
import math  
import random  
print(random.random())
```



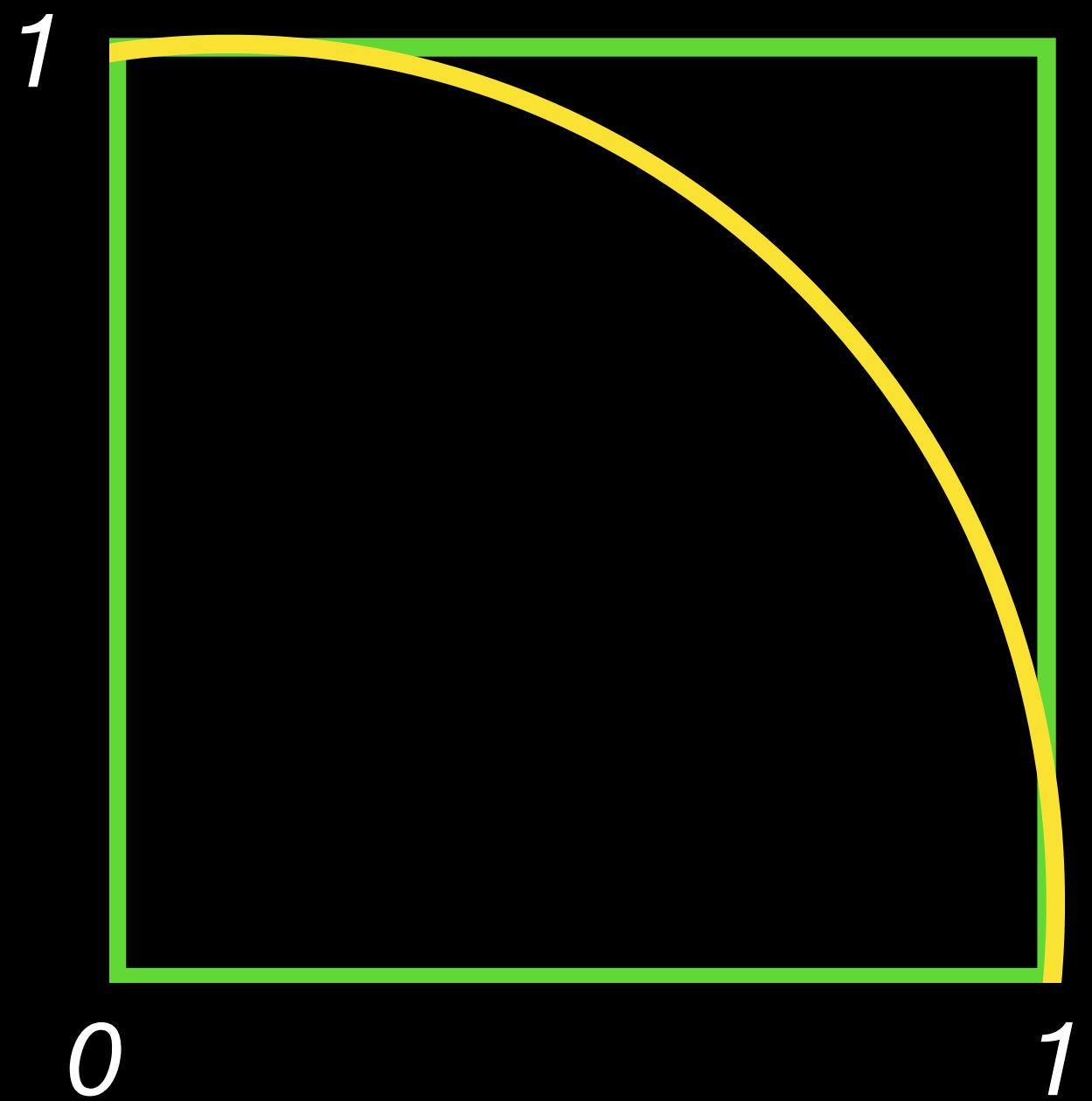
# Pi Dartboard 2 Solution

- **Challenge:** Modify your program
  - Store the random number in a variable x
  - Store a second random number in a variable y
  - Print x and y

```
import math  
import random  
  
x = random.random()  
y = random.random()  
  
print(x)  
print(y)
```



# Pi Dartboard 3

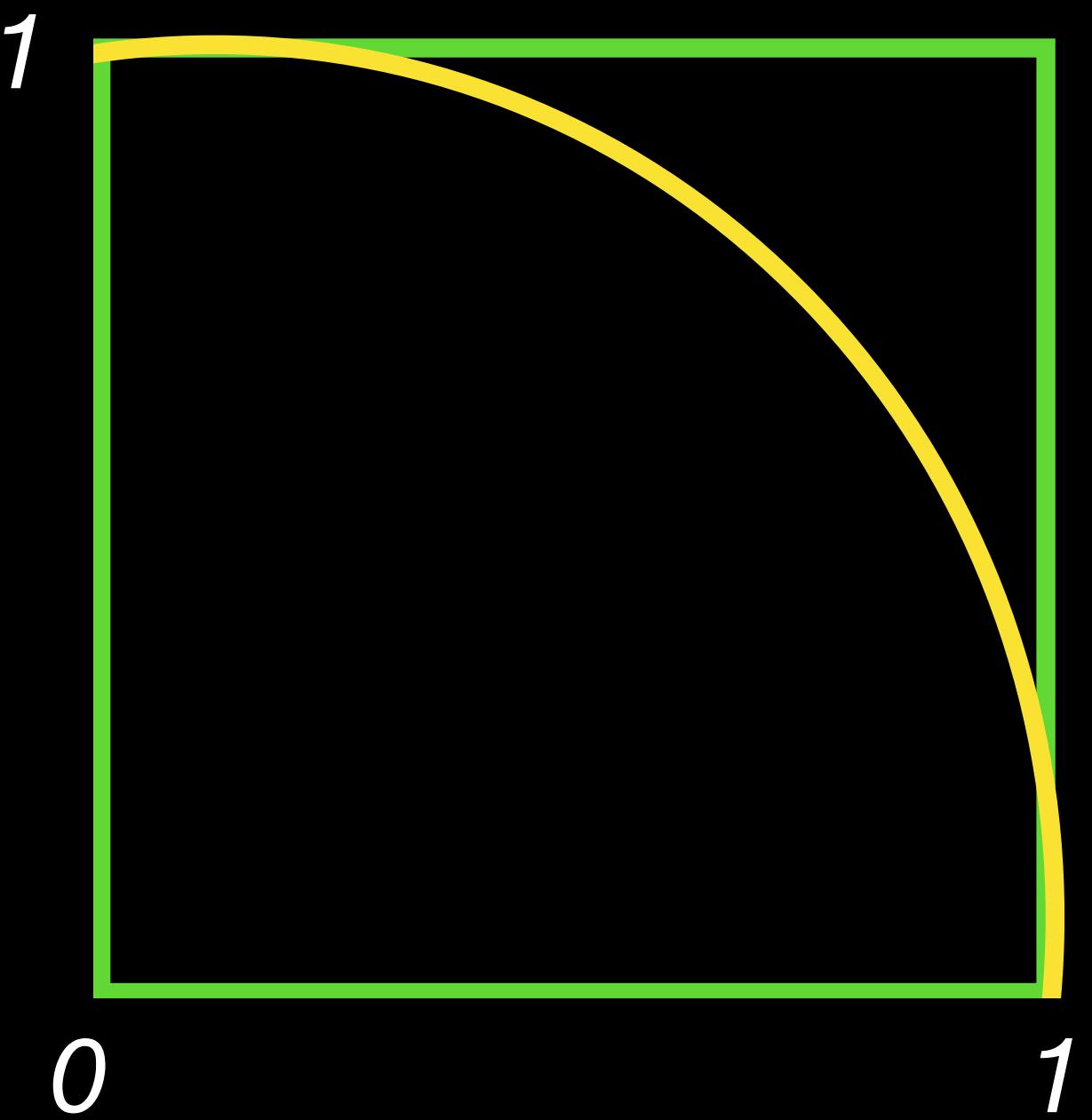


- **Challenge:** Modify your program
  - Print  $x^2 + y^2$  instead of just x and y

```
import math  
import random  
  
x = random.random()  
y = random.random()  
  
print(x)  
print(y)
```

# Pi Dartboard 3

- **Challenge:** Modify your program
  - Compute  $x^2 + y^2$  and store it in a variable rSquared
  - Print rSquared instead of just x and y

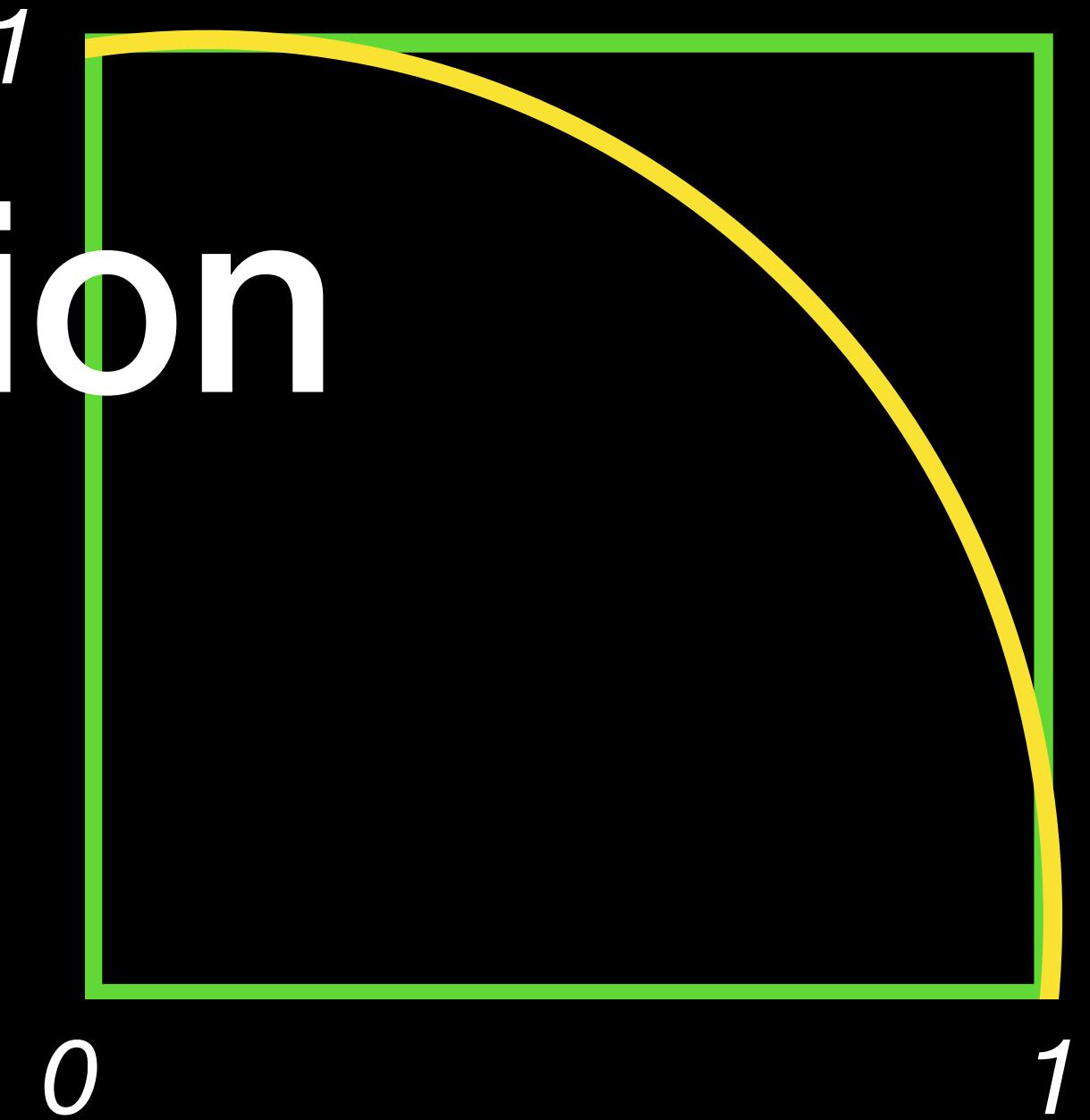


```
import math  
import random  
  
x = random.random()  
y = random.random()  
  
print(x)  
print(y)
```

# Pi Dartboard 3 Solution

- **Challenge:** Modify your program
  - Compute  $x^2 + y^2$  and store it in a variable rSquared
  - Print rSquared instead of just x and y

```
import math  
import random  
  
x = random.random()  
y = random.random()  
rSquared = x**2 + y**2  
print(rSquared)
```

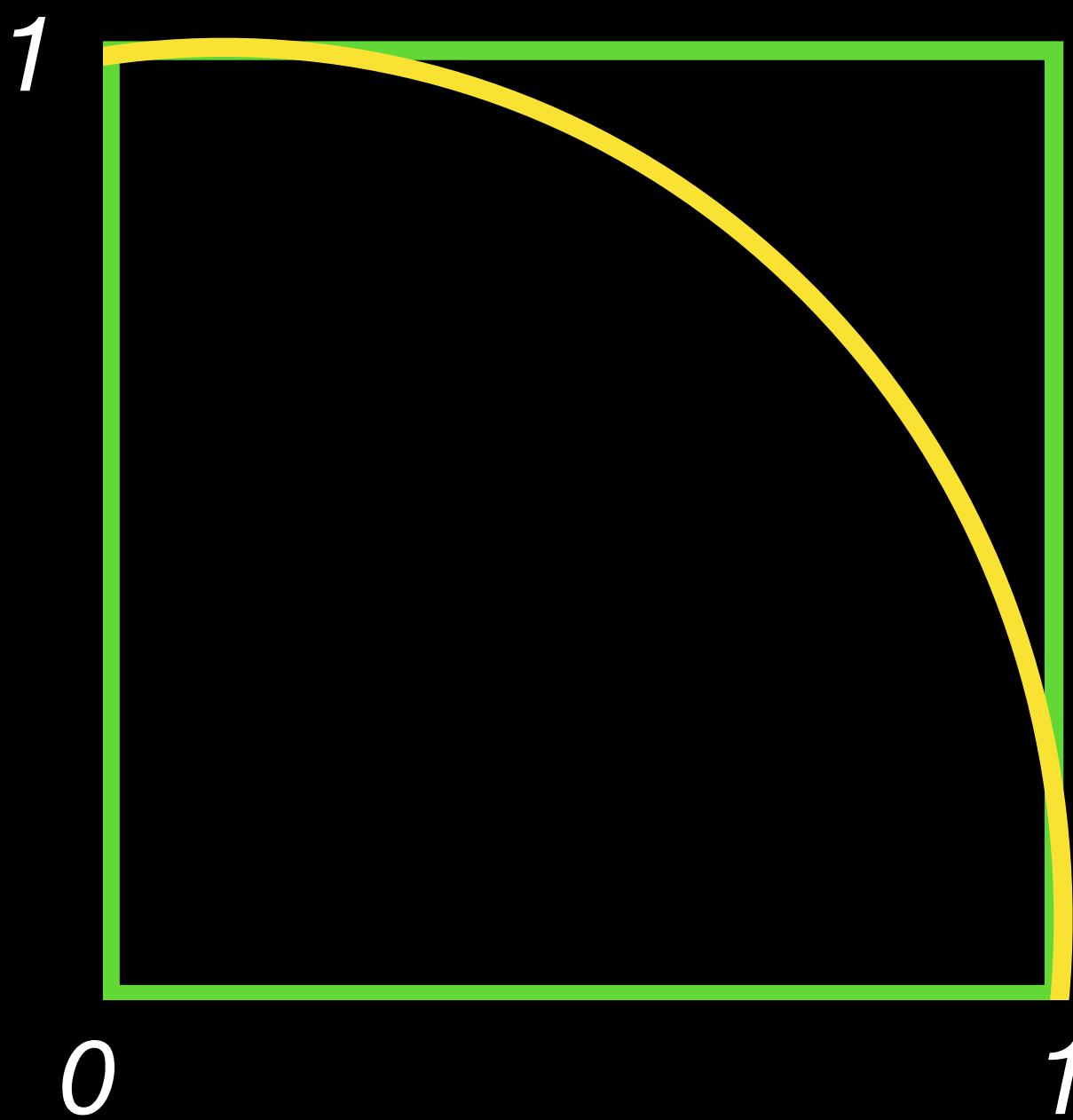


# Clicker question #2.5

- Which could be a number the program prints?

```
import math  
import random  
  
x = random.random()  
y = random.random()  
rSquared = x**2 + y**2  
print(rSquared)
```

- |   |       |
|---|-------|
| A | -1.51 |
| B | 2.43  |
| C | -0.32 |
| D | 1.01  |



# Clicker question #2.5

- If the dart is inside the **circle**, which could be the number printed by the program?

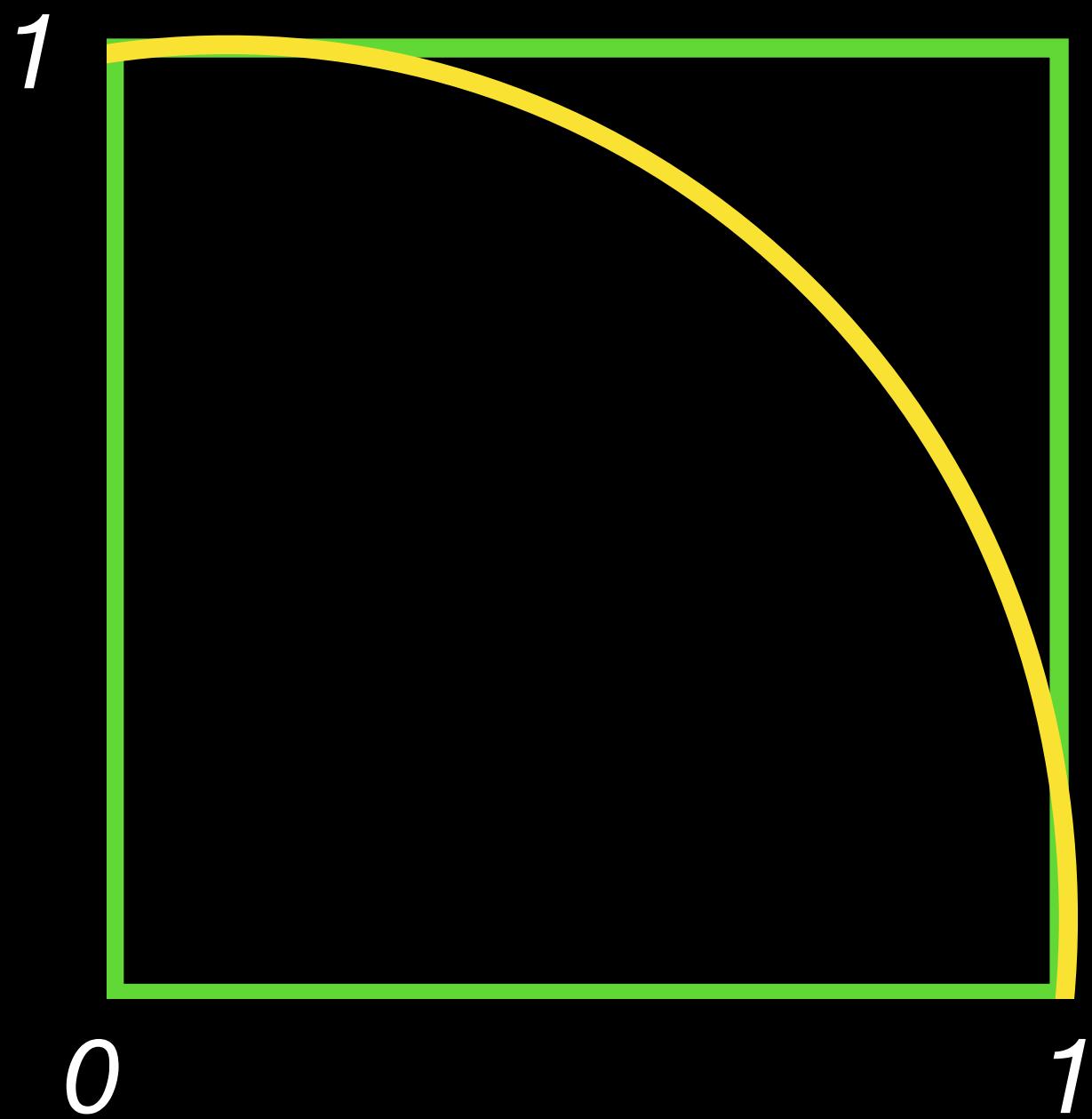
```
import math  
import random  
  
x = random.random()  
y = random.random()  
rSquared = x**2 + y**2  
print(rSquared)
```



# Pi Dartboard 4

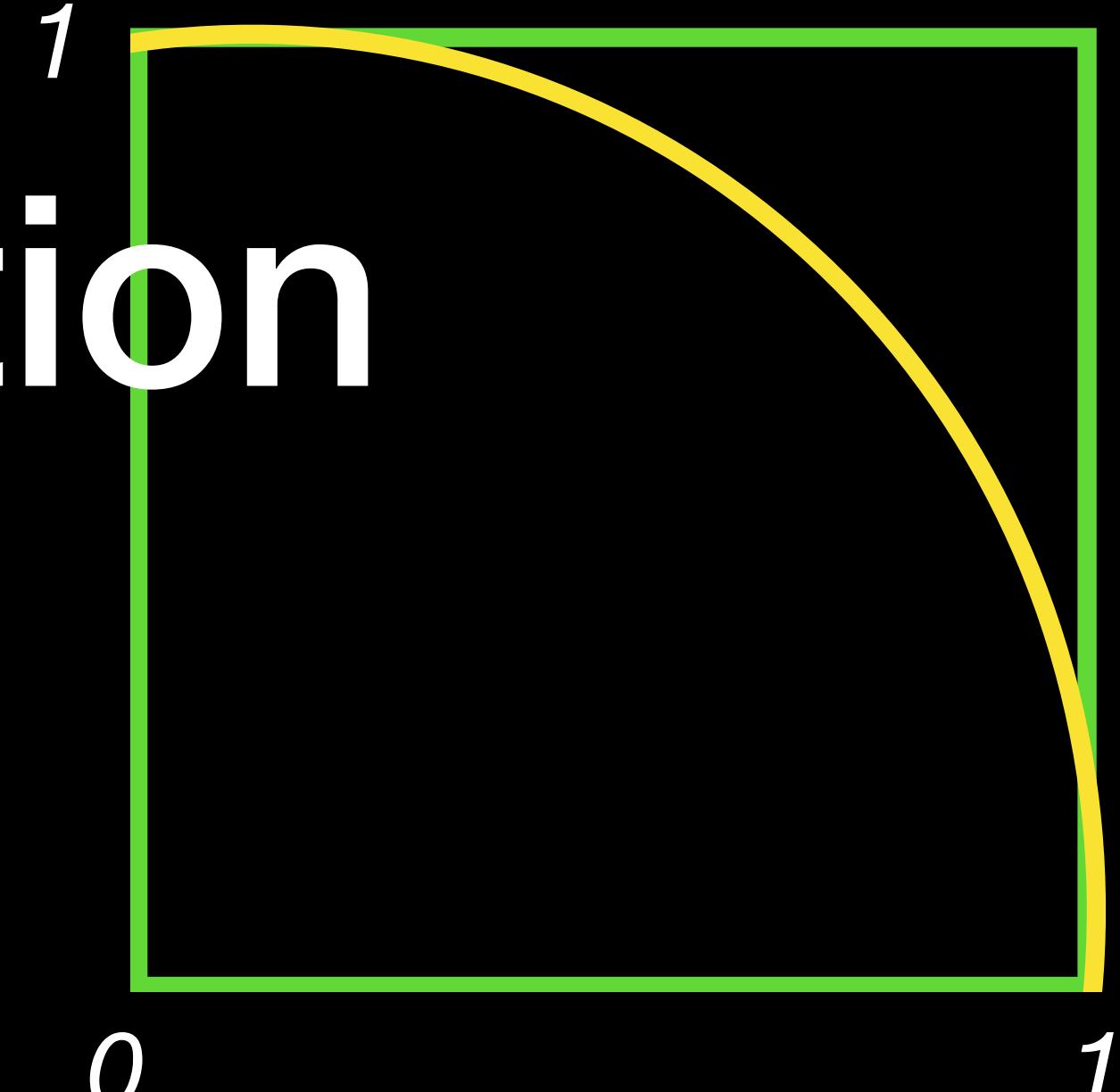
- **Challenge:** Modify your program
  - Just below import random, make a new variable called “hits”, set to 0
  - If rSquared < 1, add 1 to hits
  - Print hits instead of rSquared

```
import math  
import random  
  
x = random.random()  
y = random.random()  
  
rSquared = x**2 + y**2  
print(rSquared)
```



# Pi Dartboard 4 Solution

- **Challenge:** Modify your program
  - Just below import random, make a new variable called “hits”, set to 0
  - If rSquared < 1, add 1 to hits
  - Print hits instead of rSquared

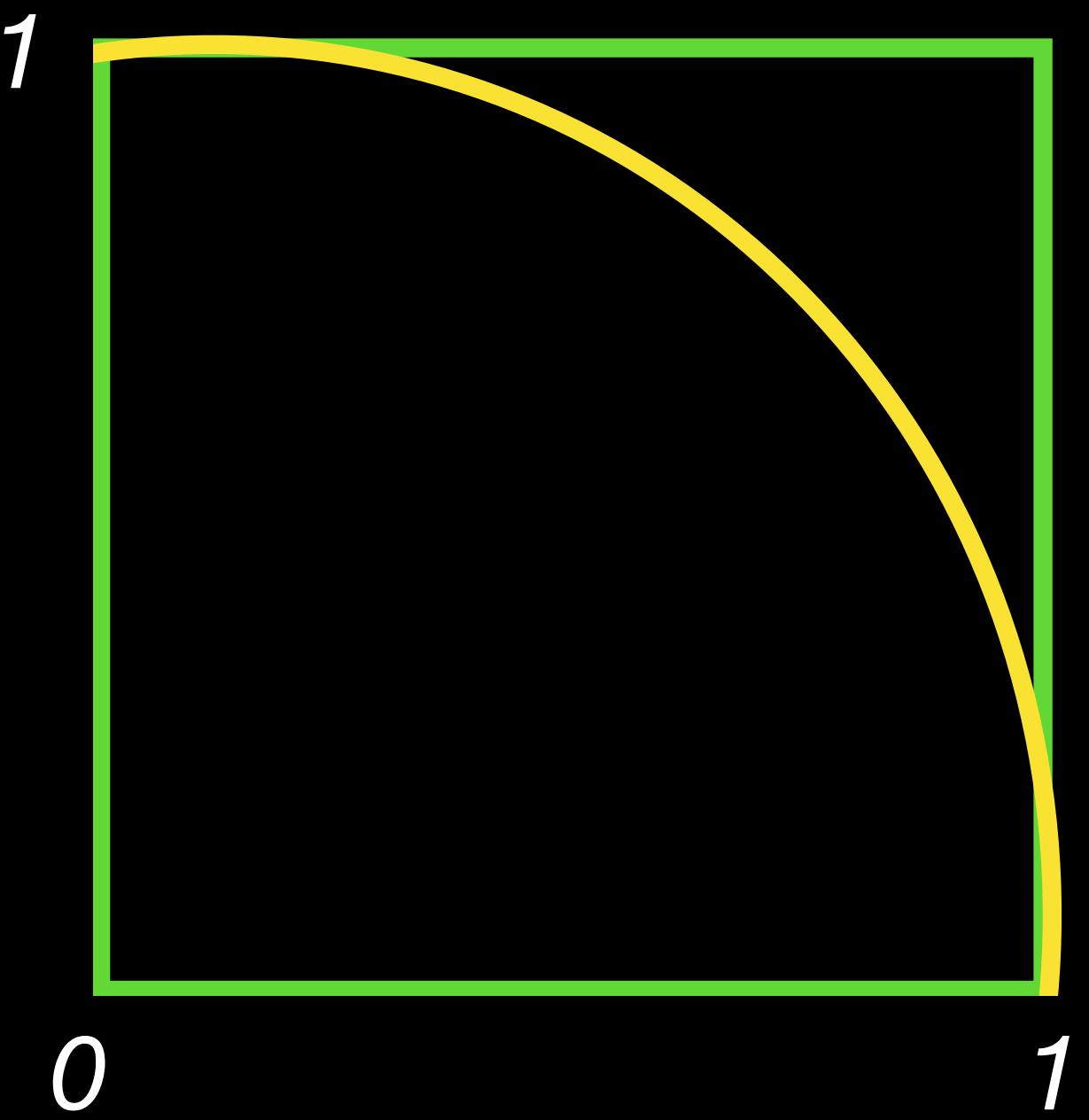


```
import math
import random
hits = 0
x = random.random()
y = random.random()
rSquared = x**2 + y**2
if rSquared < 1:
    hits = hits + 1
print(hits)
```

# Pi Dartboard 5

- **Challenge:** Modify your program
  - Add a new variable, just below hits, called throws. Set it equal to 10.
  - Put the code that throws the dart and sees if it hit inside a while loop, so that you throw 10 darts instead of 1 dart
  - Don't forget to increment your while loop counter variable (i or j or whatever)

```
import math  
import random  
  
hits = 0  
  
x = random.random()  
y = random.random()  
  
rSquared = x**2 + y**2  
if rSquared < 1:  
    hits = hits + 1  
print(hits)
```



# Pi Dartboard 5 Solution

- **Challenge:** Modify your program
- Add a new variable, just below hits, called throws. Set it equal to 10.
- Put the code that throws the dart and sees if it hit inside a while loop, so that you throw 10 darts instead of 1 dart

```
import math
import random

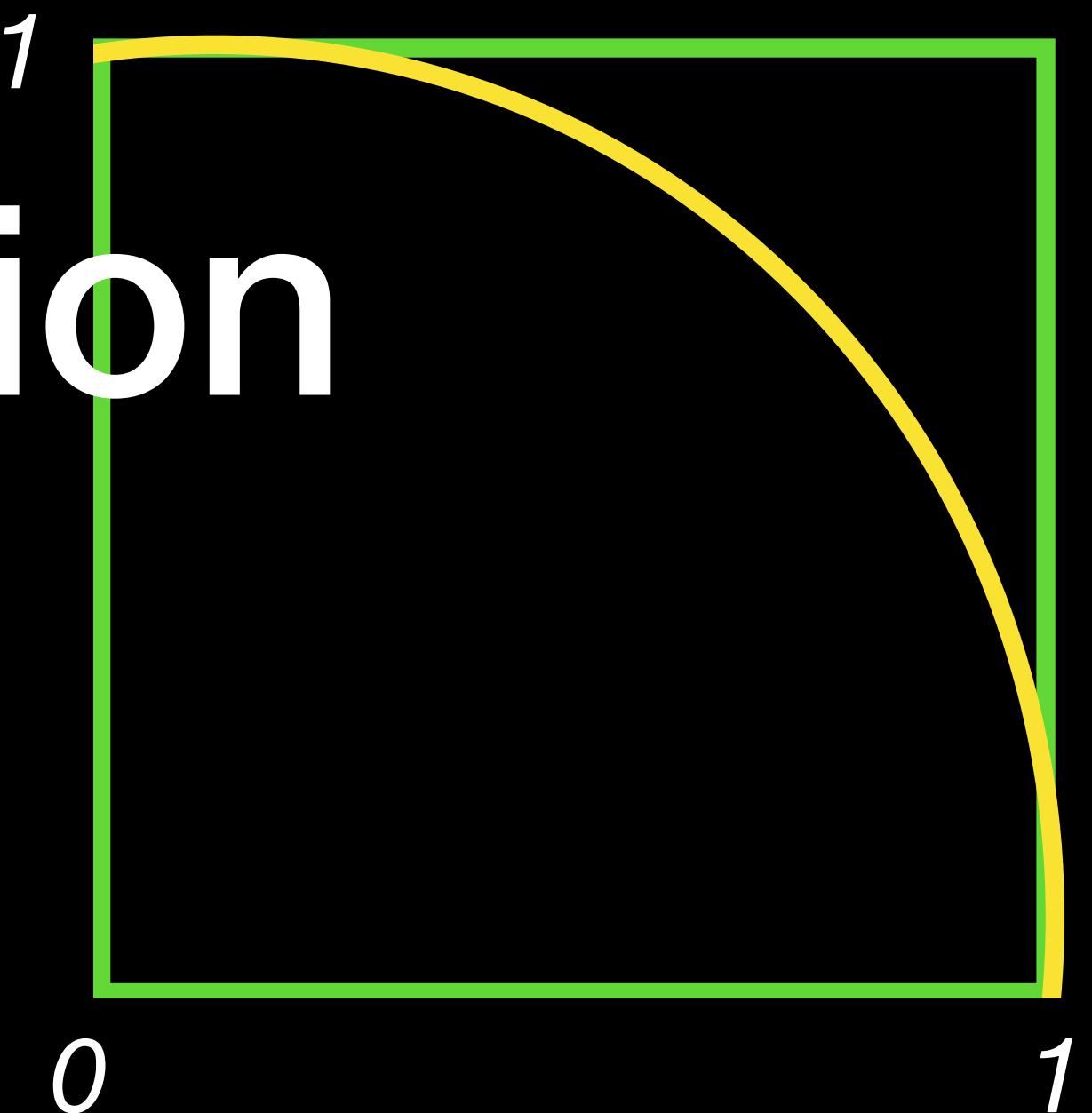
hits = 0
throws = 10

i = 0
while i < throws:
    x = random.random()
    y = random.random()

    rSquared = x**2 + y**2

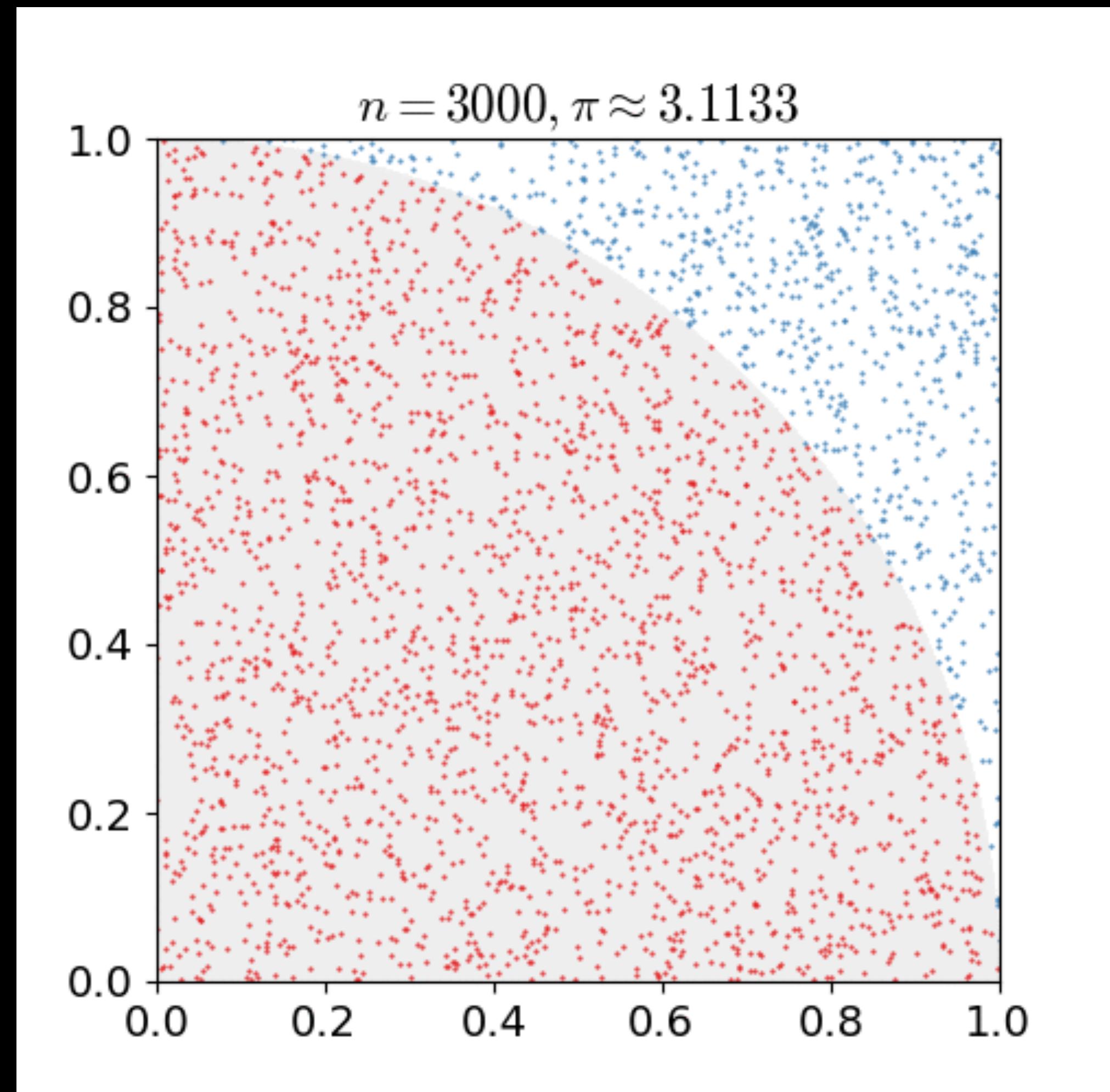
    if rSquared < 1:
        hits = hits + 1
    i = i + 1

print(hits)
```



# A silly way to compute $\pi$

- Throw darts in square
  - $(\text{circle area}) \div (\text{square area}) \approx \text{hits} \div \text{throws} = \pi/4$
  - So  $\pi \approx 4 * (\text{hits} \div \text{throws})$



Courtesy wikipedia

# Pi Dartboard 6

- Finish the dartboard
- Compute pi as  $4.0 * \text{float(hits)} / \text{float(throws)}$
- Print your pi estimate

```
import math
import random

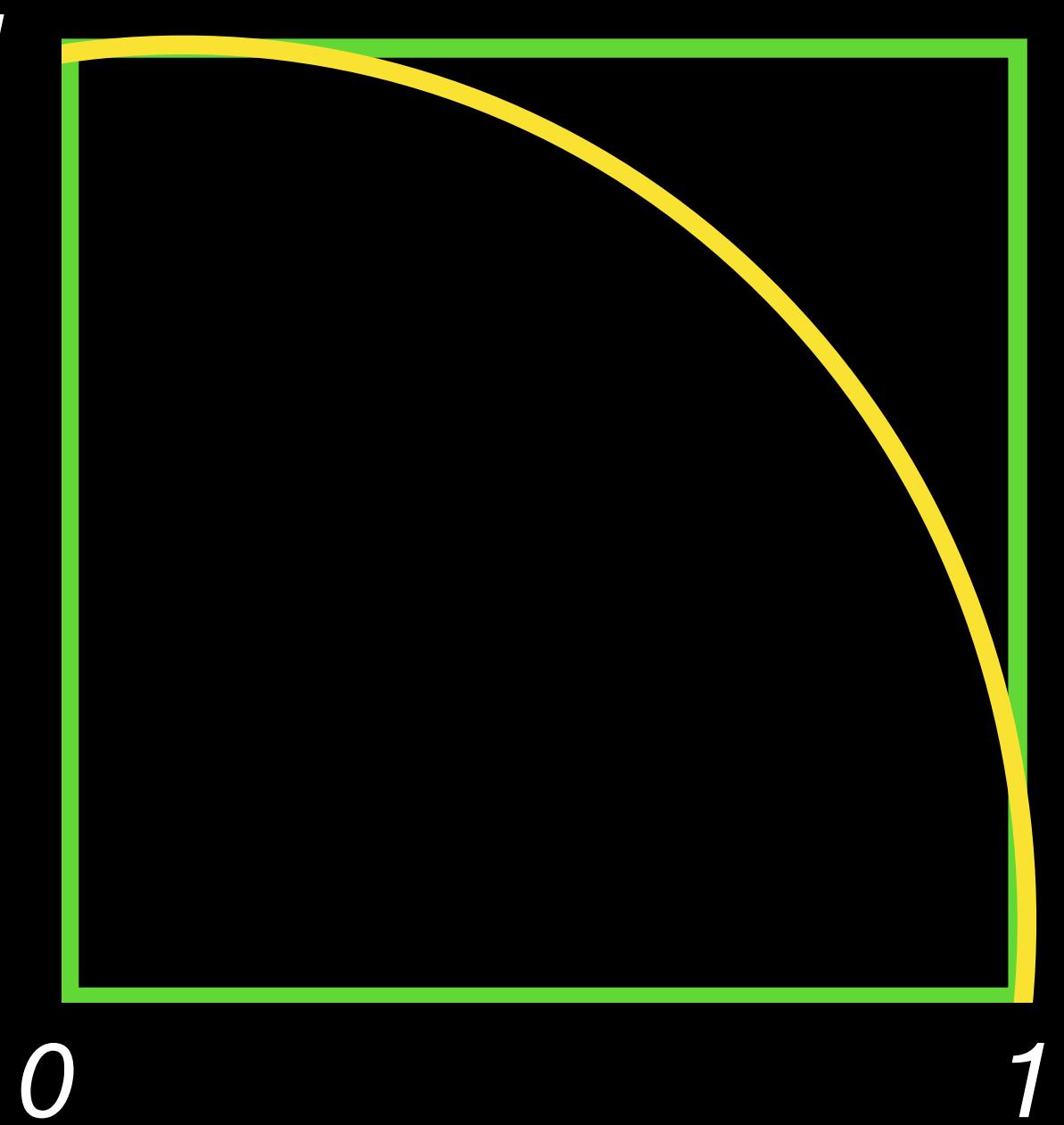
hits = 0
throws = 10

i = 0
while i < throws:
    x = random.random()
    y = random.random()

    rSquared = x**2 + y**2

    if rSquared < 1:
        hits = hits + 1
    i = i + 1

print(hits)
```



# Pi Dartboard 6 Solution

- Finish the dartboard
- Compute pi as  $4.0 * \text{float(hits)} / \text{float(throws)}$
- Print your pi estimate

```
import math
import random

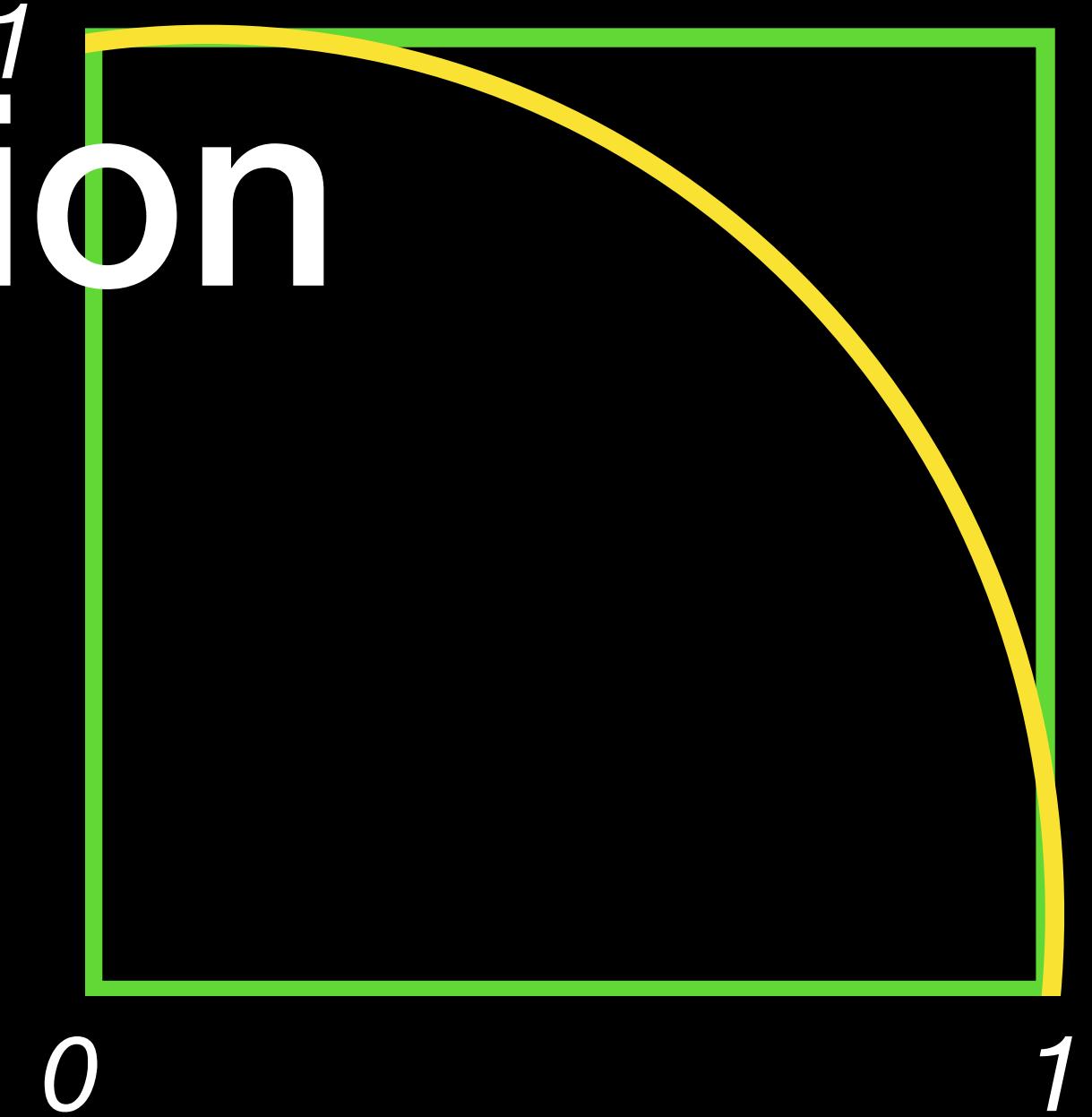
hits = 0
throws = 10

i = 0
while i < throws:
    x = random.random()
    y = random.random()

    rSquared = x**2 + y**2

    if rSquared < 1:
        hits = hits + 1
    i = i + 1

pi = 4.0 * float(hits) / float(throws)
print(pi)
```



# Pi Dartboard 7

- The tutor won't let us run lots of darts
- So paste this into a cell in Jupyter on [colab.google.com](https://colab.google.com) and run it
- See what happens as you make throws  $10^{**n}$ ,  $n=1,2,3,4,5,6,7$

```
import math
import random

hits = 0
throws = 10

i = 0
while i < throws:
    x = random.random()
    y = random.random()

    rSquared = x**2 + y**2

    if rSquared < 1:
        hits = hits + 1
    i = i + 1

pi = 4.0 * float(hits) / float(throws)
print(pi)
```

