

# Gravitational Waves

Prof. Jocelyn Read

# Gravity



Earth and Its Moon  
as seen from NASA's Mars Reconnaissance Orbiter, Nov. 20, 2016

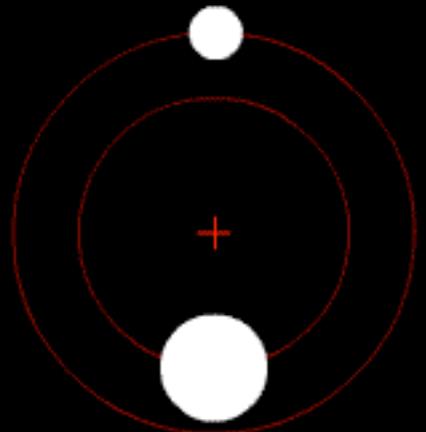
# Gravity in our Solar System

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Newton: Falling and orbiting are explained by the same gravitational force

All masses attract each other:

$$F = G \frac{m_1 m_2}{r^2}$$



NASA's New Horizons spacecraft observes  
Pluto and its largest moon, Charon, as it  
approaches. Jan 25–Jan 31, 2015

*NASA/Johns Hopkins University Applied Physics  
Laboratory/Southwest Research Institute*

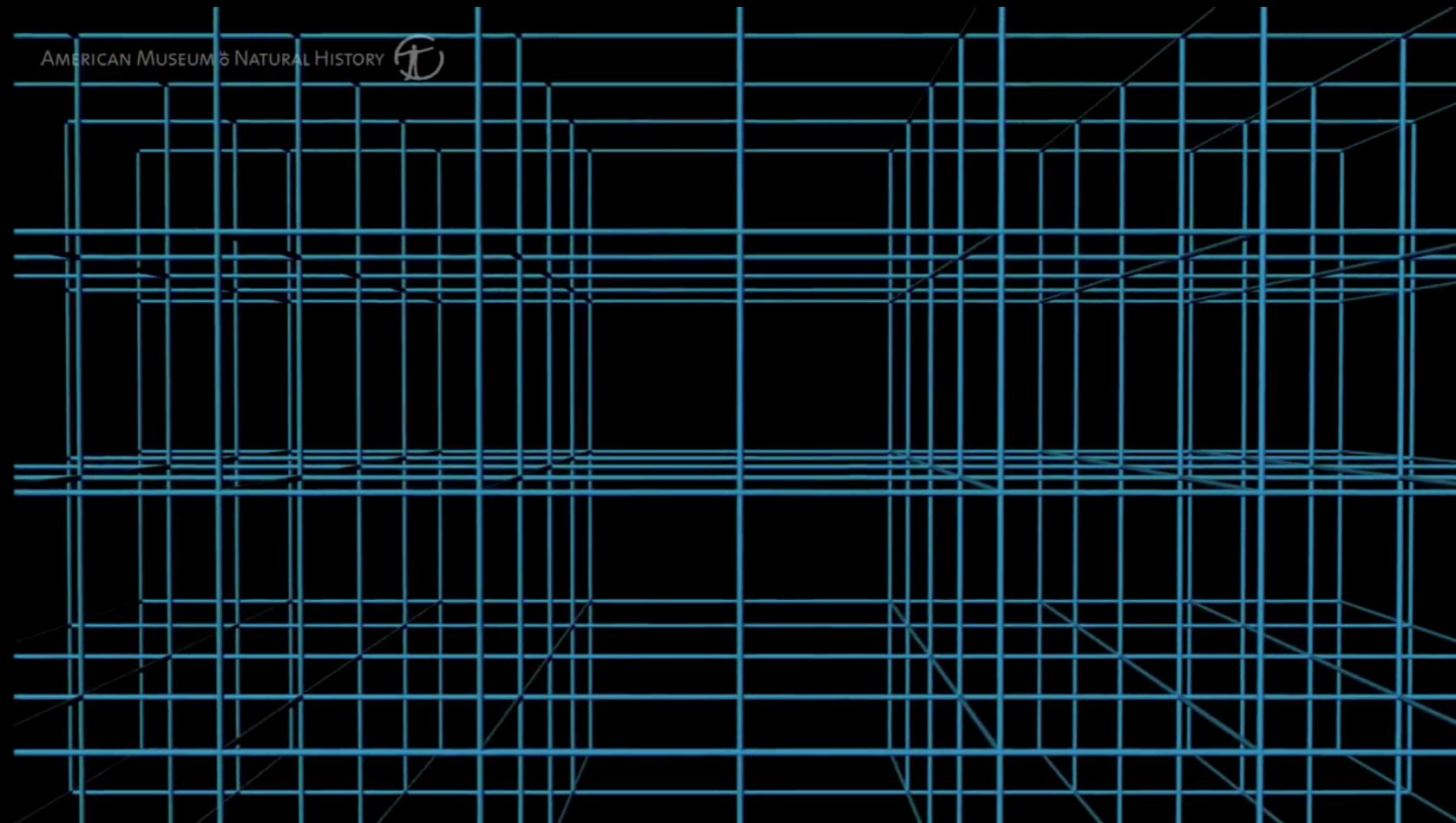
$$F = G M m / r^2$$

If you make an object smaller in size,  
but keep the mass the same, the  
gravitational effects get stronger

# General Relativity

“Matter tells space-time how to curve and  
space-time tells matter how to move.”

- John A. Wheeler

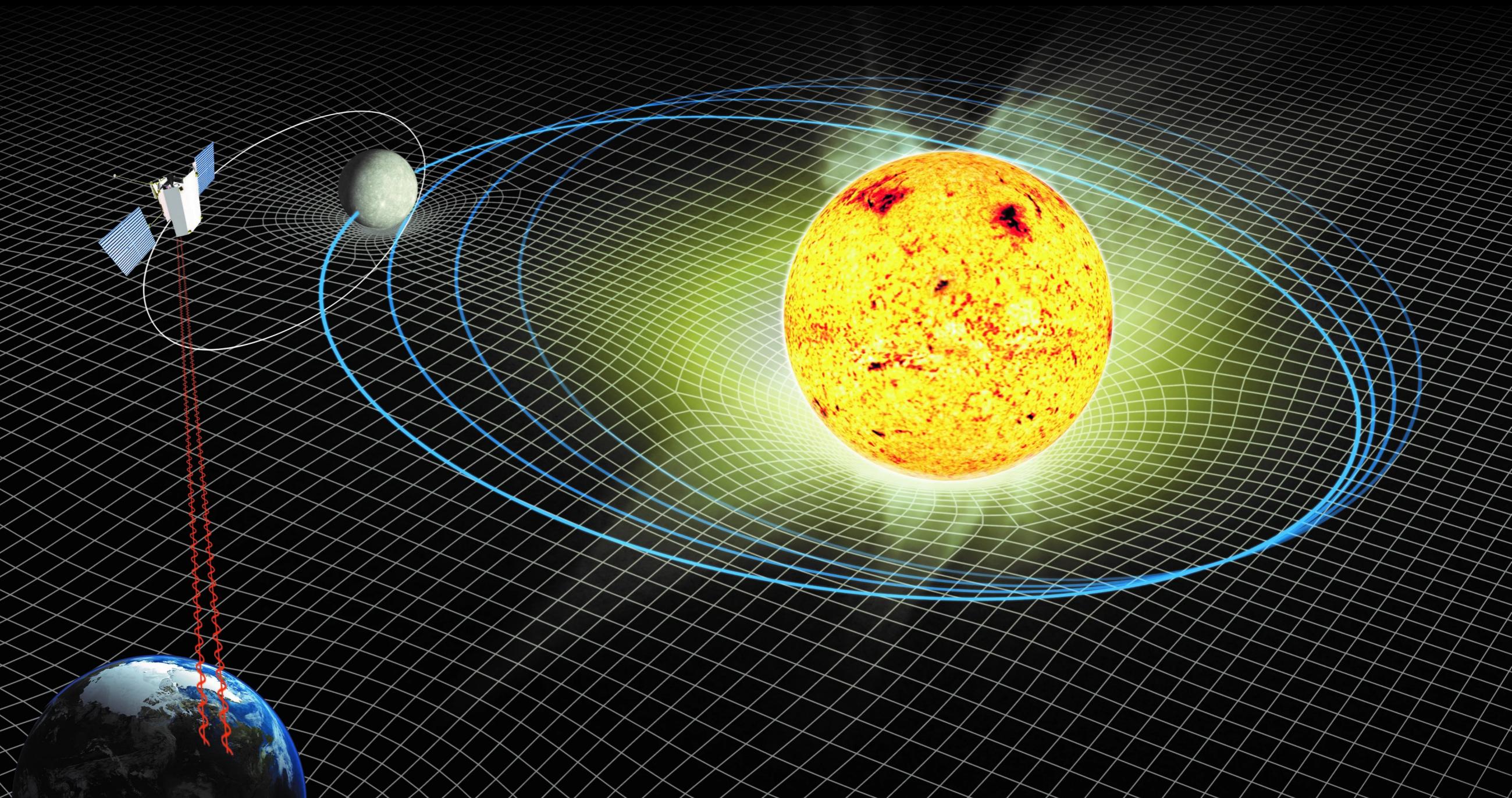


American Museum of Natural History  
“Gravity: Making Waves”

# Mercury orbits our Sun

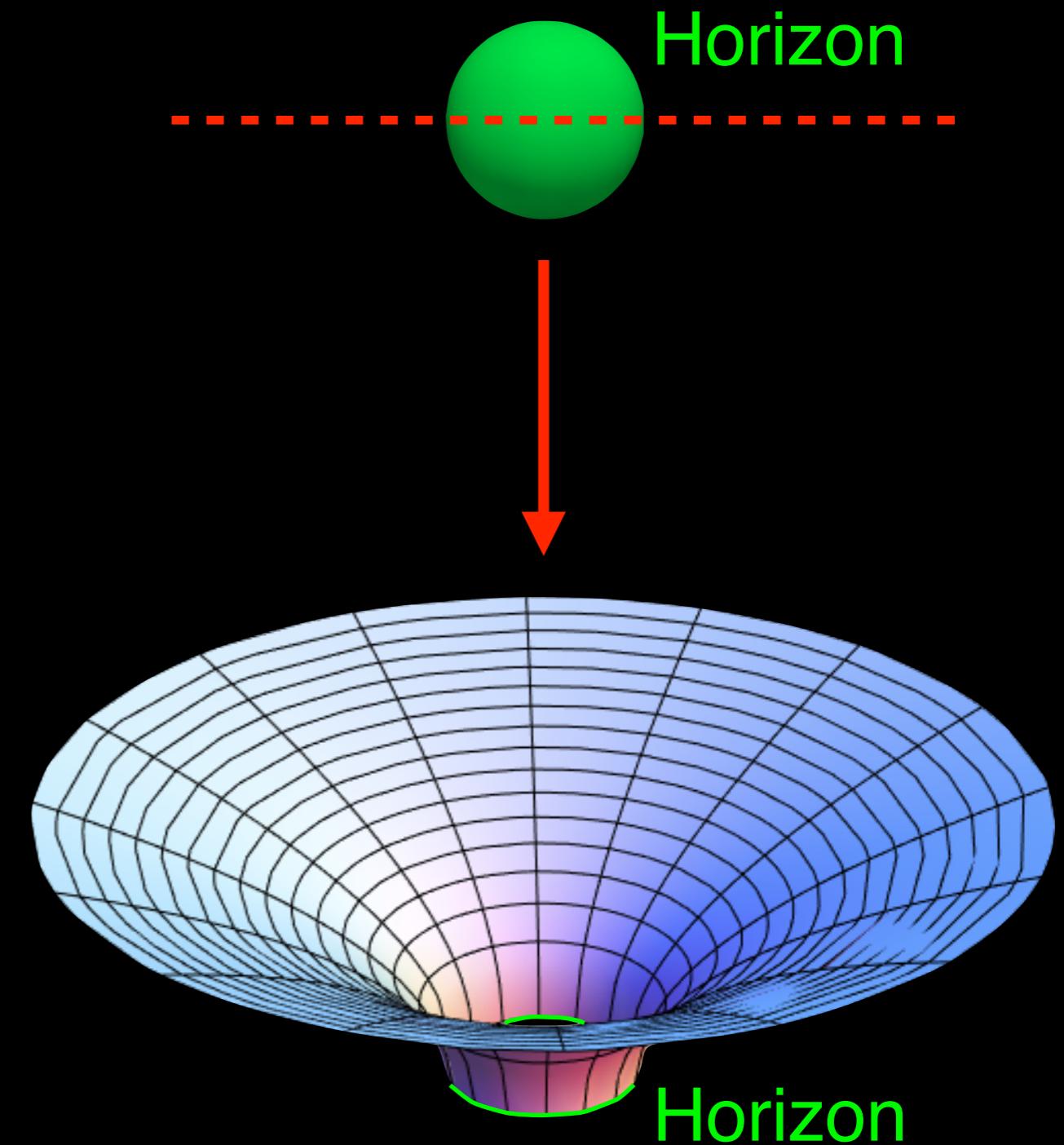
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Orbital precession: GR fits, Newton doesn't



# Black holes: extremes of space-time curvature

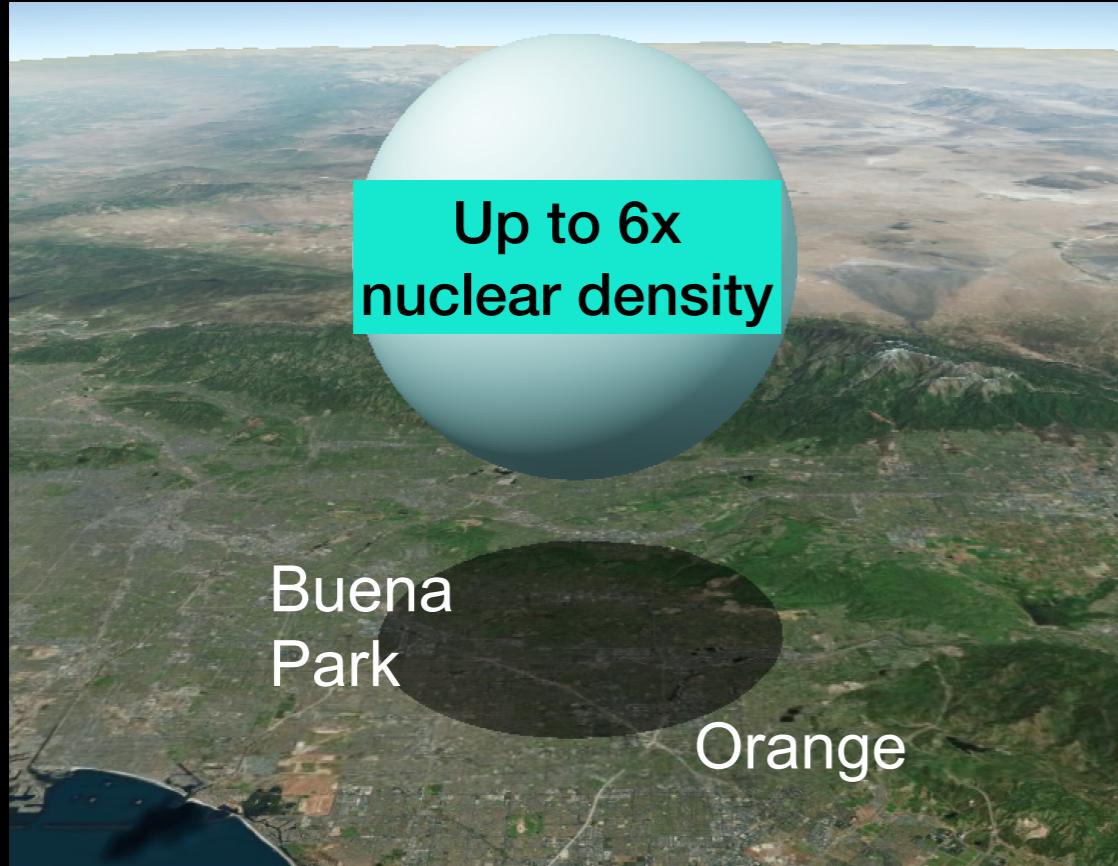
- *Stellar-mass* formed when the massive stars collapse
- *Supermassive* found in the centers of galaxies
- Gravity so strong...
  - Nothing can escape from within the **horizon** (surface)
  - *Singularity* inside horizon



# Compact objects: lots of mass in a small volume

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Neutron star: Mass = 1-2 ☀  
Radius  $\approx$  10 - 13 km



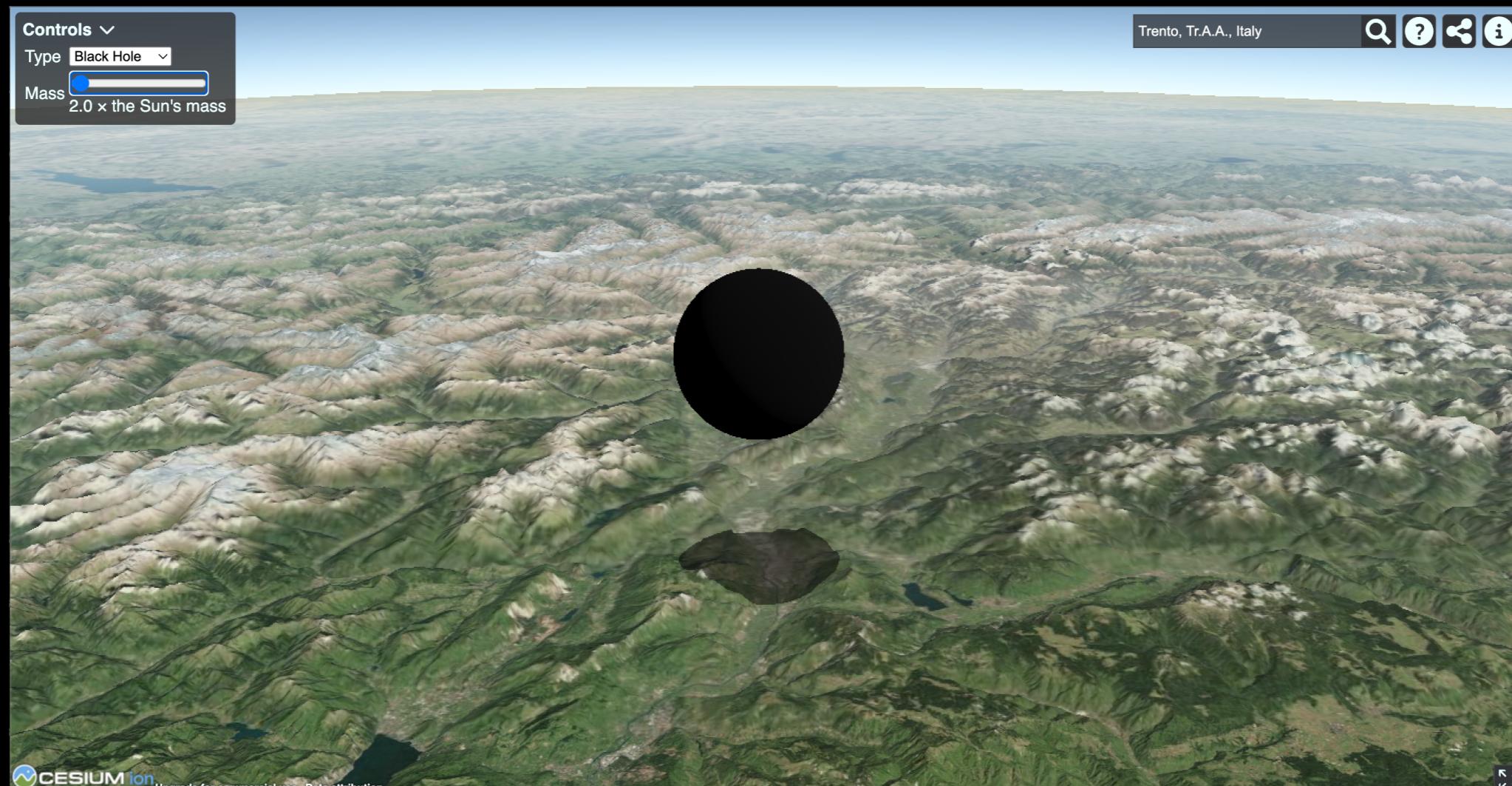
(small) Black hole: Mass = 2 ☀  
Radius = 6 km



# Black hole sizes

$2.0 M_{\odot}$  Black hole

$$(R_S = 2GM/c^2)$$



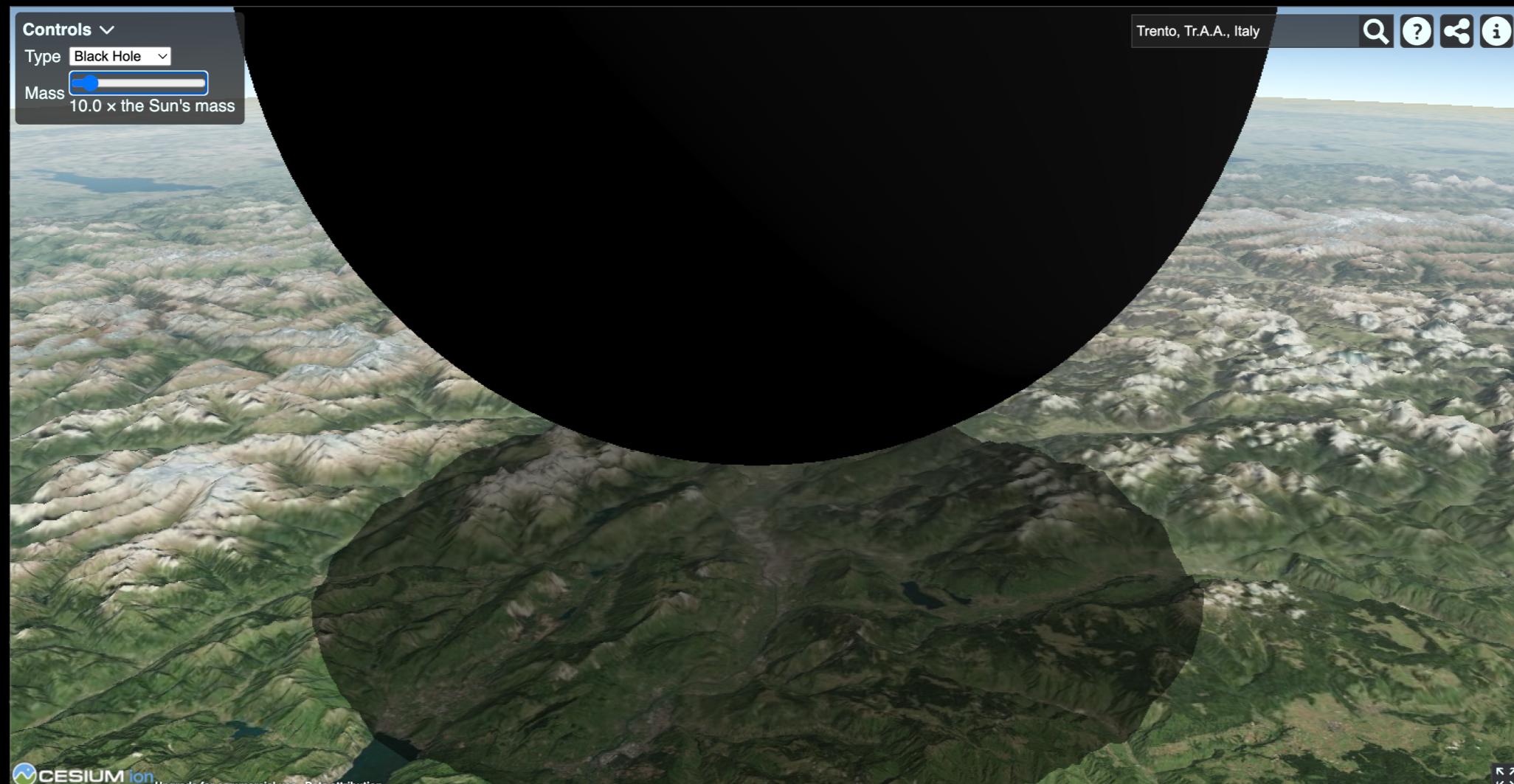
<https://ns-in-my-city.daniel-wysocki.info/>

# Black hole sizes

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$10 M_{\odot}$  Black hole

$$(R_S = 2GM/c^2)$$



# The Crab Nebula: supernova observed in 1054

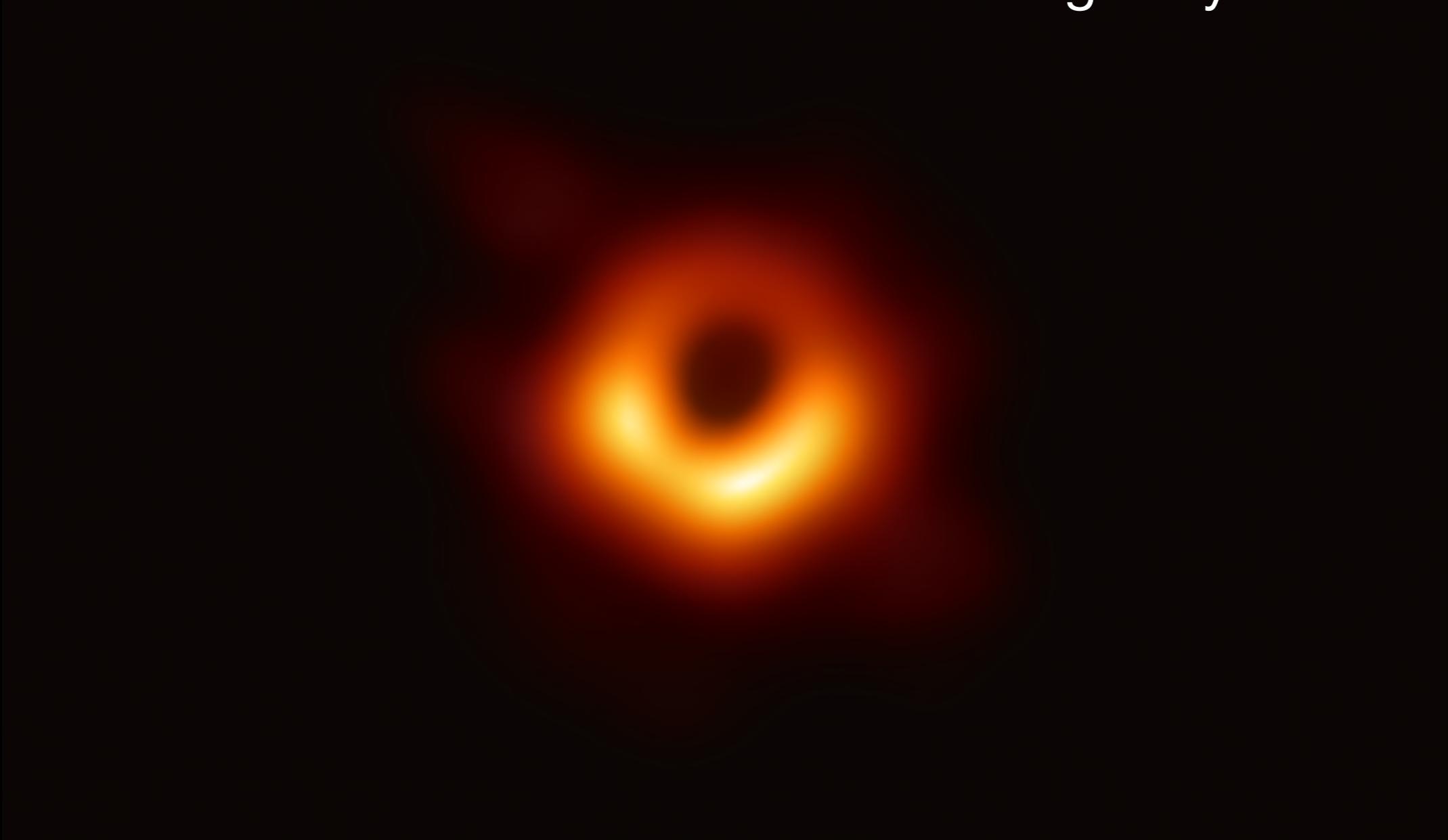


X-ray: NASA/CXC/SAO/F.Seward; Optical: NASA/ESA/ASU/J.Hester & A.Loll;  
Infrared: NASA/JPL-Caltech/Univ. Minn./R.Gehrz

6.5 billion solar mass black hole

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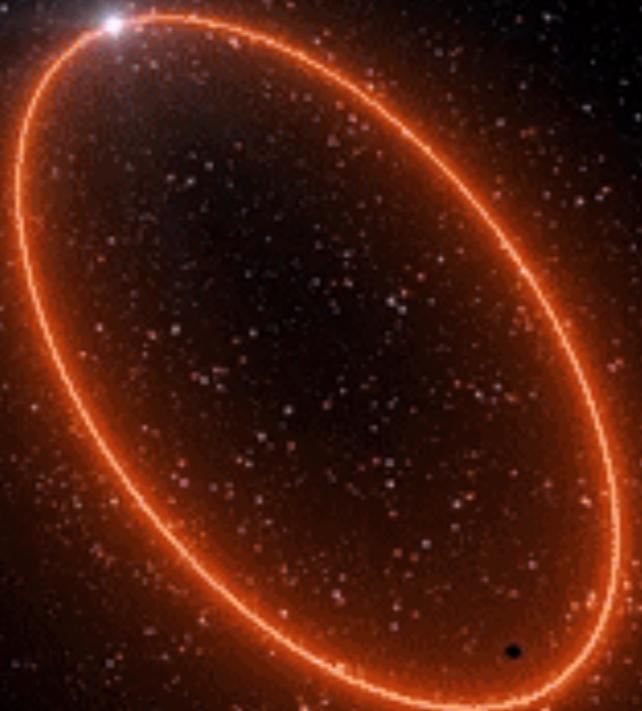
Supermassive black hole at the center of the galaxy M87



The star S2 orbits the Milky Way's central black hole Sagittarius A\*

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Orbital precession: GR fits, Newton doesn't



# Mass in Motion

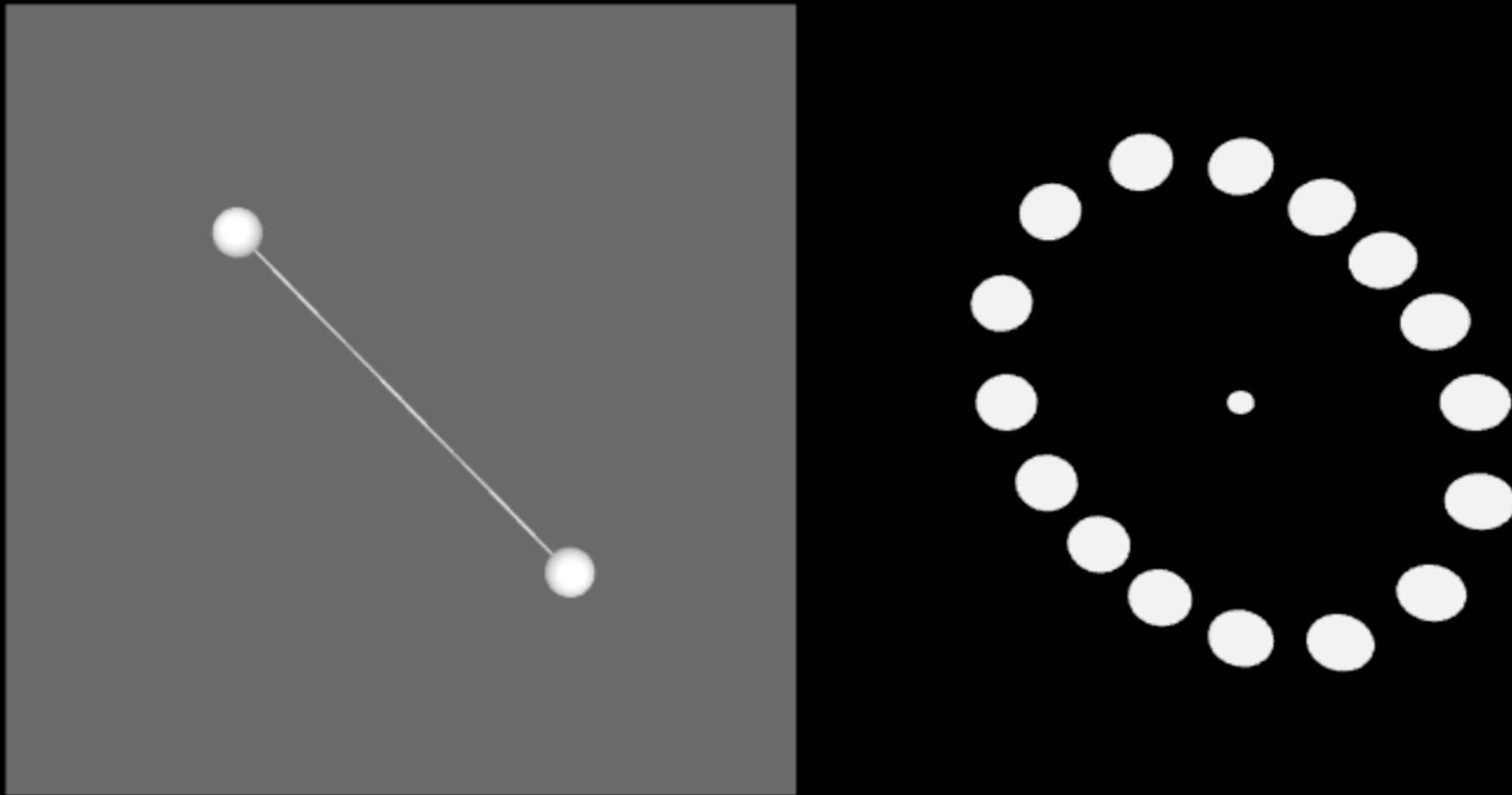
- Newtonian Gravity:  
“Action at a distance”
  - Instantly feel the new position of a moving object
- General Relativity:
  - Changes in curved spacetime ripple out at the speed of light



Moon passing Earth  
as seen from NASA's DSCOVR spacecraft (NASA/NOAA)  
at the L1 Point between the Earth and the Sun, 5 light seconds from Earth

Two objects orbit,  
gravitational pull *changes*

At your observing  
location, a ring of particles  
stretches and squeezes in  
response

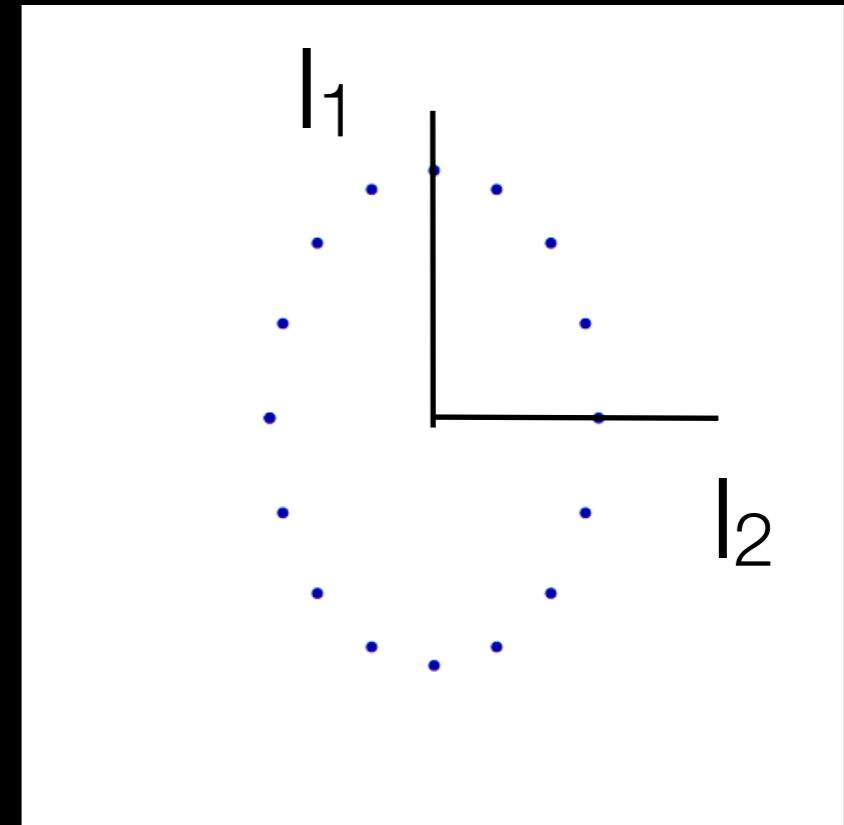
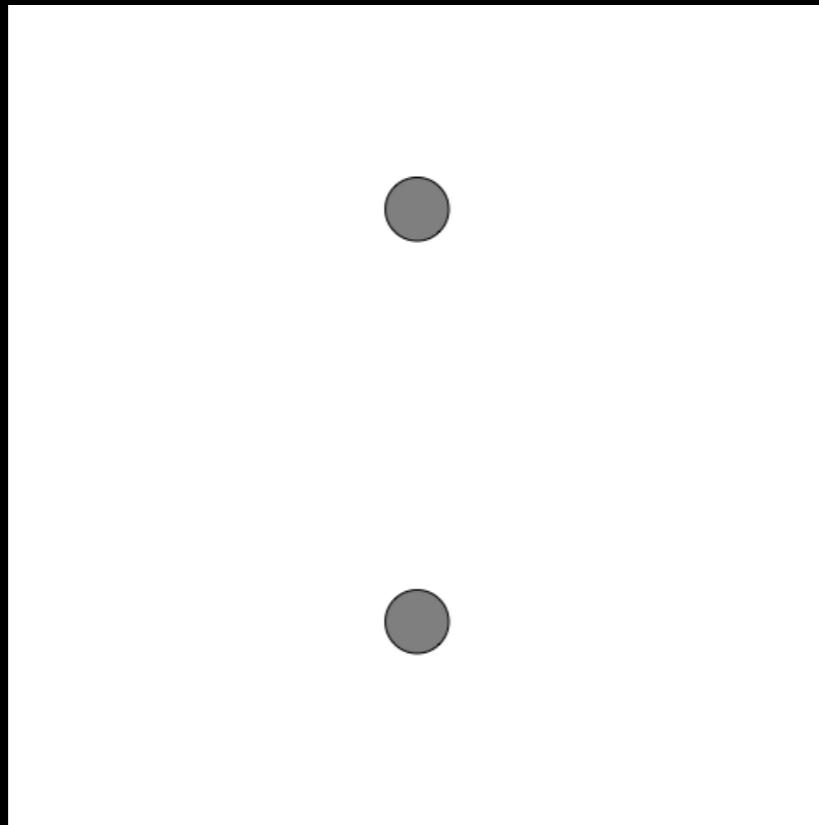


Which of the following would emit zero gravitational waves?

Hint: would the gravitational pull you feel change?

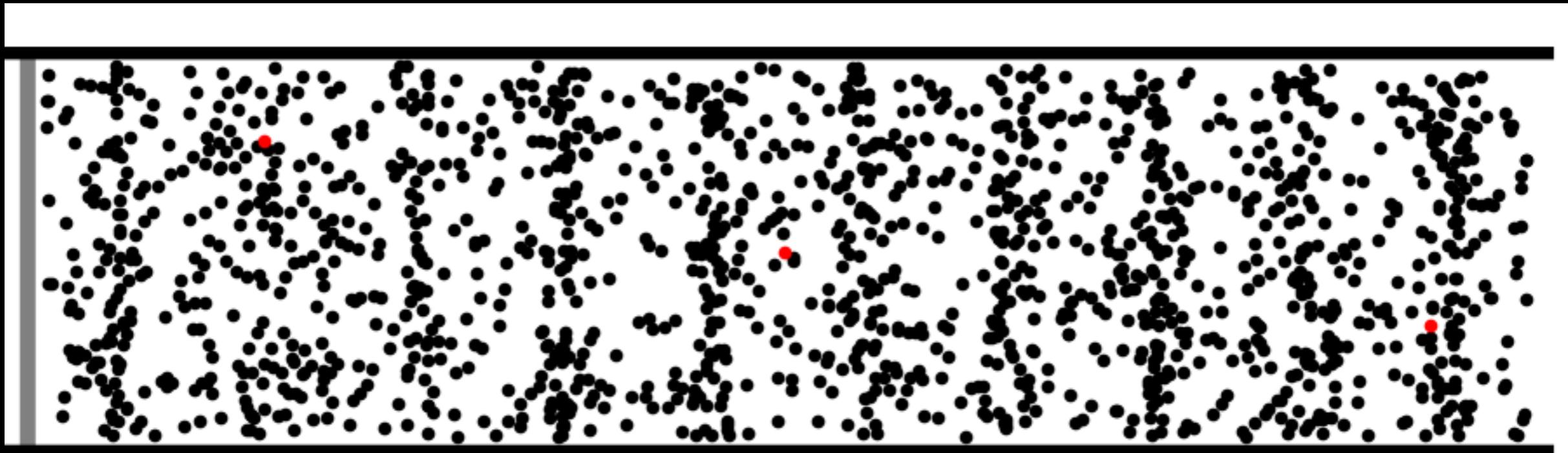
- A. A spinning spherical star
- B. The earth orbiting the sun
- C. A professor wildly waving her hands
- D. All of the above would emit gravitational waves

How many stretch/squeeze cycles are there during the time the stars take to make a full orbit?

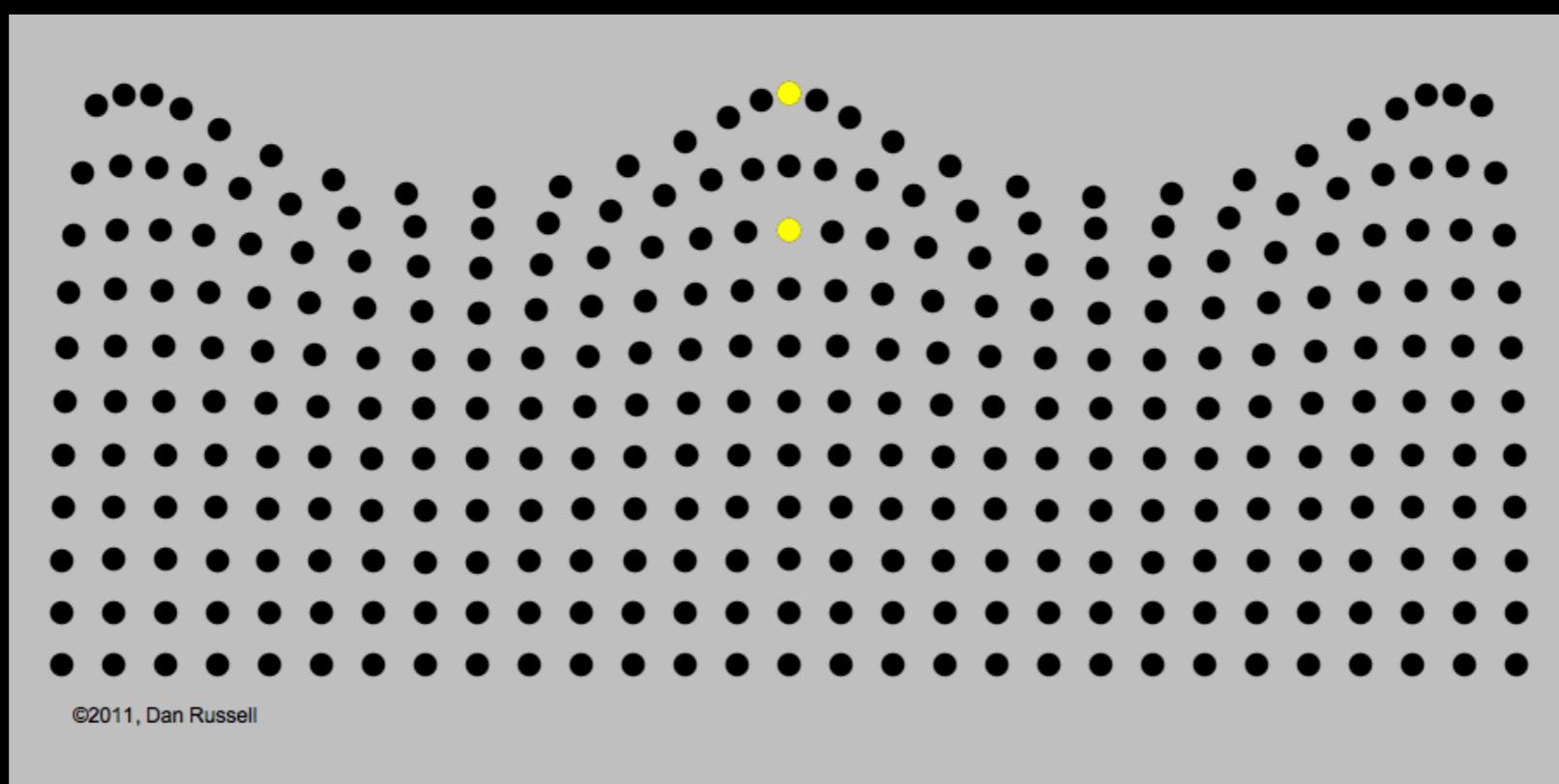


- A. One
- B. Two
- C. Half
- D. Four

# Waves

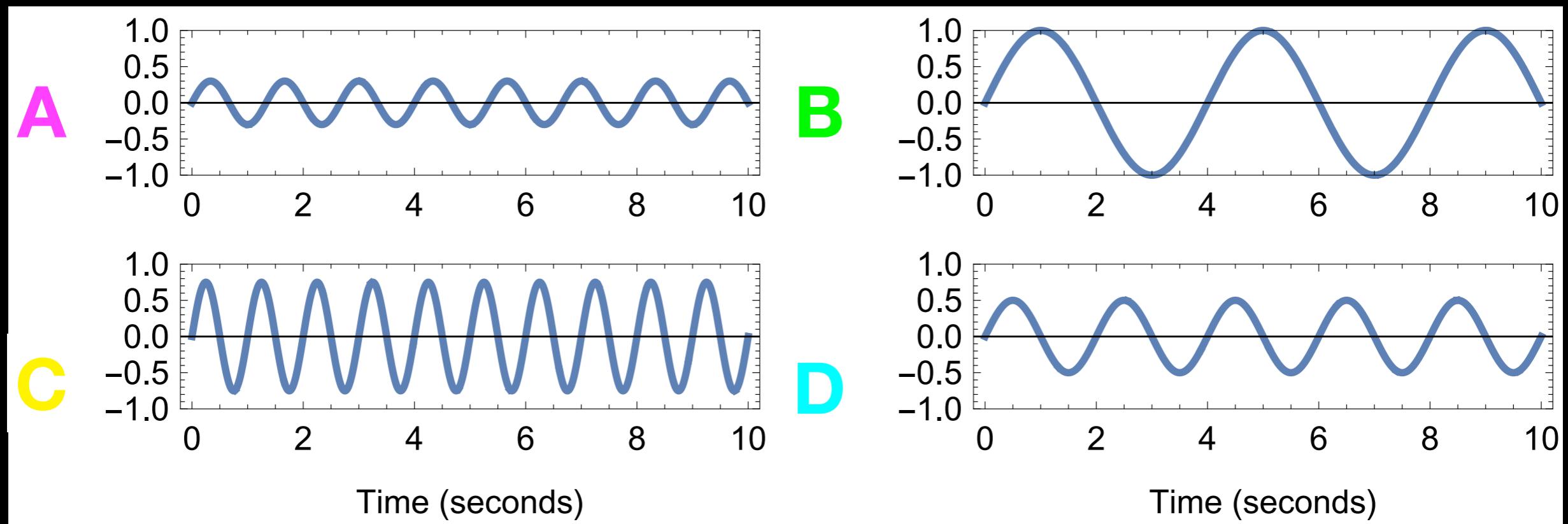


©2011. Dan Russell



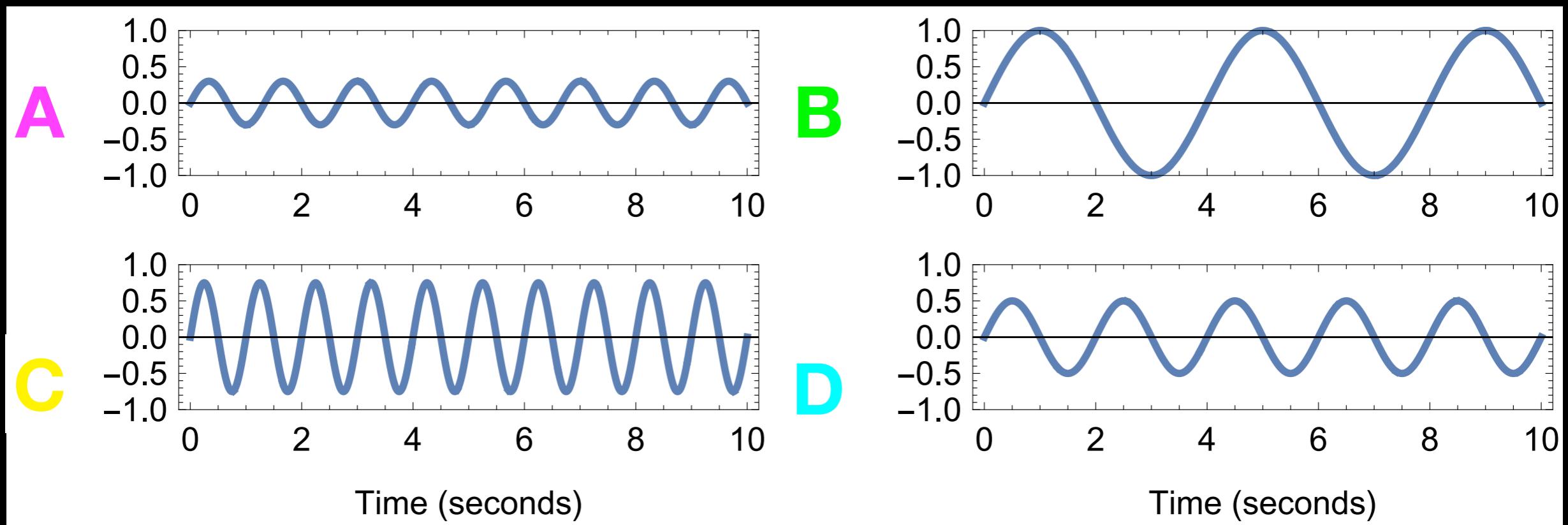
©2011. Dan Russell

- Consider the following four waves, plotted over time:



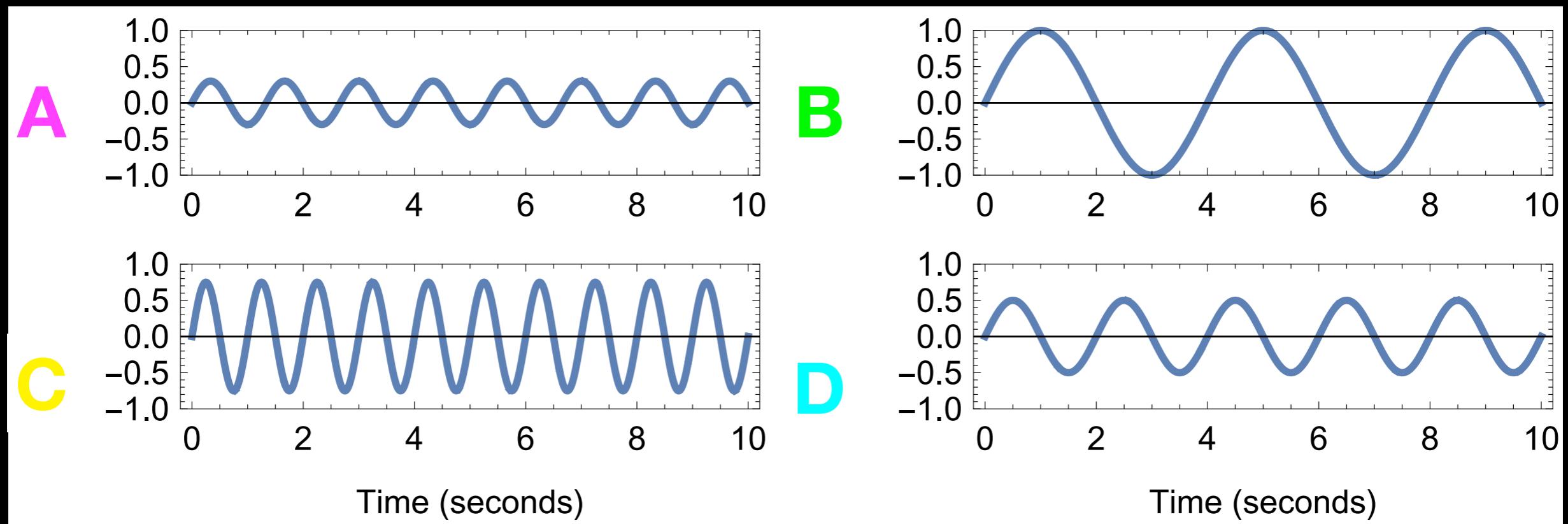
- Which has the largest amplitude?

- Consider the following four waves, plotted over time:



- Which has the shortest period (*time taken for one wave cycle*)?

- Consider the following four waves, plotted over time:

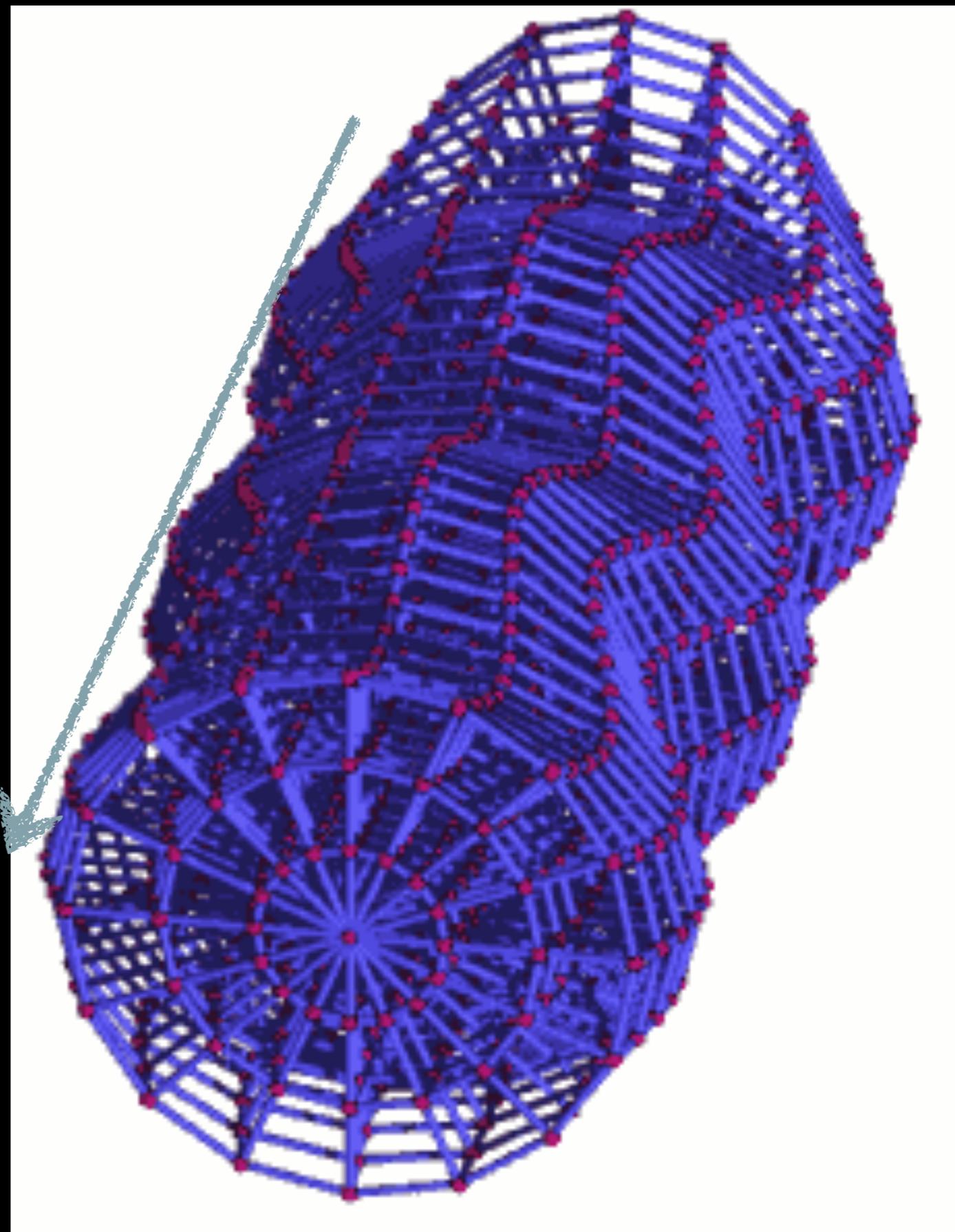


- Which has the highest frequency (*number of wave cycles observed in a given amount of time*)?

# Gravitational wave

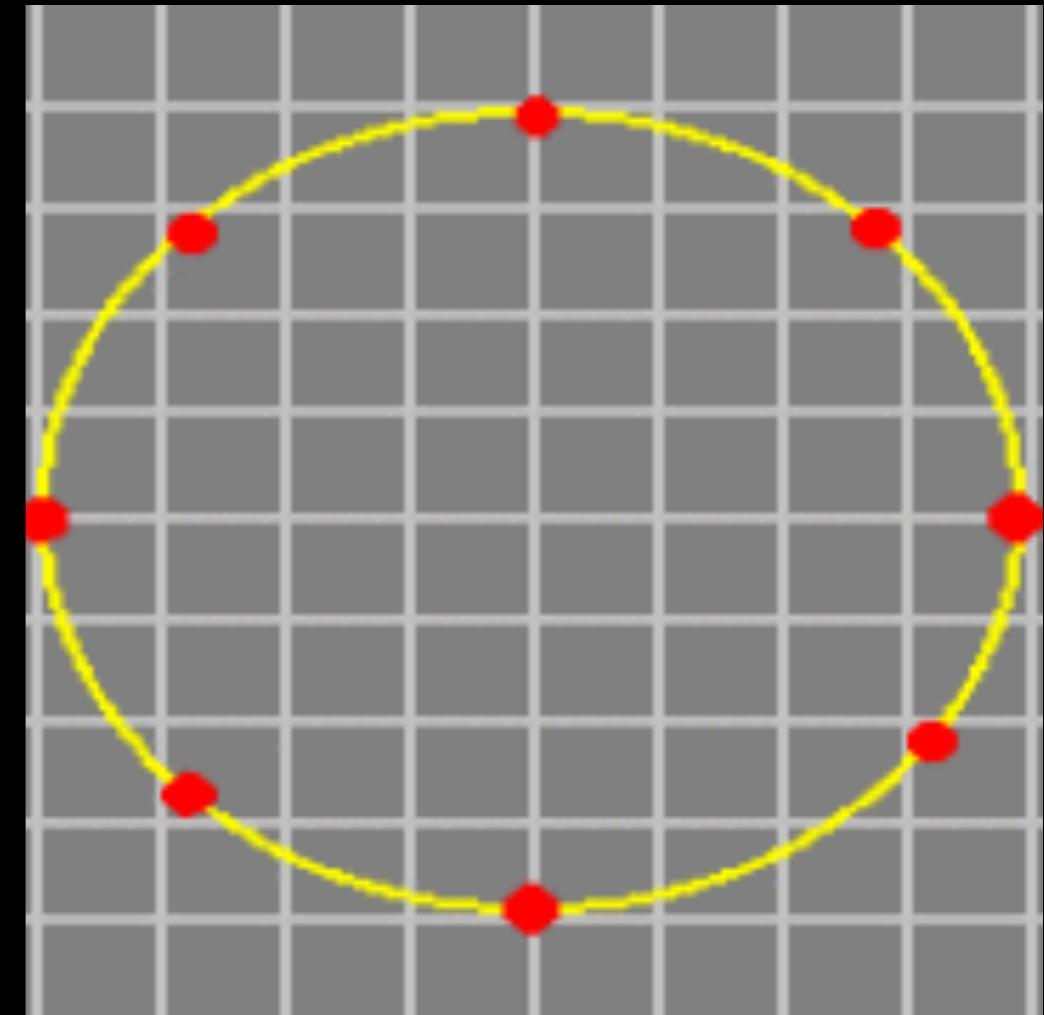
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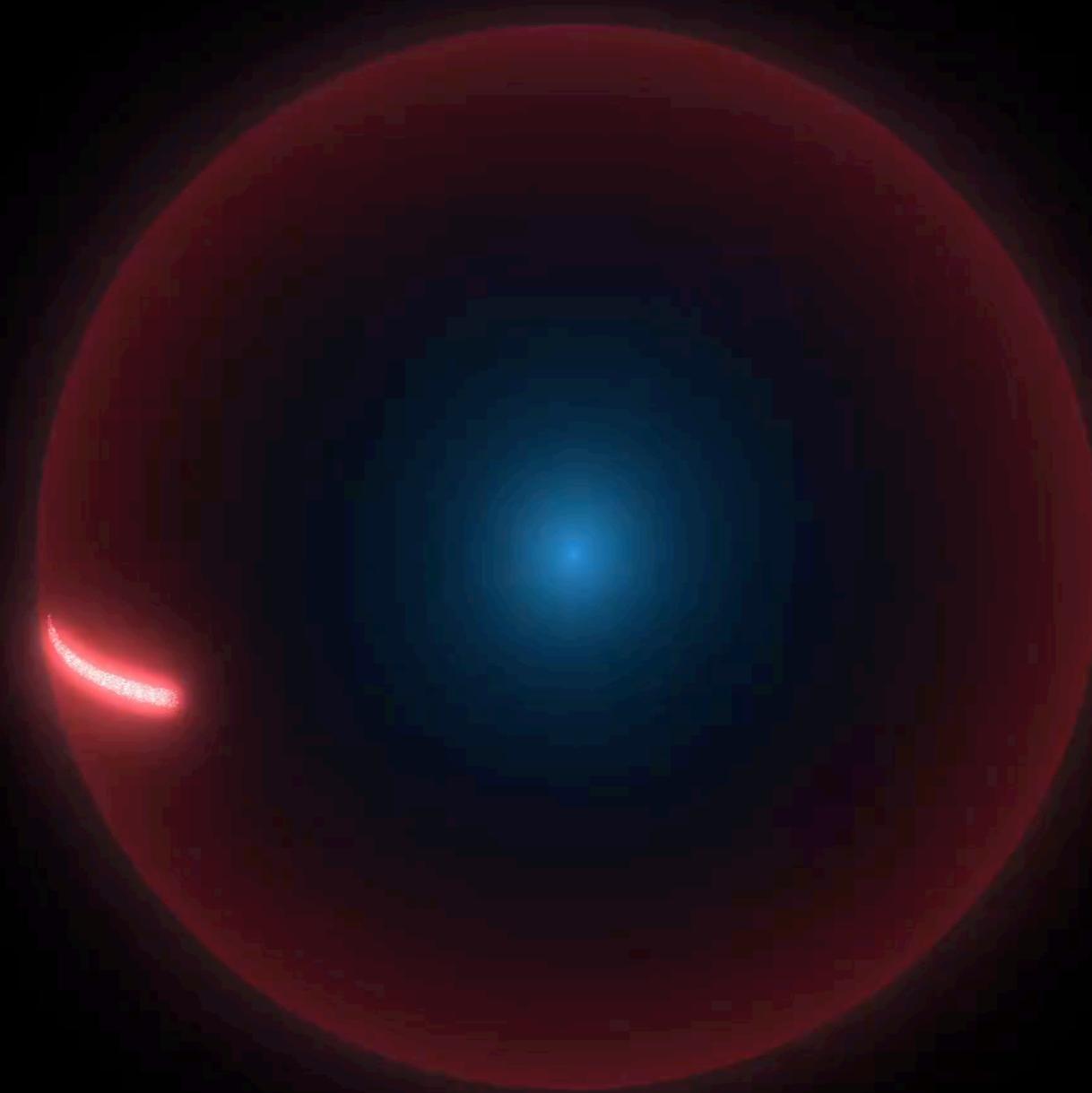
- Stretching and squeezing distances between objects
- Traveling at the speed of light



# Effects of gravitational waves

- Cause the distance between objects to change
- Fractional change shown  
10% 
- Fractional change from gravitational waves arriving at Earth  
0.00000000000000000001%





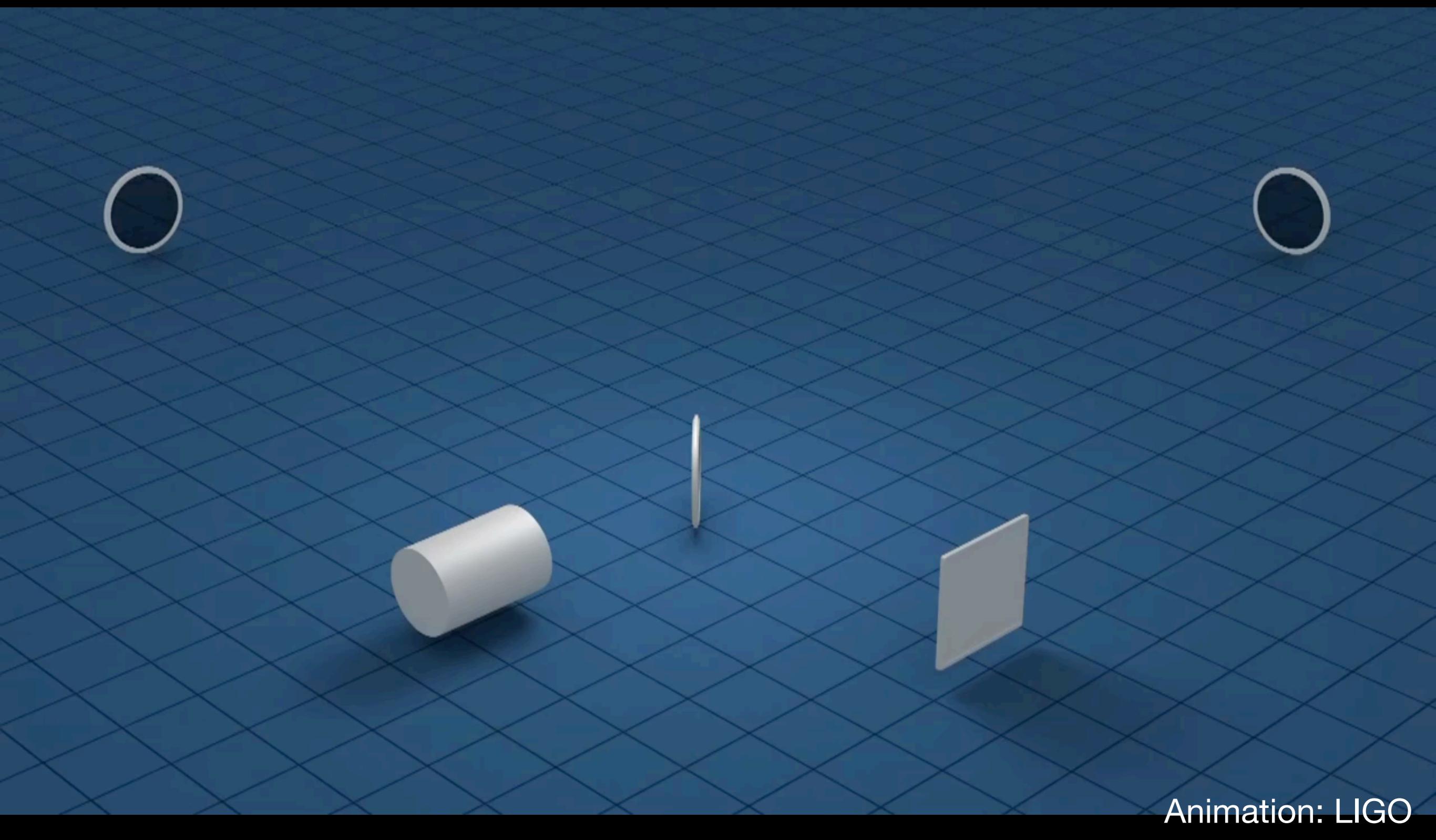
Animation: LIGO

If a gravitational wave and a pulse of light were both emitted **at the same time** from a cataclysmic event in a distant galaxy, which wave would get to earth first?

- A. Gravitational Wave
- B. Light
- C. Both would reach earth at the same time

# Measuring gravitational waves

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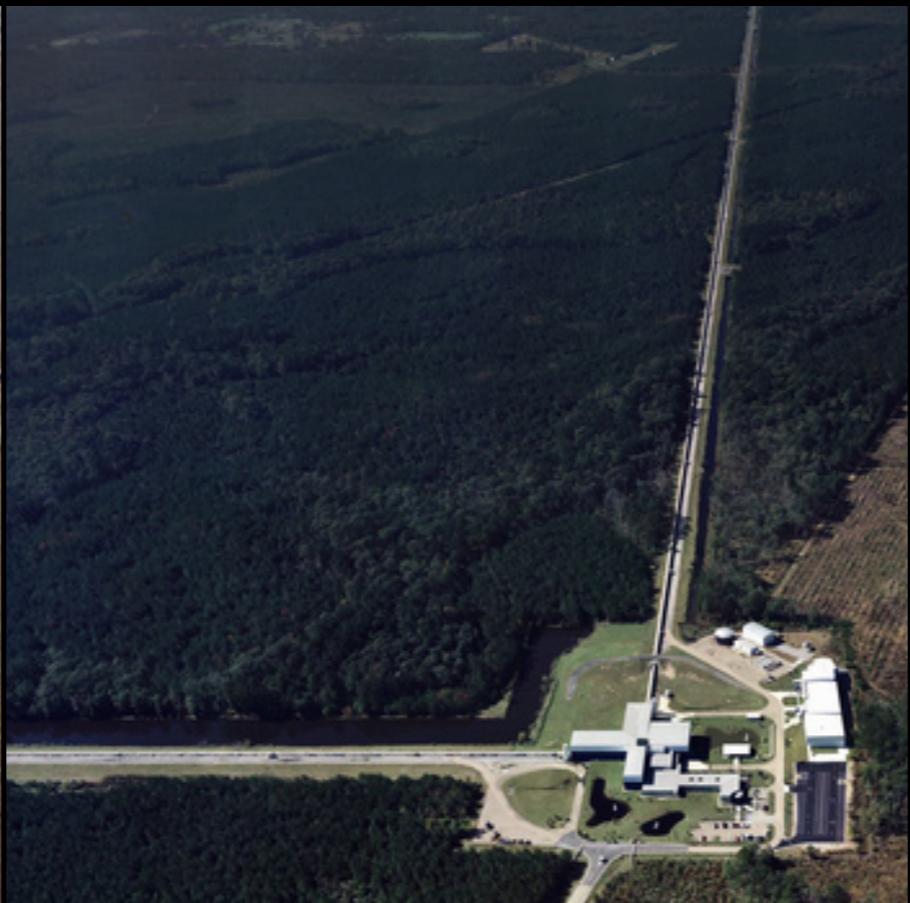


Animation: LIGO

LIGO



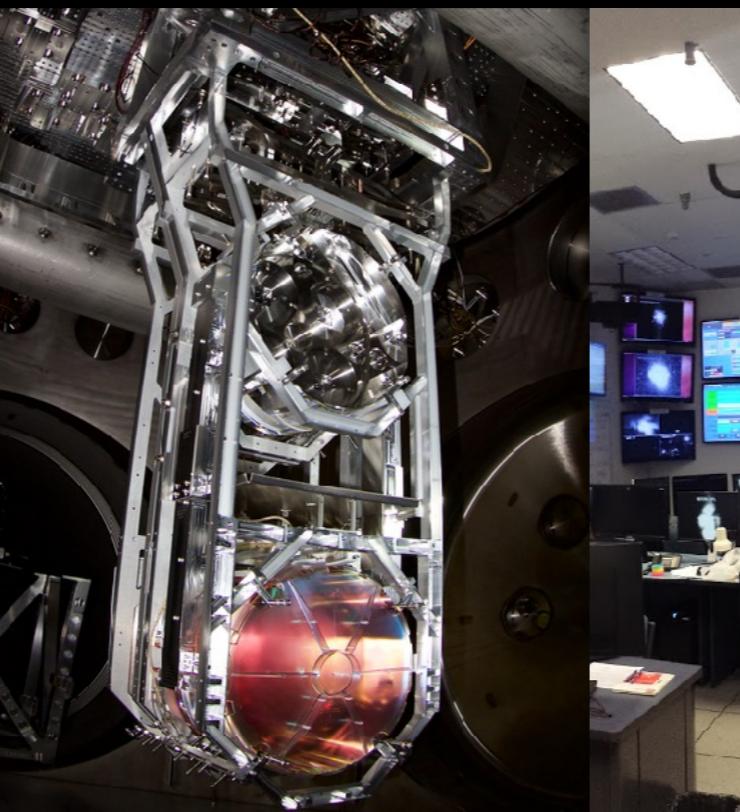
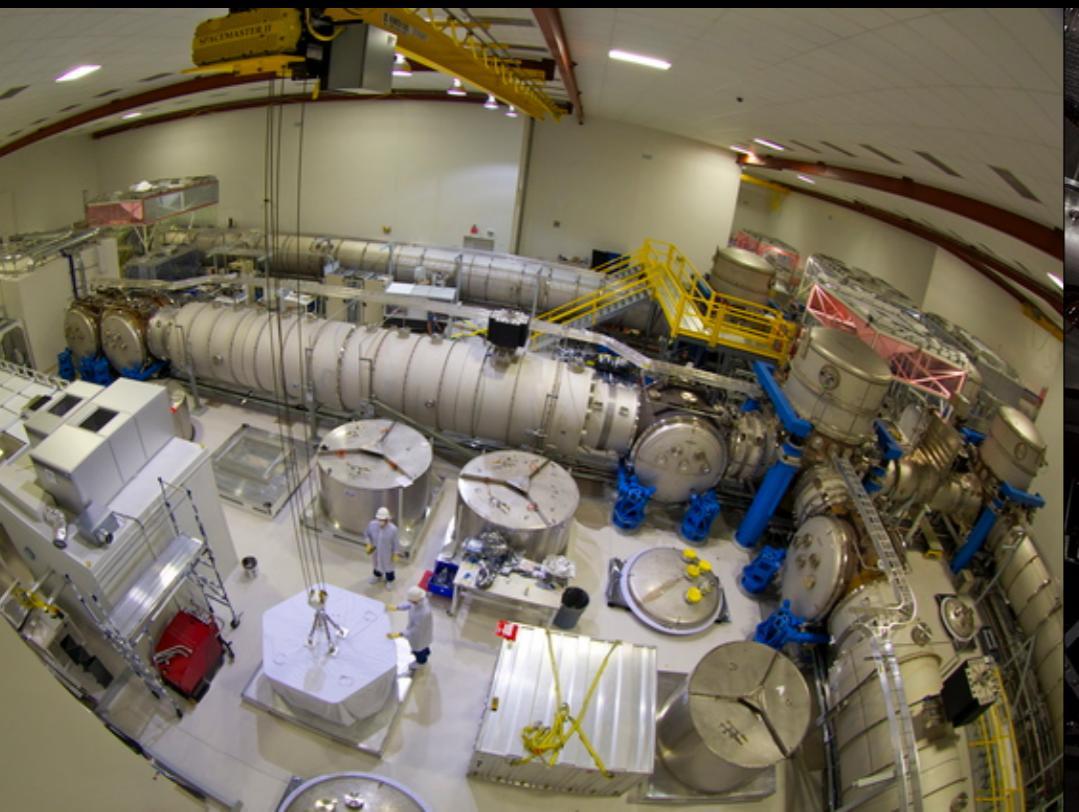
LIGO Hanford, Washington  
2015+



LIGO Livingston, Louisiana  
2015+



Virgo, Italy  
2017+



# Ground-Based gravitational-wave observatories



$LIGO_H$



$LIGO_L$

Kagra



$LIGO_I$



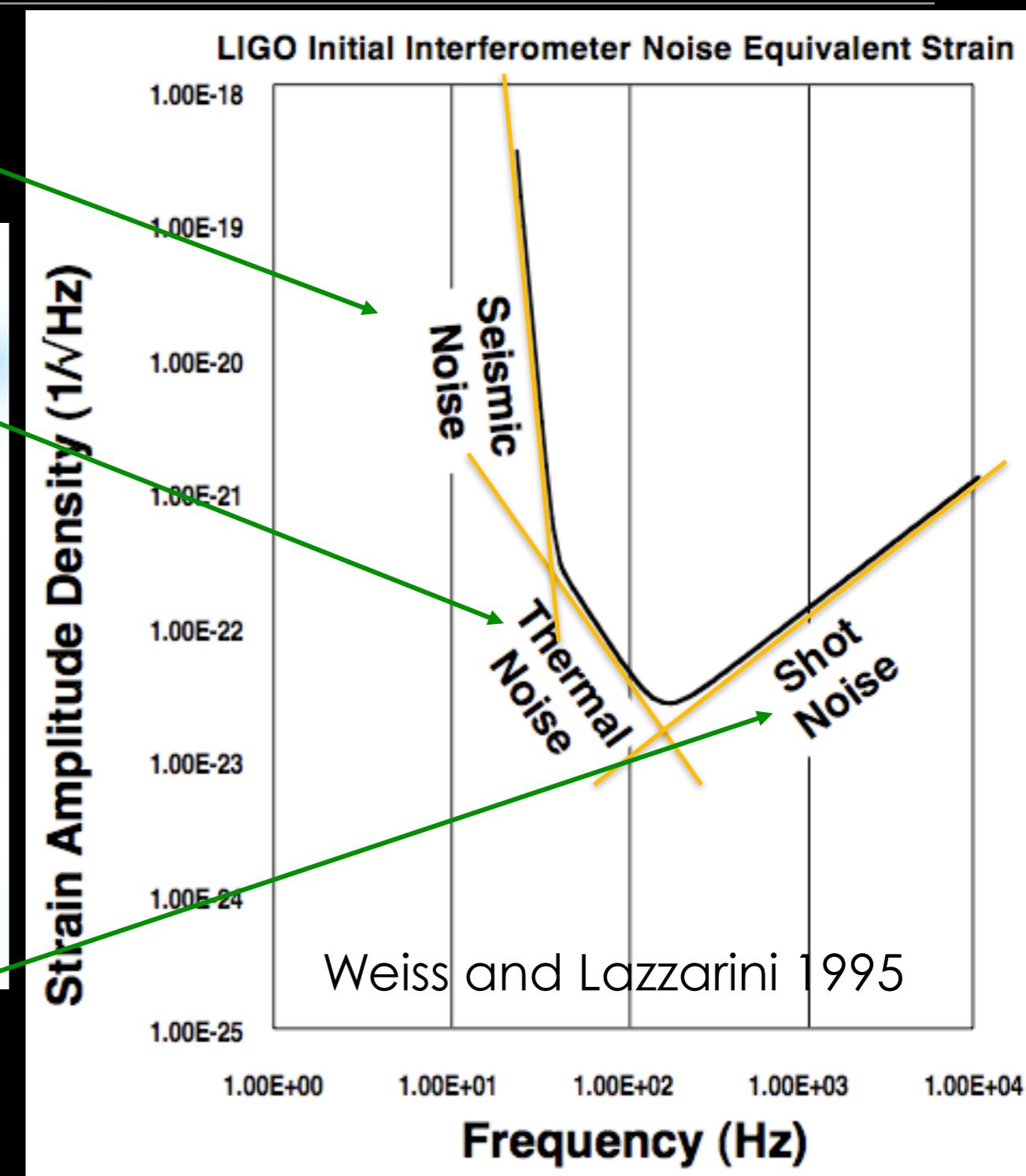
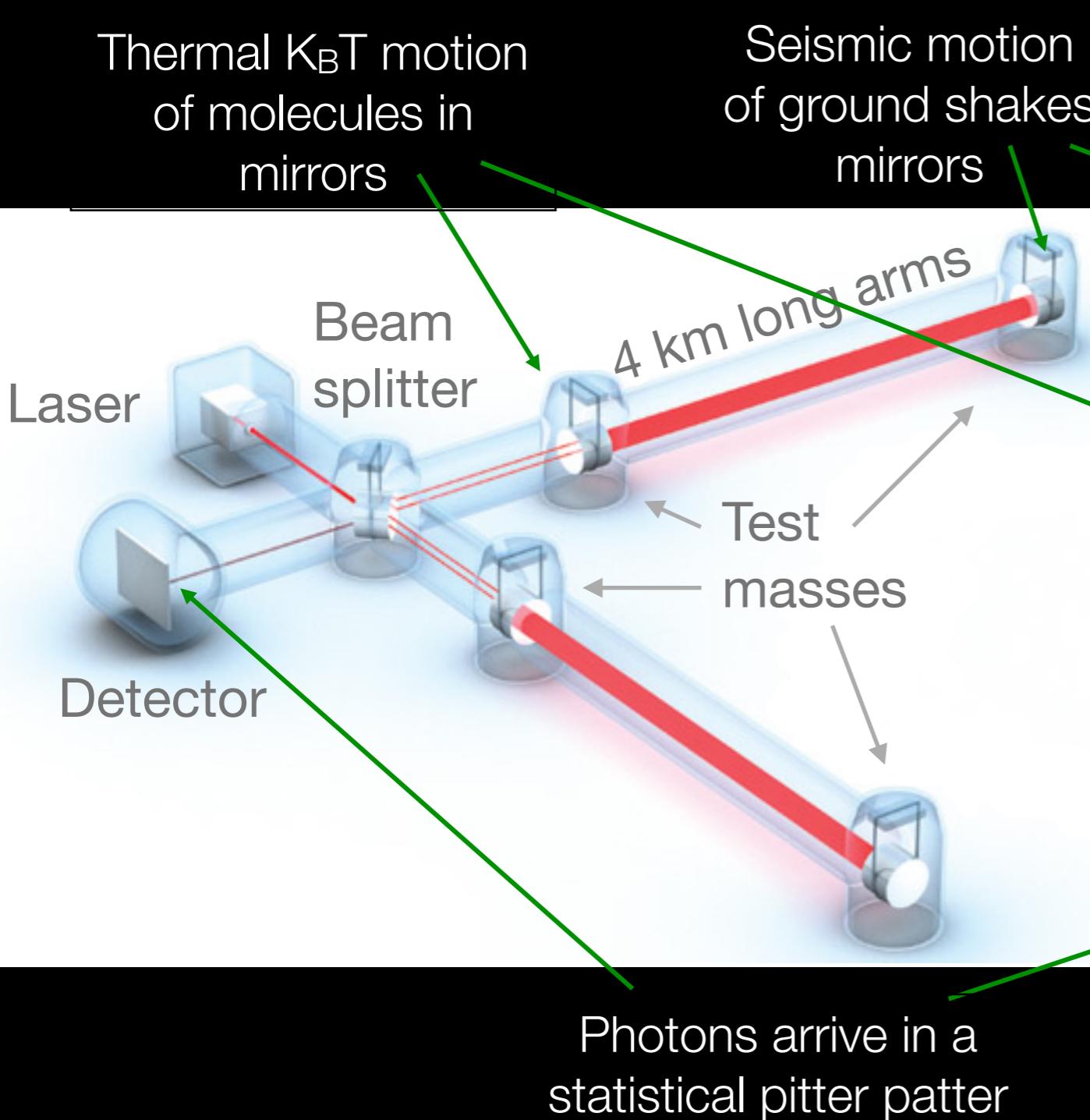
GEO600



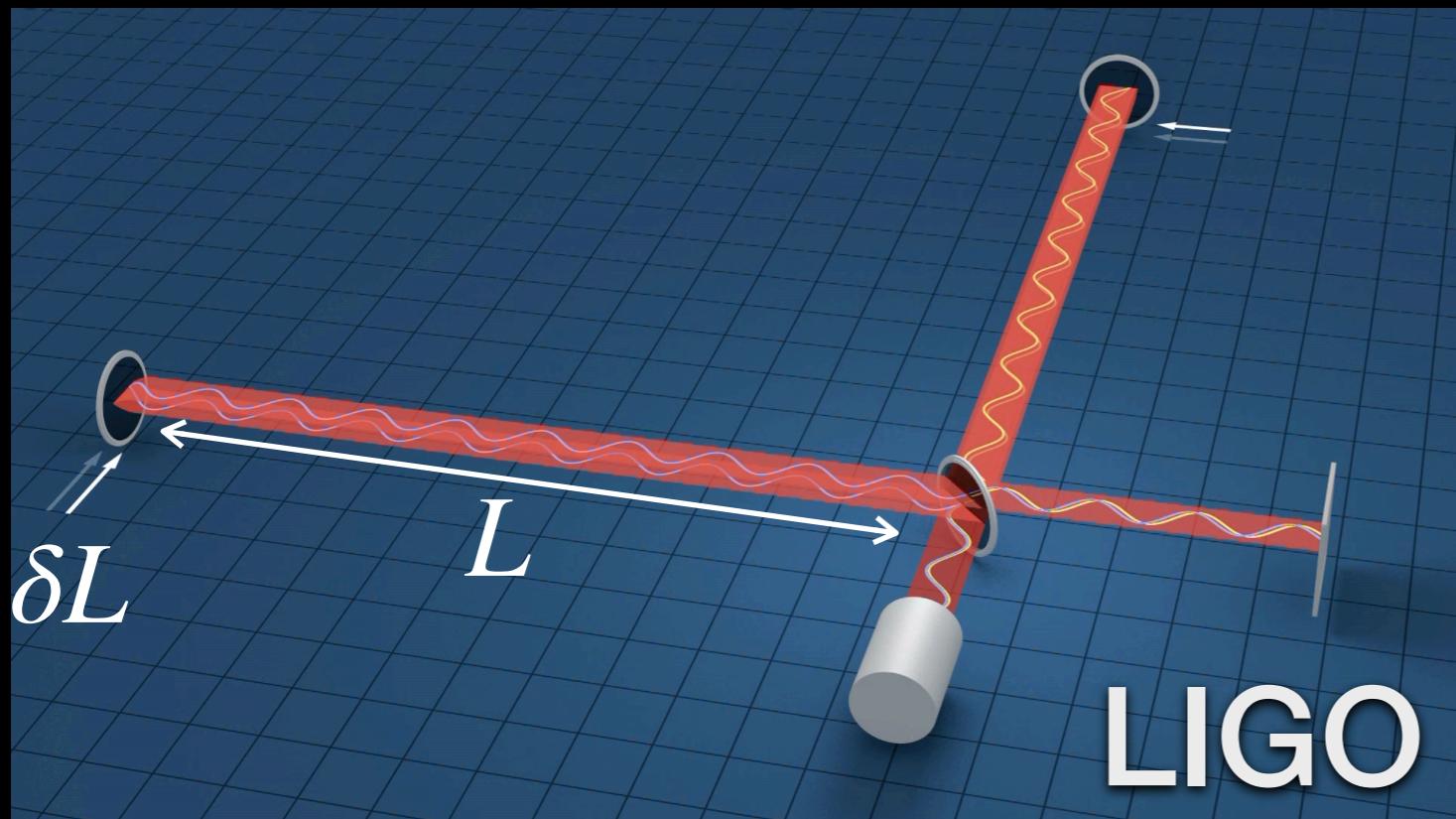
Virgo



# Competing sources of mirror motion



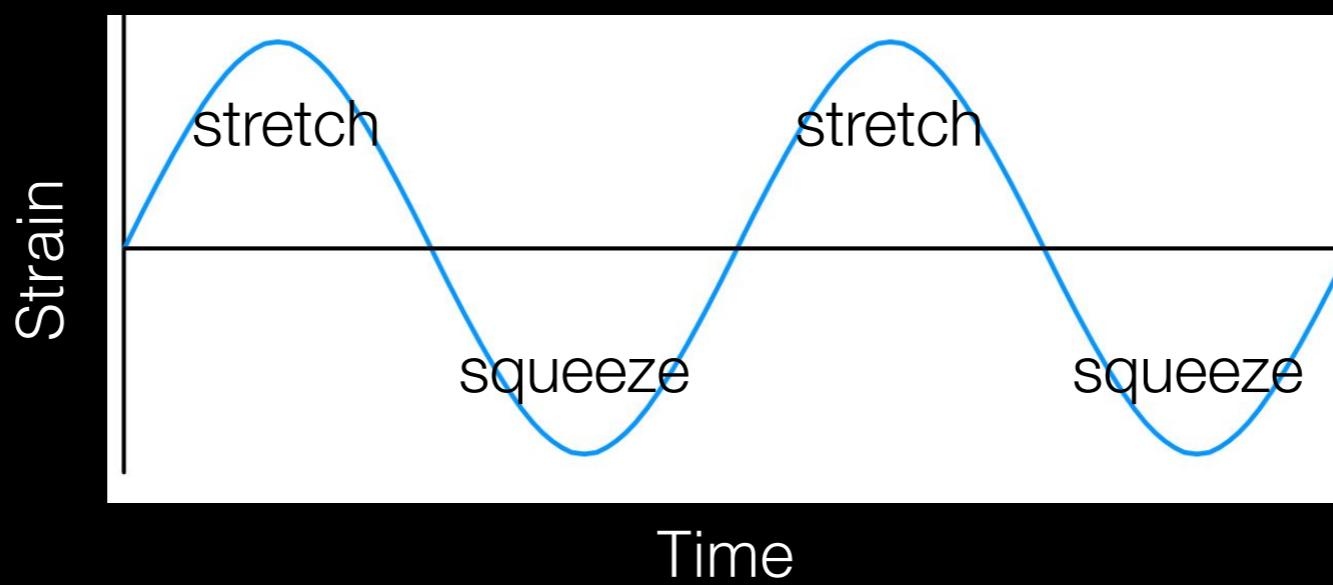
# Plotting gravitational waves



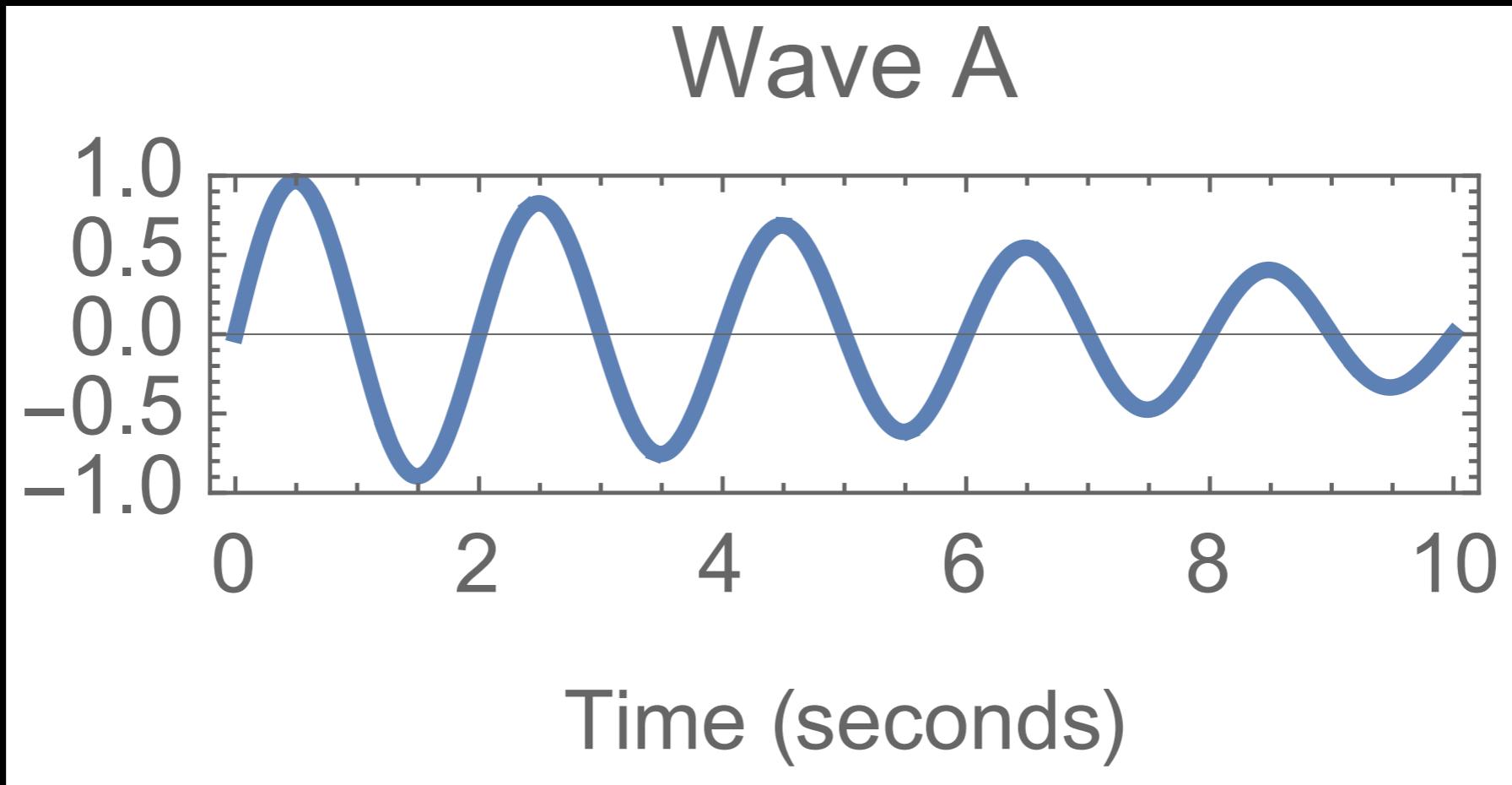
Gravitational-wave  
*strain*

$$h_+ \sim \frac{L_1 - L_2}{L}$$

Change in length  
original length

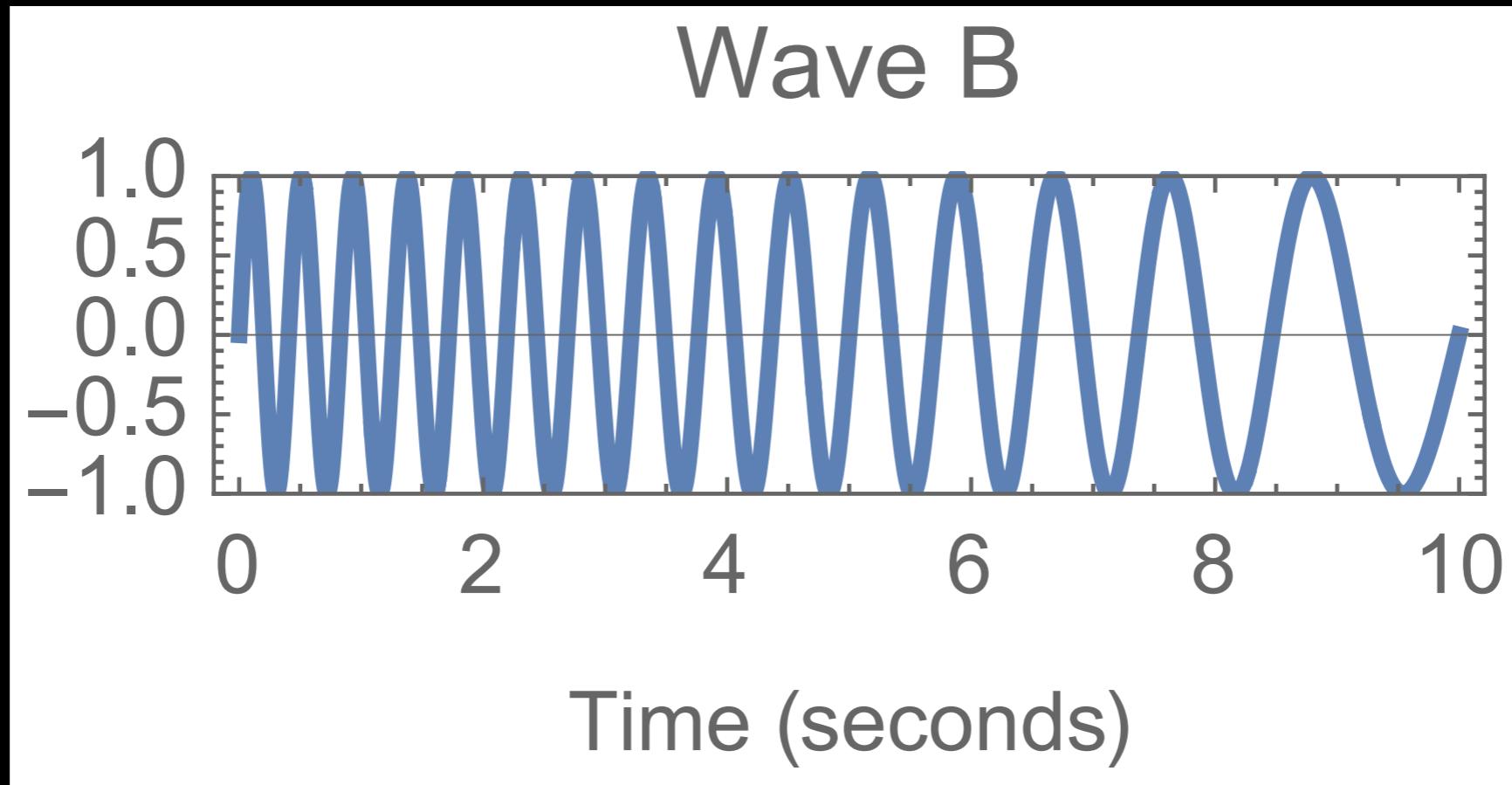


- This wave is changing with time. What is changing, and how?

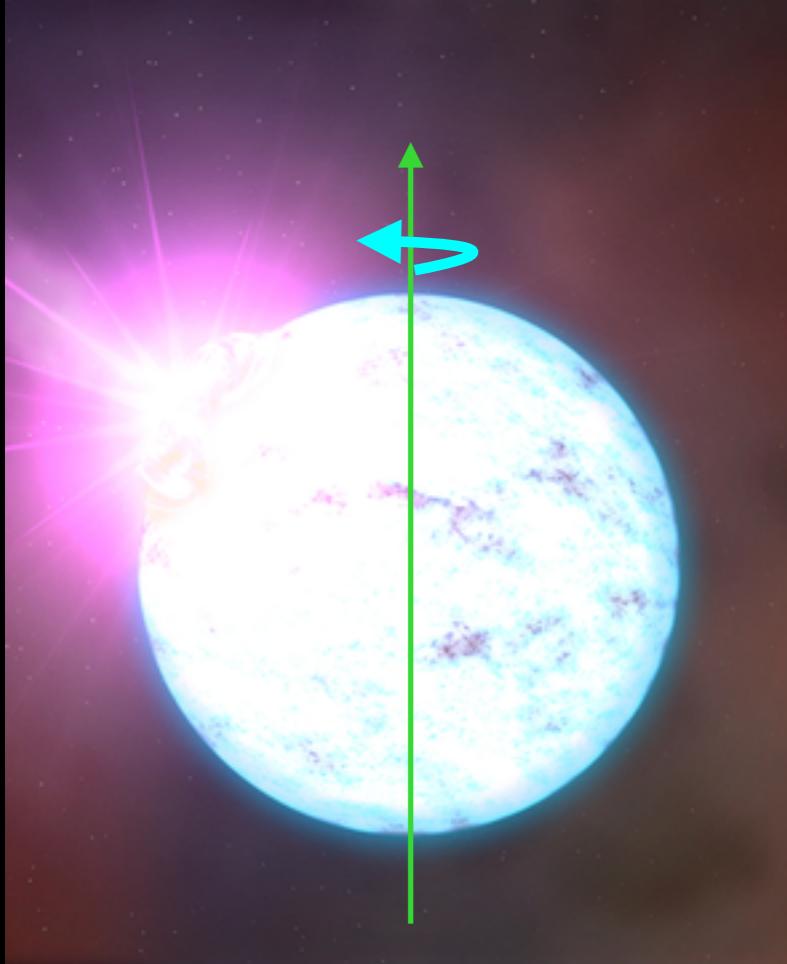


- A. Amplitude is increasing
- B. Amplitude is decreasing
- C. Frequency is increasing
- D. Frequency is decreasing

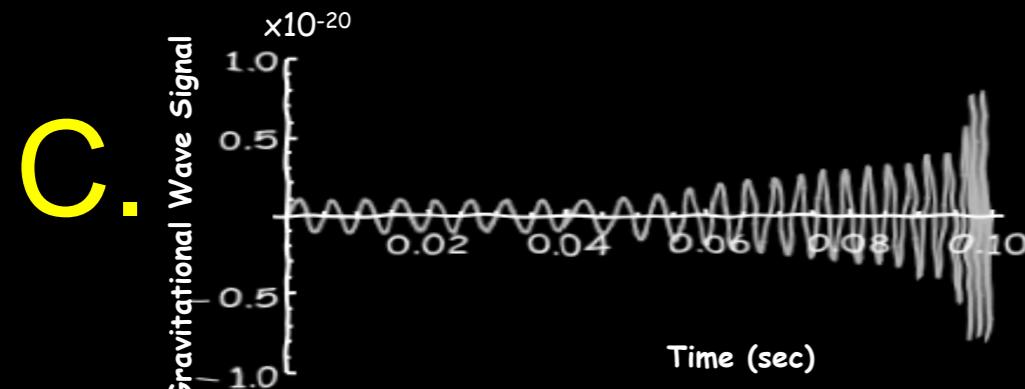
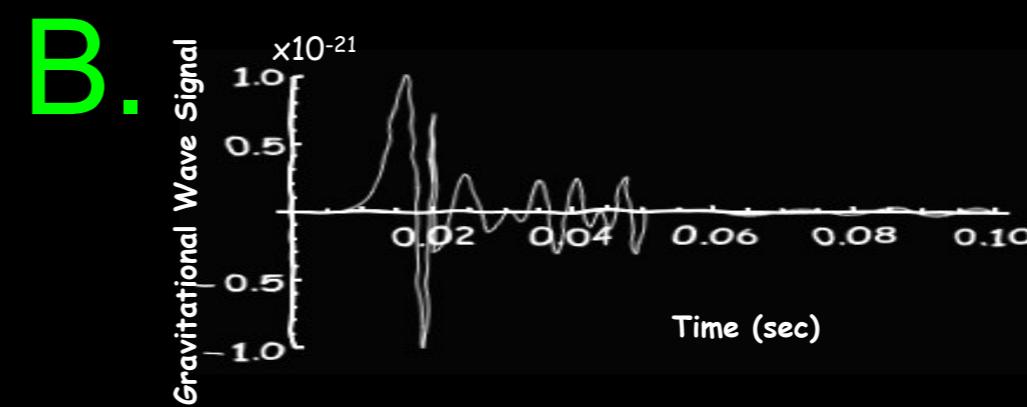
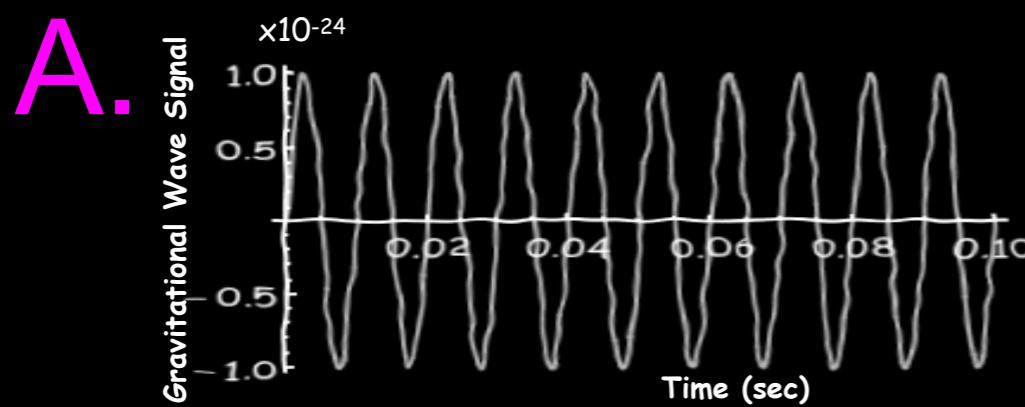
- This wave is changing with time. What is changing, and how?



- A. Amplitude is increasing
- B. Amplitude is decreasing
- C. Frequency is increasing
- D. Frequency is decreasing

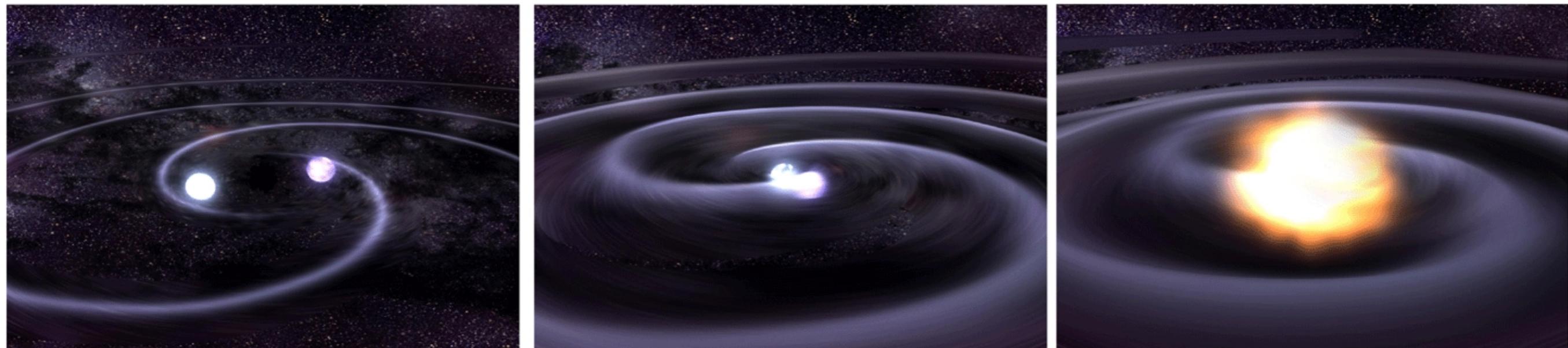


A neutron star is *spinning* at a steady rate. A heavy mountain on its surface is carried around by the star's rotation. What GW pattern is produced?



**D. No GW produced**

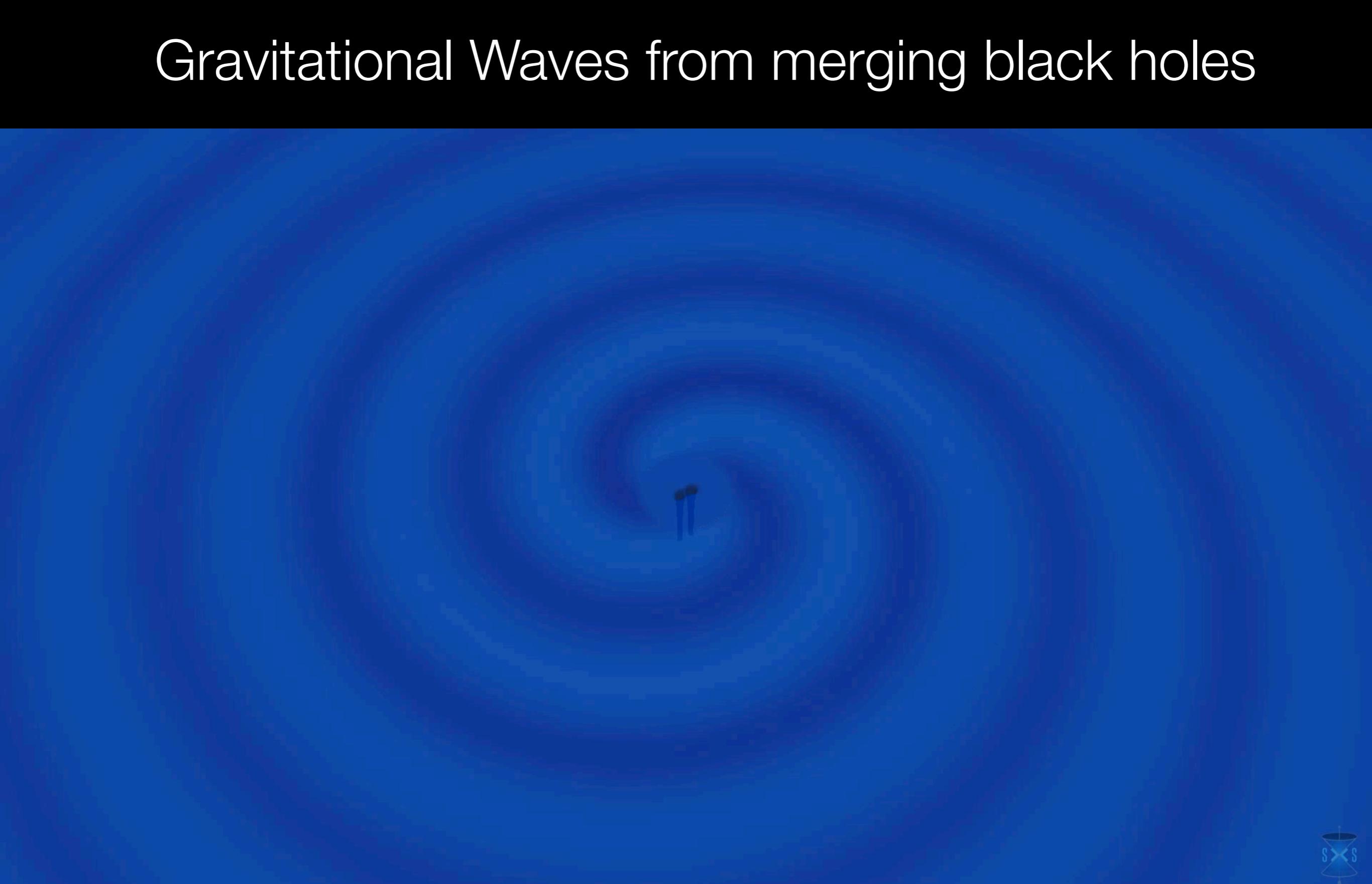
# Merger / Coalescence



- Orbiting stars emit gravitational waves; waves carry away **energy**
- Orbits with lower energy are closer together
- Closer orbits produce stronger waves



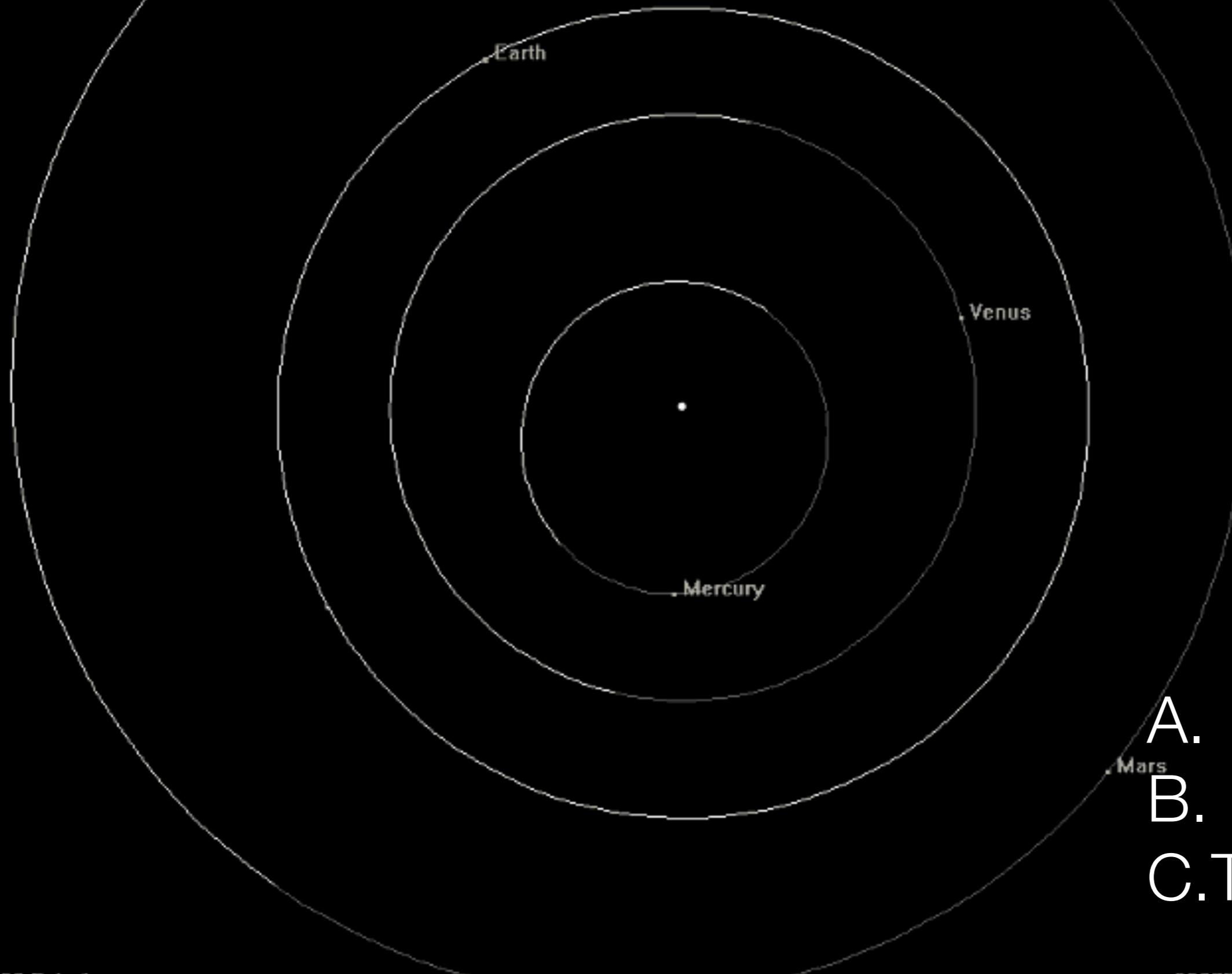
# Gravitational Waves from merging black holes



Movie by CSUF student Nick Demos,  
Simulating eXtreme Spacetimes collaboration

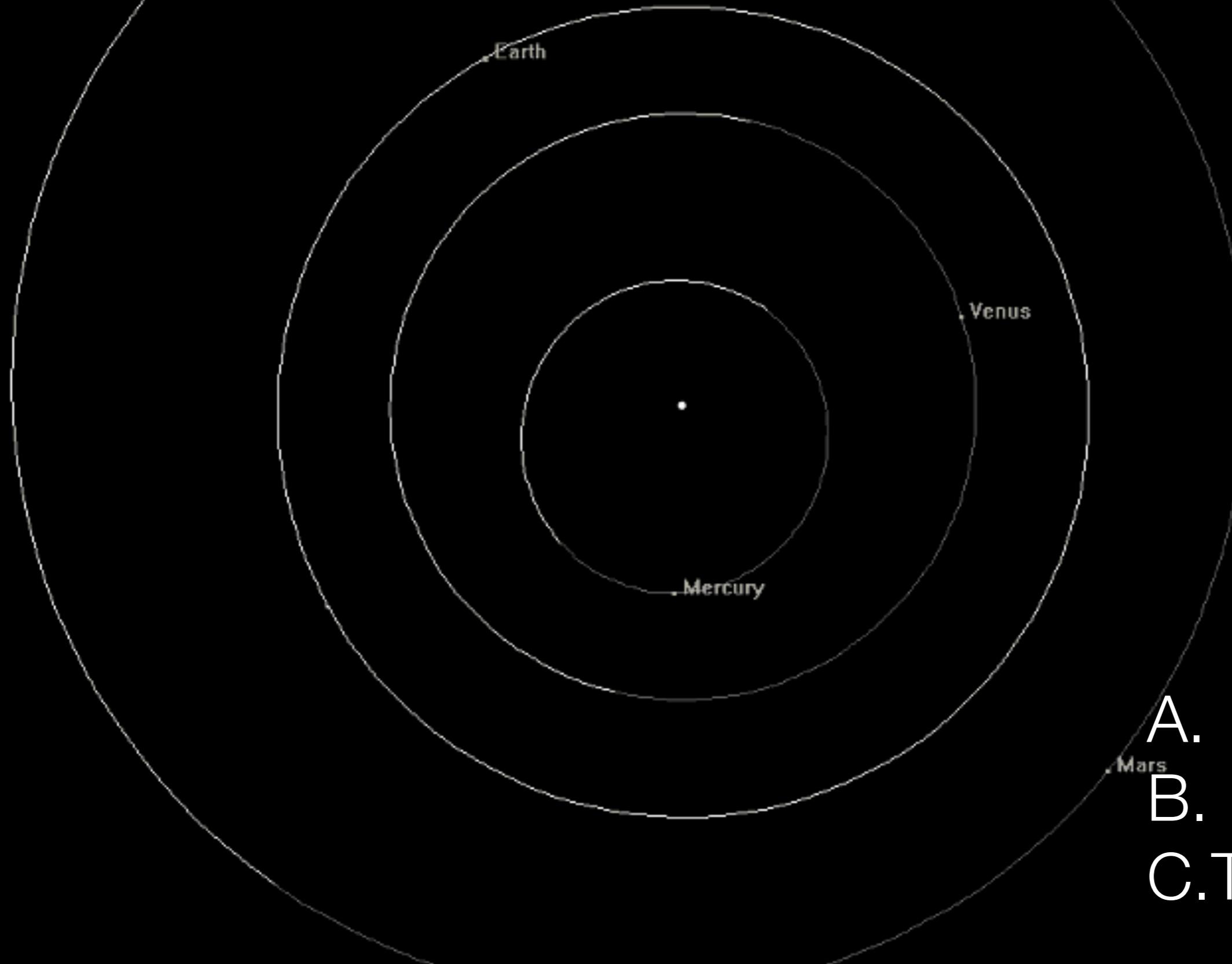


Inner orbits have \_\_\_\_\_ periods compared to outer orbits



- A. Longer
- B. Shorter
- C. The Same

Inner orbits have \_\_\_\_\_ frequencies compared to outer orbits



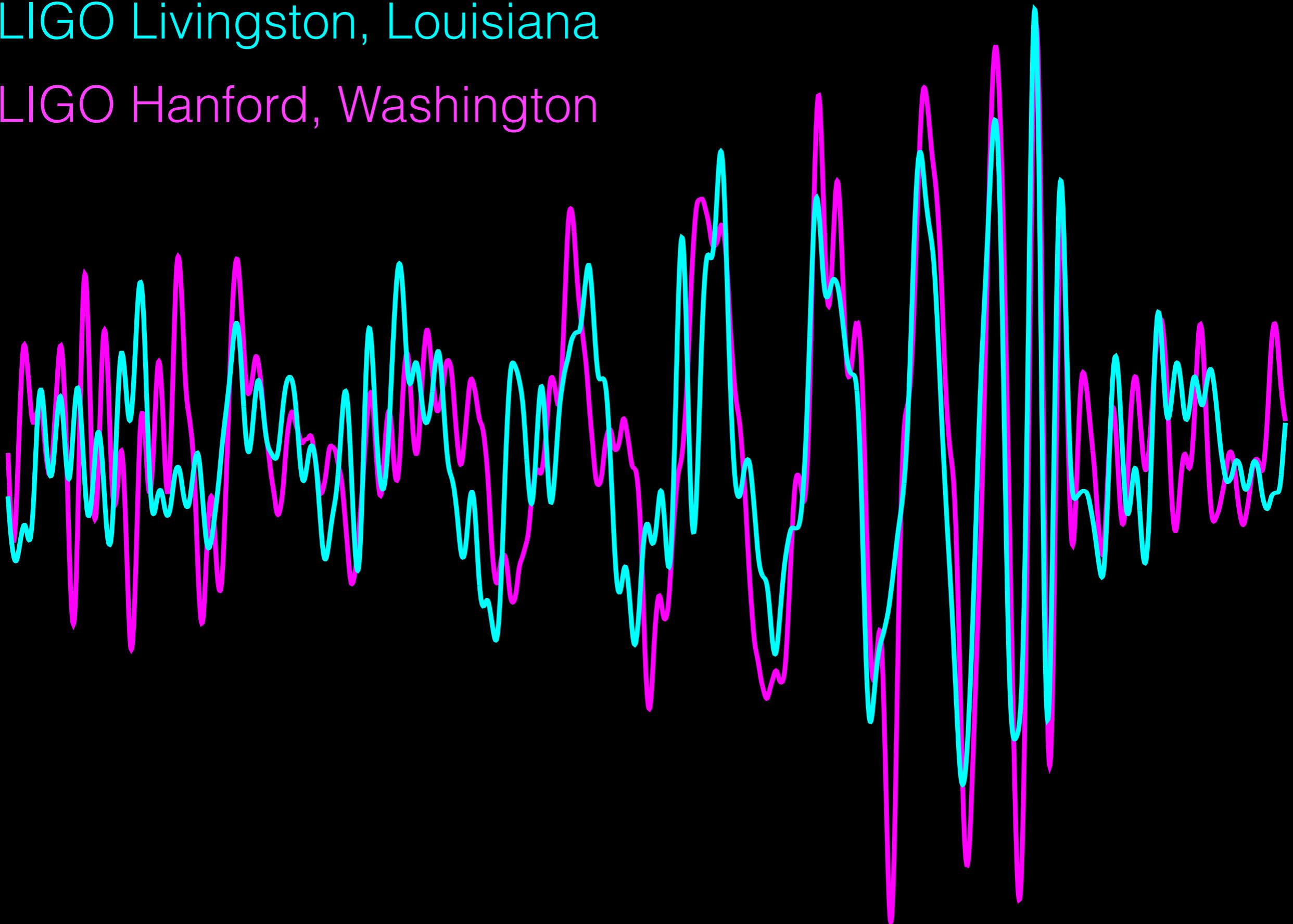
- A. Higher
- B. Lower
- C. The Same

- As a binary black hole system emits gravitational waves, the separation of the two black holes will \_\_\_\_\_ and the frequency of the binary orbit will \_\_\_\_\_.  
\_\_\_\_\_.
- As the black holes “inspiral”— fall together while orbiting— the gravitational-wave amplitude will \_\_\_\_\_.  
\_\_\_\_\_.
- *Sketch what you think the gravitational wave from merging black holes would look like*



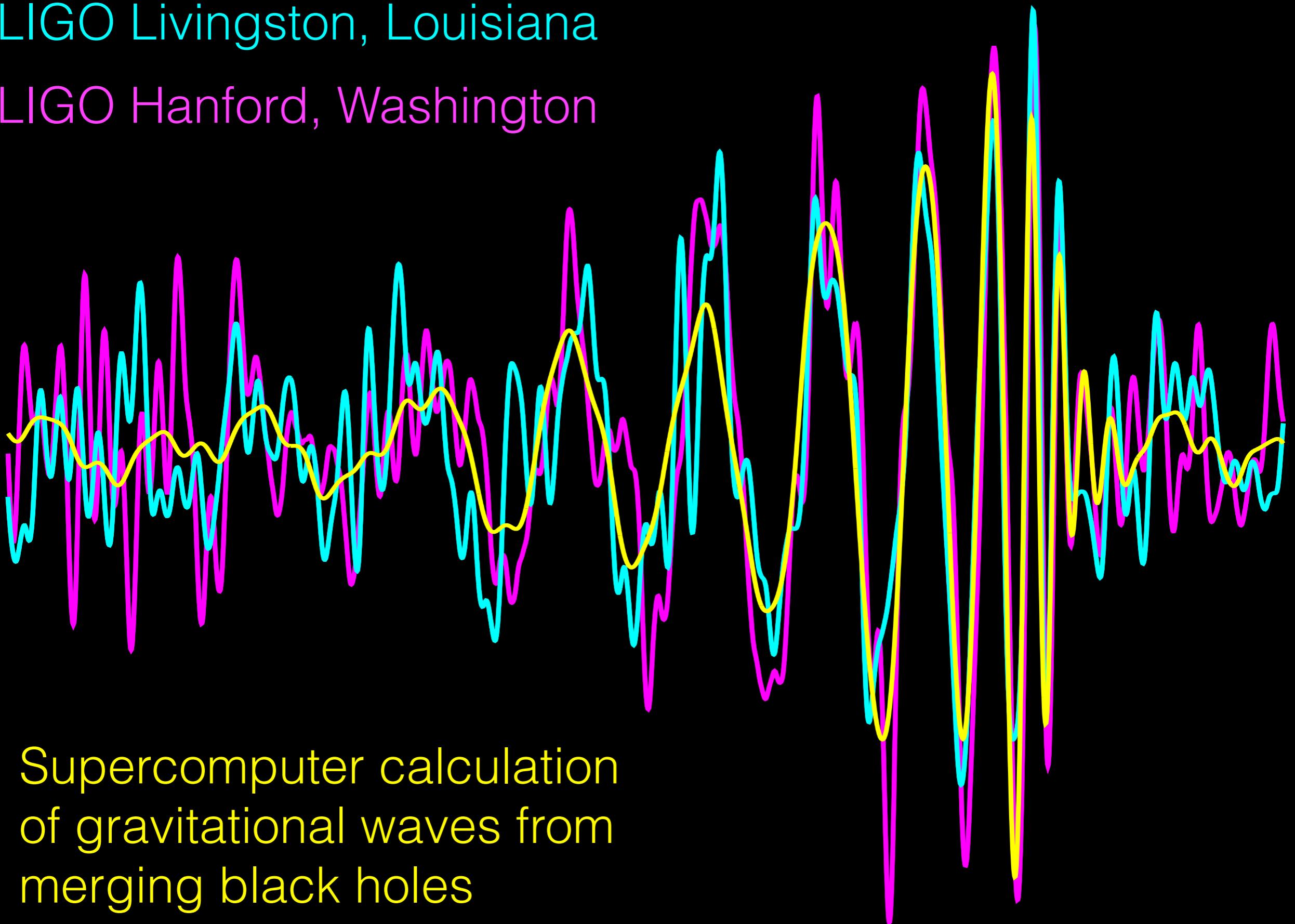
LIGO Livingston, Louisiana

LIGO Hanford, Washington

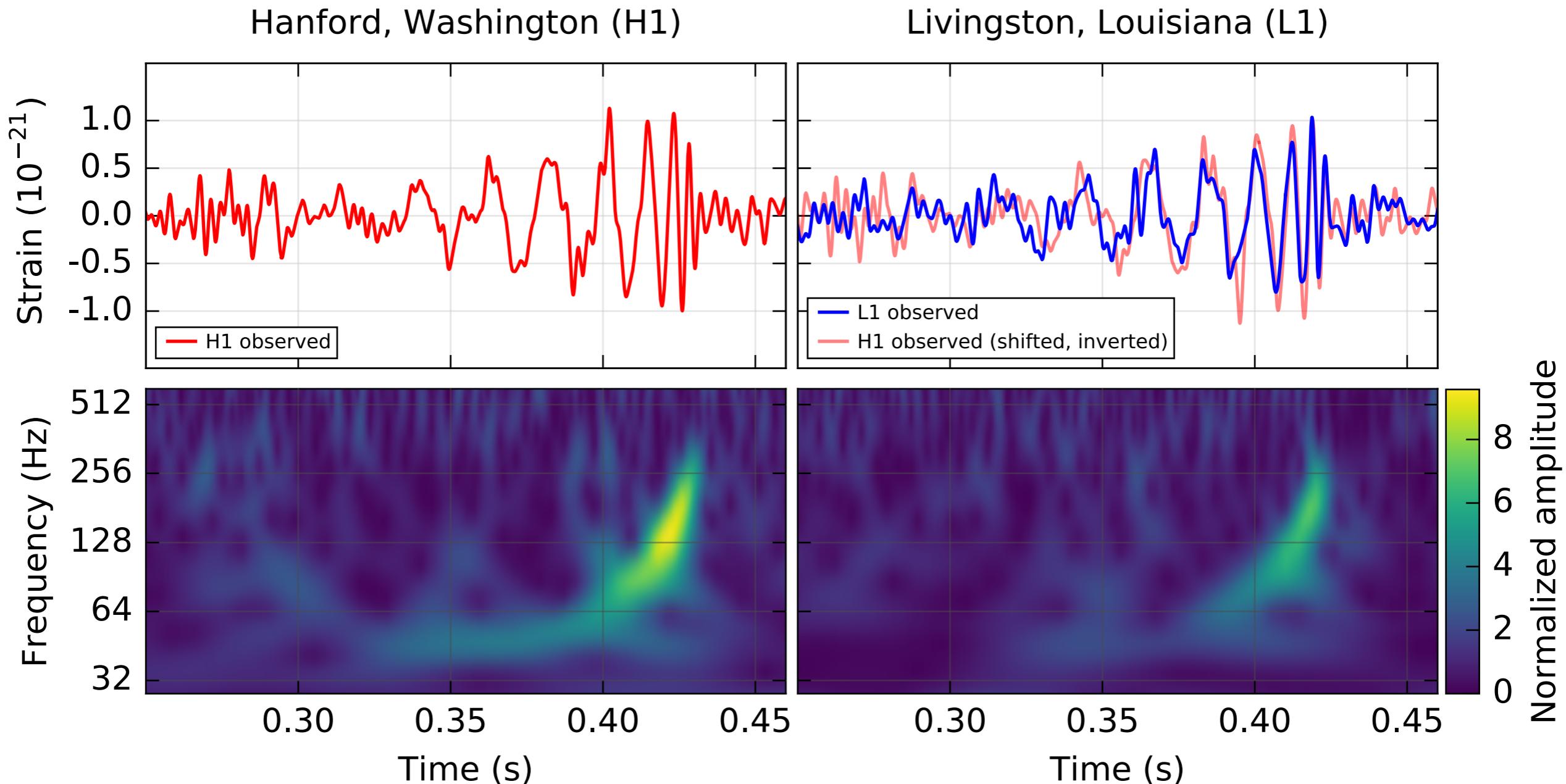


LIGO Livingston, Louisiana

LIGO Hanford, Washington



# Observation of Gravitational Waves from a Binary Black Hole Merger



September 14, 2015 at 09:50:45 GMT

PRL 116, 061102 (2016)

