

Problem 2

```
In [1]: import load_helper

import pandas as pd
import matplotlib.pyplot as plt
import numpy as np

import importlib

from torch import tensor
```

```
In [14]: fname = '2.daphne'
graph = load_helper.graph_helper(fname)
%cat 2.daphne

(defn observe-data [_ data slope bias]
  (let [xn (first data)
        yn (second data)
        zn (+ (* slope xn) bias)]
    (observe (normal zn 1.0) yn)
    (rest (rest data)))))

(let [slope (sample (normal 0.0 10.0))
      bias  (sample (normal 0.0 10.0))
      data (vector 1.0 2.1 2.0 3.9 3.0 5.3
                   4.0 7.7 5.0 10.2 6.0 12.9)]
  (loop 6 data observe-data slope bias)
  (vector slope bias))
```

```
In [3]: import bbvi
importlib.reload(bbvi)

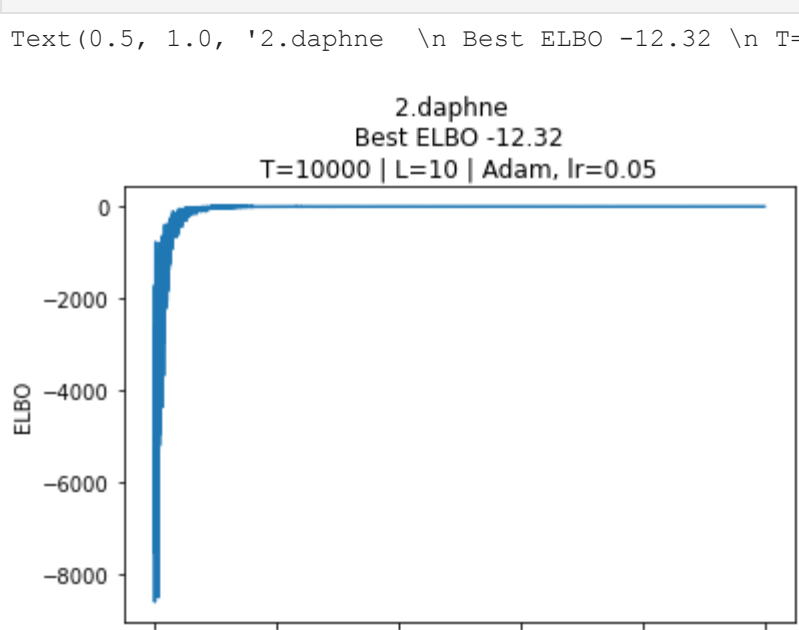
from bbvi import graph_bbvi_algo12
```

```
In [4]: %%time
T=10000
L=10
lr=0.05
r, logW, sigma = bbvi.graph_bbvi_algo12(graph,T=T,L=L,lr=lr,
                                         do_log=False)

t=0, Q after step={'sample1': Normal(loc: 0.04999999701976776, scale: 9.999954223632812), 'sample2': Normal(lo
c: 0.04999999701976776, scale: 9.999954223632812)}
t=1000, Q after step={'sample1': Normal(loc: 1.966282606124878, scale: 0.35881099104881287), 'sample2': Normal(
loc: -0.07611042261123657, scale: 2.1672756671905518)}
t=2000, Q after step={'sample1': Normal(loc: 2.102851629257202, scale: 0.18338362872600555), 'sample2': Normal
(loc: -0.42446640133857727, scale: 0.6566195487976074)}
t=3000, Q after step={'sample1': Normal(loc: 2.1381676197052, scale: 0.12904785573482513), 'sample2': Normal(lo
c: -0.4206306040287018, scale: 0.45331424474716187)}
t=4000, Q after step={'sample1': Normal(loc: 2.13557505607605, scale: 0.11017777770757675), 'sample2': Normal(l
oc: -0.5013607144355774, scale: 0.4187203347682953)}
t=5000, Q after step={'sample1': Normal(loc: 2.1337504386901855, scale: 0.10388973355293274), 'sample2': Normal
(loc: -0.506049394607544, scale: 0.4013504683971405)}
t=6000, Q after step={'sample1': Normal(loc: 2.173062324523926, scale: 0.10475638508796692), 'sample2': Normal
(loc: -0.5092238187789917, scale: 0.4144499897956848)}
t=7000, Q after step={'sample1': Normal(loc: 2.187255620956421, scale: 0.10510562360286713), 'sample2': Normal
(loc: -0.696744441986084, scale: 0.39388900995254517)}
t=8000, Q after step={'sample1': Normal(loc: 2.1886229515075684, scale: 0.10825375467538834), 'sample2': Normal
(loc: -0.5877746939659119, scale: 0.41785284876823425)}
t=9000, Q after step={'sample1': Normal(loc: 2.0912787914276123, scale: 0.09985072910785675), 'sample2': Normal
(loc: -0.5837337374687195, scale: 0.4200637638568878)}
CPU times: user 4min 27s, sys: 888 ms, total: 4min 28s
Wall time: 4min 29s
```

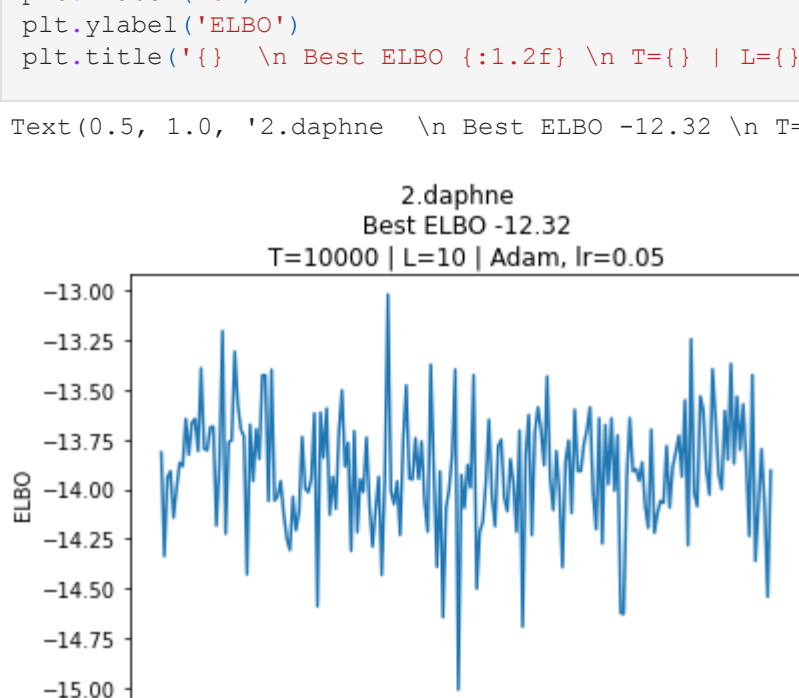
```
In [5]: elbo = logW.mean(1)
pd.Series(elbo).plot()
plt.xlabel('t')
plt.ylabel('ELBO')
plt.title('{} \n Best ELBO {:.1,2f} \n T={} | L={} | Adam, lr={} '.format(fname,elbo.max(),T,L,lr))
```

```
Out[5]: Text(0.5, 1.0, '2.daphne \n Best ELBO -12.32 \n T=10000 | L=10 | Adam, lr=0.05 ')
```



```
In [6]: sr = pd.Series(elbo[-200:])
sr.index = np.arange(elbo.size-200,elbo.size)
sr.plot()
plt.xlabel('t')
plt.ylabel('ELBO')
plt.title('{} \n Best ELBO {:.1,2f} \n T={} | L={} | Adam, lr={} '.format(fname,elbo.max(),T,L,lr))
```

```
Out[6]: Text(0.5, 1.0, '2.daphne \n Best ELBO -12.32 \n T=10000 | L=10 | Adam, lr=0.05 ')
```



```
In [7]: r_array = np.zeros((T,L,2))
for t in range(T):
    for l in range(L):
        r_array[t,l,:] = r[t][l].detach().numpy()
```

```
In [8]: probs = np.exp(logW)
probs /= probs.sum()
probs = probs.reshape(T,L,1)
posterior_r = (probs * r_array).sum(axis=(0,1))
posterior_r2 = (probs * r_array**2).sum(axis=(0,1))

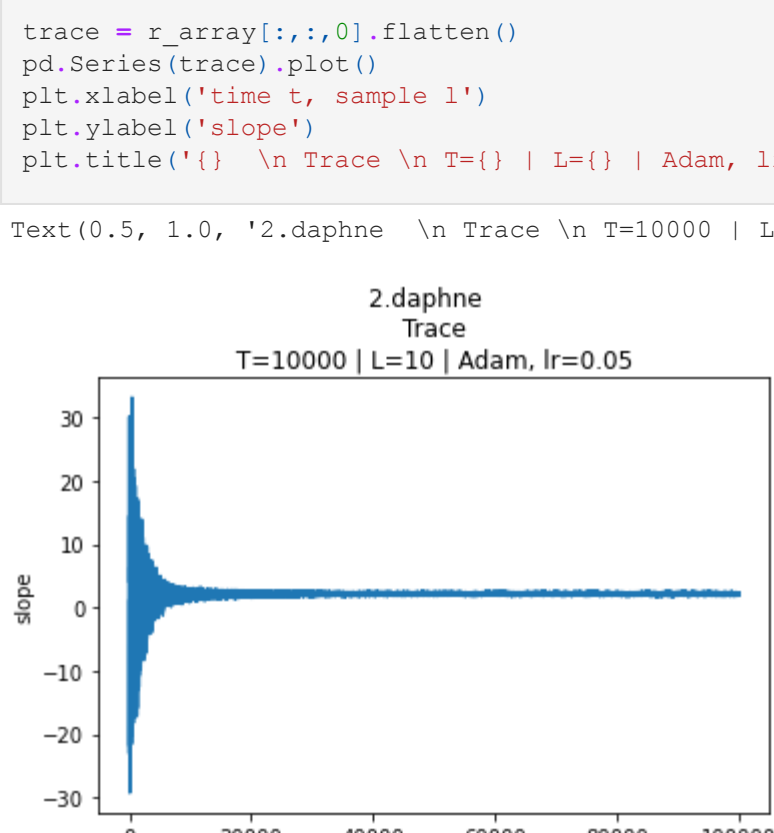
std_r = np.sqrt(posterior_r2 - posterior_r**2)
```

```
In [9]: idx=0
print('{} expected posterior slope {:.1,3f} | std posterior slope {:.1,3f}'.format(fname,posterior_r[idx],std_r[idx])
idx=1
print('{} expected posterior bias {:.1,3f} | std posterior bias {:.1,3f}'.format(fname,posterior_r[idx],std_r[idx])

2.daphne expected posterior slope 2.154 | std posterior slope 0.206
2.daphne expected posterior bias -0.530 | std posterior bias 0.800
```

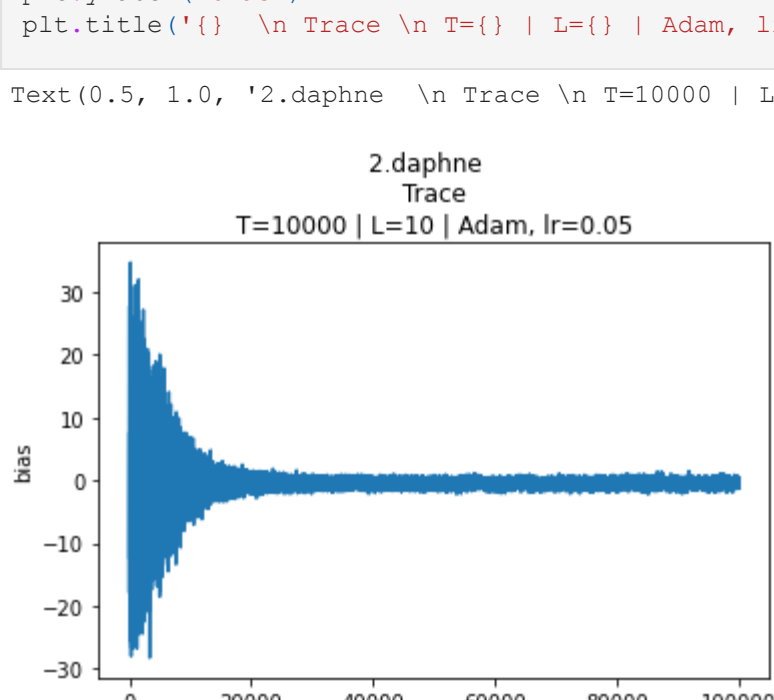
```
In [10]: trace = r_array[:, :, 0].flatten()
pd.Series(trace).plot()
plt.xlabel('time t, sample 1')
plt.ylabel('slope')
plt.title('{} \n Trace \n T={} | L={} | Adam, lr={} '.format(fname,T,L,lr))
```

```
Out[10]: Text(0.5, 1.0, '2.daphne \n Trace \n T=10000 | L=10 | Adam, lr=0.05 ')
```



```
In [11]: trace = r_array[:, :, 1].flatten()
pd.Series(trace).plot()
plt.xlabel('time t, sample 1')
plt.ylabel('bias')
plt.title('{} \n Trace \n T={} | L={} | Adam, lr={} '.format(fname,T,L,lr))
```

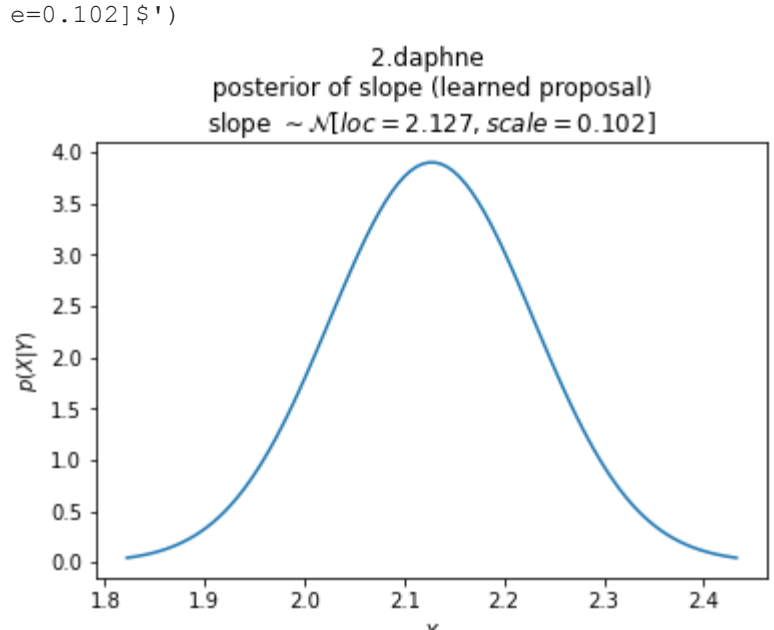
```
Out[11]: Text(0.5, 1.0, '2.daphne \n Trace \n T=10000 | L=10 | Adam, lr=0.05 ')
```



```
In [12]: Q = sigma['Q_best_t']
q = Q['sample1']
loc = q.loc.detach().numpy()
scale = q.scale.detach().numpy()
support = np.linspace(loc-3*scale,loc+3*scale,100)
log_pdf = np.zeros_like(support)
for idx,c in enumerate(support):
    log_pdf[idx] = q.log_prob(tensor(c))
pdf = np.exp(log_pdf)

sr = pd.Series(pdf)
sr.index = support
sr.plot()
plt.xlabel('$X$')
plt.ylabel('$p(X|Y)$')
plt.title(\
'{} \n posterior of slope (learned proposal) \n'.format(fname) + \
'slope $\sim \mathcal{N}(\text{N})$' + \
'$[loc={:1.3f}, scale={:1.3f}]$'.format(loc,scale)
)
```

```
Out[12]: Text(0.5, 1.0, '2.daphne \n posterior of slope (learned proposal) \nslope $\sim \mathcal{N}(\text{N})$ $[loc=2.127, scale=0.102]$')
```



```
In [13]: Q = sigma['Q_best_t']
q = Q['sample2']
loc = q.loc.detach().numpy()
scale = q.scale.detach().numpy()
support = np.linspace(loc-3*scale,loc+3*scale,100)
log_pdf = np.zeros_like(support)
for idx,c in enumerate(support):
    log_pdf[idx] = q.log_prob(tensor(c))
pdf = np.exp(log_pdf)

sr = pd.Series(pdf)
sr.index = support
sr.plot()
plt.xlabel('$X$')
plt.ylabel('$p(X|Y)$')
plt.title(\
'{} \n posterior of bias (learned proposal) \n'.format(fname) + \
'bias $\sim \mathcal{N}(\text{N})$' + \
'$[loc={:1.3f}, scale={:1.3f}]$'.format(loc,scale)
)
```

```
Out[13]: Text(0.5, 1.0, '2.daphne \n posterior of bias (learned proposal) \nbias $\sim \mathcal{N}(\text{N})$ $[loc=-0.504, scale=0.463]$')
```

