import pandas as pd import matplotlib.pyplot as plt import seaborn as sns import importlib from evaluation based sampling import evaluate, evaluate program from daphne import daphne from graph\_based\_sampling import sample\_from\_joint **Problem 1** In [2]: from load helper import ast helper, graph helper Importance sampling 10k in 3.34s implies 1.7e6 in 10 min In [3]: import parse import importance\_sampling  ${\bf import} \ {\bf importlib}$ importlib.reload(parse) <module 'parse' from '/Users/gw/repos/prob\_prog/hw/hw3/parse.py'> Out[3]: In [35]: fname = '1.daphne' ast = ast\_helper(fname) ast [['let', Out[35]: ['mu', ['sample', ['normal', 1, ['sqrt', 5]]]], ['let', ['sigma', ['sqrt', 2]], ['let', ['lik', ['normal', 'mu', 'sigma']], ['let', ['dontcare0', ['observe', 'lik', 8]], ['let', ['dontcare1', ['observe', 'lik', 9]], 'mu']]]]] In [53]: %%time num samples=1790000 samples, sigmas = parse.take\_samples(num\_samples,ast) CPU times: user 10min 27s, sys: 3.59 s, total: 10min 31s Wall time: 10min 32s In [54]: samples = np.array([sample.item() for sample in samples]) In [55]: posterior\_mean, probs = importance\_sampling.weighted\_average(samples, sigmas) posterior\_mean 7.2549860583141825 Out[55]: In [60]: # pd.Series(samples).plot.hist() \_ = plt.hist(samples, weights=probs, bins=100) plt.title('Problem {} \n Importance sampling \n importance sampling weighted counts from proposal'.format(fname plt.xlabel('mu') plt.ylabel('(weighted) Counts') Text(0, 0.5, '(weighted) Counts') Out[60]: Problem 1.daphne Importance sampling 0.10 0.08 (weighted) Counts 0.06 0.04 0.02 0.00 -10In [57]: expectation\_samples\_2, probs = importance\_sampling.weighted\_average(samples\*\*2, sigmas) posterior\_variance = expectation\_samples\_2 - posterior\_mean\*\*2 In [58]: "Importance sampling: posterior mean of mu {:1.3f} | variance {:1.3e}".format(posterior\_mean,posterior\_variance 'Importance sampling: posterior mean of mu 7.255 | variance 8.292e-01' Out[58]: MH within Gibbs 5k in 5.58s implies 537k samples in 10 min In [11]: import mh\_gibbs from hmc import compute\_log\_joint\_prob importlib.reload(mh\_gibbs) <module 'mh\_gibbs' from '/Users/gw/repos/prob\_prog/hw/hw3/mh\_gibbs.py'> Out[11]: In [12]: fname = '1.daphne' graph = graph\_helper(fname) graph Out[12]: [{}, {'V': ['observe3', 'observe4', 'sample2'], 'A': {'sample2': ['observe3', 'observe4']}, 'P': {'sample2': ['sample\*', ['normal', 1, ['sqrt', 5]]], 'observe3': ['observe\*', ['normal', 'sample2', ['sqrt', 2]], 8], 'observe4': ['observe\*', ['normal', 'sample2', ['sqrt', 2]], 9]}, 'Y': {'observe3': 8, 'observe4': 9}}, 'sample2'] In [13]: %%time num steps=537000 return\_list, samples\_whole\_graph = mh\_gibbs.mh\_gibbs\_wrapper(graph,num\_steps=num\_steps) CPU times: user 9min 48s, sys: 2.11 s, total: 9min 51s Wall time: 9min 54s In [14]: samples = np.array([x.item() for x in return\_list]) In [15]: burn\_in = int(0.01\*num\_steps) sr = pd.Series(samples[burn\_in:]) sr.plot.hist() plt.title('burn in {:} / {:} total steps \n E[mu]={:1.2f}'.format(burn\_in, len(samples), sr.mean())) plt.xlabel('mu') Out[15]: Text(0.5, 0, 'mu') burn in 5370 / 537001 total steps E[mu] = 7.31160000 140000 120000 100000 80000 60000 40000 20000 0 7 9 11 10 In [16]: "MH Gibbs: posterior mean of mu {:1.3f} | variance {:1.3e}".format(sr.mean(),sr.var()) 'MH Gibbs: posterior mean of mu 7.310 | variance 8.421e-01' Out[16]: In [17]: pd.Series(samples).plot() plt.xlabel('Iteration') plt.ylabel('mu') plt.title('{} | MH Gibbs \n Sample trace'.format(fname)) Text(0.5, 1.0, '1.daphne | MH Gibbs \n Sample trace') Out[17]: 1.daphne | MH Gibbs Sample trace 10 8 2 0 100000 200000 300000 400000 500000 Iteration In [18]: G = graph[1]Y = G['Y']Y = {key:evaluate([value])[0] for key, value in Y.items()} P = G['P']In [19]: size = len(samples\_whole\_graph) jll = np.zeros(size) for idx in range(size): jll[idx] = compute\_log\_joint\_prob(samples\_whole\_graph[idx],Y,P) In [20]: pd.Series(jll).plot() plt.xlabel('Iteration (t)') plt.ylabel(r'\$-\log p( $X=x_t, Y=y_t$ )\$') plt.title('{} | MH Gibbs \n Joint density'.format(fname)) Text(0.5, 1.0, '1.daphne | MH Gibbs \n Joint density') Out[20]: 1.daphne | MH Gibbs Joint density -10-20 -30 $-\log p(X = x_t, Y = y_t)$ -40 -50 -60 -70 -80 -90 100000 200000 300000 400000 500000 Iteration (t) **HMC** 5k samples in 41.4 s implies 72k in 10 min In [61]: fname = '1.daphne' graph = graph\_helper(fname) In [62]: import hmc importlib.reload(hmc) from hmc import hmc\_wrapper In [ ]: num samples=72000 return list, samples whole graph = hmc wrapper(graph, num samples, T=20, epsilon=0.1) In [70]: samples = np.array([x.item() for x in return list]) In [71]: burn in = int(0.01\*num samples) # ~500 from inspecting joint density plot, with given hyper params T, epsilon, sr = pd.Series(samples[burn\_in:]) sr.plot.hist() sr.mean()  $plt.title('\{\} \mid HMC \setminus n \ \{:\} \ total \ steps \setminus n \ E[mu] = \{:1.2f\}'.format(fname, len(samples), sr.mean()))$ plt.xlabel('mu') Text(0.5, 0, 'mu') Out[71]: 1.daphne | HMC 72000 total steps E[mu]=7.25 20000 15000 Frequency 10000 5000 0 11 7 mu In [72]: "HMC: posterior mean of mu  $\{:1.3f\}$  | variance  $\{:1.3e\}$ ".format(sr.mean(),sr.var()) 'HMC: posterior mean of mu 7.249 | variance 8.324e-01' In [73]: pd.Series(samples).plot() plt.xlabel('Iteration') plt.ylabel('mu') plt.title('{} | HMC \n Sample trace'.format(fname)) Text(0.5, 1.0, '1.daphne | HMC \n Sample trace') Out[73]: 1.daphne | HMC Sample trace 12 10 2 6 20000 30000 40000 50000 0 10000 60000 Iteration In [74]: size = len(samples whole graph) jll = np.zeros(size) for idx in range(size): jll[idx] = compute\_log\_joint\_prob(samples\_whole\_graph[idx],Y,P) In [75]: pd.Series(jll).plot() plt.xlabel('Iteration (t)') plt.ylabel(r' $\$-\log p(X=x_t,Y=y_t)\$'$ ) plt.title('{} | HMC \n Joint density'.format(fname)) Text(0.5, 1.0, '1.daphne | HMC \n Joint density') Out[75]: 1.daphne | HMC Joint density -10.0-12.5 $-\log p(X = x_t, Y = y_t)$ -15.0-17.5-20.0-22.5-25.0

> -27.5 -30.0

10000 20000 30000 40000

Iteration (t)

50000 60000 70000

In [1]:

import torch

import numpy as np
import os, json