

```
In [1]: import torch
import numpy as np
import os, json
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import importlib

from evaluation_based_sampling import evaluate, evaluate_program
from daphne import daphne

from graph_based_sampling import sample_from_joint
```

Problem 2

10k samples in 1.59s implies 384k samples

```
In [2]: from load_helper import ast_helper, graph_helper
```

Importance sampling

```
In [3]: import parse
import importance_sampling
import importlib
importlib.reload(parse)
```

```
Out[3]: <module 'parse' from '/Users/gw/repos/prob_prog/hw/hw3/parse.py'>
```

```
In [52]: fname = '2.daphne'
ast = ast_helper(fname)
```

```
In [53]: %%time
num_samples=384000
samples, sigmas = parse.take_samples(num_samples,ast=ast)
```

CPU times: user 10min 28s, sys: 918 ms, total: 10min 29s
Wall time: 10min 29s

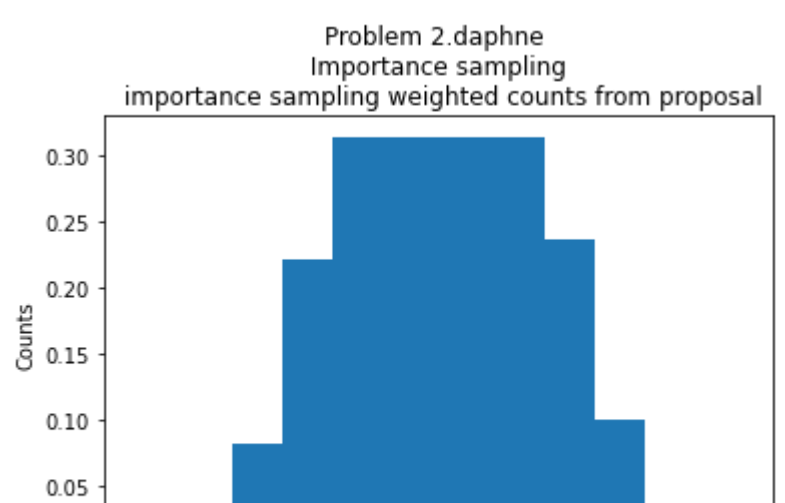
```
In [54]: samples = np.array([sample.tolist() for sample in samples])
```

```
In [55]: posterior_mean, probs = importance_sampling.weighted_average(samples,sigmas,reshape_probs=(-1,1),axis=0)
posterior_mean
```

```
Out[55]: array([ 2.15895652, -0.53834023])
```

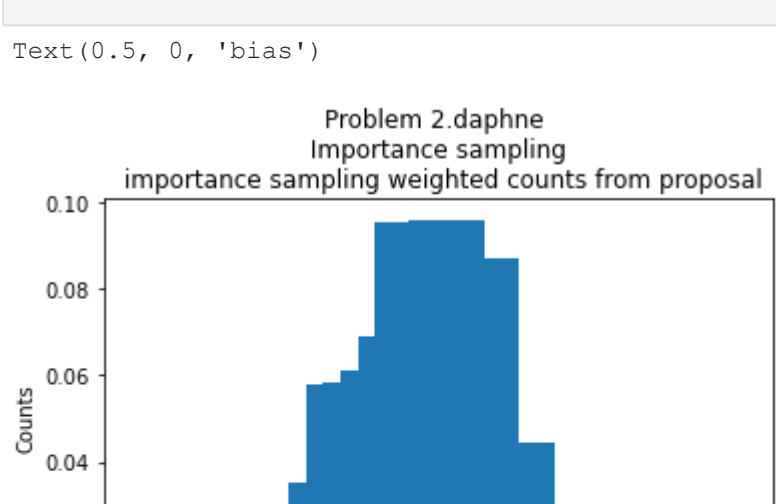
```
In [106... counts_bins = np.histogram(samples[:,0], weights=probs, bins=500)
counts, bins = counts_bins[0], counts_bins[1]
idx = (counts > counts.max()*0.005)
plt.bar(bins[1:][idx],counts[idx])
plt.title('Problem {} \n Importance sampling \n importance sampling weighted counts from proposal'.format(fname))
plt.ylabel('Counts')
plt.xlabel('slope')
```

```
Out[106... Text(0.5, 0, 'slope')
```



```
In [104... counts_bins = np.histogram(samples[:,1], weights=probs, bins=500)
counts, bins = counts_bins[0], counts_bins[1]
idx = (counts > counts.max()*0.005)
plt.bar(bins[1:][idx],counts[idx])
plt.title('Problem {} \n Importance sampling \n importance sampling weighted counts from proposal'.format(fname))
plt.ylabel('Counts')
plt.xlabel('bias')
```

```
Out[104... Text(0.5, 0, 'bias')
```



```
In [58]: expectation_samples_2, probs = importance_sampling.weighted_average(samples**2,sigmas,reshape_probs=(-1,1),axis=0)
posterior_variance = expectation_samples_2 - posterior_mean**2
posterior_variance
```

```
Out[58]: array([0.05376331, 0.79199928])
```

```
In [59]: expectation_samplex_sampley, probs = importance_sampling.weighted_average(samples[:,0]*samples[:,1],sigmas)
covariance = expectation_samplex_sampley - posterior_mean[0]*posterior_mean[1]
covariance
```

```
Out[59]: -0.18463132614140898
```

```
In [60]: for result in [
    "() Importance sampling: posterior mean slope {:.13f} | variance slope {:.13e}".format(fname,posterior_mean[0],posterior_variance[0]),
    "() Importance sampling: posterior mean bias {:.13f} | variance bias {:.13e}".format(fname,posterior_mean[1],posterior_variance[1]),
    "() Importance sampling: posterior covariance of slope and bias variance bias {:.13e}".format(fname,covariance),
]:
    print(result)
```

2.daphne Importance sampling: posterior mean slope 2.159 | variance slope 5.376e-02
2.daphne Importance sampling: posterior mean bias -0.538 | variance bias 7.920e-01
2.daphne Importance sampling: posterior covariance of slope and bias variance bias -1.846e-01

Numpy contains it's own method for computing this, and we can check it agrees with our results (where things are spelt out a bit more for learning purposes).

```
In [61]: np.cov(samples.T,aweights=probs,ddof=0)
```

```
Out[61]: array([[ 0.05376331, -0.18463133],
                [-0.18463133, 0.79199928]])
```

MH Gibbs

5k samples in 21.3s implies 140k samples in 10 min

```
In [12]: import mh_gibbs
from hmc import hmc_wrapper, compute_log_joint_prob
importlib.reload(mh_gibbs)
```

```
Out[12]: <module 'mh_gibbs' from '/Users/gw/repos/prob_prog/hw/hw3/mh_gibbs.py'>
```

```
In [13]: fname = '2.daphne'
graph = graph_helper(fname)
graph
```

```
Out[13]: [{'observe-data': {'fn',
  ['.', 'data', 'slope', 'bias'],
  ['let',
  ['xn', ['first', 'data']],
  ['let',
  ['yn', ['second', 'data']],
  ['let',
  ['zn', ['+', ['*', 'slope', 'xn'], 'bias']],
  ['let',
  ['dontcare9', ['observe', ['normal', 'zn', 1.0], 'yn']],
  ['rest', ['rest', 'data']]]]]],
{'V': {'observe3',
'observe6',
'observe4',
'observe7',
'sample2',
'sample1',
'observe8',
'observe5'},
'A': {'sample2': ['observe3',
'observe6',
'observe4',
'observe7',
'observe8',
'observe5'],
'sample1': ['observe3',
'observe6',
'observe4',
'observe7',
'observe8',
'observe5']}},
'P': {'sample1': ['sample*', ['normal', 0.0, 10.0]],
'sample2': ['sample*', ['normal', 0.0, 10.0]],
'observe3': ['observe*',
['normal', ['+', ['*', 'sample1', 1.0], 'sample2'], 1.0],
2.1],
'observe4': ['observe*',
['normal', ['+', ['*', 'sample1', 2.0], 'sample2'], 1.0],
3.9],
'observe5': ['observe*',
['normal', ['+', ['*', 'sample1', 3.0], 'sample2'], 1.0],
5.3],
'observe6': ['observe*',
['normal', ['+', ['*', 'sample1', 4.0], 'sample2'], 1.0],
7.7],
'observe7': ['observe*',
['normal', ['+', ['*', 'sample1', 5.0], 'sample2'], 1.0],
10.2],
'observe8': ['observe*',
['normal', ['+', ['*', 'sample1', 6.0], 'sample2'], 1.0],
12.9]},
'Y': {'observe3': 2.1,
'observe4': 3.9,
'observe5': 5.3,
'observe6': 7.7,
'observe7': 10.2,
'observe8': 12.9}},
['vector', 'sample1', 'sample2']}]
```

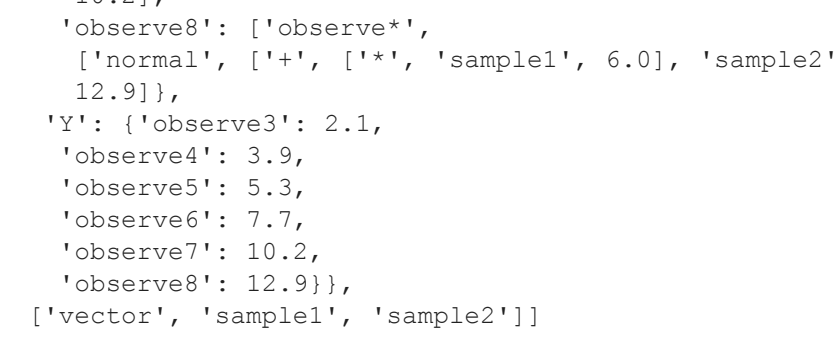
```
In [14]: %%time
num_steps=140000
return_list, samples_whole_graph = mh_gibbs.mh_gibbs_wrapper(graph,num_steps)
```

CPU times: user 10min 14s, sys: 2.36 s, total: 10min 16s
Wall time: 10min 20s

```
In [15]: samples = np.array([sample.tolist() for sample in return_list])
```

```
In [16]: burn_in = int(0.01*num_steps)
df = pd.DataFrame(samples[burn_in:])
df.columns = ['slope','bias']
df['iteration'] = df.index
tall = pd.melt(df, id_vars='iteration')
g = sns.FacetGrid(tall, col="variable")
g.map(sns.histplot, "value")

plt.suptitle('MH Gibbs | {}'.format(fname))
plt.subplots_adjust(top=0.8)
```



```
In [17]: posterior_mean = samples[burn_in:].mean(0)
cov_matrix = np.cov(samples[burn_in:].T,ddof=0)
posterior_variance = samples[burn_in:].var(0)
covariance = cov_matrix[0,1]
assert np.isclose(cov_matrix[0,0],posterior_variance[0])
assert np.isclose(cov_matrix[1,1],posterior_variance[1])
```

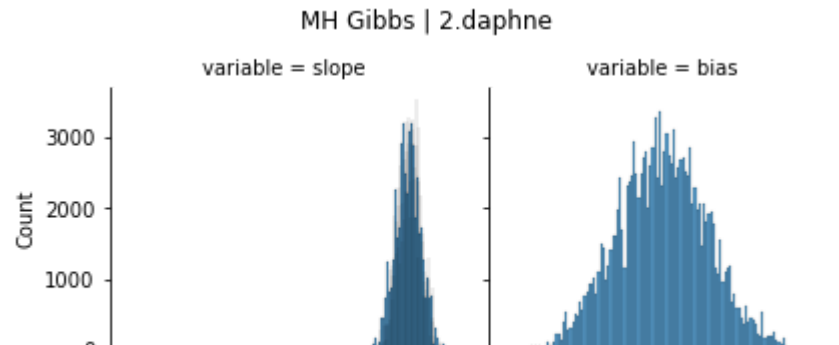
```
In [18]: for result in [
    "() MH Gibbs: posterior mean slope {:.13f} | variance slope {:.13e}".format(fname,posterior_mean[0],posterior_variance[0]),
    "() MH Gibbs: posterior mean bias {:.13f} | variance bias {:.13e}".format(fname,posterior_mean[1],posterior_variance[1]),
    "() MH Gibbs: posterior covariance of slope and bias variance bias {:.13e}".format(fname,covariance),
]:
    print(result)
```

2.daphne MH Gibbs: posterior mean slope 2.149 | variance slope 5.918e-02
2.daphne MH Gibbs: posterior mean bias -0.515 | variance bias 8.965e-01
2.daphne MH Gibbs: posterior covariance of slope and bias variance bias -2.070e-01

```
In [19]: g = sns.FacetGrid(tall, col="variable")
g.map(plt.plot, "iteration", "value")

plt.suptitle('MH Gibbs | {}'.format(fname))
plt.subplots_adjust(top=0.75)
plt.suptitle('{} | MH Gibbs \n Sample trace'.format(fname))
```

```
Out[19]: Text(0.5, 0.98, '2.daphne | MH Gibbs \n Sample trace')
```

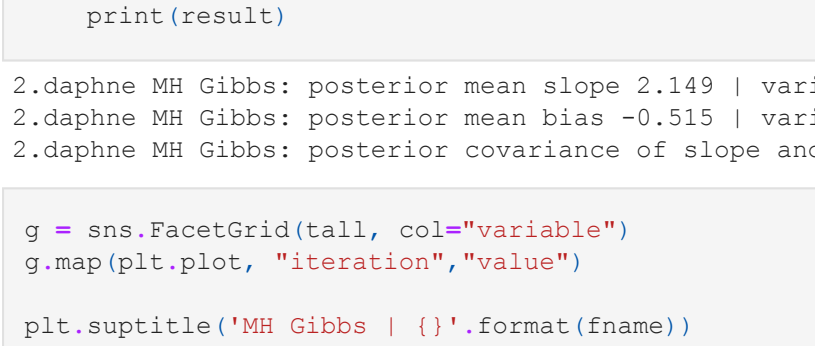


```
In [20]: G = graph[1]
Y = G['Y']
Y = [key:evaluate([value])[0] for key,value in Y.items()]
P = G['P']
```

```
In [21]: size = len(samples_whole_graph)
jll = np.zeros(size)
for idx in range(size):
    jll[idx] = compute_log_joint_prob(samples_whole_graph[idx],Y,P)
```

```
In [22]: pd.Series(jll).plot()
plt.xlabel('Iteration (t)')
plt.ylabel(r'$-\log p(X=x_t,Y=y_t)$')
plt.title('{} | MH Gibbs \n Joint density'.format(fname))
```

```
Out[22]: Text(0.5, 1.0, '2.daphne | MH Gibbs \n Joint density')
```



HMC

4.2s/ 200 samples implies 28.5k samples in 10 min 1k samples in 21.3 s implies 28k samples

```
In [143... fname = '2.daphne'
graph = '2.daphne'
```

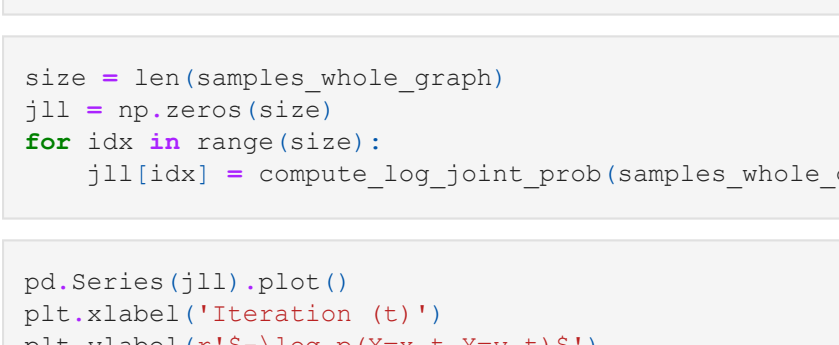
```
In [144... import hmc
importlib.reload(hmc)
from hmc import hmc_wrapper
```

```
In [ ]: num_samples=28000
return_list, samples_whole_graph = hmc_wrapper(graph,num_samples,T=20,epsilon=0.01)
```

```
In [154... samples = np.array([sample.tolist() for sample in return_list])
```

```
In [155... burn_in = int(0.01*num_samples)
df = pd.DataFrame(samples[burn_in:])
df.columns = ['slope','bias']
df['iteration'] = df.index
tall = pd.melt(df, id_vars='iteration')
g = sns.FacetGrid(tall, col="variable")
g.map(sns.histplot, "value")

plt.suptitle('HMC | {}'.format(fname))
plt.subplots_adjust(top=0.8)
```



```
In [156... posterior_mean = samples[burn_in:].mean(0)
cov_matrix = np.cov(samples[burn_in:].T,ddof=0)
posterior_variance = samples[burn_in:].var(0)
covariance = cov_matrix[0,1]
assert np.isclose(cov_matrix[0,0],posterior_variance[0])
assert np.isclose(cov_matrix[1,1],posterior_variance[1])
```

```
In [157... for result in [
    "() HMC: posterior mean slope {:.13f} | variance slope {:.13e}".format(fname,posterior_mean[0],posterior_variance[0]),
    "() HMC: posterior mean bias {:.13f} | variance bias {:.13e}".format(fname,posterior_mean[1],posterior_variance[1]),
    "() HMC: posterior covariance of slope and bias variance bias {:.13e}".format(fname,covariance),
]:
    print(result)
```

2.daphne HMC: posterior mean slope 2.161 | variance slope 5.652e-02
2.daphne HMC: posterior mean bias -0.556 | variance bias 8.609e-01
2.daphne HMC: posterior covariance of slope and bias variance bias -1.984e-01

```
In [158... g = sns.FacetGrid(tall, col="variable")
g.map(plt.plot, "iteration", "value")

plt.suptitle('HMC | {}'.format(fname))
plt.subplots_adjust(top=0.75)
plt.suptitle('{} | HMC \n Sample trace'.format(fname))
```

```
Out[158... Text(0.5, 0.98, '2.daphne | HMC \n Sample trace')
```



```
In [159... G = graph[1]
Y = G['Y']
Y = [key:evaluate([value])[0] for key,value in Y.items()]
P = G['P']
```

```
In [160... size = len(samples_whole_graph)
jll = np.zeros(size)
for idx in range(size):
    jll[idx] = compute_log_joint_prob(samples_whole_graph[idx],Y,P)
```

```
In [161... pd.Series(jll).plot()
plt.xlabel('Iteration (t)')
plt.ylabel(r'$-\log p(X=x_t,Y=y_t)$')
plt.title('{} | HMC \n Joint density'.format(fname))
```

```
Out[161... Text(0.5, 1.0, '2.daphne | HMC \n Joint density')
```

