

# Introduction to Data Structures

Kurt Schmidt

Dept. of Computer Science, Drexel University

September 13, 2016

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

# Intro

# Algorithms and Data Structures

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

## Objectives:

- Review the fundamental algorithms and data structures that are commonly used in programs
- To see how to use and implement these algorithms and data structures in different languages and to see what language and library support exists for them

# Topics

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors  
Resizing, C

Lists

Searching &  
Sorting  
Binary Search  
Quick Sort

Dictionary  
BST  
Hash Table

- Arrays and Vectors
- Lists
- Linear/Binary Search
- Quicksort
- Dictionaries

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

**Vectors**

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

# Vectors

# Vectors (Arrays)

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

- Sequence of items
- Indexable
  - Same time to access any element
- (Conceptually) contiguous chunks of memory
- In CS, *array* and *vector* are interchangeable enough

0	1	2	3	4	5	6
α	β	γ	δ	ε	ζ	η

# Time, Operations on Vectors

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- Access: constant time ( $\Theta(1)$ )
- Searching:
  - Sorted array –  $\Theta(\log n)$
  - Unsorted –  $\Theta(n)$
- Inserting, removing items:
  - Unordered –  $\Theta(1)$ 
    - Add to end
    - Replace deleted item w/last guy
  - Ordered –  $\Theta(n)$ 
    - Need to make (or fill in) a hole
    - Move  $n/2$  items, on average, to maintain relative order

# Resizing Arrays

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary  
BST

Hash Table

- Many languages have arrays which manage themselves
  - Awk, Python<sup>1</sup>, Perl<sup>1</sup>, etc.
- Other languages have smart arrays in their library:
  - C++ vector in the STL
  - Java ArrayList
- This doesn't mean the operations are free
  - What goes on underneath the hood may be important
- We shall create our own machinery in C

---

<sup>1</sup>Called *lists*



# Some C Memory Management Functions

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

`void* malloc(int n)` allocates  $n$  contiguous bytes from heap, returns address of first byte (NULL upon failure)

`void free(void *p)` returns to the heap memory addressed by  $p$ . Does *nothing* to  $p$  itself

`void* memmove(void* d, void* s, size_t n)` moves  $n$  bytes from  $s$  to (possibly overlapping) region starting at  $d$

`void* memcpy(void* d, void* s, size_t n)` copies  $n$  bytes from  $s$  to (non-overlapping) region starting at  $d$

`int sizeof()` actually an operator, returns size, in bytes, of given object or type

`void* realloc(void* src, int n)` attempts to resize array in place, or a bigger section elsewhere, copies contents for you. Returns pointer to array

# Growing Arrays in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
enum { INIT_SIZE=1, GROW_FACTOR=2 };
int curr_size = INIT_SIZE;
int nr_elems = 0; /* # of useful elements */
int *a = (int*)malloc( INIT_SIZE * sizeof( int ));
... /* some stuff here */
/* attempt to insert 24 */
if( nr_elems >= curr_size ) { /* need to grow */
    int *t = realloc( a, curr_size*GROW_FACTOR*sizeof( int ))
    if( t != NULL ) { /* success! */
        curr_size *= GROW_FACTOR;
        a = t;
        a[nr_elems++] = 24;
    }
    else
        /* FAILURE! */
}
```

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

**Lists**

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

# Lists

# Lists

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

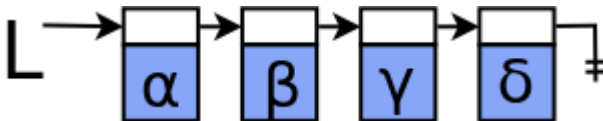
Binary Search  
Quick Sort

Dictionary

BST

Hash Table

- A sequence of elements
- *Not* indexable (immediately)
  - To access 5<sup>th</sup> element, must visit the preceding 4
- Space is allocated for each new element
- Consecutive elements are linked together with a pointer
- Middle can be modified in constant time



# Lists as Ordered Pairs

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- For languages w/out explicit pointers, such as Bash, Maple, Python, and Java, it might be helpful to consider a list as an ordered pair

- 1 The item (payload)

- 2 The rest of the list

$$(\alpha, (\beta, (\gamma, (\delta, ())))))$$

- Where  $()$  is the empty list
- We might use a class
- Or, simply, nested arrays, of size 2 (or, empty)
  - This is a very LISP notion

# Time, Operations on Lists

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors  
Resizing, C

**Lists**

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

- Access (same as searching) – linear time ( $\Theta(n)$ )
- Modifying anywhere – constant time ( $\Theta(1)$ )
- Inserting
  - At front –  $\Theta(1)$
  - Append –  $\Theta(n)$ , unless pointer to last element kept

# Lists in Python

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- Python's `list` is really an array
  - Really? How might we tell?
  - In any case, elements are accessed in constant time
- We'll use Python's `list` to hold our duples
  - We'll call them *cells*, or *nodes*
- Let the empty `list`, `[]`, be an empty list
- Remember, *everything* in Python is a reference (pointer)

# “Linked” Lists in Python

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

**Lists**

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
L = []  
    # add 24 to front  
L = [ 24, L ]  
print L  
    # add 3 to the front  
L = [ 3, L ]  
print L
```

Would output:

```
[ 24, [] ]  
[ 3, [ 24, [] ] ]
```



# Append to end of List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
def append( L, e ) :  
    '''Append item e to end of L  
    Note, reference L doesn't change'''  
  
    t = L # start at beginning  
  
    while t != [] :  
        t = t[1] # move to next cell  
  
    # We have our hands on the last cell (empty list)  
  
    # Make it a pair, w/a new end-of-list  
    t.extend( [ e, [] ] )
```

# Searching a List in Python

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
def search( L, t ) :  
    '''Return cell of L that contains t,  
    None if not found'''  
  
    while L != [] :  
        if L[0] == t :  
            return L  
        L = L[1] # move to next cell  
  
    return None # didn't find it
```

# Map – Apply Function to a List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

**Lists**

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
def apply( L, fn ) :  
  
    while L != [] :  
        fn( l )  
        L = L[1] # move to next cell
```

`fn` is any function that takes a single cell, modifies it. E.g.:

```
def square( c ) :  
  
    c[0] *= c[0]
```

# Examples of Apply

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

Given:

```
L = [ 1, [ 2, [ 3, [] ]]]
```

Print the list:

```
def printCell( c ) :  
    print cell[0]  
  
apply( L, printCell )
```

```
1 2 3
```

```
apply( L, square )  
apply( L, printCell )
```

```
1 4 9
```

# Lists in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST  
Hash Table

```
typedef struct sNode sNode;

struct sNode { /* a node (cell) in a singly-link list */
    int data; /* the payload */
    sNode* next;
};

/* Wrap an item in a node (cell) */
sNode* newNode( int d ) {
    sNode *newp;
    newp = (sNode*) malloc( sizeof( sNode ) );
    if( newp != NULL ) {
        newp->data = d;
        newp->next = NULL;
    }
    return newp;
}

typedef sNode* List ;
```

# Insert at Front of C List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* addfront: add newp to front of listp *  
 *   return ptr to new list           */  
sNode* addfront( sNode *listp, sNode *newp )  
{  
    newp->next=listp;  
    return newp;  
}  
  
list = addfront( list, newitem( 13 ));  
list = addfront( list, newitem( 12 ));  
list = addfront( list, newitem( 5  ));
```

List would be ( 5 12 13 )

# Append to End of C List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

**Lists**

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* append: add newp to end of listp *  
 * return ptr to new list */  
sNode* append( sNode* listp, sNode* newp )  
{  
    sNode *p;  
    if( listp == NULL )  
        return newp;  
    for( p=listp; p->next!=NULL; p=p->next )  
        ; /* Find last node */  
    p->next = newp;  
    return listp;  
}  
  
list = append( list, newitem( 42 ) ) ;
```

List would be ( 5 12 13 42 )

# Search a List in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* lookup: linear search for t in listp */
/* return ptr to node containing t, or NULL */
sNode* lookup( sNode *listp, int t )
{
    for( ; listp != NULL; listp = listp->next )
        if( listp->data == t )
            return listp;

    return NULL; /* no match */
}
```



# Map/Apply on List in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* apply: execute fn for each element of listp */  
void apply( sNode *listp,  
            void (*fn)(sNode*, void* ), void* arg )  
{  
    for ( ; listp != NULL; listp = listp->next )  
        (*fn)( listp, arg ); /* call the function */  
}
```

- The 2<sup>nd</sup> argument is a function pointer
  - void return type
  - It takes 2 arguments
    - 1 List
    - 2 Generic pointer, to be used by function, as needed

# Use Map to Square Elements in List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

**Lists**

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
void squareVal( sNode *p, void *arg )
{
    /* note, arg is unused */

    p->data *= p->data ;
}

apply( list, squareVal, NULL )
```

# Use Map to Print

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* printVal: print value, using arg as format string */  
  
void printVal( sNode *p, void *arg )  
{  
    char* fmt = (char*) arg ;  
    printf( fmt, p->data ) ;  
}  
  
apply( list, prntVal, "%d" )
```

# Use Map to Compute Size

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST  
Hash Table

```
/* incCounter: increment counter in arg */  
void incCounter( sNode *p, void *arg )  
{  
    /* NOTE: p is unused. We were called, there's a node. */  
  
    int* ip = (int*) arg ;  
    (*ip)++ ;  
}  
  
int size = 0 ;  
apply( list, incCounter, &n )  
printf( "%d elements in list\n", n ) ;
```

# Freeing Nodes in a List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* freeall: free all elements of listp */  
void freeall( sNode *listp )  
{  
    sNode *t;  
    for ( ; listp != NULL; listp = t ) {  
        t = listp->next;  
        free(listp)  
    }  
}
```

What's the problem with the following?

```
for ( ; listp != NULL; listp = listp->next )  
    free( listp );
```

# Removing Element from List

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* delitem: delete first t from listp */
sNode *delitem( sNode *listp, int t ) {
    sNode *p, *prev = NULL;
    for( p=listp; p!=NULL; p=p->next ) {
        if( p->data == t ) {
            if( prev == NULL ) /* front of list */
                listp = p->next;
            else
                prev->next = p->next;
            free( p );
            break;
        }
        prev = p;
    }
    return listp;
}
```

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

# Searching & Sorting

# Linear Search

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- Exhaustively examine each element
- Examine each element, until you find what you seek, or you've examined every element
  - Note that order of examination doesn't matter
- The *only* search for a linked-list
- Need  $\Theta(n)$  comparisons, worst and average



# Linear Search on Array in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* return index of first find, -1 otherwise */
int linSearch( int *a, int size, int t )
{
    int i ;
    for( i=0; i<size; ++i )
        if( a[i] == t )
            return i ;

    return i ;
}

int test[ 12 ] = { ... } ;
int l = linSearch( test, 12, 17 ) ;
```

# Binary Search

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- Only works on *sorted* collections
- Only efficient on collections with random (direct) access (vectors)
  - Find it?
- Start in the middle:
  - Find it?
  - Less than? Look in lower  $\frac{1}{2}$
  - Greater than? Look in upper  $\frac{1}{2}$
- Cut search space in  $\frac{1}{2}$
- Need  $\Theta(\log n)$  time, worst and avg.

# Binary Search in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* Search integer array
   Return index of target, or -1 */
int binSearch( int* arr, int size, int target )
{
    int low = 0,
        high = size-1 ;
    int mid ;

    while( low <= high )
    {
        mid = (low+high) / 2 ;
        if( arr[mid] == target )
            return mid ;
        if( target < arr[mid] )
            high = mid-1 ;
        else
            low = mid+1 ;
    }

    return( -1 ) ;
}
```

# Quick Sort

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- Choose one element of the array (the *pivot*)
- Partition the other elements into two groups:
  - those less than the pivot
  - those greater than or equal to the pivot
- Pivot is now in the right place
- Recursively sort each (strictly smaller) group
- Can be done in place

# Quick Sort – Run Time

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- Each partition requires  $\Theta(n)$  comparisons, moves
- Best case –  $\Theta(n \log n)$ 
  - Each partition splits collection in half
  - Can do that about  $n$  times
- Worst case –  $\Theta(n^2)$ 
  - Each partition gets pivot in place
  - Leaves  $n - 1$  elements in one partition to sort
  - Looks like a Selection Sort
- On random data, average run time is  $\Theta(n \log n)$

# Quick Sort – Description

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

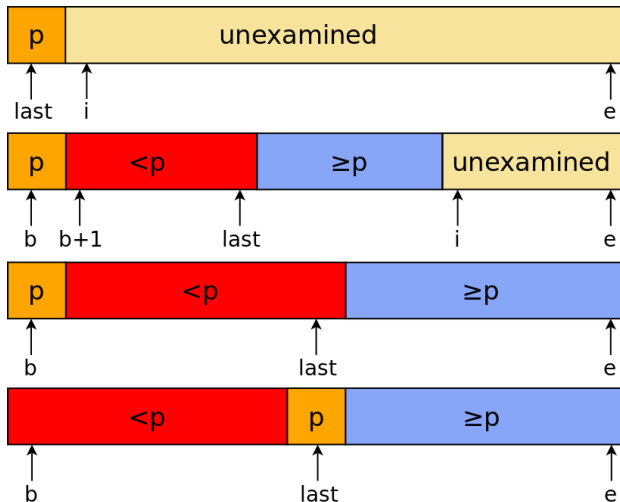
Binary Search

Quick Sort

Dictionary

BST

Hash Table



# Recursive Quicksort in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* quicksort: sort v[0]..v[n-1] into increasing order */  
void quicksort( int v [], int n )  
{  
    if( n <= 1 )      /* nothing to do */  
        return ;  
  
    int piv = partition( v, n ) ;  
  
    quicksort( v, piv ) ; /* recursively sort each part. */  
    quicksort( v+piv+1, n-piv-1 ) ;  
}
```

# Quicksort – Partition

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* partition, return index of pivot */
int partition( int *v, int n )
{
    int i, last=0 ;
    swap( v,0,rand() % n ); /* move pivot element to v[0] */
    last = 0;
    for ( i = 1; i < n; i++ ) /* partition */
        if ( v[i] < v[0] )
            swap( v, ++last, i );
    swap( v, 0, last ); /* restore pivot */

    return last ;
}
```



# Library Sorts for Some Languages

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

C `qsort` (in `stdlib.h`)  
C++ `STL sort` (in `algorithm`)  
Java `java.util.Collections.sort`  
Perl `sort`  
Python `list.sort`, `sorted`

# qsort – C Standard Library

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
qsort( void* a, int n, int s,  
       int (*cmp)(void *a, void *b) ) ;
```

- Sorts the first  $n$  elements of array  $a$
- Each element is  $s$  bytes
- $cmp$  is a function you must provide
  - Compares 2 single elements,  $*a$  and  $*b$ 
    - $qsort$  must pass void pointers, since it doesn't know the type
    - $cmp$  does, since you provide it
- Returns integer  $-1$  if  $a < b$ ,  $0$  if  $a == b$ , and  $1$  if  $a > b$

# qsort Example for Integers

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* icmp: integer compare of *p1 and *p2 */
int icmp( const void *p1, const void *p2 )
{
    const int v1 = *((const int*) p1) ;
    const int v2 = *((const int*) p2) ;
    if( v1 < v2 )
        return -1 ;
    else if( v1 == v2 )
        return 0 ;
    else
        return 1 ;
}

int arr[N] ;
...
qsort( arr, N, sizeof(arr[0]), icmp ) ;
```

# qsort Example for Strings

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

```
/* scmp: string compare of *p1 and *p2. p1 is a ptr to a
 * string, ptr to a char*, so is a ptr to a ptr, or a char**
 */
int scmp( const void *p1, const void *p2 )
{
    const char *v1, *v2 ;

    v1 = *((const char**) p1) ;
    v2 = *((const char**) p2) ;

    return strcmp( v1, v2 ) ;
}

char *str[N];
...
qsort(str, N, sizeof(str[0]), scmp);
```

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

# Dictionary

# Dictionary (Map)

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

- A *set* of (key, value) pairs
- Allows us to associate satellite data w/a key
- E.g., phone book (sorta), student record, given an ID, an error string (given an error number)
- Keys are unique
- Operations:
  - Lookup (find)
  - Insert
  - Remove

# Times – Simple Dictionaries

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

## Unordered Vector

- Lookup –  $\Theta(n)$
- Insertion –  $\Theta(1)$  (given a find)
- Removal –  $\Theta(1)$  (given a find)

## Ordered Vector

- Lookup –  $\Theta(\log n)$
- Insertion –  $\Theta(n)$  (given a find)
- Removal –  $\Theta(n)$  (given a find)

# Some Other Dictionaries

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

## Binary Search Tree<sup>1</sup>

- Lookup –  $\Theta(\log n)$
- Insertion –  $\Theta(\log n)$
- Removal –  $\Theta(\log n)$

## Hash Table

- Lookup –  $\Theta(1)$
- Insertion –  $\Theta(1)$
- Removal –  $\Theta(1)$

---

<sup>1</sup>Balanced; random data



# Binary Search Tree

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

- A binary tree is either:
  - The empty tree, or
  - contains a key/value pair, and a left and right subtree, themselves trees
- A binary search tree (BST) has the *sibling order* property
  - The key of a node is greater than all keys in the left subtree
  - The key of a node is less than all keys in the right subtree
- Note, every subtree of a BST is a BST
- $O(\log n)$  expected search and insertion time
  - If the tree is balanced
- In-order traversal yields keys in sorted order

# BST Example

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

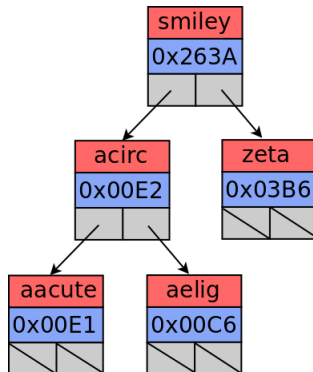
Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary  
BST

Hash Table

- In the following examples each node stores a key/value pair:
  - key – String, name of the character
  - value – Hexadecimal integer, Unicode encoding
- A reference (pointer) to each of the 2 subtrees



# BST in Python

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

- Let an empty tree be the empty list
- Use a list of size 3:
  - 1 The key/value pair (another list)
  - 2 The left subtree
  - 3 The right subtree
- The following is a tree w/one node:

```
T = [ [ 'smiley', 0x263A ], [], [] ]
```

# BST Lookup – Python

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
def lookup( T, name ) :  
    '''lookup: look up name in tree T, return the  
    cell, None if not found'''  
  
    if T == [] : # T is the empty tree  
        return None  
    if T[0][0] == name :  
        return T  
    elif name < T[0][0] : # look in left subtree  
        return lookup( T[1], name );  
    else : # look in right subtree  
        return lookup( T[2], name );
```

# BST in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

BST

Hash Table

We will use a struct to hold the key, value and pointers to the subtrees.

```
typedef struct bNode bNode;  
struct bNode {  
    char *name ;  
    int value ;  
    bNode *left ;  
    bNode *right ;  
} ;
```

# BST in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* lookup: look up name in tree treep *  
 *   Return pointer to node, NULL if not found */  
  
bNode* lookup( bNode *treep, char *name )  
{  
    int cmp;  
  
    if( treep == NULL )  
        return NULL; /* Didn't find it */  
    cmp = strcmp( name, treep->name );  
    if( cmp == 0 )  
        return treep;  
    else if( cmp < 0 )  
        return lookup( treep->left, name );  
    else  
        return lookup( treep->right, name );  
}
```

# Hash Table (Open)

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

- Provides key lookup and insertion with constant expected cost
- At the heart is a vector with  $m$  slots, where it is not usually possible to reserve a slot for each possible element
- Hash function maps key to index (should evenly distribute keys)
  - $H(k, m) \rightarrow [0, m - 1]$
  - Two keys might have the same hash value – collision
- Duplicates stored in a chain (list) – other strategies exist

# Hash Table (Open)

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search

Quick Sort

Dictionary

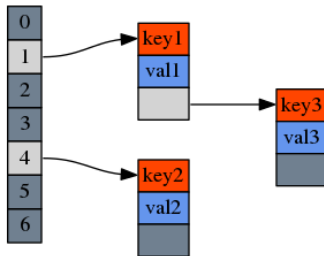
BST

Hash Table

```
typedef struct sNode sNode ;

/* An entry */
struct sNode {
    char* name ;
    int value ;
    sNode* next; /* in chain */
} ;

/* The table (array) */
sNode* symtab[NHASH] ;
```



In this example, *key1* and *key3* have the same hash value, 1



# A Simple Hash Function in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
const MULTIPLIER = 31 ;  
/* hash: compute hash value of string */  
unsigned int hash(char* str)  
{  
    unsigned int h ;  
    unsigned char *p ;  
    h = 0 ;  
  
    for( p=(unsigned char*) str; *p != '\0'; p++ )  
    {  
        h = MULTIPLIER * h + *p ;  
        h %= NHASH ;  
    }  
    return h ;  
}
```

# Hash Table Lookup/Insert in C

Introduction  
to Data  
Structures

Kurt Schmidt

Intro

Vectors

Resizing, C

Lists

Searching &  
Sorting

Binary Search  
Quick Sort

Dictionary

BST

Hash Table

```
/* lookup: find name in symtab, with optional create */
sNode* lookup( char* name, int create, int value )
{
    sNode* sym ;
    int h = hash(name) ;

    for( sym=symtab[h]; sym != NULL; sym=sym->next)
        if( strcmp( name, sym->name ) == 0 )
            return sym ;
    if( create ) {
        sym = (sNode*) malloc( sizeof( sNode )) ;
        sym->name = name ; /* assumed allocated elsewhere */
        sym->value = value ;
        sym->next = symtab[h] ; /* insert at front */
        symtab[h] = sym ;
    }
    return sym ;
}
```