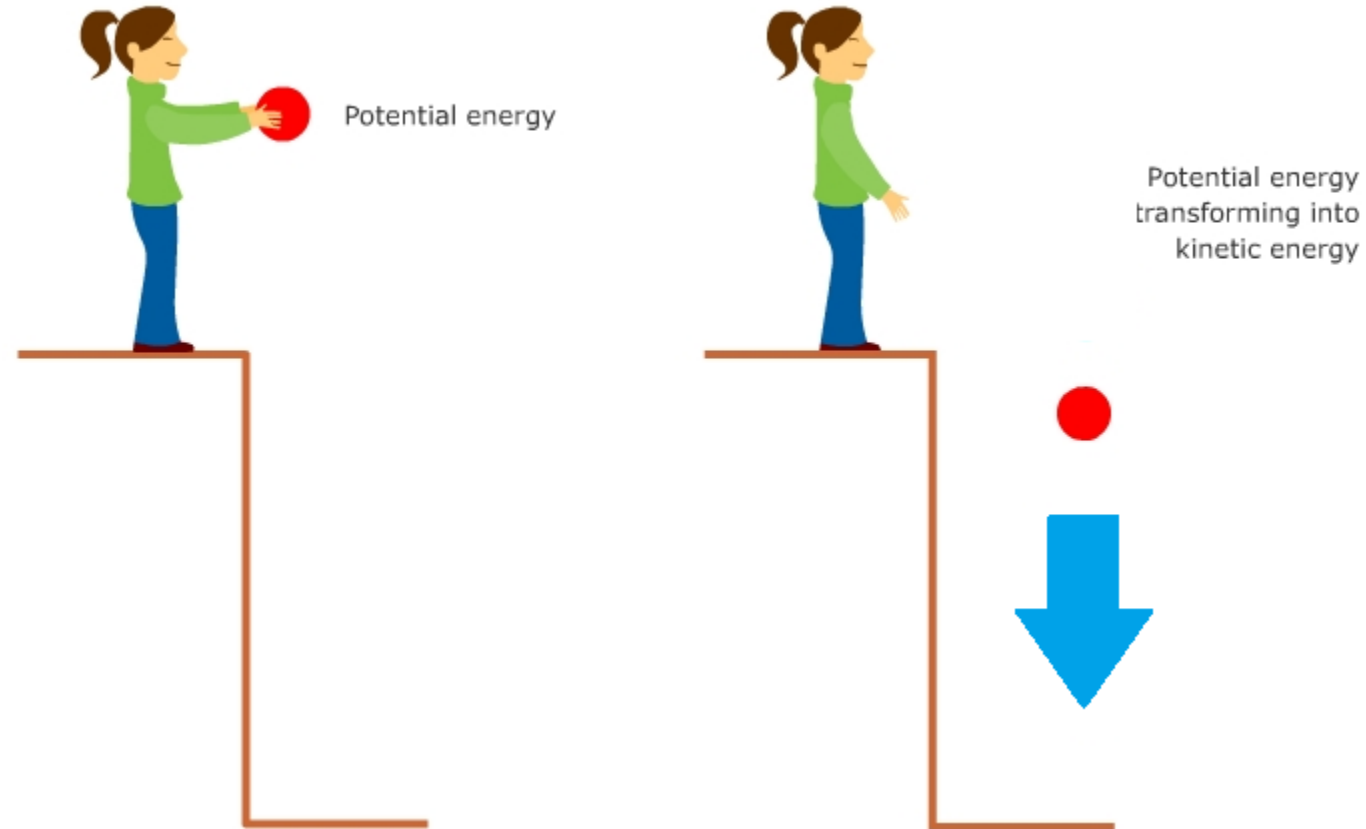


Thermodynamics of Ferroelectrics

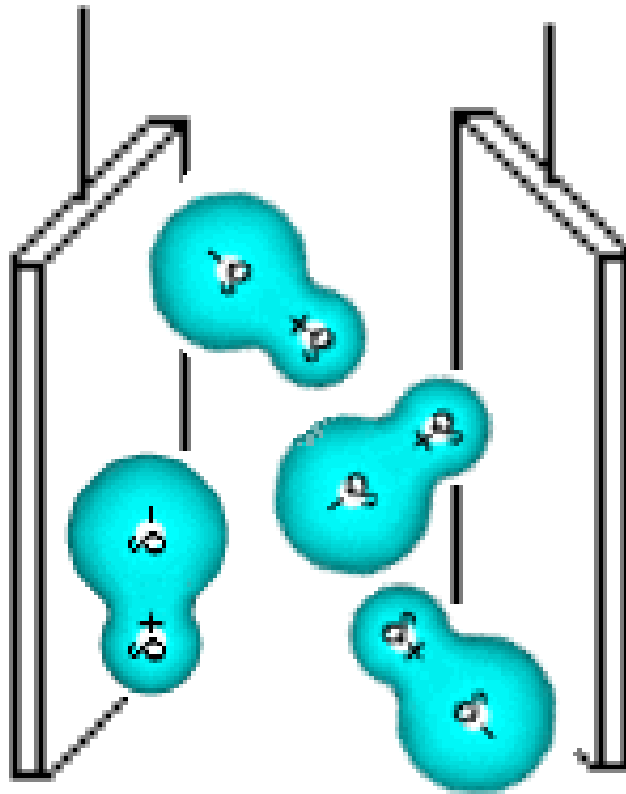
Geoffrey Xiao

Universe tends towards lower energy

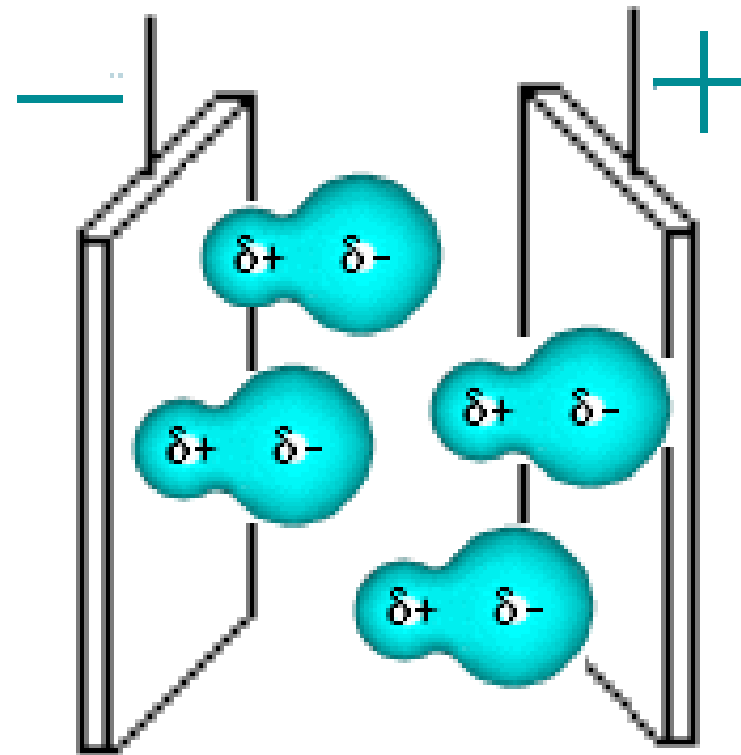


Universe tends towards lower energy

Field off

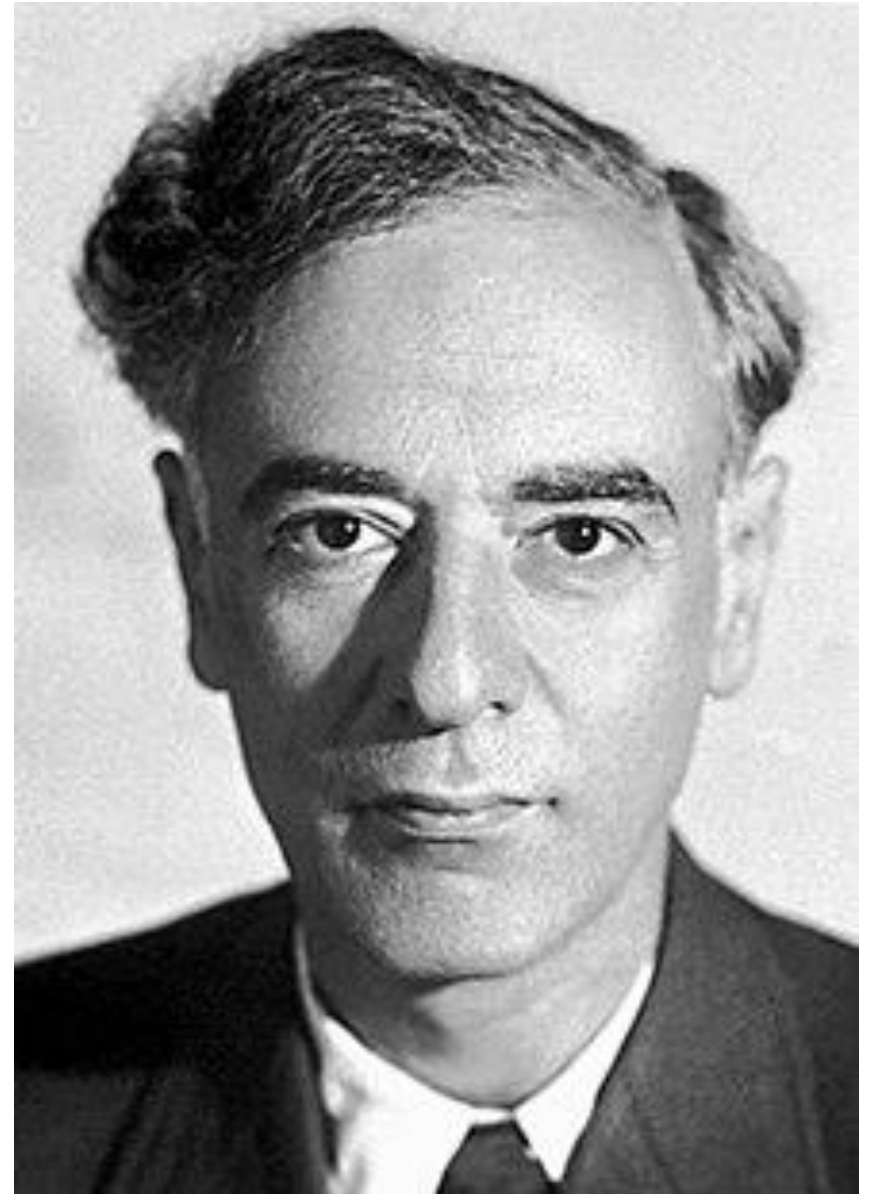


Field on



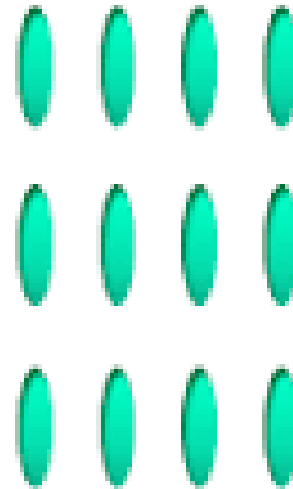
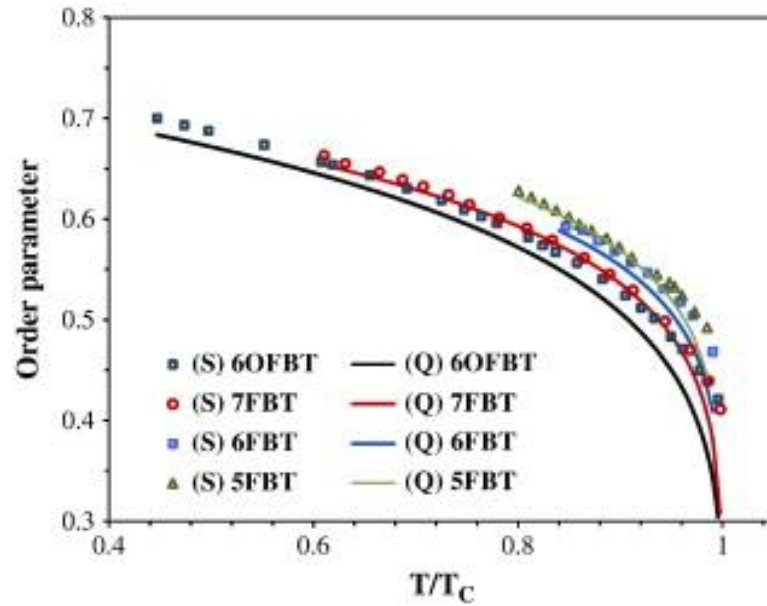
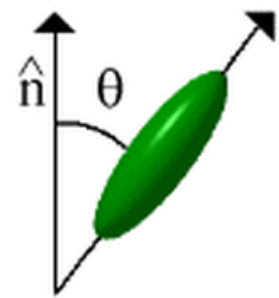
Landau Free Energy

- $F = a_0 + a_1\Psi^2 + a_2\Psi^4 + \dots$
- Ψ = Order Parameter
 - Characterize the transition
 - $\Psi = 0$ above the transition temperature
 - Polynomial order depends on symmetry



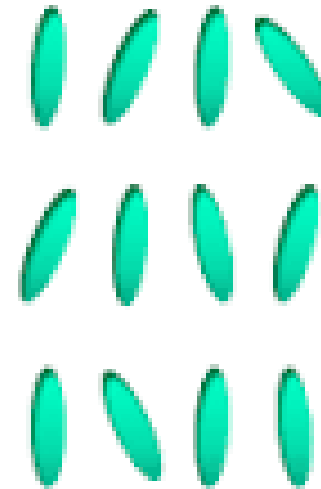
Liquid Crystals

$$\bullet \Psi = \left\langle \frac{3 \cos^2 \theta - 1}{2} \right\rangle$$

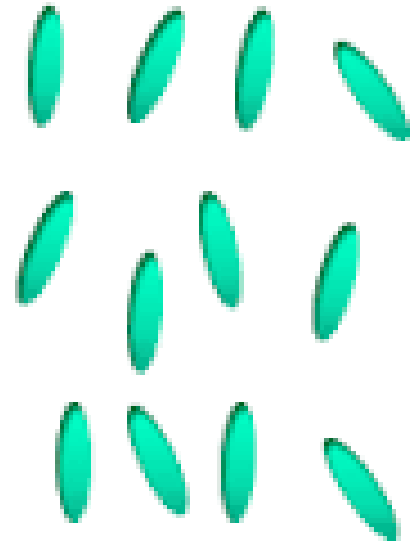


Solid

$$\Psi \neq 0$$



Liquid Crystal

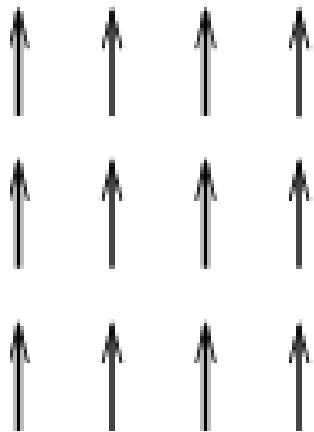


Liquid

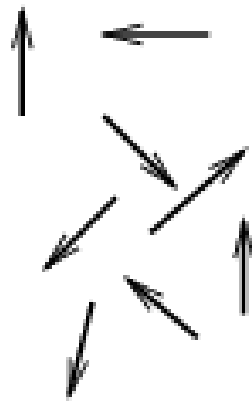
$$\Psi = 0$$

Ferromagnet

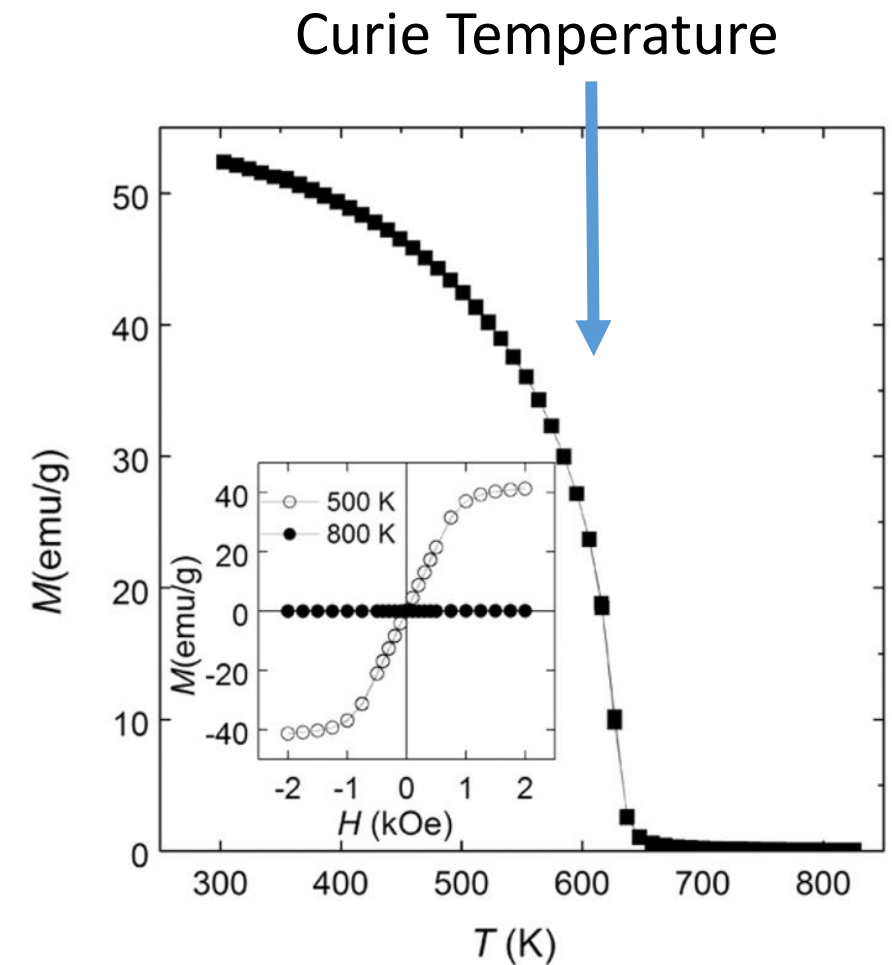
- Permanent magnet
- $\Psi = \|\vec{M}\|$
- \vec{M} = magnetization vector



Ferromagnet
 $\Psi \neq 0$

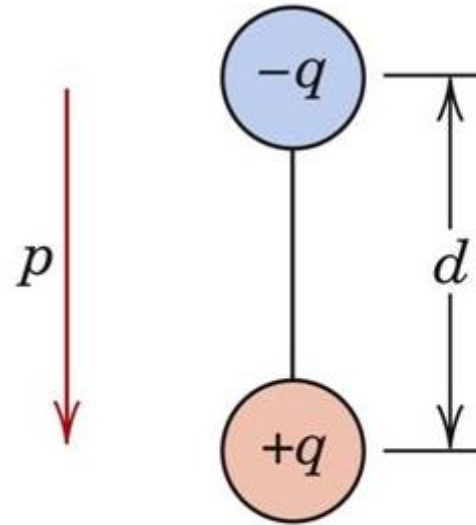


Paramagnet
 $\Psi = 0$

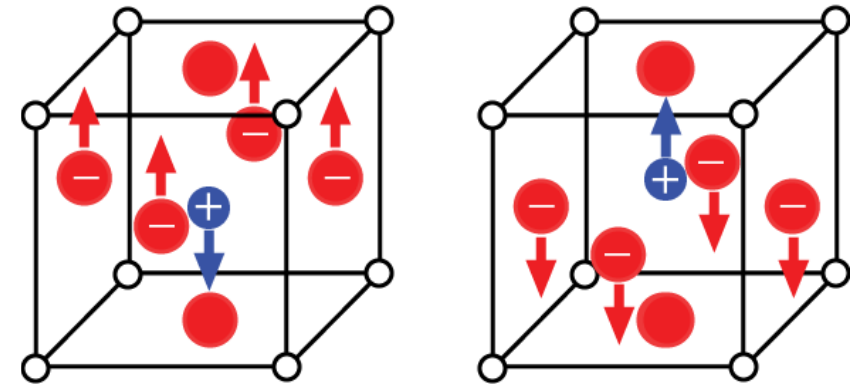


Ferroelectric

- Permanent electric dipole
- $\Psi = \|\vec{P}\|$
- \vec{P} = Polarization vector

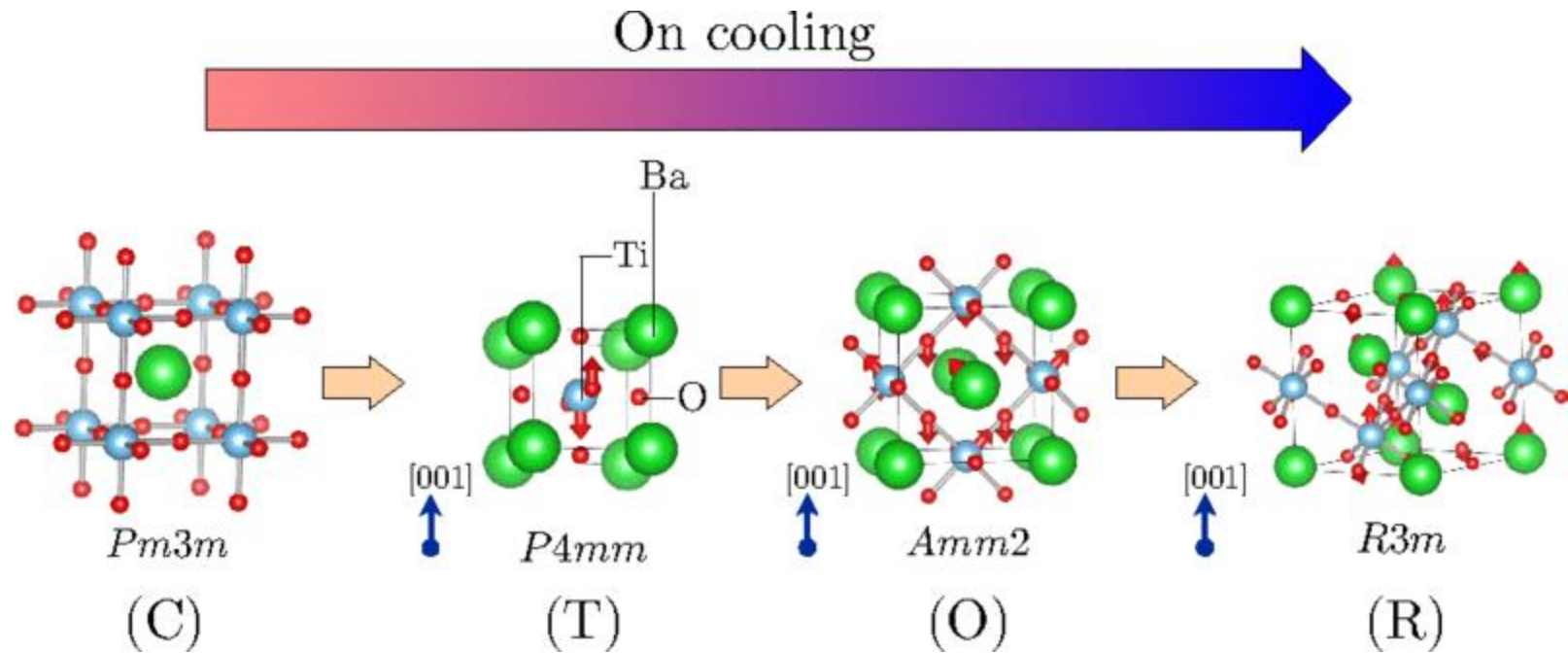
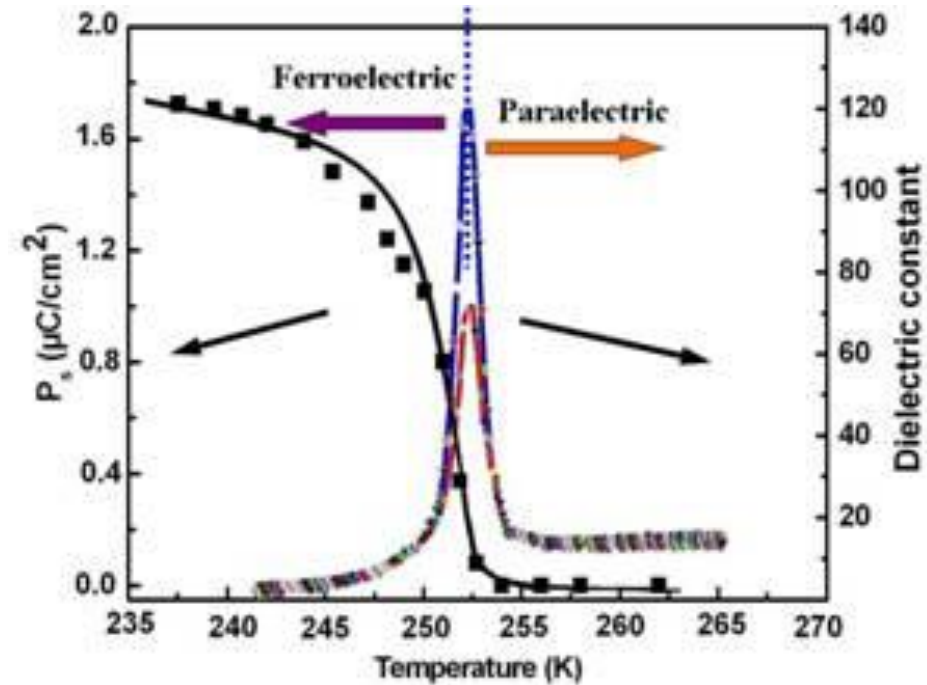


$$\mathbf{p} = q \mathbf{d}$$



○ A ● B ● Oxygen

Ferroelectric

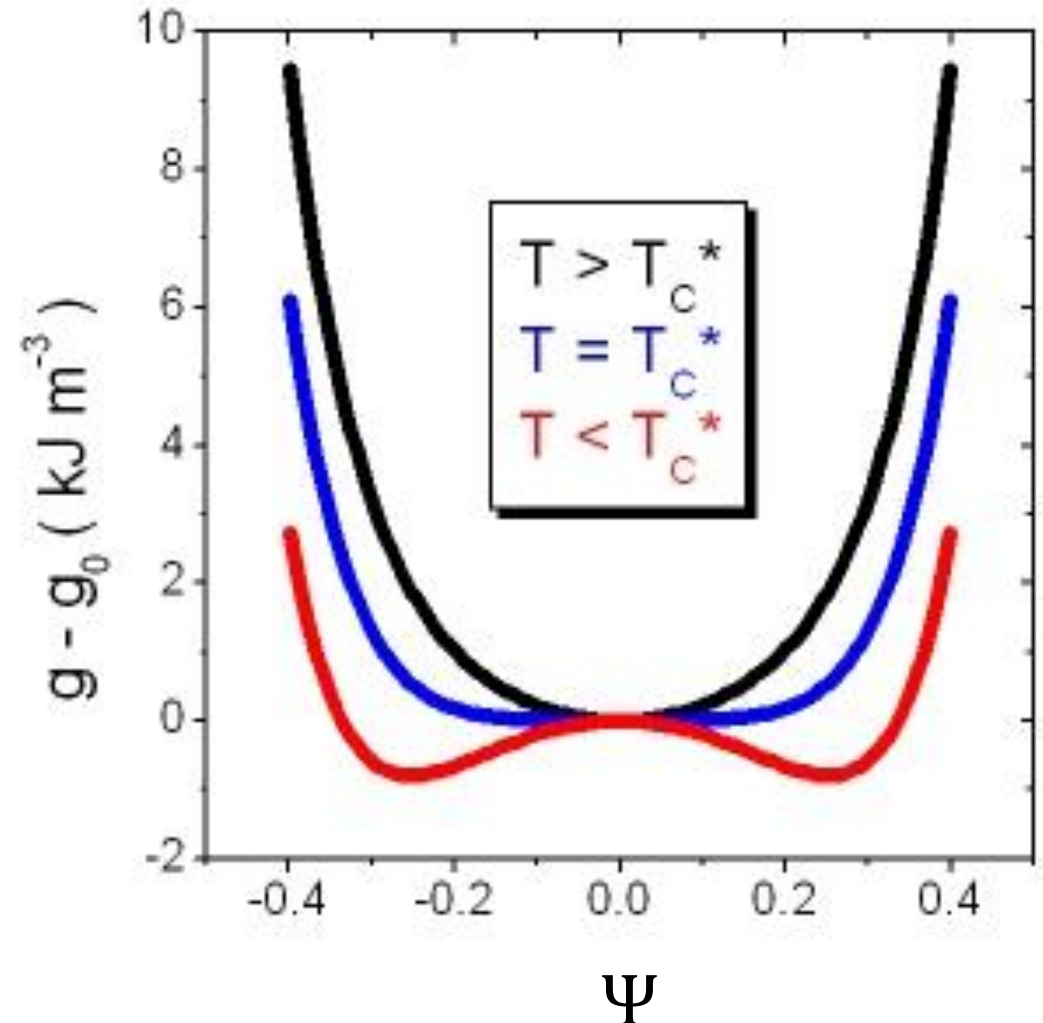


$$\Psi = 0$$

$$\Psi \neq 0$$

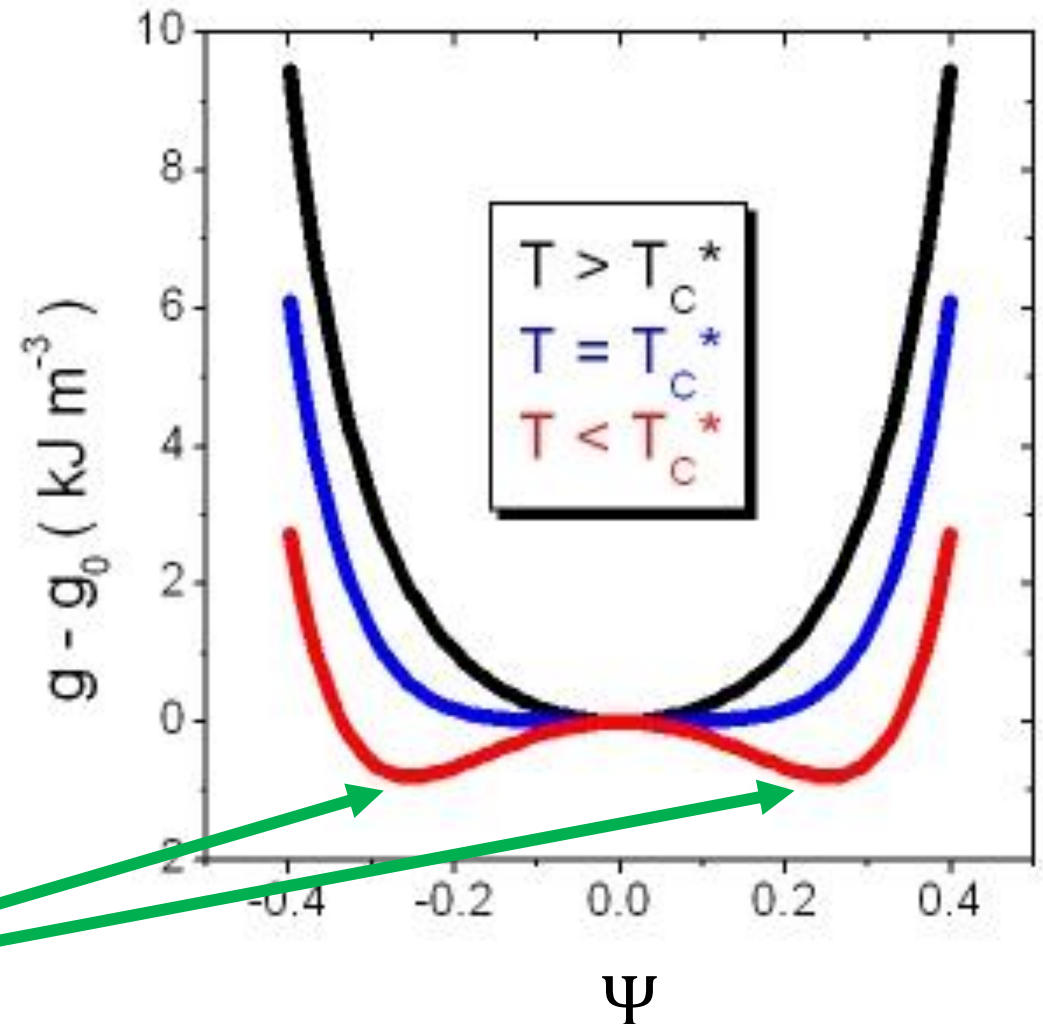
Landau Free Energy

- $F = a_0 + a_1\Psi^2 + a_2\Psi^4 + \dots$
- Energy minimization!
 - Above $T_c \rightarrow \Psi = 0$
 - Below $T_c \rightarrow$ Symmetry breaking



Symmetry

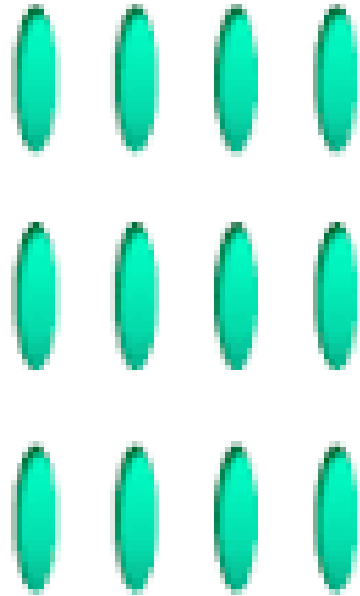
- Degeneracy of stable states when $T < T_c$



Symmetry
breaking

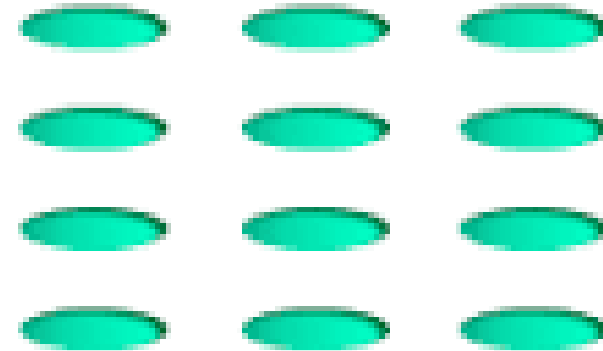
Liquid Crystals

- Absent an external field



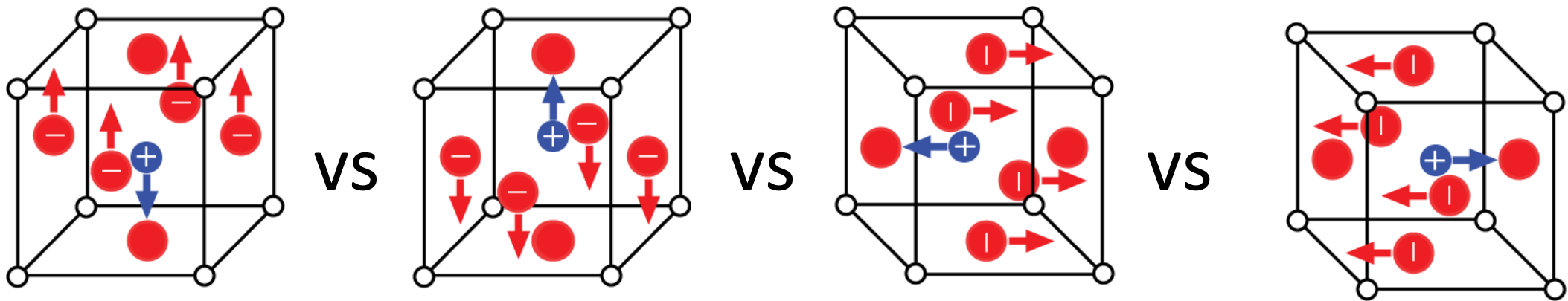
Solid

VS

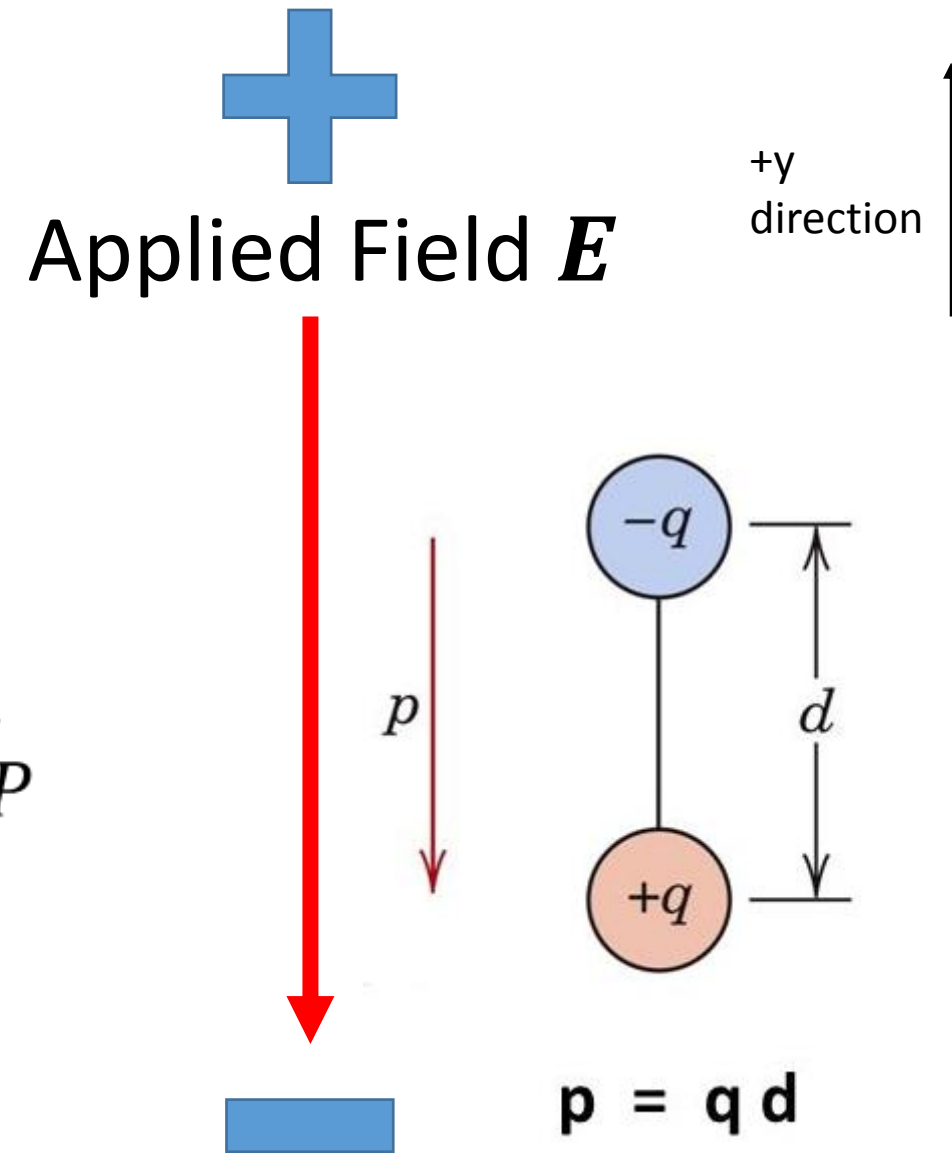
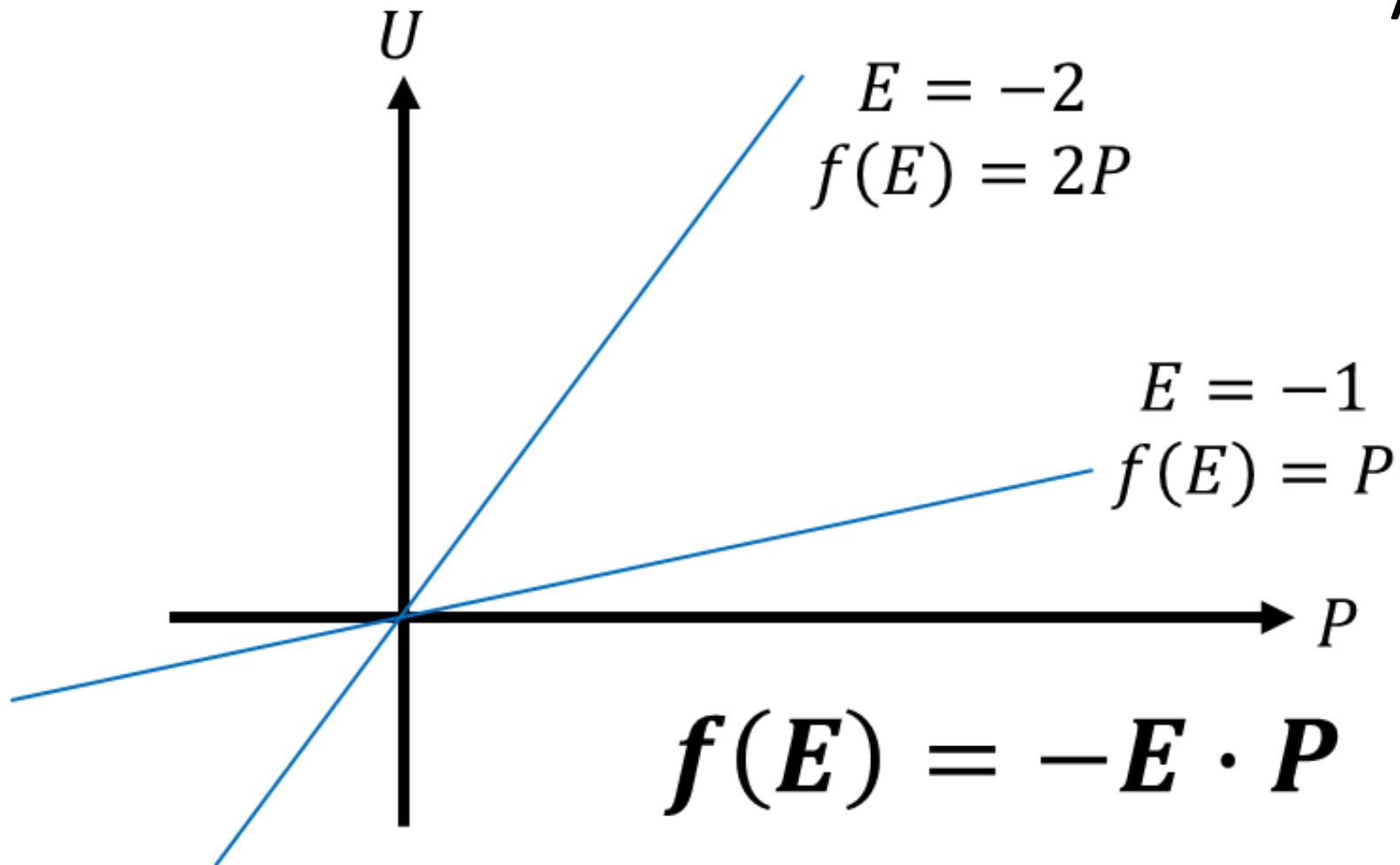


Ferroelectric

- Symmetry breaking = system adopts one of the symmetric states
- $F = a_0 + a_1\Psi^2 + a_2\Psi^4 + \dots$
- Symmetry \rightarrow Why free energy expansion only has even polynomials

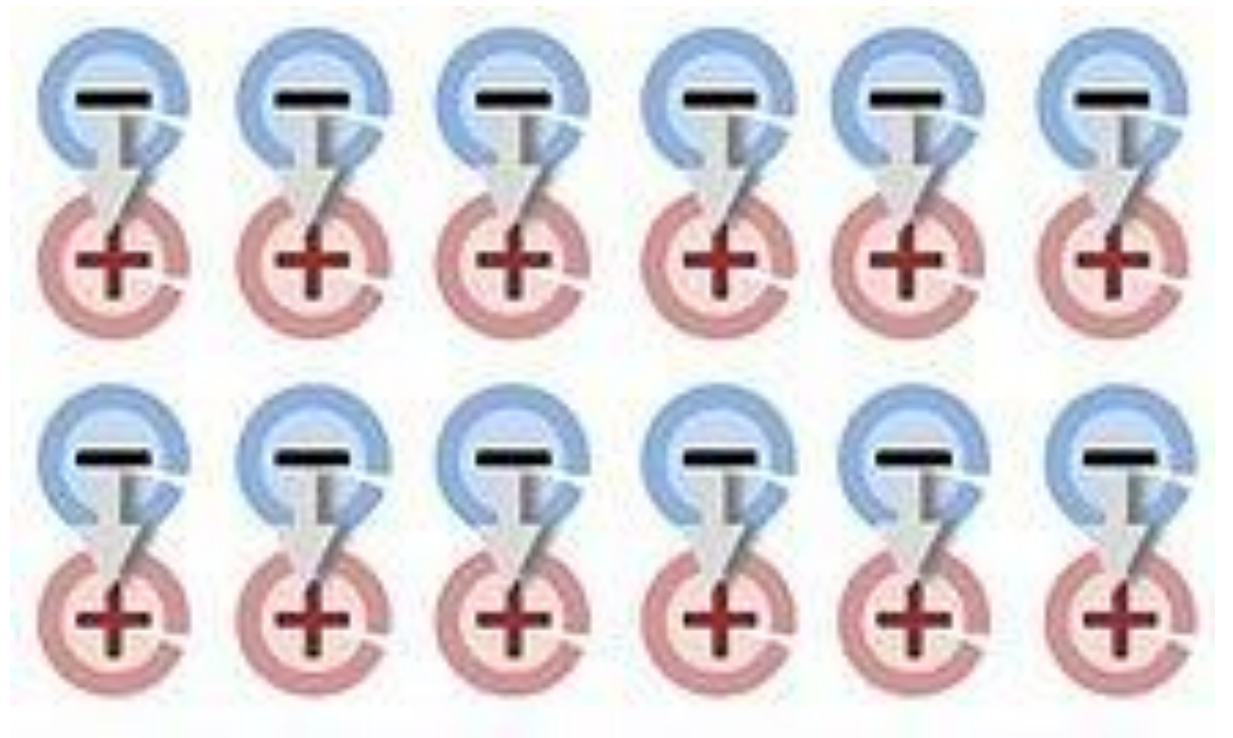
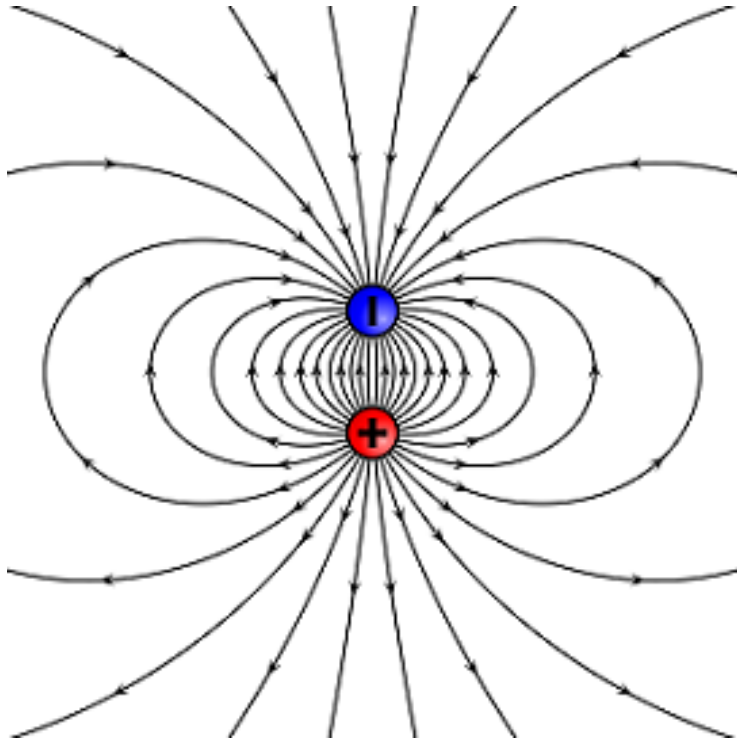


Electrical Energy

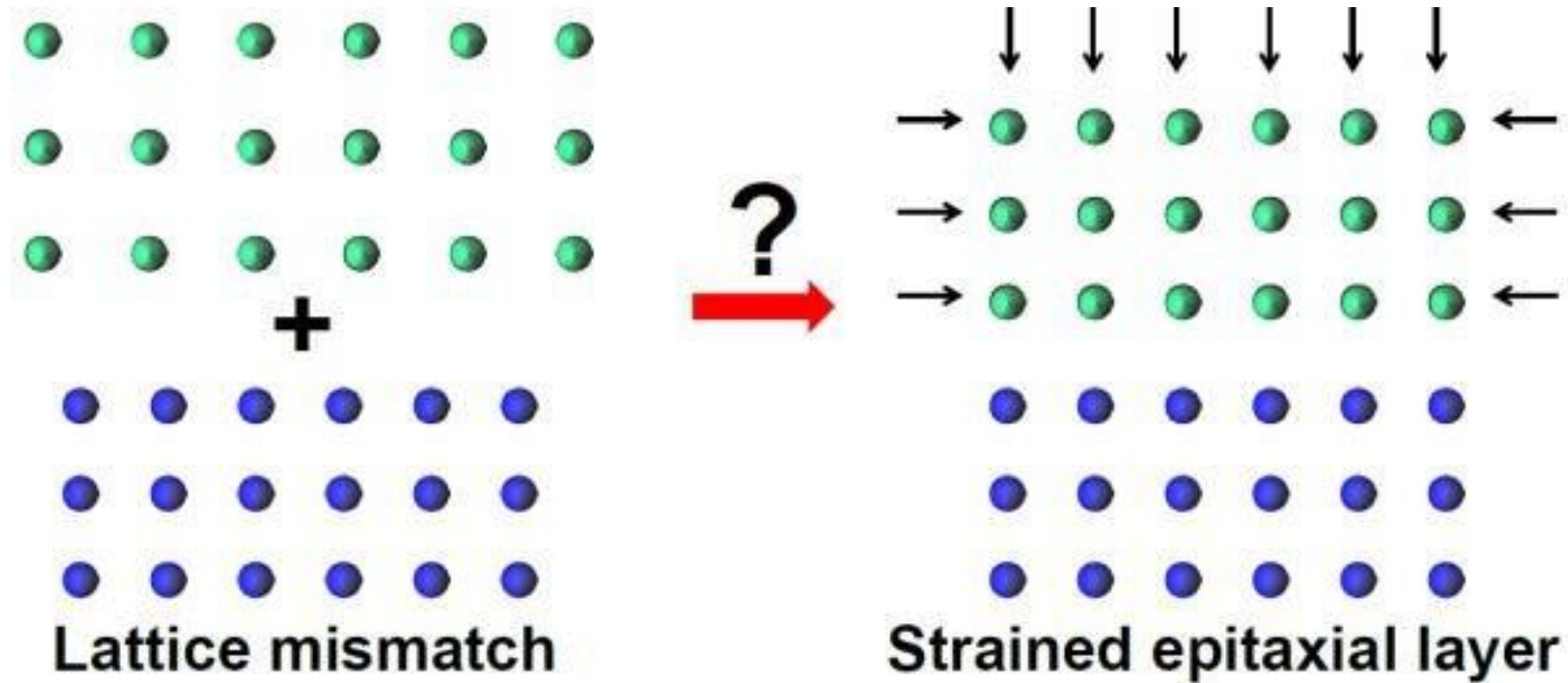


Long Range Electrical Energy

- Each dipole produces a field
- What is the total electrical energy?

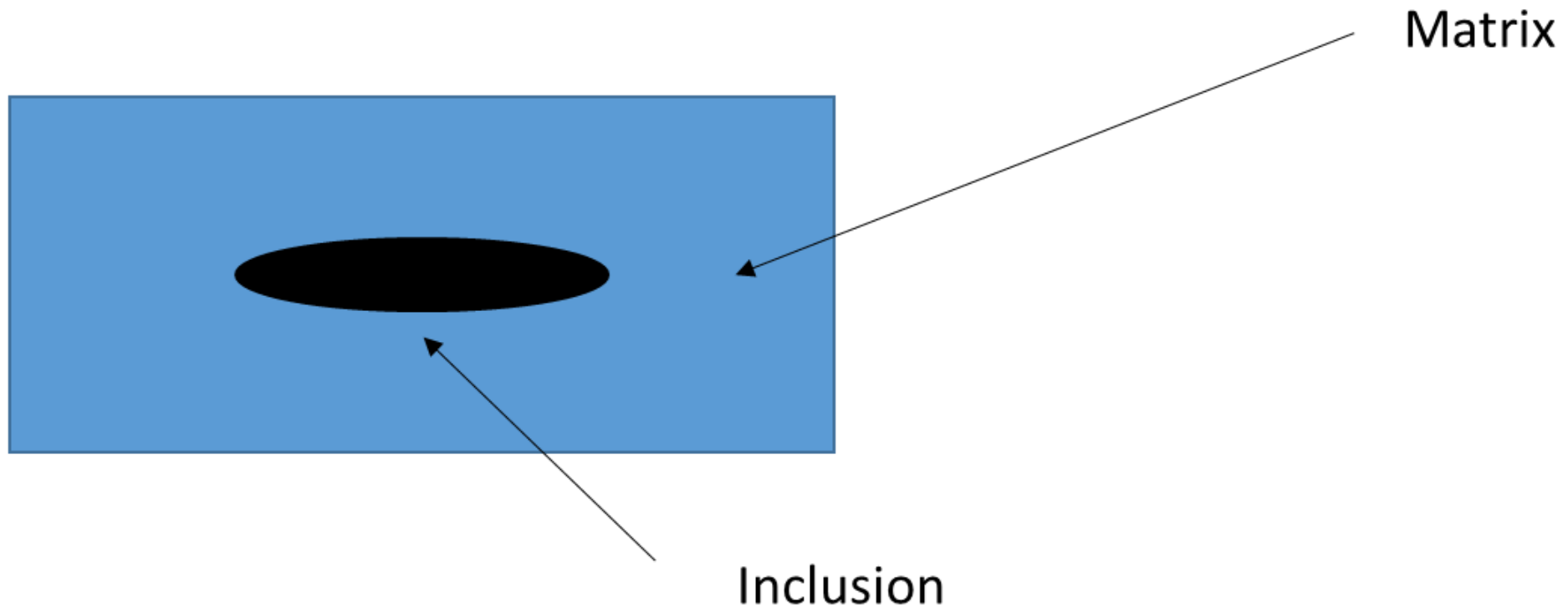


Elastic Energy



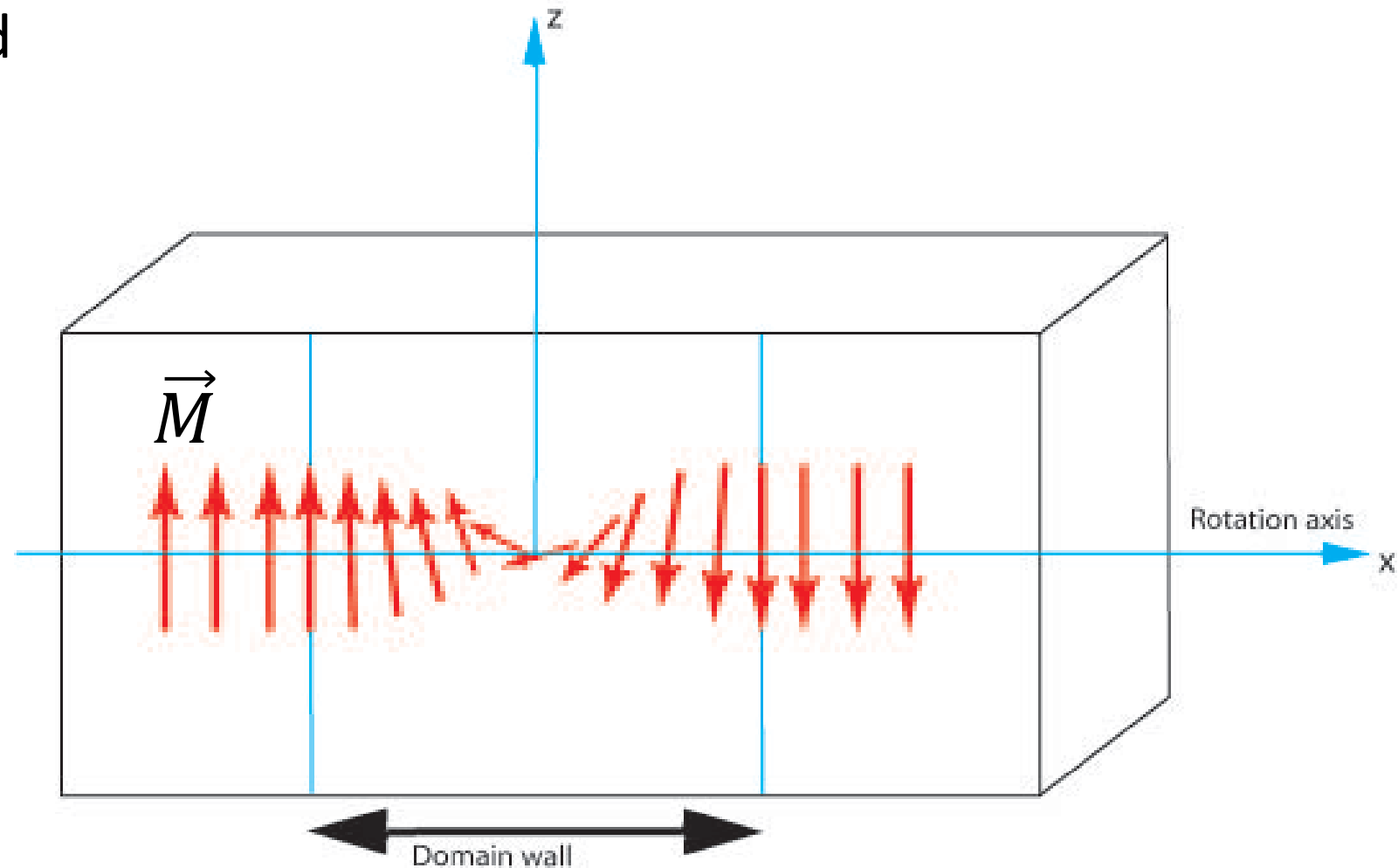
Elastic Energy

- Inclusion changes shape? What is the lattice mismatch and the elastic energy?



Interfacial Energy

- Homogeneity preferred



Putting it all together... Phase Field Modeling

$$F = \int f_l + f_e + f_g + f_{elec} dV, \frac{\partial P_i}{\partial t} = \frac{\delta F}{\delta P_i}$$

Equilibrium Conditions

$$f_l = \frac{1}{2} a_{ij} P_i^2 P_j^2 + \frac{1}{4} a_{ijkl} P_i P_j P_k P_l + \dots \quad \text{Landau Energy}$$

$$\sum_i \frac{\partial \sigma_{ij}}{\partial x_j} = 0$$

$$f_e = \frac{1}{2} C_{ijkl} (\varepsilon_{ij} - \varepsilon_{ij}^0) (\varepsilon_{kl} - \varepsilon_{kl}^0) \quad \text{Elastic Energy}$$

$$\sum_{i,j} \varepsilon_0 \kappa_{ij} \frac{\partial E_j^d}{\partial x_i} = \sum_i -\frac{\partial P_i}{\partial x_i}$$

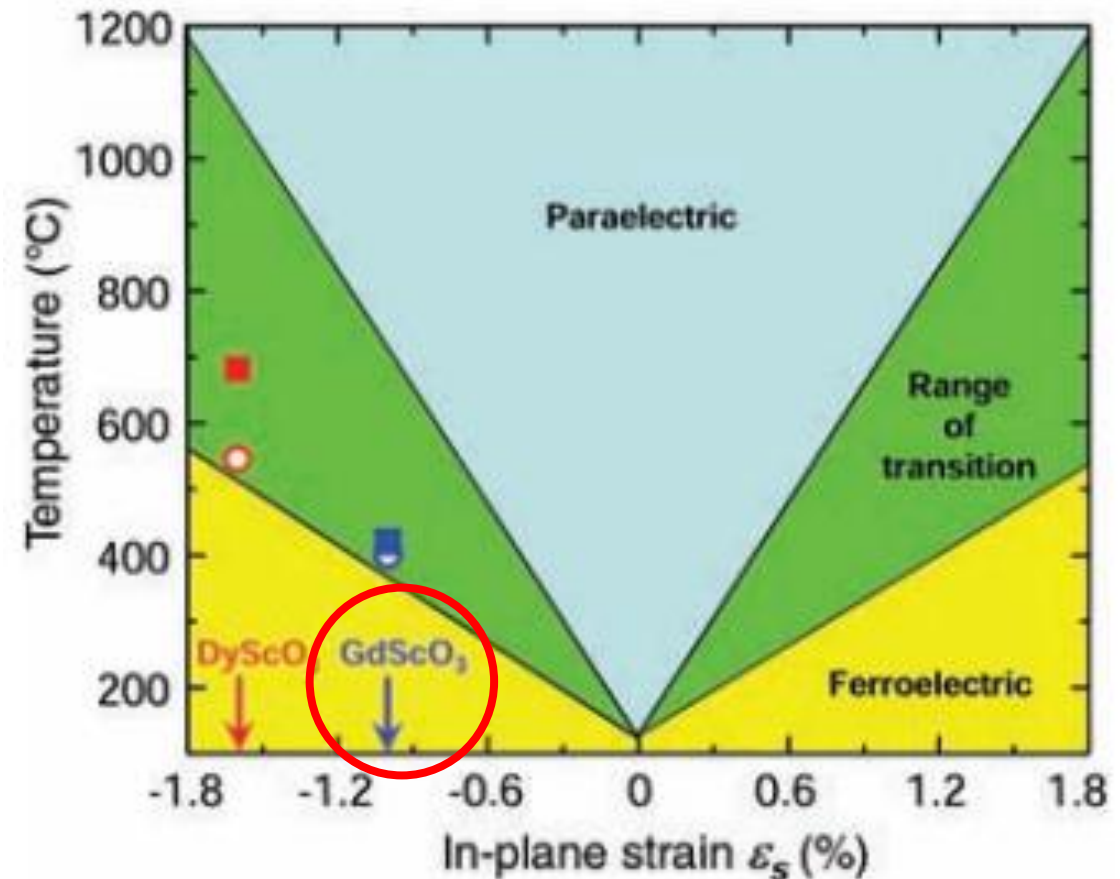
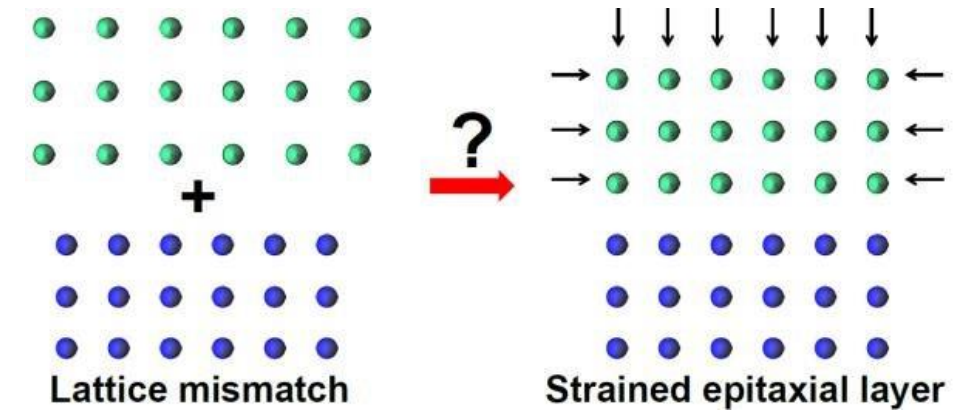
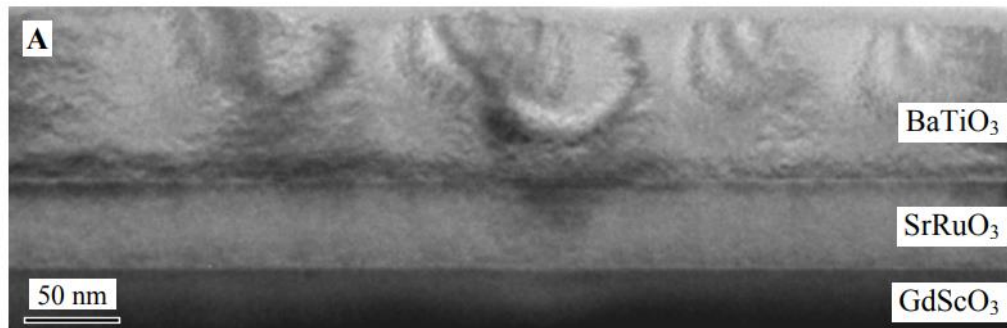
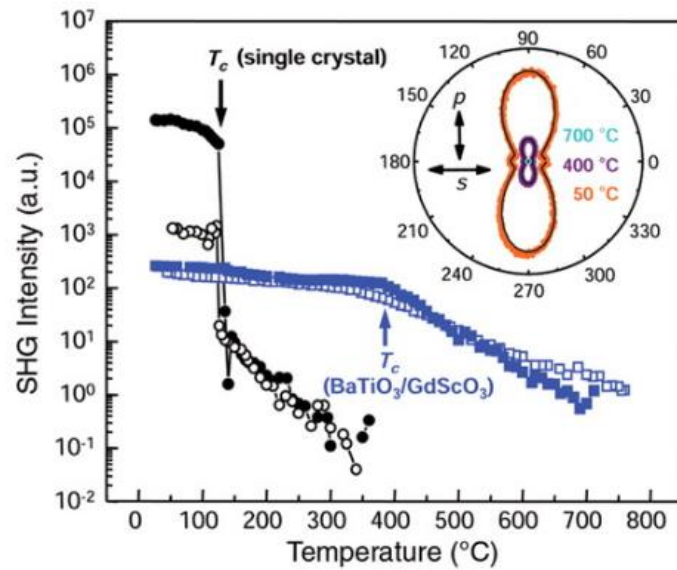
$$f_g = \frac{1}{2} G_{ijkl} \frac{\partial P_i}{\partial x_j} \frac{\partial P_k}{\partial x_l} \quad \text{Interfacial Energy}$$

$$f_{elec} = -\frac{1}{2} E_i^d P_i - E_i^{app} P_i \quad \text{Electrical Energy}$$

- Implemented in C and MATLAB
- 3-dimensional simulation of ferroelectric materials

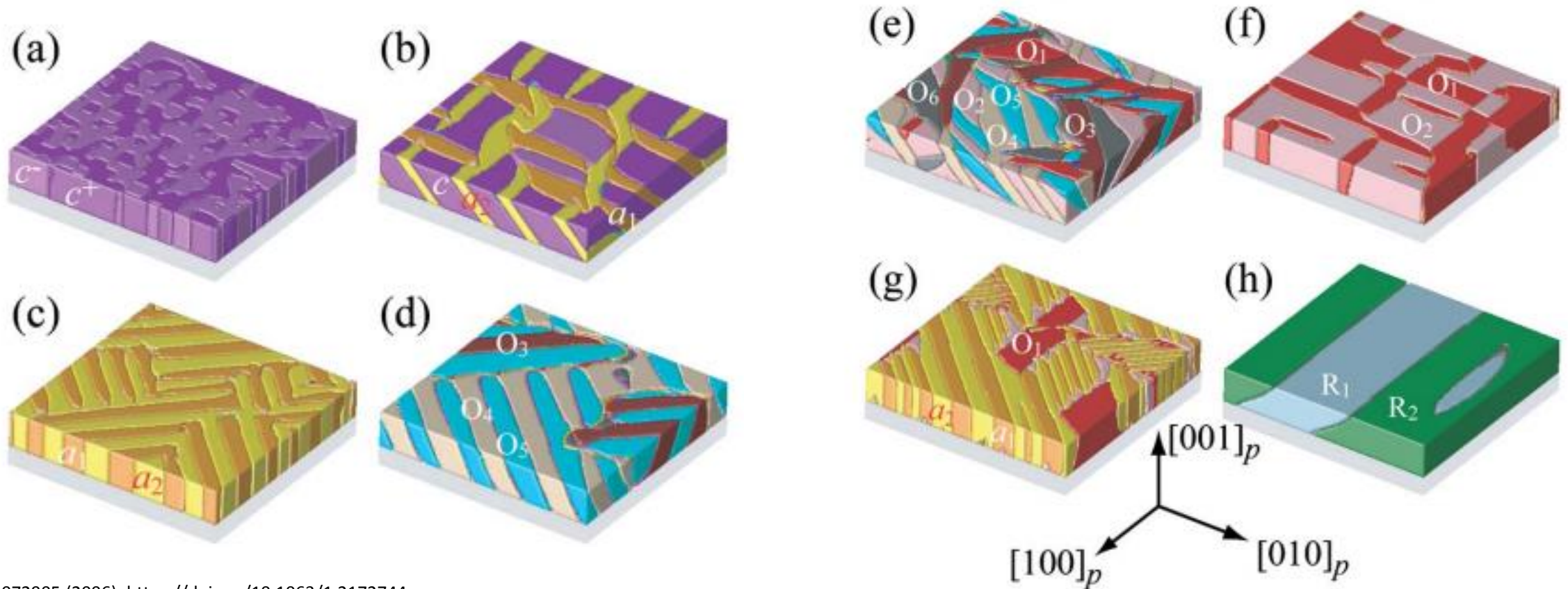
Thin Film Engineering

- Strain engineered BaTiO₃



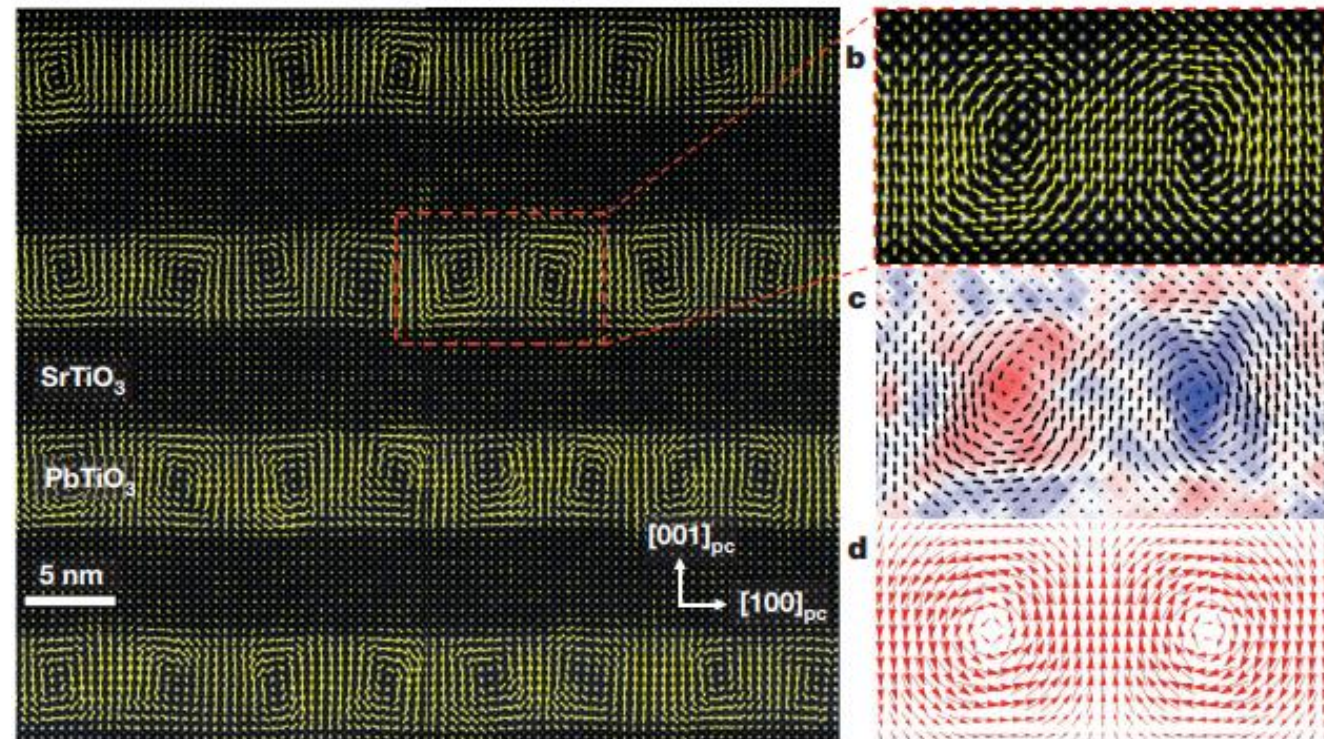
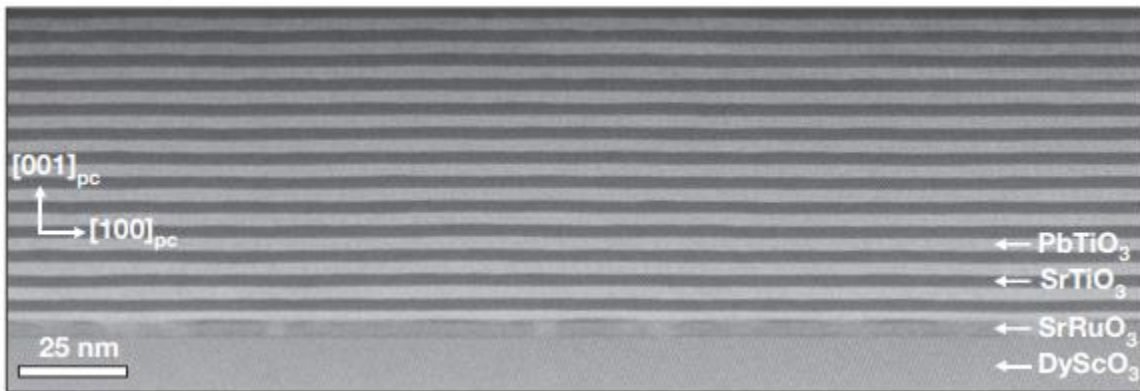
Thin Film Engineering

- Strain engineered thin films



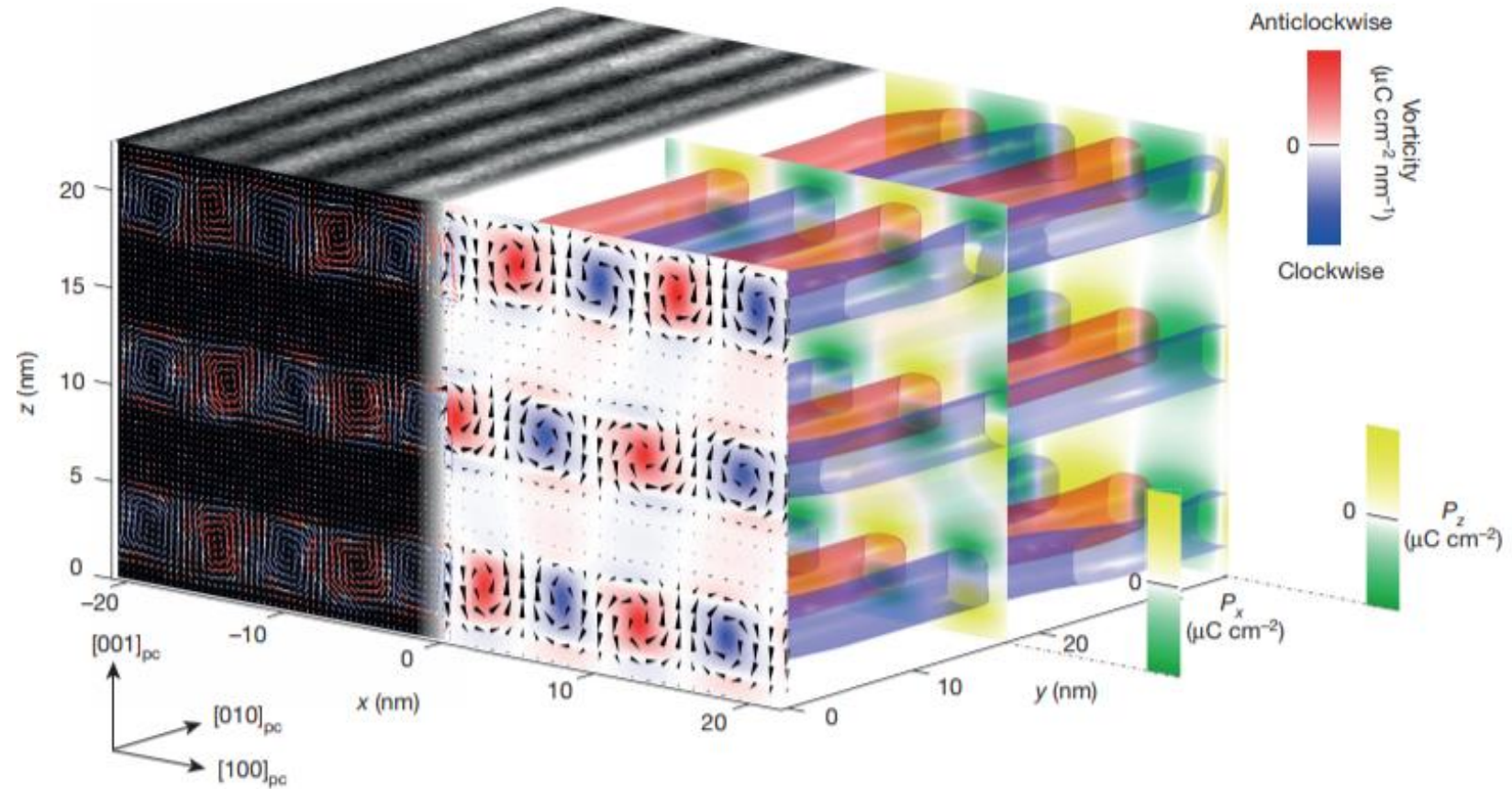
Polar Vortices

- Superlattice
- Alternating layers of material



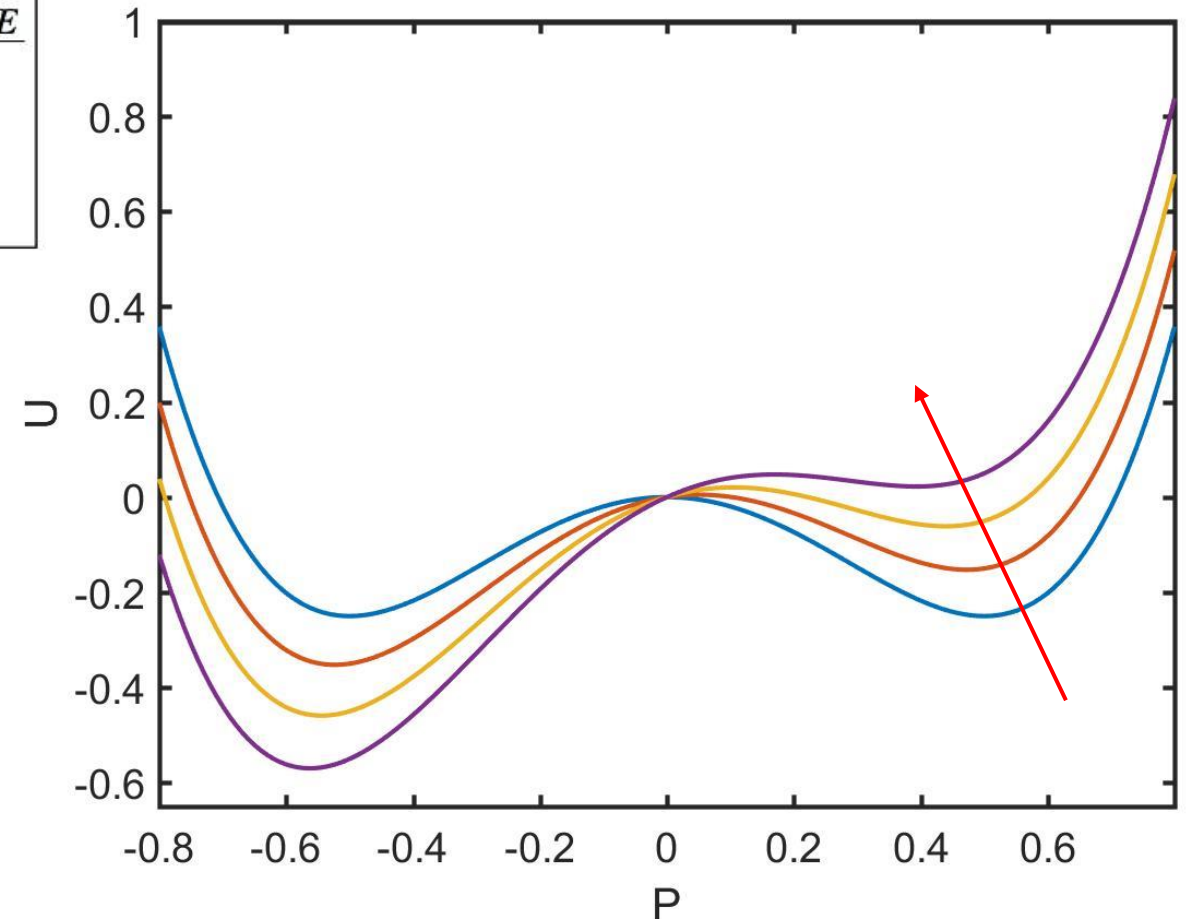
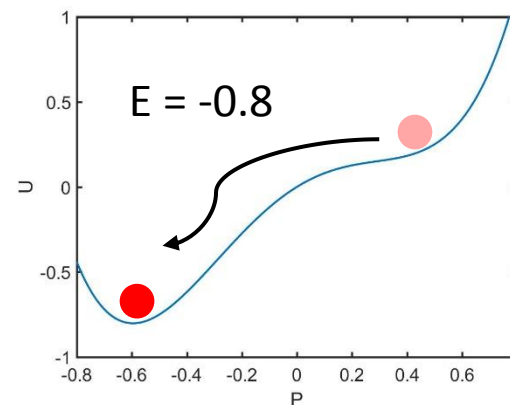
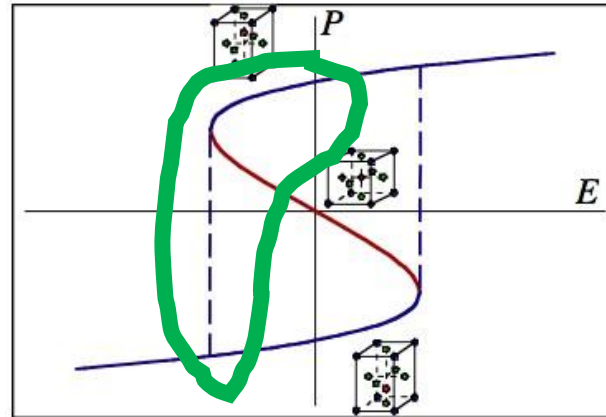
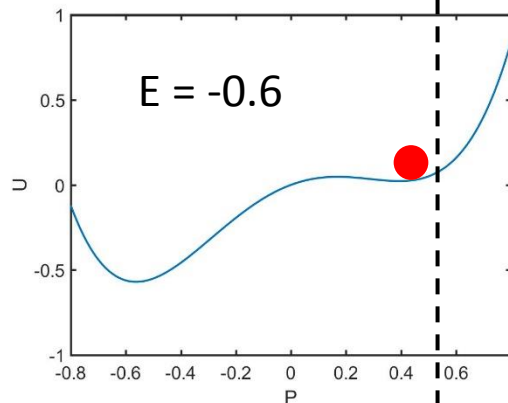
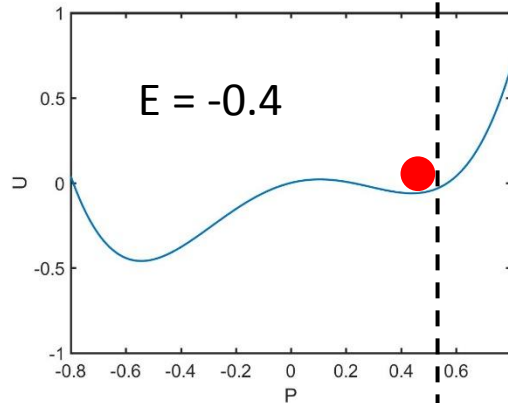
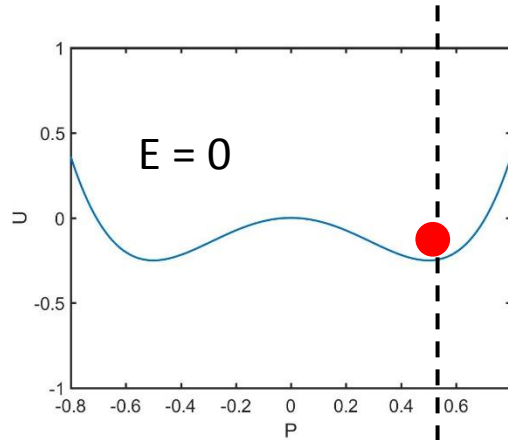
Polar Vortices

- Phase field simulation vs experimental results
- Superlattice periodicity + energy considerations lead to polar vortex formation



Positive Capacitance

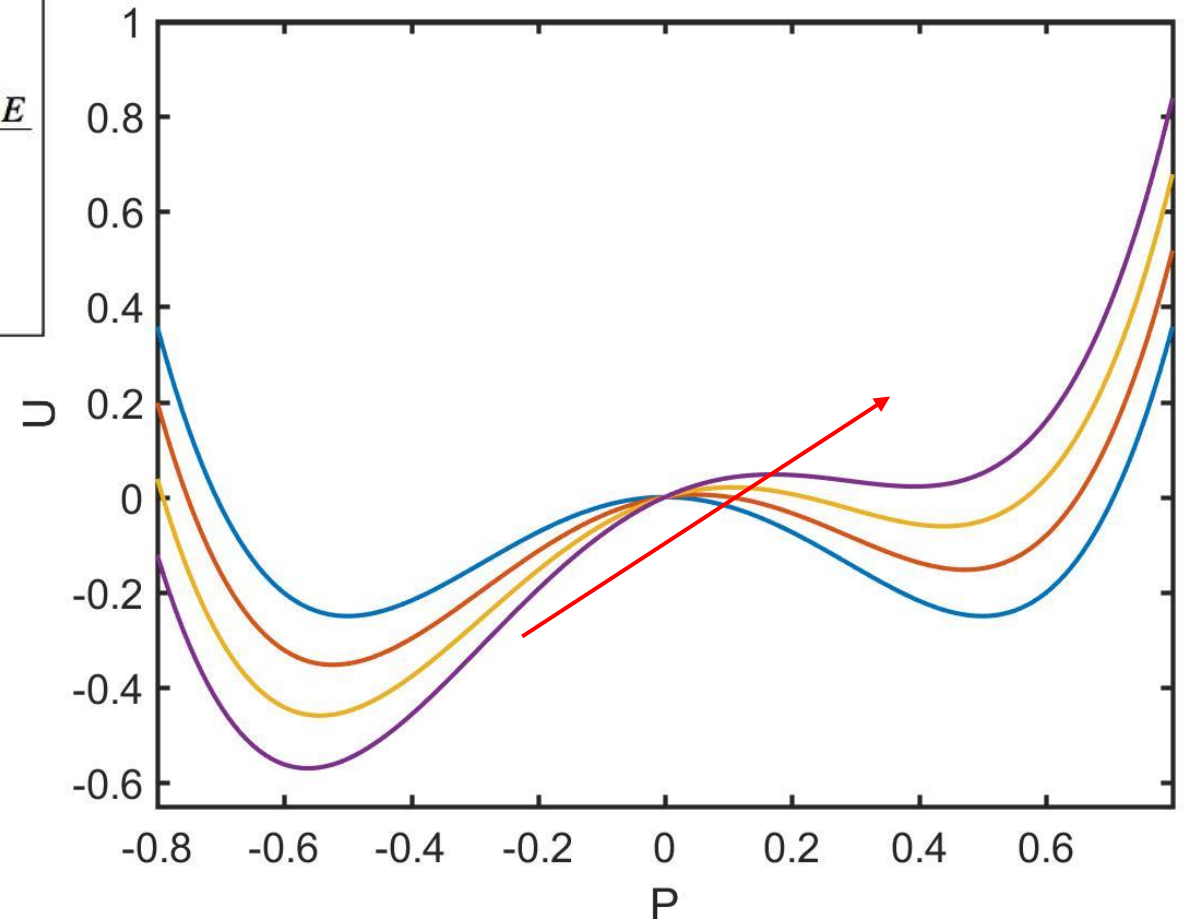
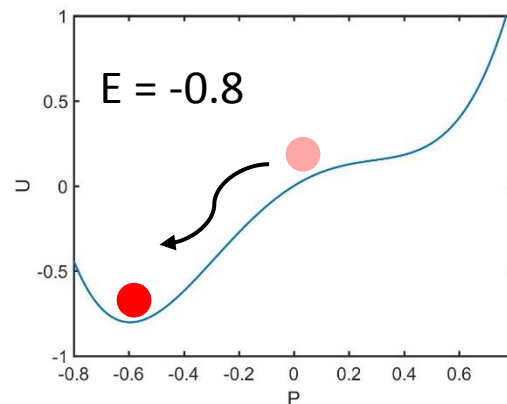
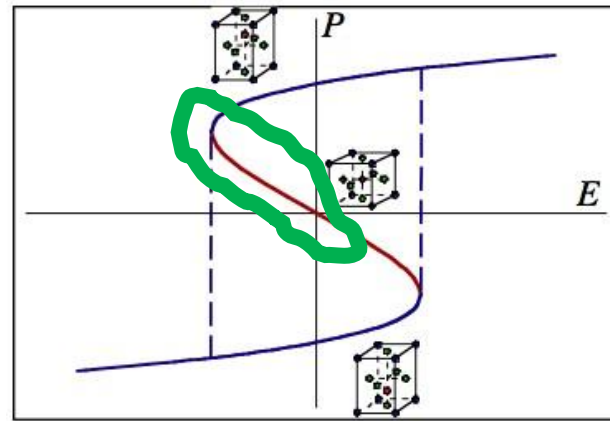
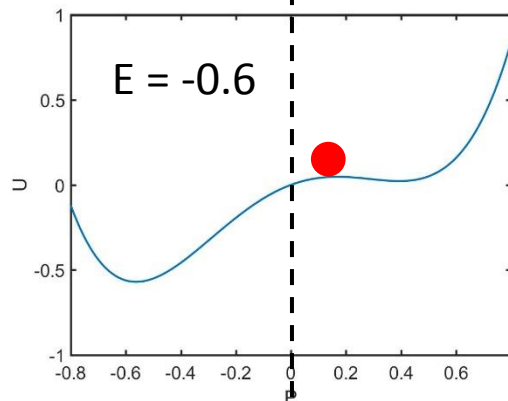
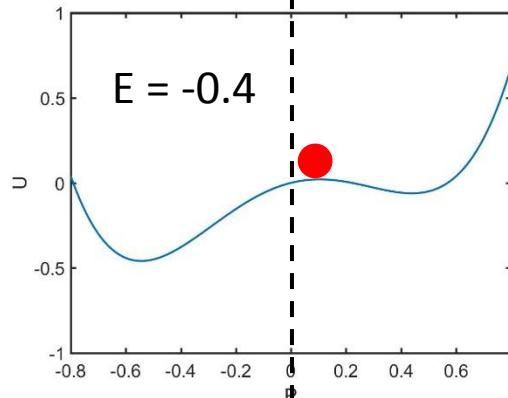
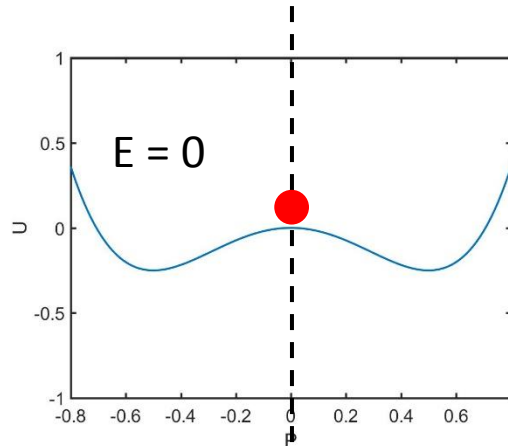
Negative E field
P becomes more negative



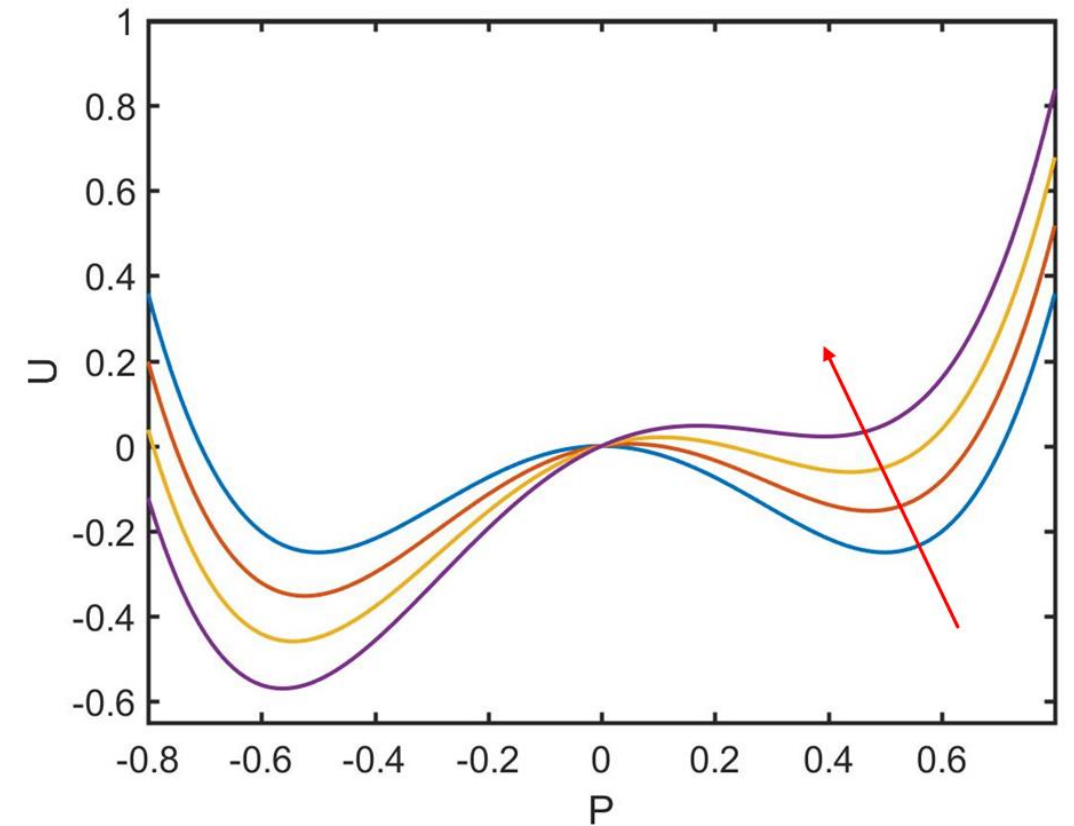
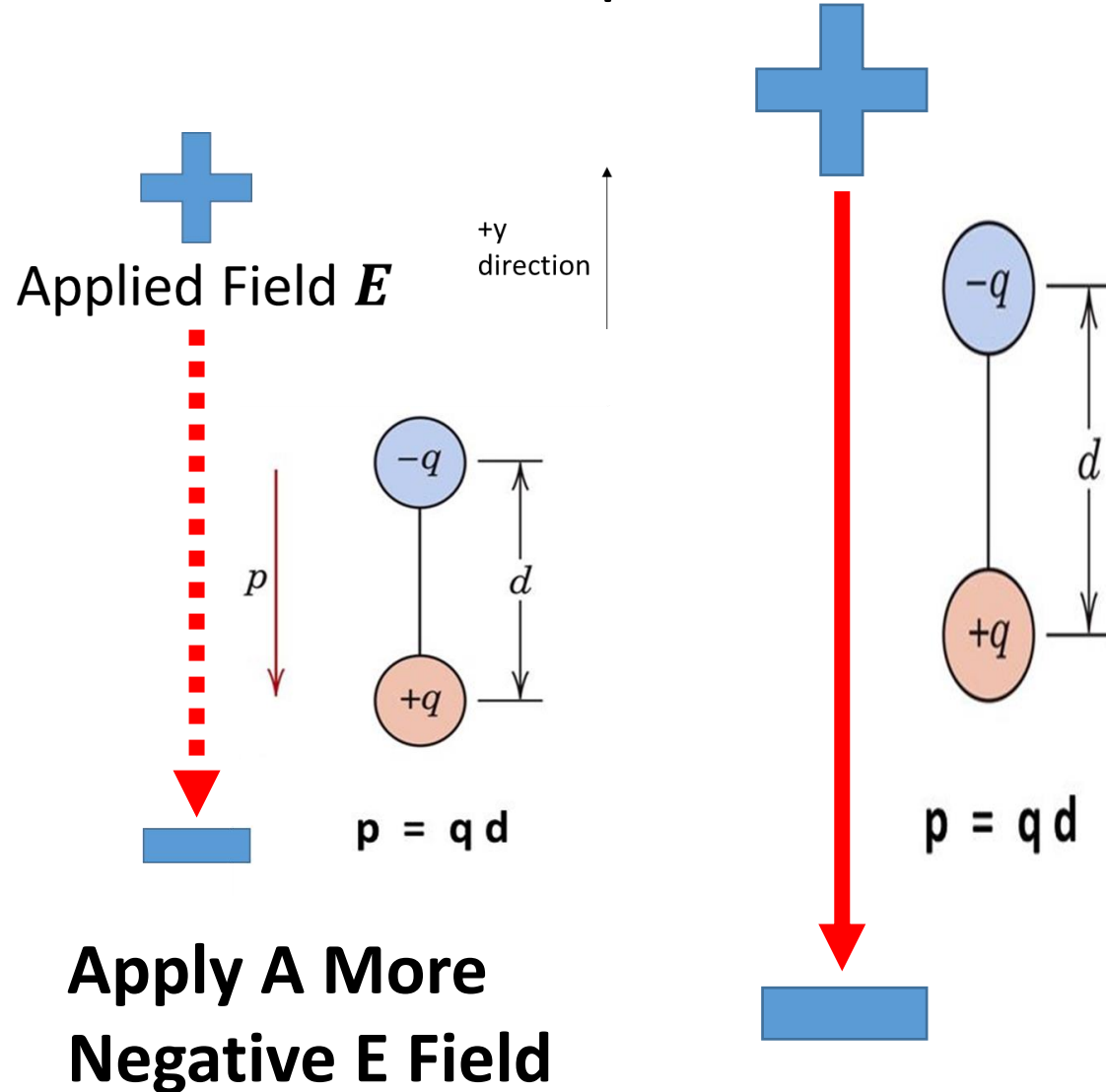
Negative Capacitance!!

Negative E field
P becomes positive!!!!

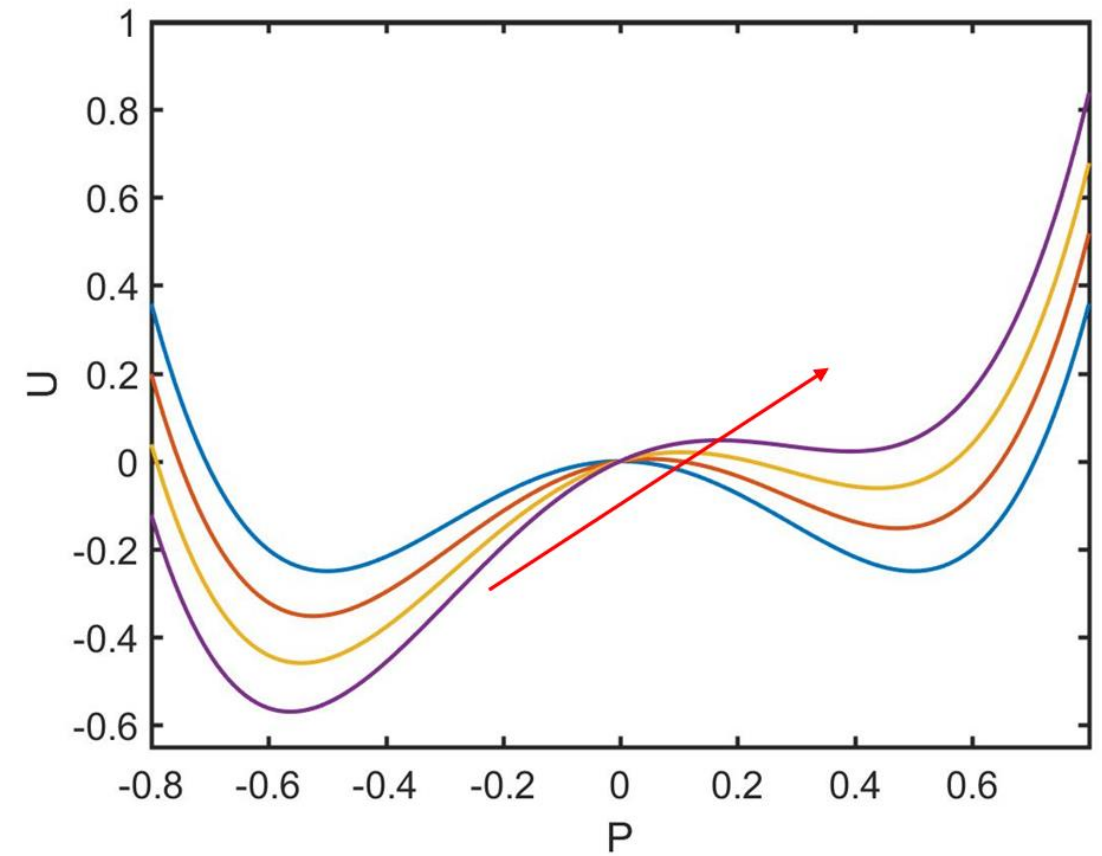
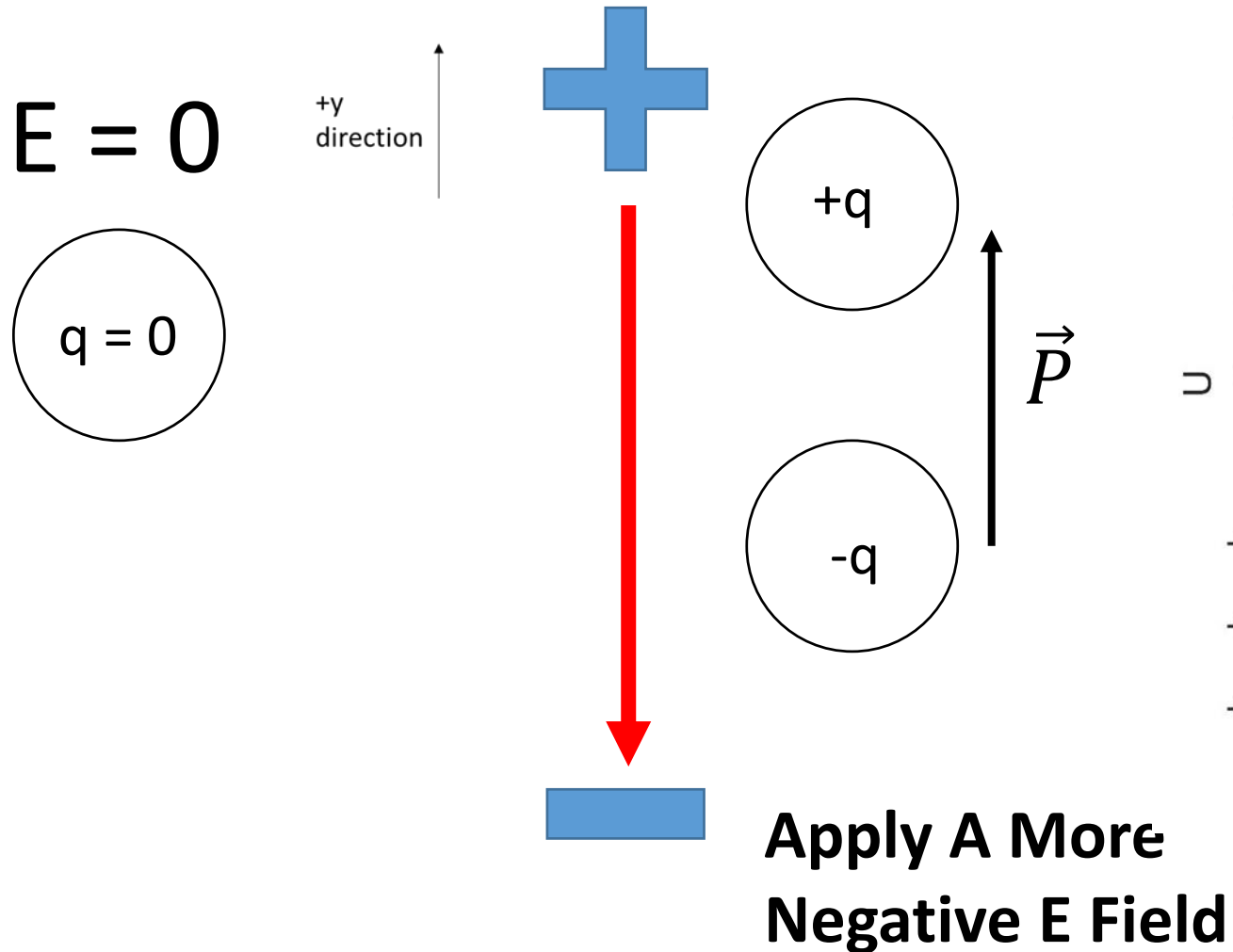
Stabilize
metastable state



Positive Capacitance



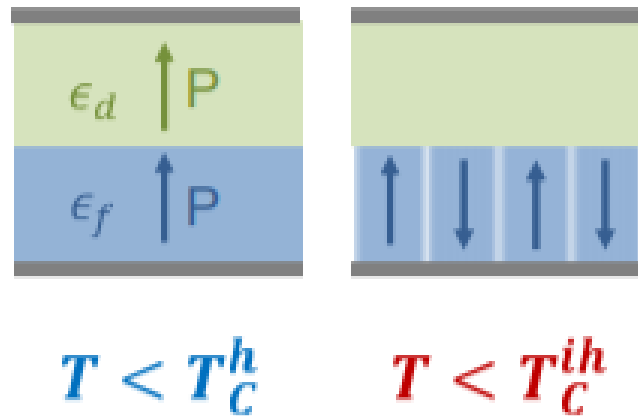
Negative Capacitance



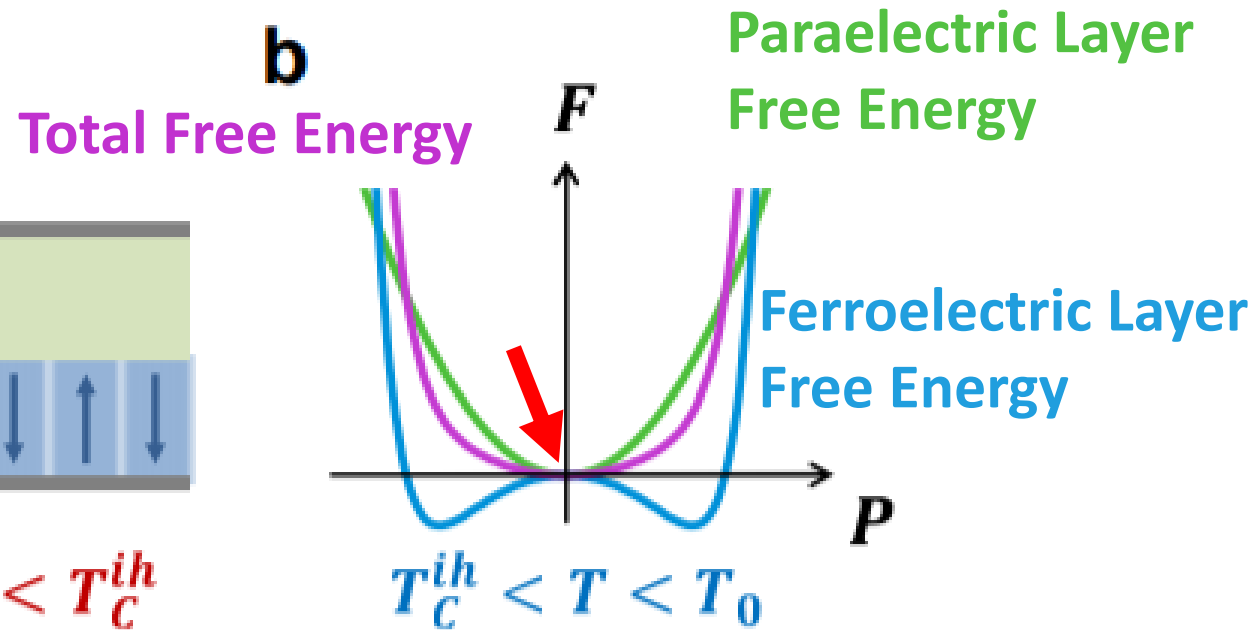
Stabilization of Negative Capacitance

- New era of low power electronics

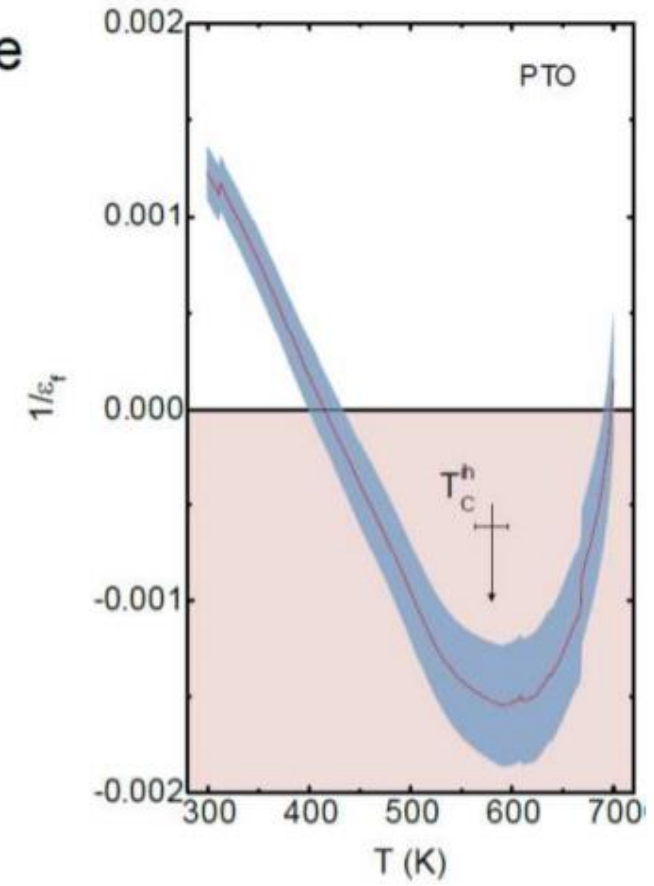
a



b



e



Questions!?

Ferroelectric

- Permanent electric dipole
- $\Psi = \|\vec{P}\|$
- \vec{P} = Polarization vector

