

Notes on Probability

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HIRE-ASSISTANT(n)

```
1   $best = 0$ 
2  for  $i = 1$  to  $n$ 
3      interview candidate  $i$ 
4      if candidate  $i$  is better than candidate  $best$ 
5           $best = i$ 
6          hire candidate  $i$ 
```

RANDOMIZED-HIRE-ASSISTANT(n)

```
1  randomly permute the list of candidates
2   $best = 0$ 
3  for  $i = 1$  to  $n$ 
4      interview candidate  $i$ 
5      if candidate  $i$  is better than candidate  $best$ 
6           $best = i$ 
7          hire candidate  $i$ 
```

PERMUTE-BY-SORTING(A)

```
1   $n = A.length$ 
2  let  $P[1...n]$  be a new array
3  for  $i = 1$  to  $n$ 
4       $P[i] = \text{RANDOM}(1, n^3)$ 
5  sort  $A$  using  $P$  as sort keys
```

RANDOMIZE-IN-PLACE(A)

```
1   $n = A.length$ 
2  for  $i = 1$  to  $n$ 
3      swap  $A[i]$  with  $A[\text{RANDOM}(i, n)]$ 
```

The birthday paradox

- How many people must be in a room before there is a 50% chance of two of them having the same birthday? Assumptions:

-

$$\Pr \{b_i = r\} = 1/n \text{ for } i = 1..k \text{ and } r = 1..n$$

-

$$\Pr \{b_i = r \text{ and } b_j = r\} = \Pr \{b_i = r\} \Pr \{b_j = r\}$$