Ray Tracing, Part I

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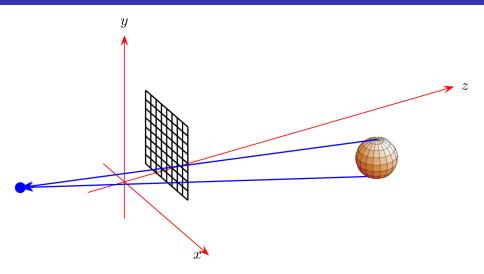
Readings

- https://www.siggraph.org/education/materials/ HyperGraph/raytrace/rtrace0.htm
- https: //www.cs.unc.edu/~rademach/xroads-RT/RTarticle.html
- http://www.cs.utah.edu/~shirley/books/fcg2/rt.pdf
- http://www.povray.org/
- http://www.pbrt.org/

Ray Traced Images Achieve Maximal Realism

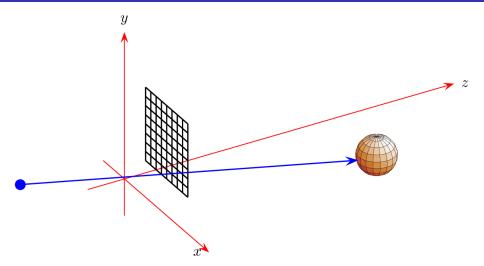


Two ways of rendering a picture: object order



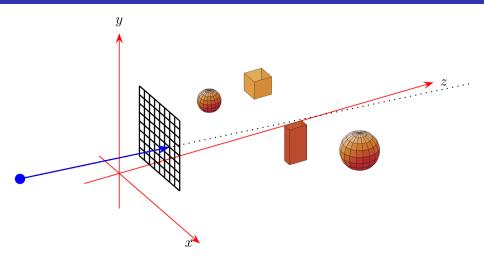
• For each object in the world, find the colors it would put on the screen.

Two ways of rendering a picture: image order



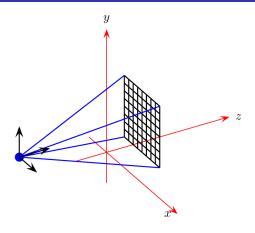
• For each pixel on the screen, find the objects that would color it.

Ray casting, a simplified ray tracing



- Given an eye position and a pixel position, construct a ray.
- Project the ray into the scene and find the closest intersection.
- Use object to compute color.

Camera

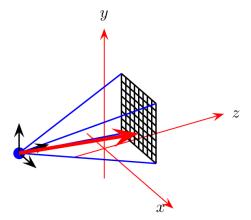


- A frame: origin point, and right, up, forward vectors.
- A distance, width and height for the image plane.

$$\langle p, r, u, f, d, w, h \rangle$$

Would it matter if d, w, h were all doubled?

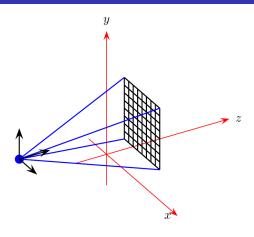
Finding vectors from the eye to the image plane



- Give an expression for the upper left corner.
- Give an expression for the upper right corner.
- Give an expression for a point 30% of the way across the image plane and 10% up from the bottom.

$$\langle p, r, u, f, w, h \rangle$$

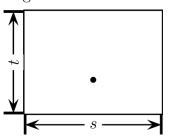
Other camera representations

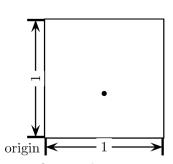


- Lookat: eye point, lookat point, up vector, width, aspect ratio.
- Eye and four points
- Eye, lower left corner, two vectors
- Eye and four vectors

Normalized screen coordinates

origin

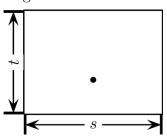


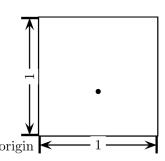


- Normalized screen coordinates map the entire surface to the $(0,1)\times(0,1)$ square.
- Suppose the screen is 640×480 , with origin in the upper left, and we have a point at (300,400) on the screen.
- What are the point's normalized screen coordinates?

Normalized screen coordinates

origin





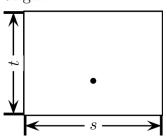
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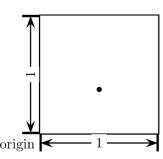
$$\left(\frac{300}{640}, 1 - \frac{400}{480}\right)$$



Normalized screen coordinates

origin



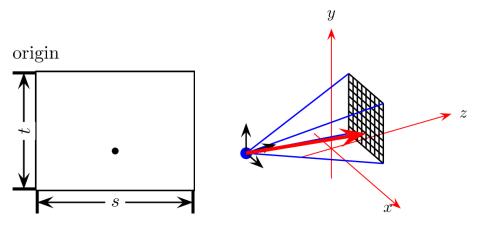


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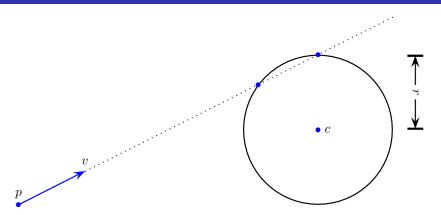
Mapping from Pixel to Camera Ray



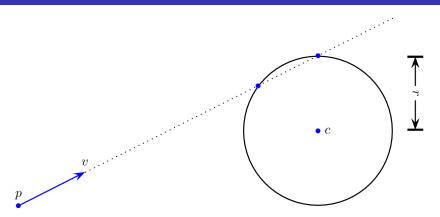
- Given a pixel position on the screen, find the ray in the camera.
- ullet Map screen position to normalized position in (0,1) imes (0,1)
- Map normalized position in $(0,1) \times (0,1)$ to vector in world space.

Ray tracing process

- Input: a camera and a set of objects
- Output: an image
- For each pixel in the image:
 - Find the ray in the camera for that pixel.
 - For all objects in the set:
 - find the closest in front of the camera that intersects the ray
 - Find the color of that object at the intersection point.
 - Color the pixel in the image with that color.



- Sphere defined by center and radius.
- Ray defined by point and vector.
- Assume sphere is centered at origin (replace p with p-c).
- Equation to solve?



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- Equation to solve?
- Solve for $t: |p + tv|^2 = r^2$



Solving quadratic

$$|p + tv|^{2} = (p + tv) \cdot (p + tv)$$

$$= \sum_{i} (p_{i} + tv_{i})(p_{i} + tv_{i})$$

$$= \sum_{i} (p_{i}^{2} + 2p_{i}v_{i}t + v_{i}^{2}t^{2})$$

$$= \sum_{i} p_{i}^{2} + 2\sum_{i} p_{i}v_{i}t + \sum_{i} v_{i}^{2}t^{2}$$

$$= (p \cdot p) + 2(p \cdot v)t + (v \cdot v)t^{2}$$

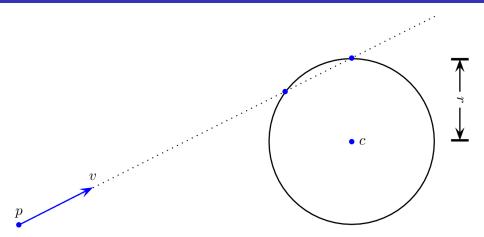
So, in the quadratic $at^2 + bt + c = 0$,

$$a = v \cdot v \quad (= 1 \text{ if you normalized your rays})$$

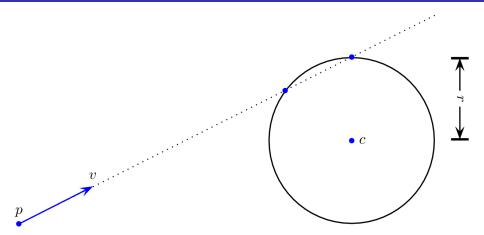
$$b = 2p \cdot v$$

$$c = p \cdot p - r^2$$





 What equation would we have to solve if we did this in world coordinates?



- What equation would we have to solve if we did this in world coordinates?
- $|(p + tv) c|^2 = r^2$
- Much simpler in object coordinates (replace p with p-c).

Still something missing ...

