

Noise

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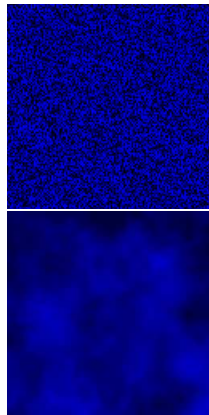
September 30, 2015

Readings

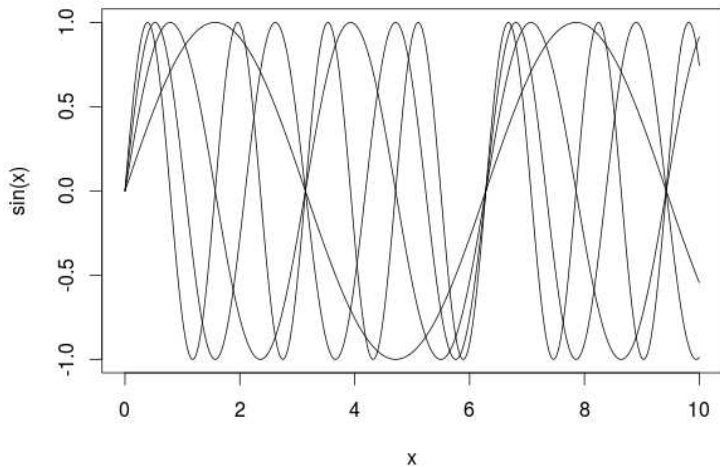
- ▶ <http://www.noisemachine.com/talk1/>
- ▶ http://freespace.virgin.net/hugo.elias/models/m_perlin.htm
- ▶ <http://mrl.nyu.edu/~perlin/doc/oscar.html>
- ▶ <http://legakis.net/justin/MarbleApplet/>
- ▶ <http://www.planetside.co.uk/>
- ▶ <http://webstaff.itn.liu.se/~stegu/simplexnoise/simplexnoise.pdf>
- ▶ Also the Wikipedia articles collected for the course:
https://en.wikipedia.org/wiki/Book:CSCI_480_Computer_Graphics

Noise

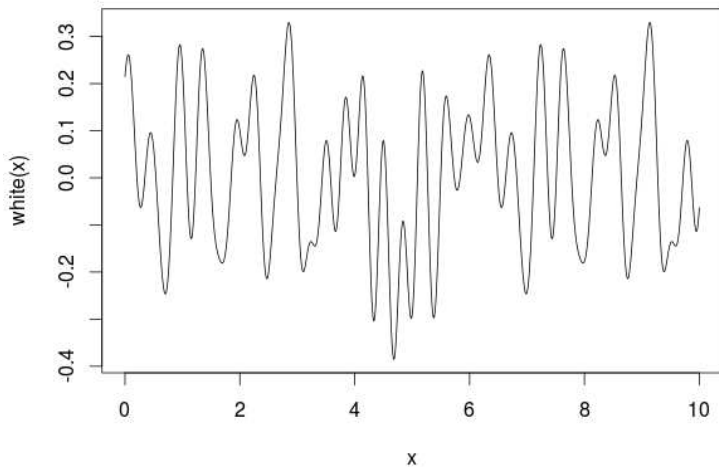
- ▶ Idea is to define a function that looks like the randomness we find in nature.
- ▶ Dirt, clouds, waves on the ocean, skin, all exhibit randomness.
- ▶ However, it is not **white noise**, seen at upper right. It is much smoother, as seen at lower right.
- ▶ Real world noise exhibits smoothness, going from dark to light gradually, with dark and light patches randomly distributed.
- ▶ How can we simulate that? We will add up smoothed white noise at different wavelengths, with the *amplitude* of the noise proportional to its *wavelength*.
- ▶ This is called **pink noise**.



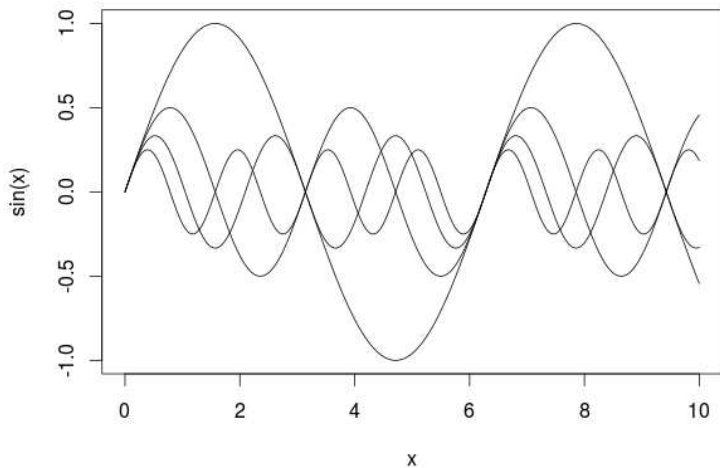
Adding up sin curves: white noise



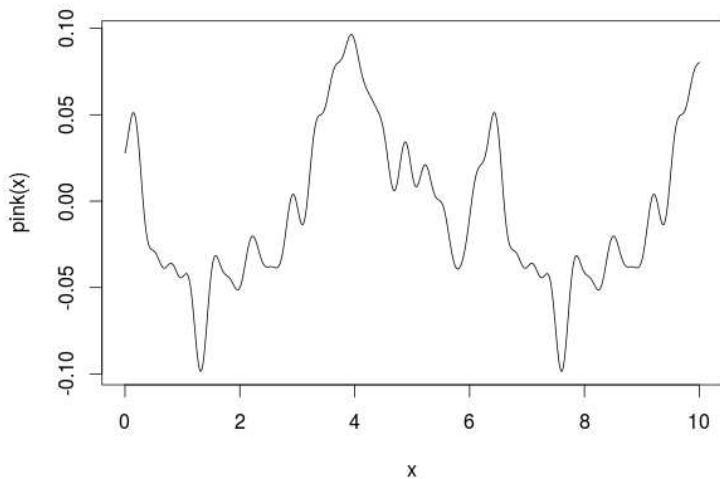
Adding up sin curves: white noise



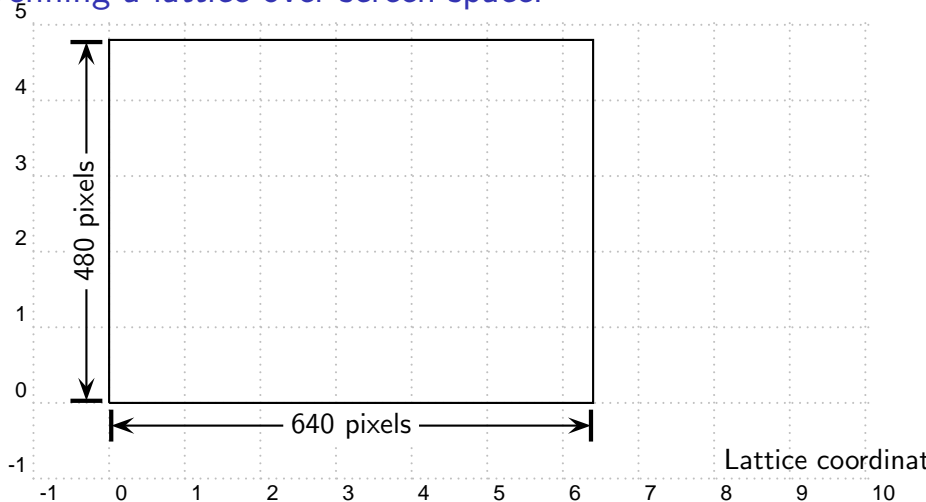
Adding up scaled sin curves: pink noise



Adding up scaled sin curves: pink noise

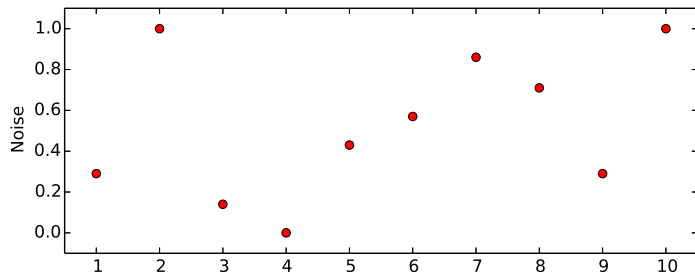


Defining a lattice over screen space.



- ▶ Divide by the *wavelength*, the distance between lattice lines.
- ▶ Optionally, flip the origin to lower left.

latticeNoise: A white noise value for lattice points



- ▶ We start with just a single dimension, x .
- ▶ x is scaled; originally the range of x is much larger.
- ▶ `latticeNoise` only defined at integers.
- ▶ White noise values between 0 and 1
- ▶ Our space is generally too big for an array for all those numbers, so we will find a function `latticeNoise(x)` that uses less memory but is still very fast.

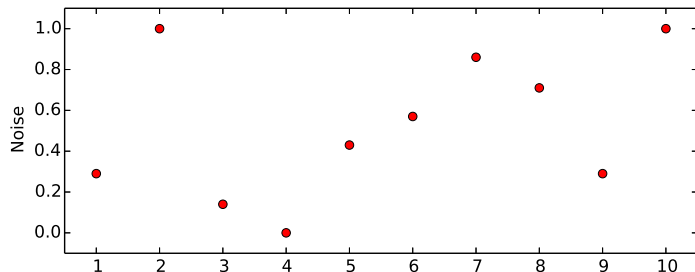
latticeNoise: a Simple Implementation

- ▶ Pick a modest array size, normally $n = 256$
... but for illustration we use $n = 8$
- ▶ Create an array of n floats evenly spaced between 0 and 1,
e.g.,
`noiseTable = (0.00,0.14,0.29,0.43,0.57,0.71,0.86,1.00)`
- ▶ We could randomize this table, but instead we randomize the index into this table. We use a permutation of the first n integers, e.g.,
`hashTable = (5,2,7,1,0,3,4,6)`
- ▶ Our function becomes
`latticeNoise(x): return noiseTable[hashTable[x%n]],`
- ▶ This will be very fast.
- ▶ *Note: The sequence repeats every n integers, but that won't be as important when we move up to 2 and 3 dimensions.*

latticeNoise: a Simple Implementation

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- ▶ This will be very fast.
- ▶ *Note: The sequence repeats every n integers, but that won't be as important when we move up to 2 and 3 dimensions.*
- ▶ Do `noiseTable` and `hashTable` have to be the same size?

latticeNoise: A white noise value for lattice points



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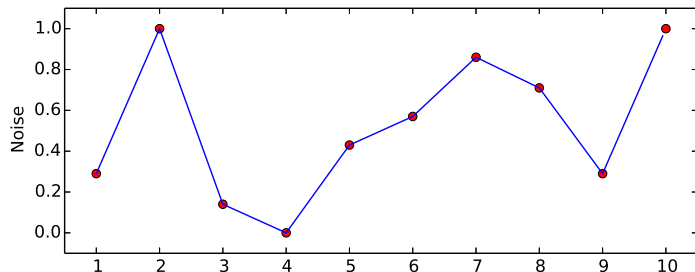


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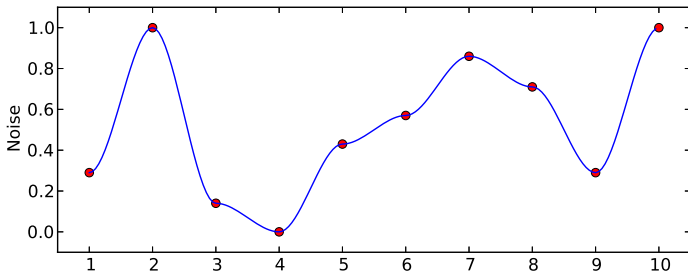
`latticeNoise(x): return noiseTable[hashTable[x%n]]`

lerpNoise: filling in between the lattice points



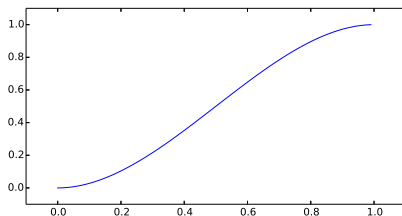
- ▶ One option is to use linear interpolation.
- ▶ Better than white noise.
- ▶ Easy to compute: `lerp(pct, a, b): a + pct*(b-a)`
- ▶ However, makes for a spikey curve, not like the noise we find in nature.

smerpNoise: Smoothly Interpolate Between the Integers



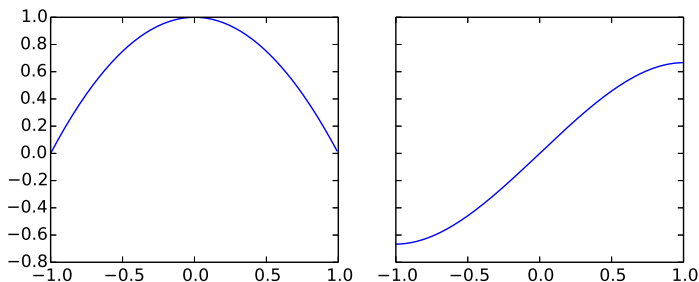
- ▶ This looks more like what we want.
- ▶ There are many ways to compute smooth curves through a set of points. Look up **B-splines**, **Hermite curves**, and **Bezier curves**.
- ▶ Here we want a simpler approach: an easily computable **S-curve** between each pair of points.

S-curve



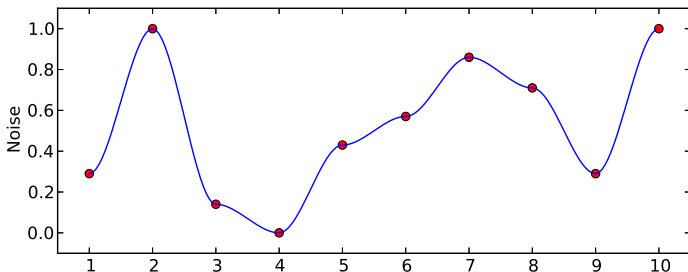
- ▶ There are many S-curves, such as the **logistic function**, or even the **cosine** function between 0 and π , but we can come up with our own easily enough. It would help if we could avoid transcendental functions, too. (Why?)
- ▶ The S-curve we need smoothly maps the 0-1 interval to itself, and is horizontal at both ends.
- ▶ What might be a good approach?

S-curve



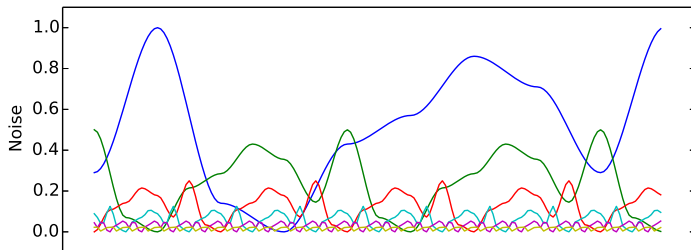
- ▶ On the left we plot $1 - x^2$. This is zero at ± 1 , which means any curve that has this as its derivative will be horizontal at ± 1
- ▶ On the right we plot $x - \frac{x^3}{3}$. Shifting and scaling leads to:
`smerp(pct, a, b):`
 `x = ???`
 `return a + (??? + ???*x - ???*x*x*x)*(b-a)`

smerpNoise: Smoothly Interpolate Between the Integers



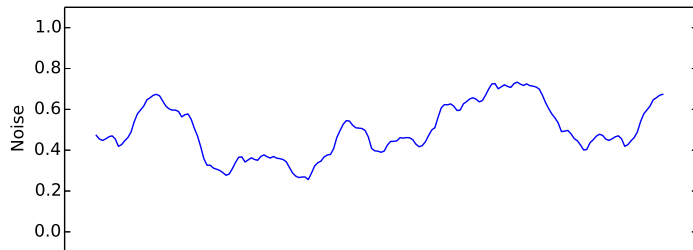
- ▶ The curve height is always between 0 and 1.
- ▶ The derivative of the curve is zero at lattice points.
- ▶ Highest and lowest points will always be at lattice points.
- ▶ Repeats after n lattice points.
- ▶ We would like the curve to have more detail at smaller scales, so we move on to *pink noise*.

Pink Noise



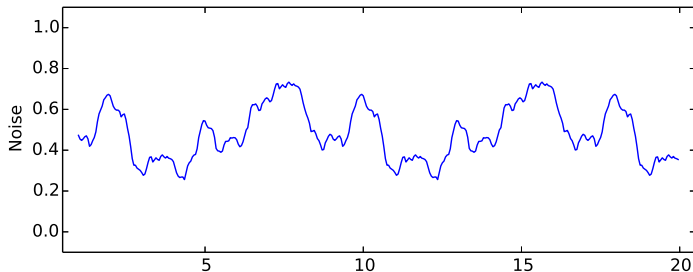
- ▶ Lattice distance is arbitrary, so we can scale the lattice frequency.
- ▶ We can also scale the maximum amplitude.
- ▶ Here we show curves for i from 0 to 5:
 - ▶ `smerpNoise(x*2**i)/2**i`
- ▶ Amplitude has a $1/f$ relationship to frequency.

Pink Noise



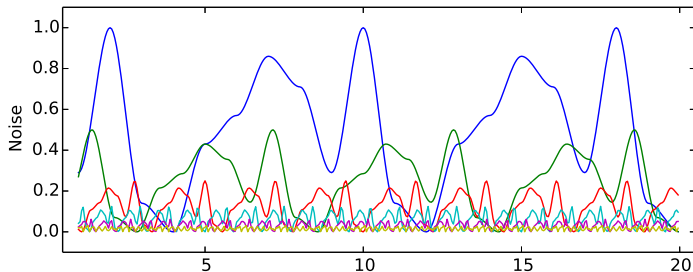
- ▶ Here we show the sum for i from 0 to 5 of:
 $\text{smerpNoise}(x*2**i)/2**i$
- ▶ Sum is divided by 2. Why?
- ▶ This is also an example of **fractal Brownian motion** (fBm).

Pink Noise



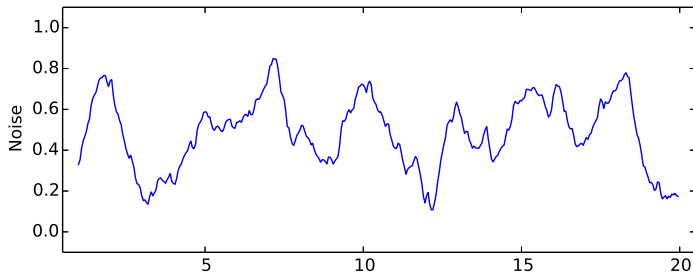
- ▶ If we look at a larger range, we can see that it still repeats after n integers. Why?
- ▶ Could we fix that? How?

Pink Noise without repeats



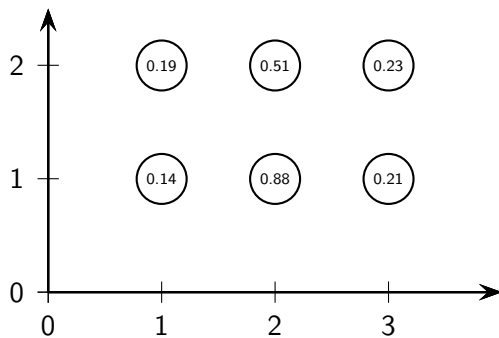
- We rescale each wavelength by a small amount, so they don't line up.

Pink Noise without repeats



- ▶ When we add them up they don't repeat for a long time.
- ▶ This would be even more effective with a larger n , e.g. 256.
- ▶ However, we won't do this because the problem will solve itself in higher dimensions.

Lattice Noise in 2D

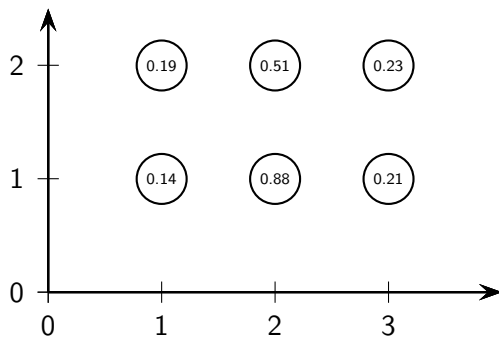


- For lattice noise in 2D we could use a two dimensional array of noise values, and a hashed lookup into that table:

```
latticeNoise(x,y):  
    noiseTable[hashTable[x%n] , hashTable[y%n]]
```

- ... but there's a better way.

Lattice Noise in 2D



- ▶ We hash both x and y to get a single lookup into the same one-dimensional noise table:

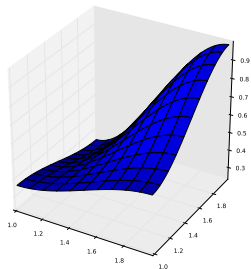
```
latticeNoise(x,y):  
    noiseTable[hashTable[(x + hashTable[y%n])%n]]
```

- ▶ This solves the repetition problem, too. Why?
- ▶ What would we do in 3D? 4D?

Smooth Noise in 2D

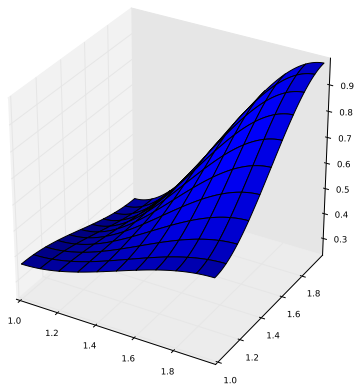
- Now that we have our random values at the corners, we need to smoothly interpolate the ones in between:

```
smerpNoise2(x, y):  
    intx = floor(x)  
    inty = floor(y)  
    pctx = x - intx  
    pcty = y - inty  
    aa = latticeNoise2(intx, inty)  
    ab = latticeNoise2(intx, inty+1)  
    ba = latticeNoise2(intx+1, inty)  
    bb = latticeNoise2(intx+1, inty+1)  
    xa = smerp(pctx, aa, ba)  
    xb = smerp(pctx, ab, bb)  
    return smerp(pcty, xa, xb)
```

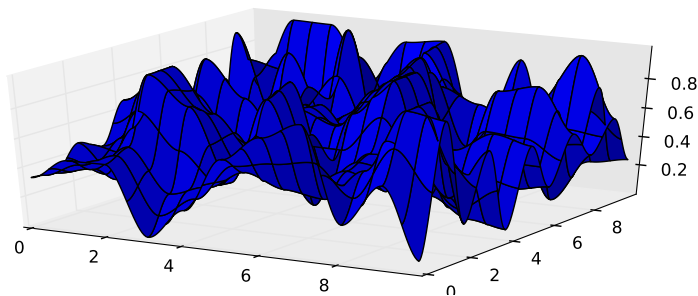


Smooth Noise in 2D

- ▶ What does the interpolation function look like in 3D?
- ▶ 4D?
- ▶ Do you see a problem?
- ▶ Look up **simplex noise**.

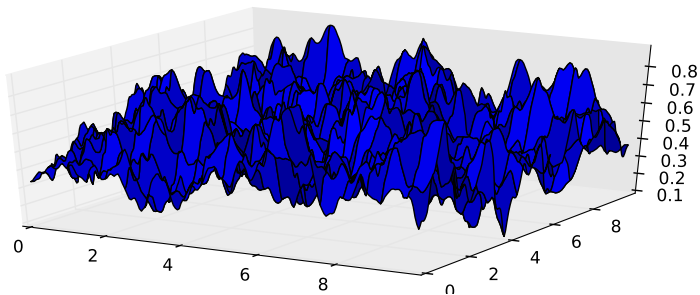


Smooth Noise in 2D



- Doing this over the whole lattice gives us smooth noise in 2D.

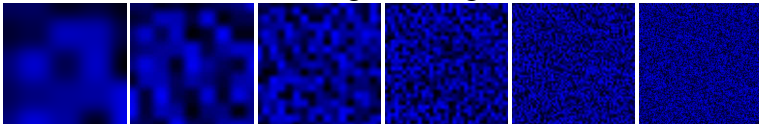
Pink Noise in 2D



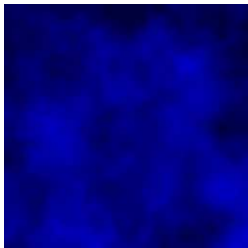
- If we add up many smooth noises of shorter wavelength and smaller amplitude we end up with 2D pink noise.

Pink Noise in 2D

- ▶ Smooth noises at diminishing wavelengths:



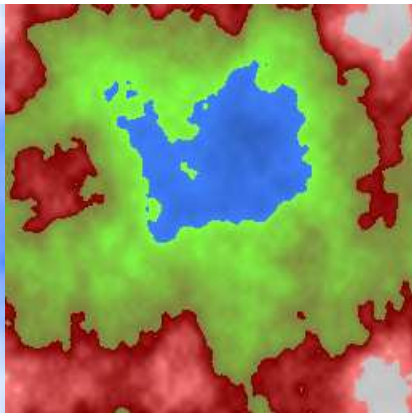
- ▶ The pink noise sum of the above, amplitude diminishing with wavelength:



Colorizing noise for different effects

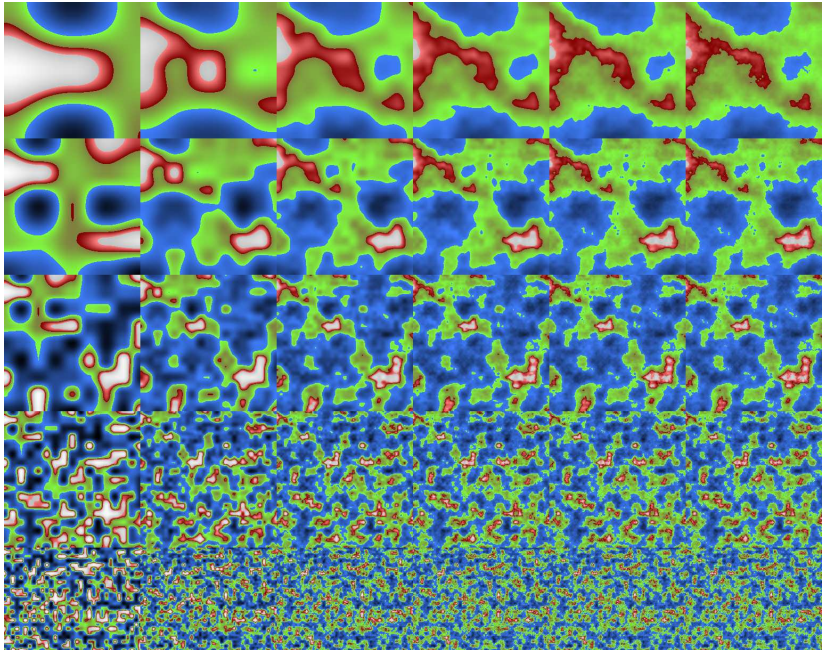


Sky

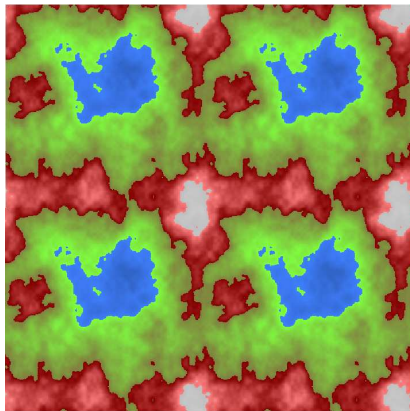
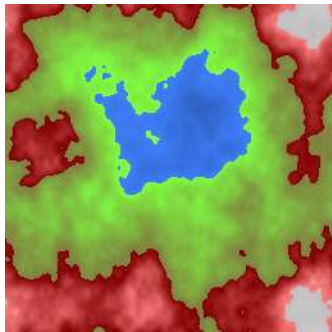


Terrain

Effects of starting wavelength and number of octaves

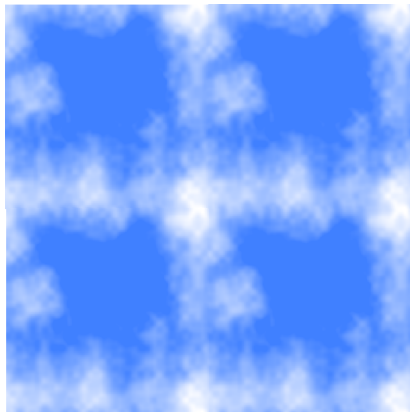


Tilable noise



- How can we do this?

Tilable noise



3D noise: solid textures and animations

