

## CSCI 510, Fall 2016, Homework # 4

YOUR NAME HERE

Due date: Wednesday, November 2, Midnight

1. Let  $A$  be a Turing-recognizable language consisting of Turing machines,  $\{\langle M_1 \rangle, \langle M_2 \rangle, \dots\}$ , where every  $M_i$  is a decider. Prove that some decidable language  $D$  is not decided by any decider  $M_i$  whose description appears in  $A$ .
2. Let  $A = \{\langle R \rangle \mid R \text{ is a regular expression describing a language containing at least one string } w \text{ that has } 111 \text{ as a substring (i.e. } w = x111y \text{ for some } x \text{ and } y)\}$ . Show that  $A$  is decidable.
3. Let  $A = \{\langle R, S \rangle \mid R \text{ and } S \text{ are regular expressions and } L(R) \subseteq L(S)\}$ . Show that  $A$  is decidable.