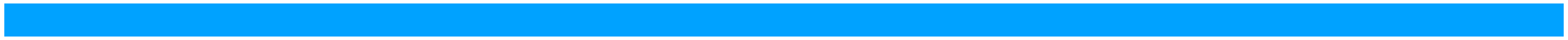


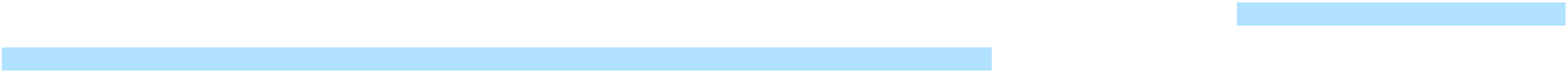
*Proof.* Let  $\square ABCD$  be a Saccheri quadrilateral with altitude  $\overline{EF}$  with  $F \in \overleftrightarrow{AB}$ . By the elliptic parallel postulate, the lines  $\overleftrightarrow{AB}$  and  $\overleftrightarrow{DC}$  must intersect at some point, say  $P$ . Relative to the ideal line  $\overleftrightarrow{AD}$ , we may say that  $F - B - P$  and  $E - C - P$ .

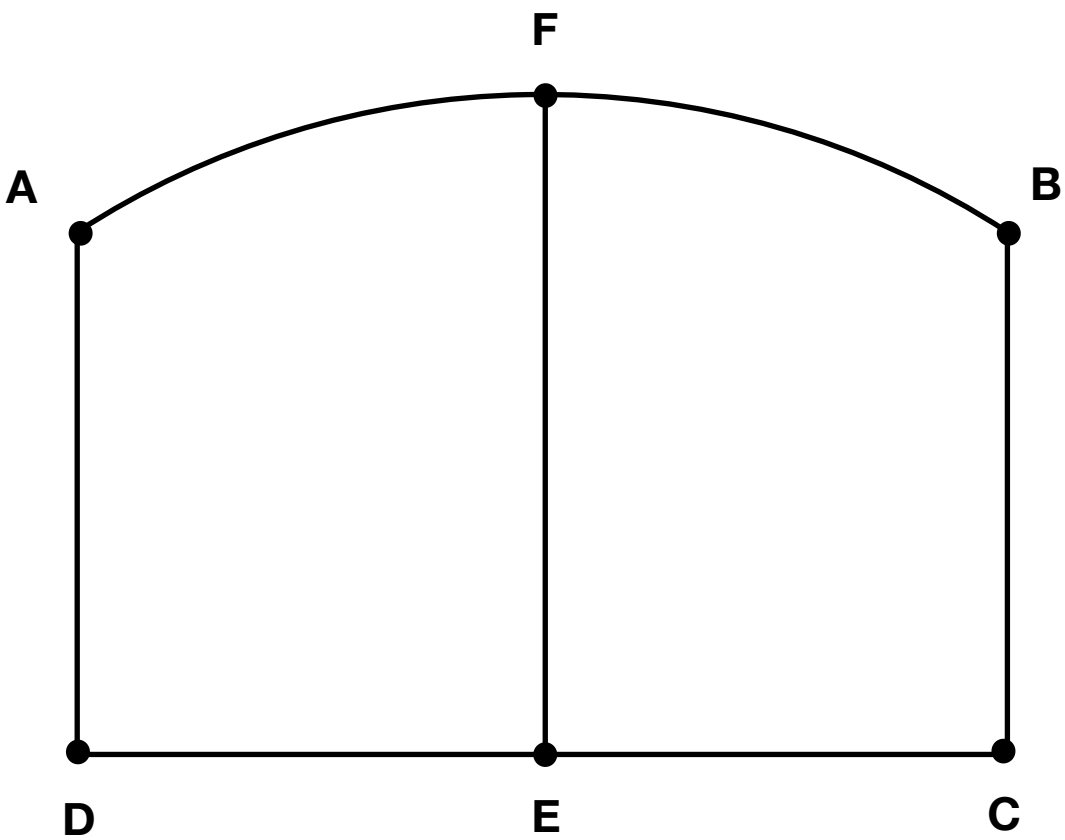
Since  $\triangle EFP$  is a double-right triangle, Theorem 6.8.4 shows that  $\overline{EP}$  and  $\overline{FP}$  are polar lengths. Also,  $\triangle BPC$  is a right, with  $m\angle B = 90^\circ$ . By Theorem 6.8.4,  $\angle BCP$  is acute since  $\overline{BP} < \overline{FP}$  (relative to  $\overleftrightarrow{AD}$ ). Then its supplement,  $\angle BCE$  is obtuse.  $\square$

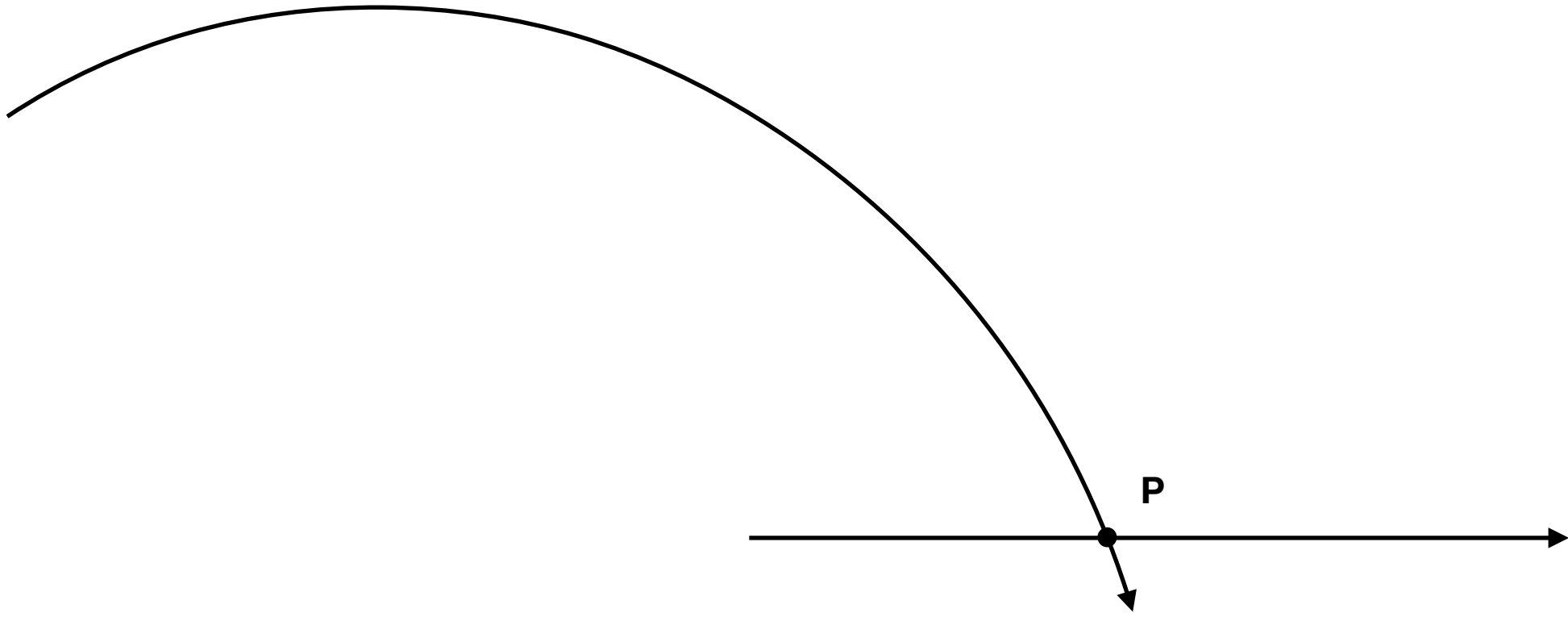




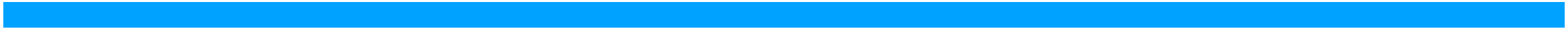










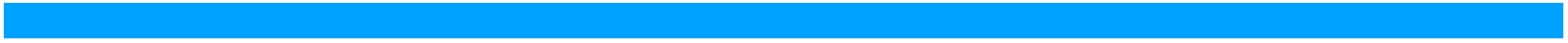


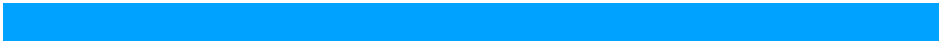




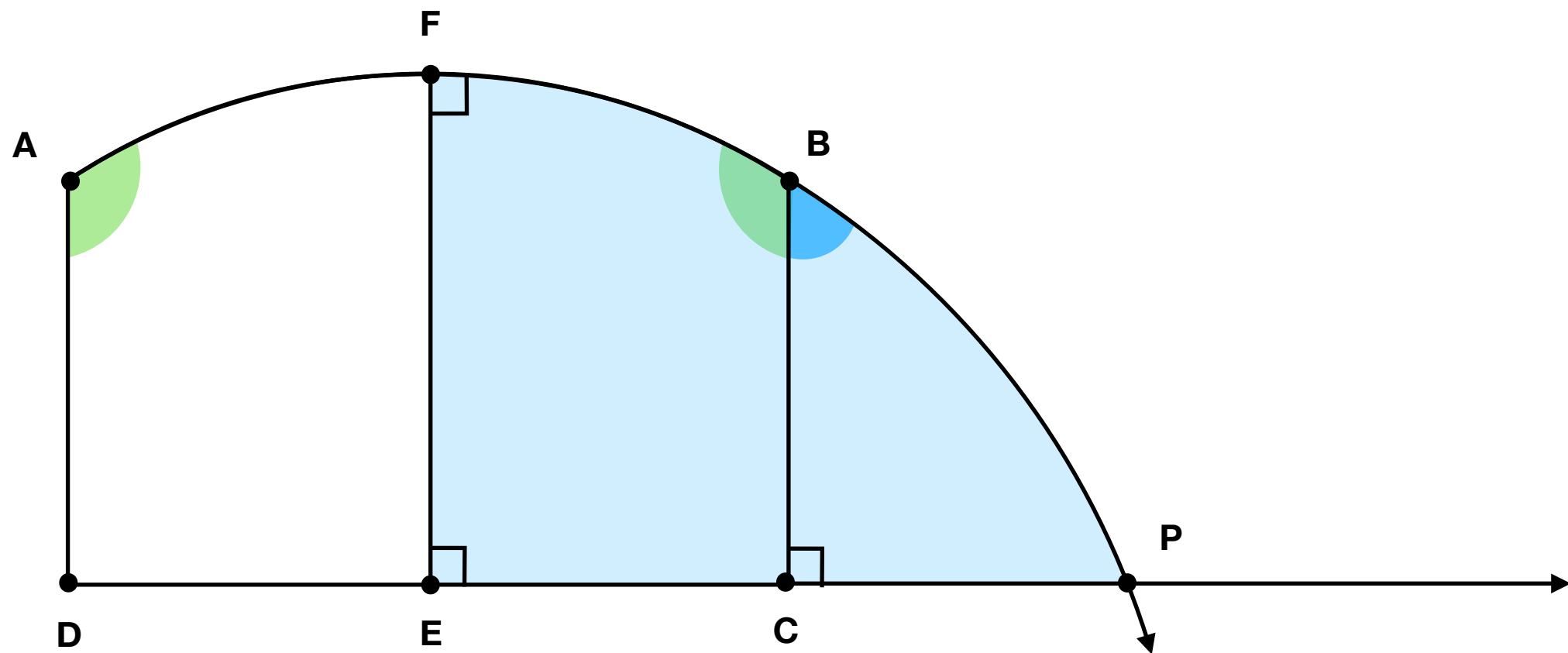












*Proof.* Let  $\square ABCD$  be a Saccheri quadrilateral with altitude  $\overline{EF}$  with  $F \in \overleftrightarrow{AB}$ . By the elliptic parallel postulate, the lines  $\overleftrightarrow{AB}$  and  $\overleftrightarrow{DC}$  must intersect at some point, say  $P$ . Relative to the ideal line  $\overleftrightarrow{AD}$ , we may say that  $F - B - P$  and  $E - C - P$ .

Since  $\triangle EFP$  is a double-right triangle, Theorem 6.8.4 shows that  $\overline{EP}$  and  $\overline{FP}$  are polar lengths. Also,  $\triangle BPC$  is a right, with  $m\angle C = 90^\circ$ . By Theorem 6.8.4,  $\angle BCP$  is acute since  $\overline{BP} < \overline{FP}$  (relative to  $\overleftrightarrow{AD}$ ). Then its supplement,  $\angle BCE$  is obtuse.  $\square$