

 $\triangle ABC = \triangle AB''C'' \cup \triangle B''C''B \cup \triangle BCC''.$ The additivity of defects implies that

By the convexity of $\triangle ABC$, the triangle can be partitioned into the union of three triangles, namely

 $d(\triangle ABC) = d(\triangle AB''C'') + d(\triangle B''C''B) + d(\triangle BCC) = d(\triangle ABC) + d(\triangle B''C''B) + d(\triangle BCC)$ $\Rightarrow 0 = d(\triangle B''C''B) + d(\triangle BCC).$

Given that defects are always positive, the above equation leads to a contradiction.



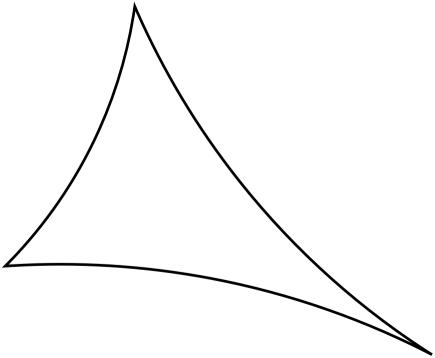


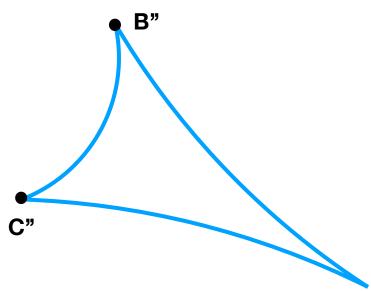




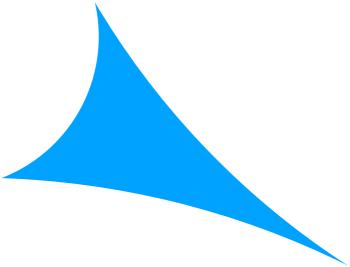


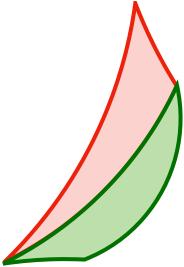






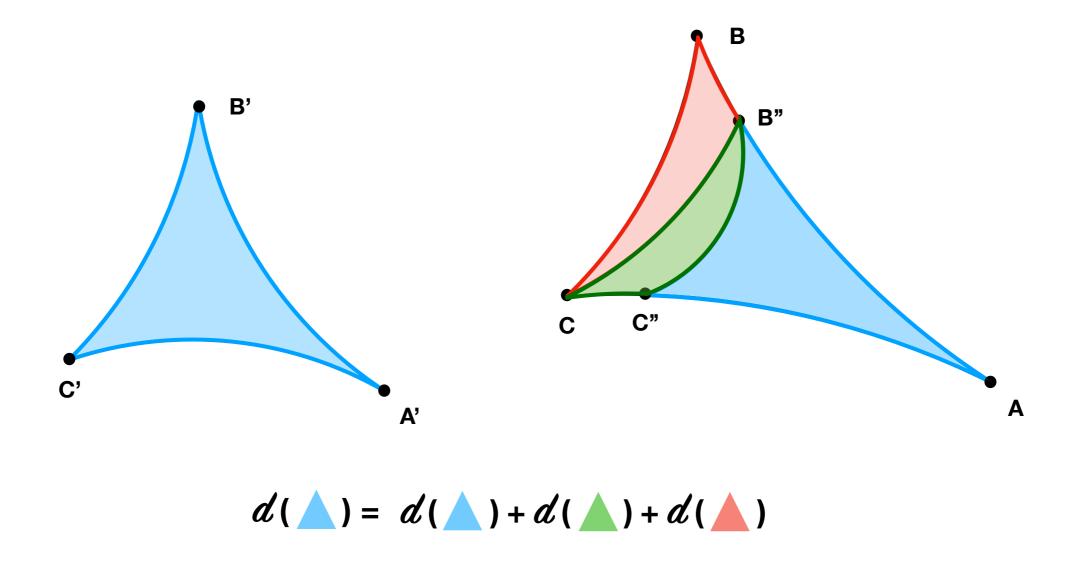






$$d(\triangle) = d(\triangle) + d(\triangle) + d(\triangle)$$





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The additivity of defects implies that

$$d(\triangle ABC) = d(\triangle AB''C'') + d(\triangle B''C''B) + d(\triangle BCC) = d(\triangle ABC) + d(\triangle B''C''B) + d(\triangle BCC)$$
$$\Rightarrow \mathbf{0} = d(\triangle B''C''B) + d(\triangle BCC).$$

Given that defects are always positive, the above equation leads to a contradiction.