

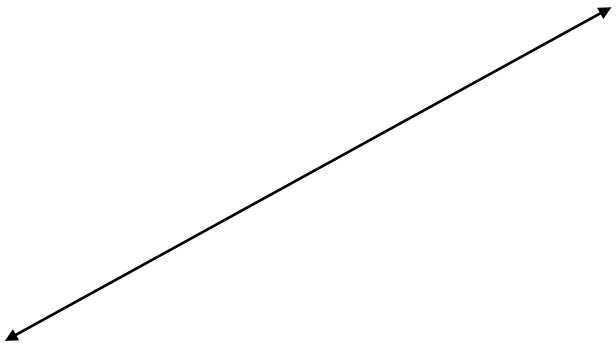
also immediate from extension with the point B and D being switched. Let F be a point not on ℓ and consider the line $m = \overrightarrow{BF}$. By Extension, there exists a point G on m such that B - F - G. Let $n = \overrightarrow{DG}$. By Extension, there exists a point H on n such that G - D - H. Finally,

Proof. The existence of point E is immediate from the Extension Axiom. Likewise, the existence of A is

consider the line \overrightarrow{FH} . This lines intersects m at the unique point F. Thus, $B, G \notin \overrightarrow{FH}$. Also, \overrightarrow{FH} intersects n at the unique point H. Thus, $D \notin \overrightarrow{FH}$. But as was mentioned earlier, \overrightarrow{FH} intersects \overrightarrow{BG} at F. Thus, Pasch's Axiom applies so that \overrightarrow{FH} intersects \overline{BD} or \overline{GD} . Again, \overrightarrow{FH} intersects n at the unique point H, but G - D - H. So, \overrightarrow{FH} does not intersect \overline{DG} . We conclude that \overrightarrow{FH} intersects \overline{BD} at a point called C. Therefore, B-C-D.

























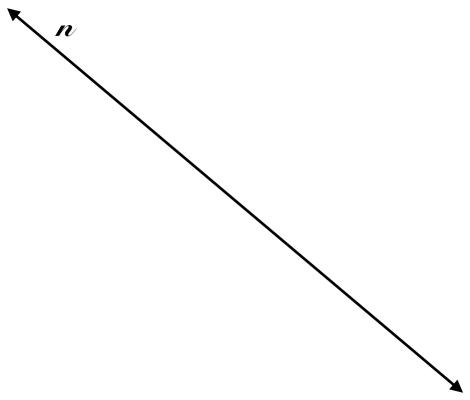












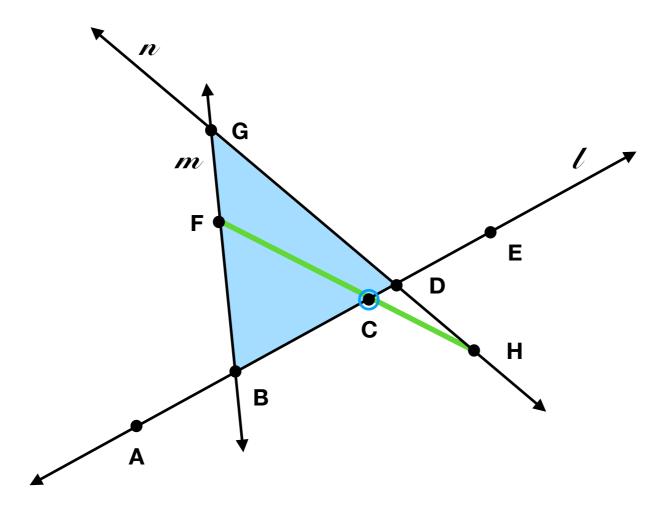












Proof. The existence of point E is immediate from the Extension Axiom. Likewise, the existence of A is also immediate from extension with the point B and D being switched.

Let F be a point not on ℓ and consider the line $m = \overrightarrow{BF}$. By Extension, there exists a point G on m such that G - D - H. Finally, consider the line FH. This lines intersects m at the unique point F. Thus, $G \notin FH$ intersects G at G