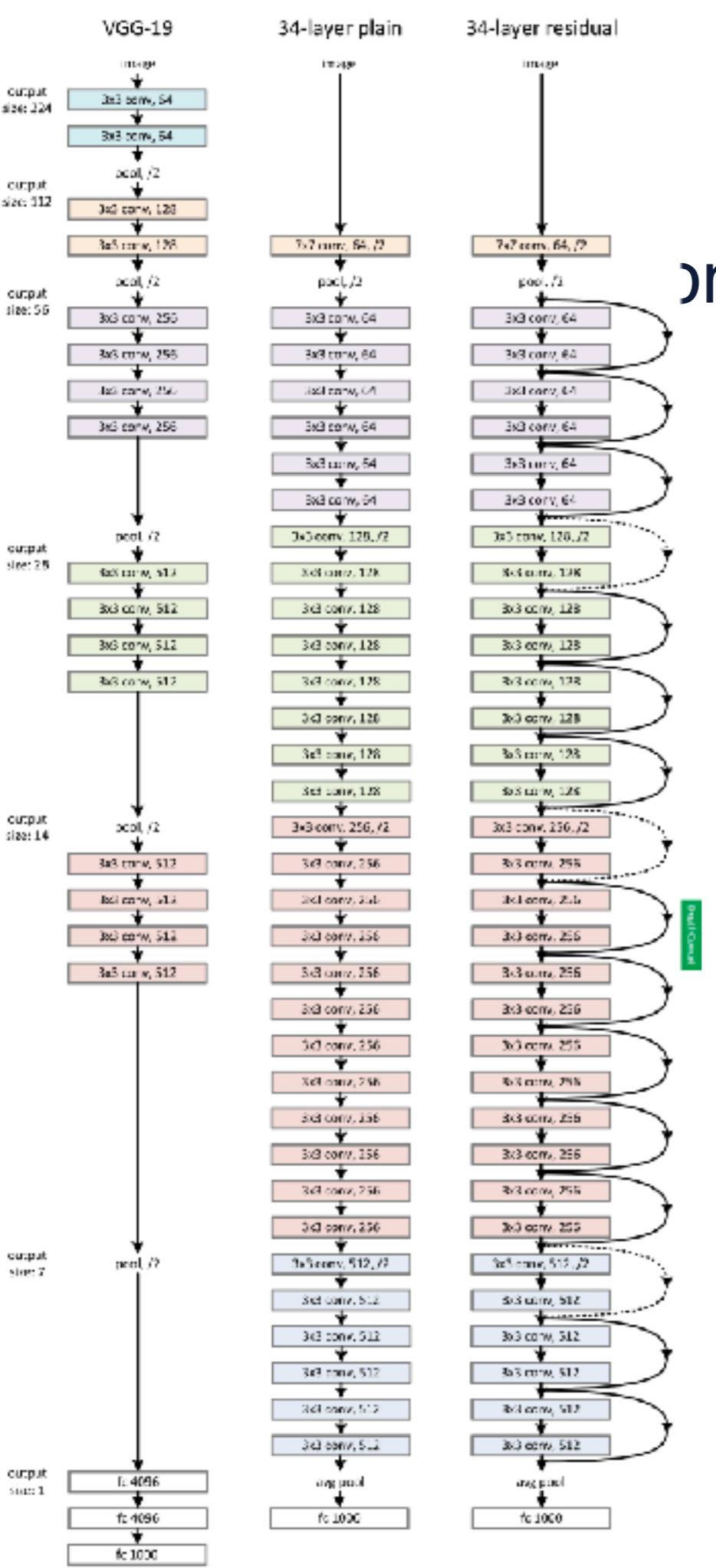


# **Deep Learning for 3D Recognition**

Instructor: Hao Su  
Presenter: Jiayuan Gu

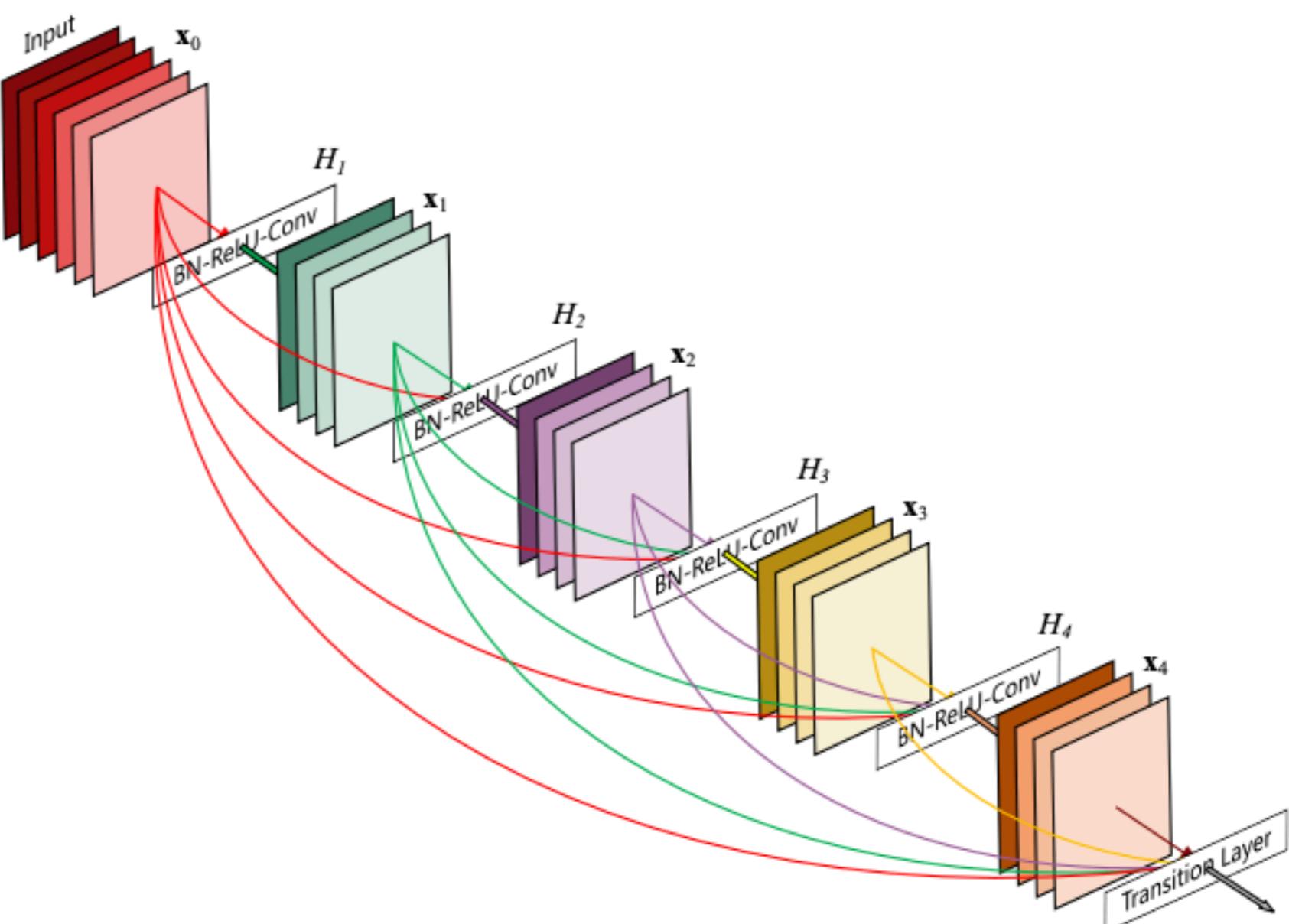
# Goal

- Get an idea of the state-of-the-art 3D deep learning methods
- Learn the underlying mathematic

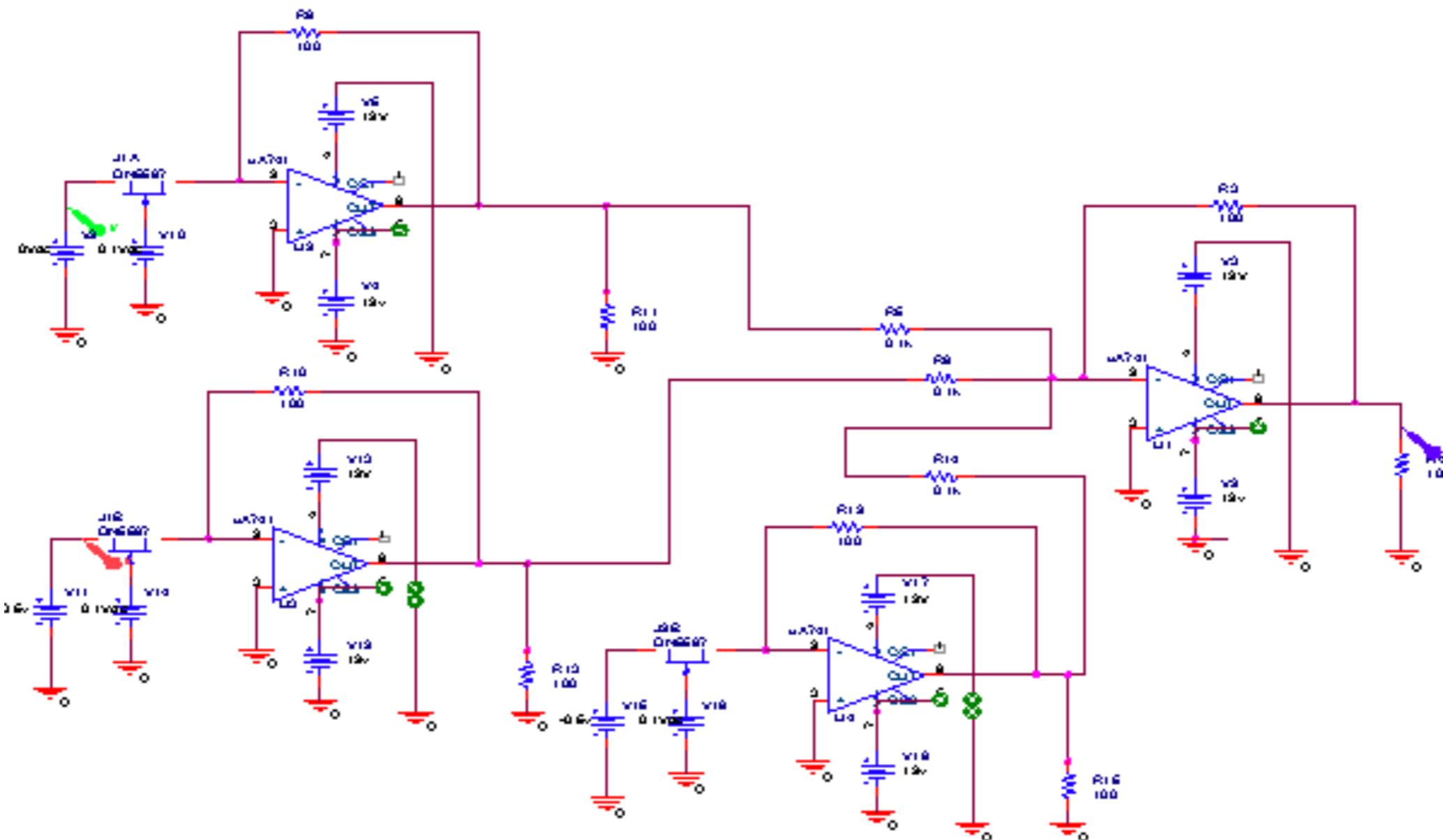


# 2D Vision

# What dominates current 2D computer vision?

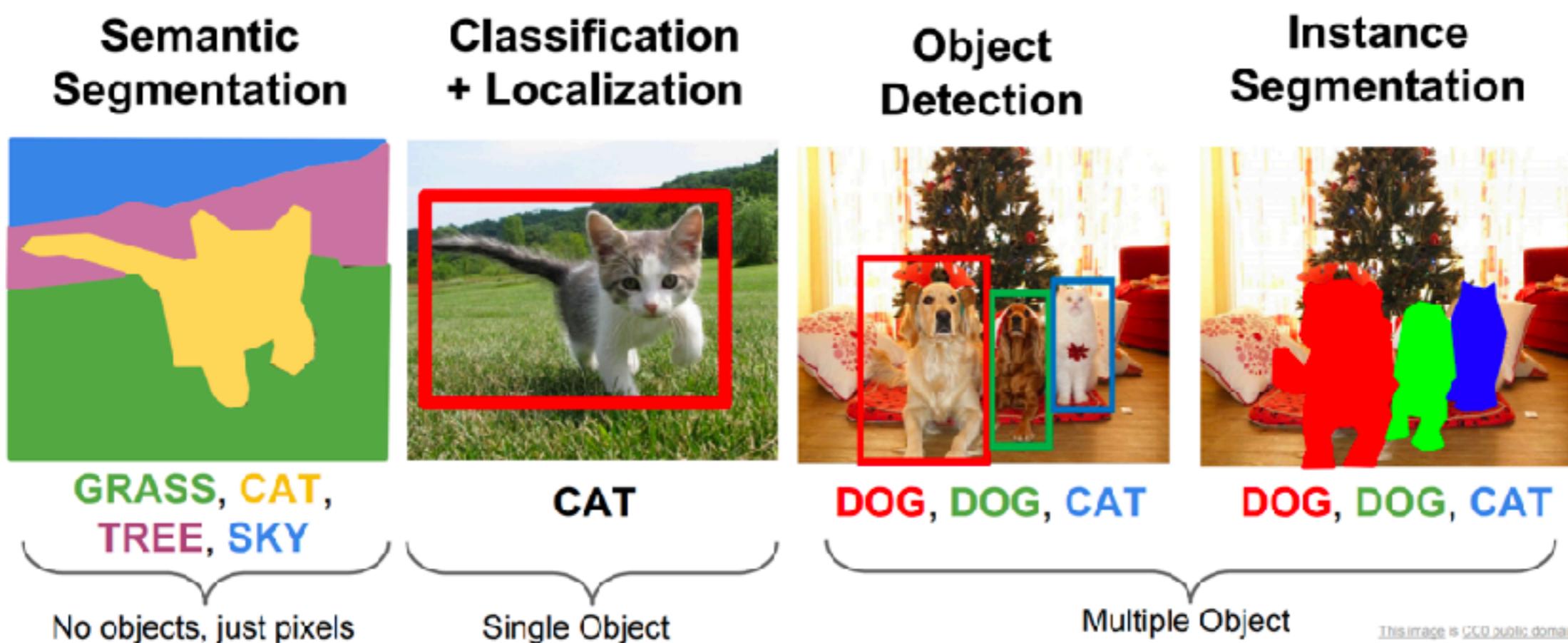


# In the future...

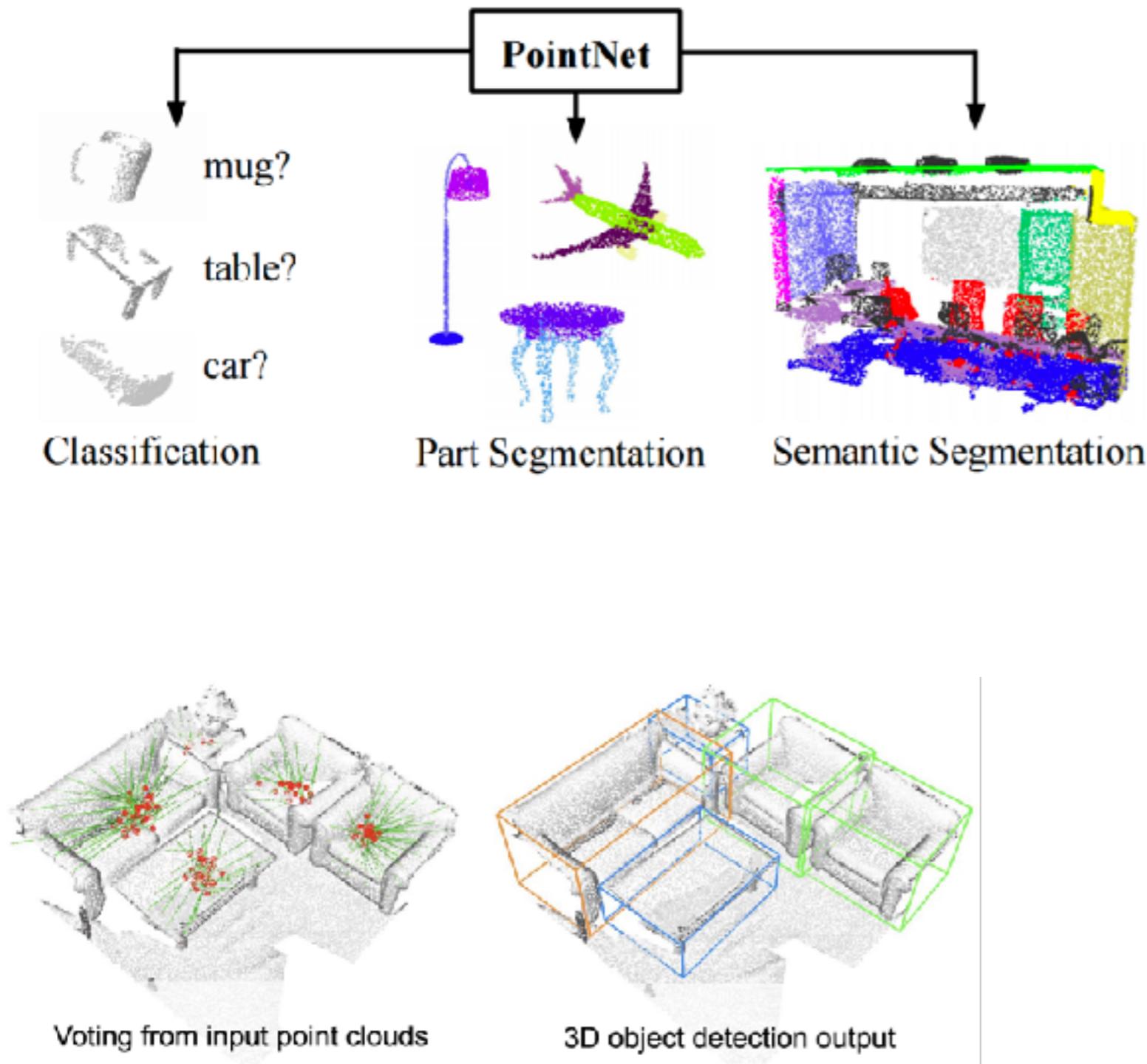


# What tasks do 2D CNNs solve?

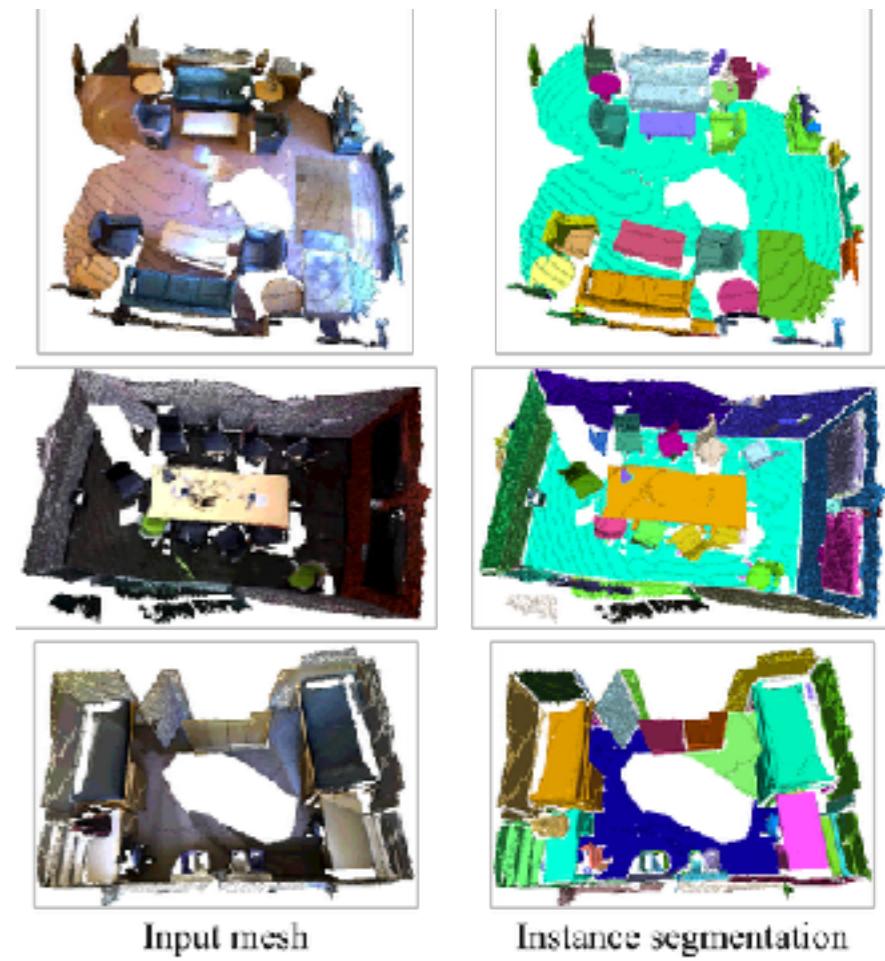
- Classification
- Detection
- Semantic Segmentation
- Instance Segmentation



# 3D tasks

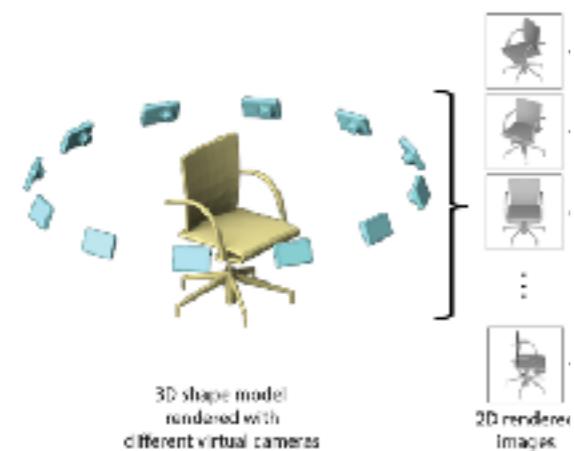


Detection

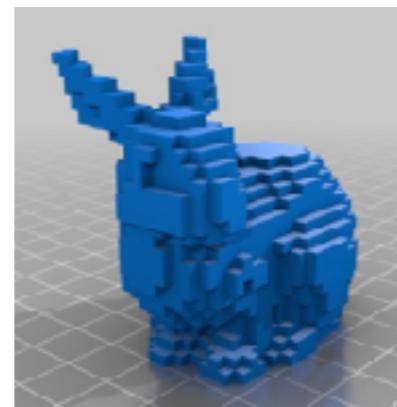


Instance segmentation

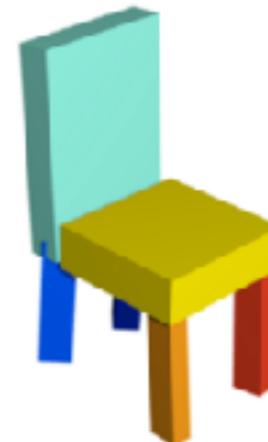
# The Representation Challenge of 3D Deep Learning



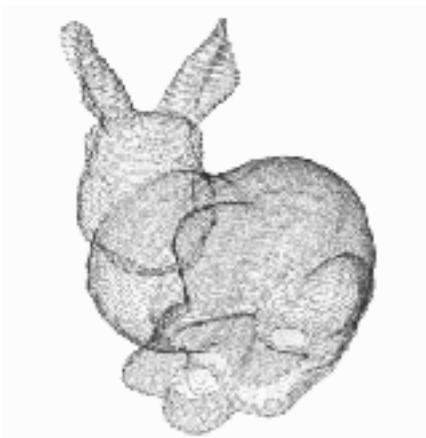
Multi-view



Volumetric



Part Assembly



Point Cloud



Mesh (Graph CNN)

$$F(x) = 0$$

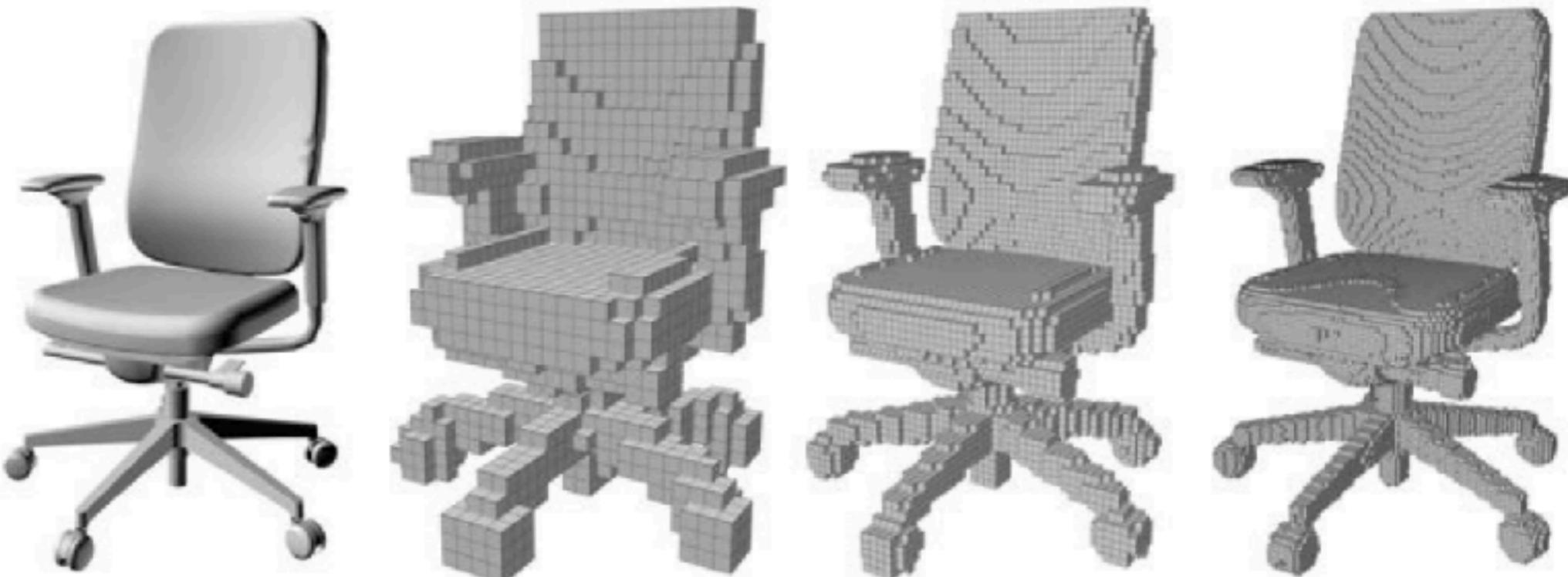
Implicit Shape

# The Representation Challenge of 3D Deep Learning

**Rasterized form  
(regular grids)**

**Geometric form  
(irregular)**

# Sparsity of 3D Shapes



Occupancy:

10.41%

5.09%

2.41%

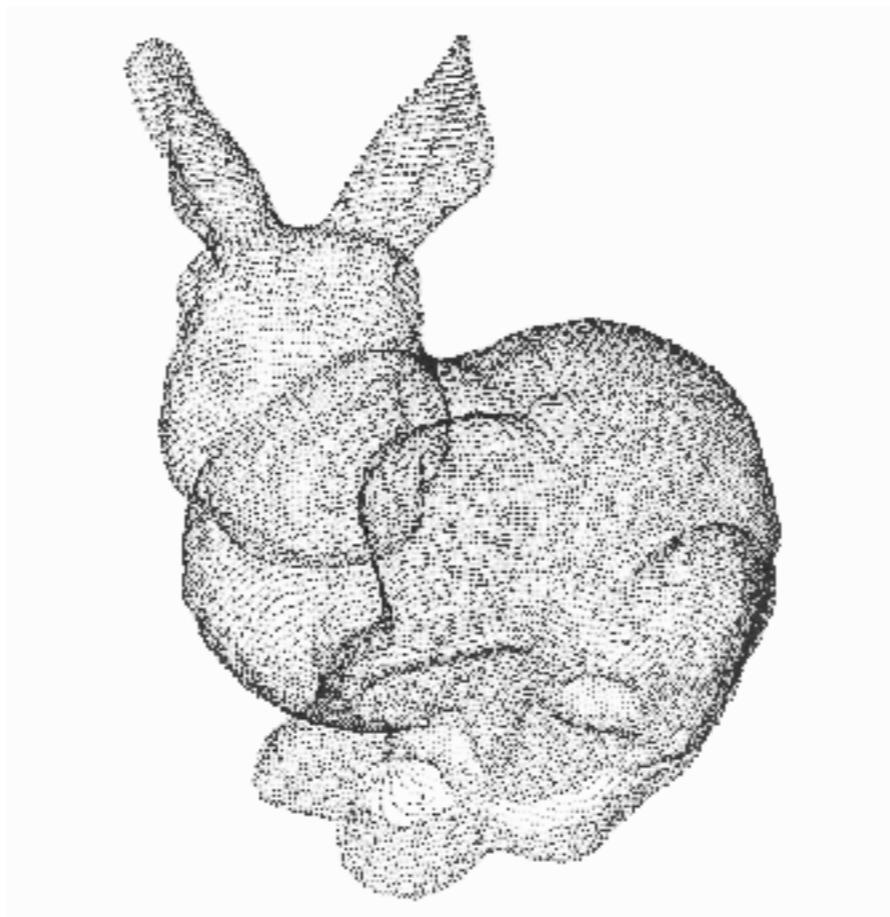
Resolution:

32

64

128

It is computationally expensive to do 3D convolution!



**Point cloud**  
(The most common 3D sensor data)

# Agenda

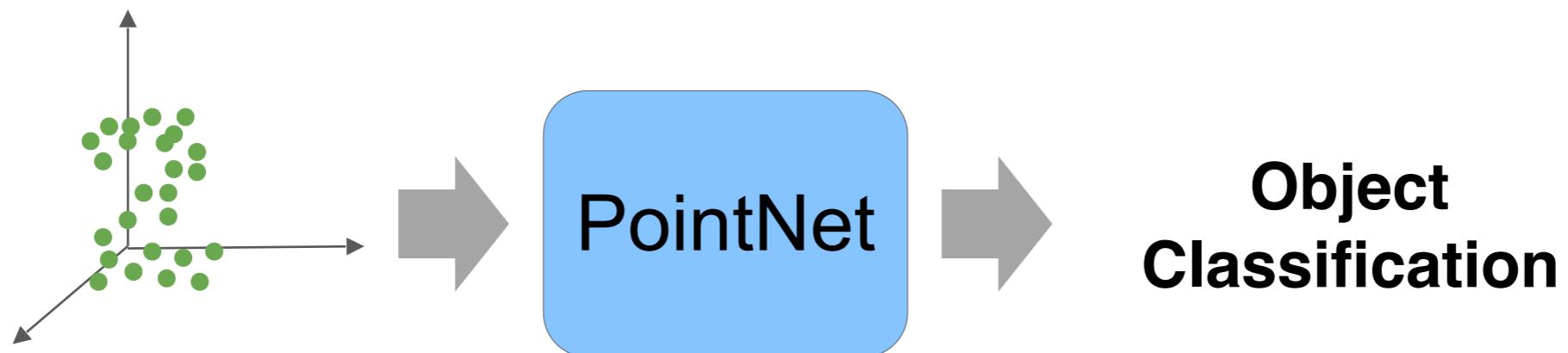
- 3D Classification
  - PointNet
- 3D Segmentation
  - SparseConv
- 3D Detection
  - VoteNet

# POINTNET

Qi, Charles R., et al. "Pointnet: Deep learning on point sets for 3d classification and segmentation." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2017.

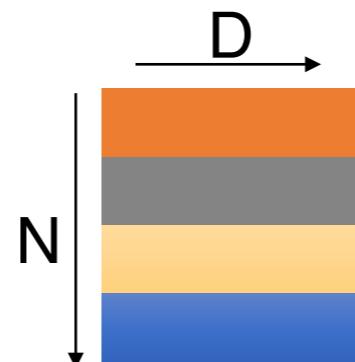
# Directly Process Point Cloud Data

End-to-end learning for **unstructured, unordered** point data



# Permutation invariance

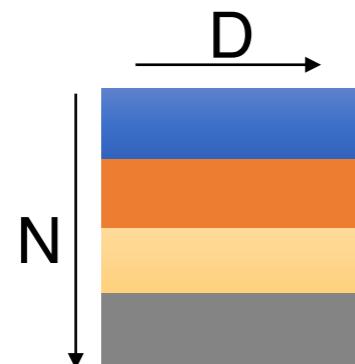
Point cloud: N **orderless** points, each represented by a D dim coordinate



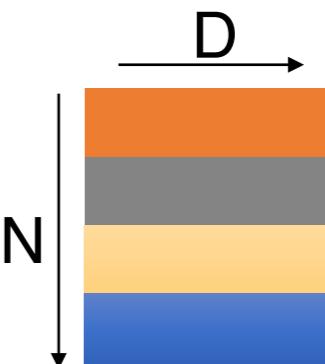
2D array representation

# Permutation invariance

Point cloud: N **orderless** points, each represented by a D dim coordinate



represents the same **set** as



2D array representation

# Symmetric Function

$$f(x_1, x_2, \dots, x_n) = f(x_{i_1}, x_{i_2}, \dots, x_{i_n})$$

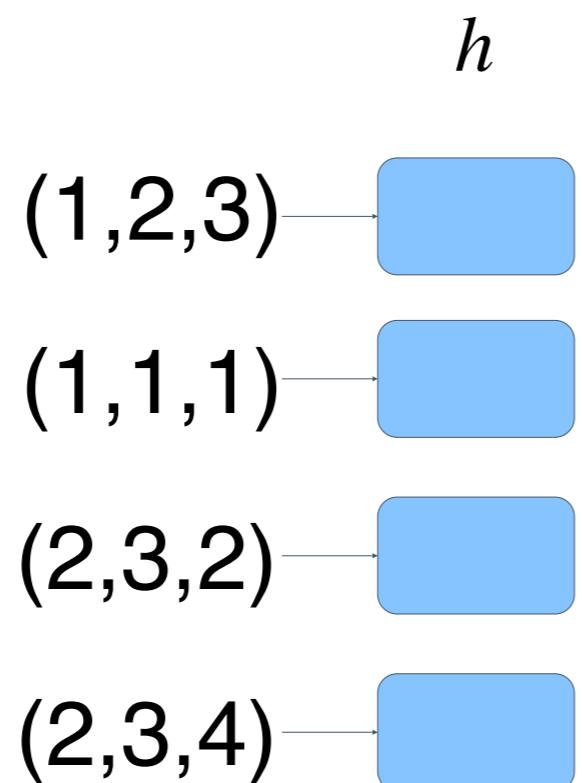
$$\mathbf{sum:} f(x_1, x_2, \dots, x_n) = \sum_{i=1}^N x_i$$

$$\mathbf{max:} f(x_1, x_2, \dots, x_n) = \max_{i=1}^N x_i$$

# Construct a Symmetric Function

**Observe:**

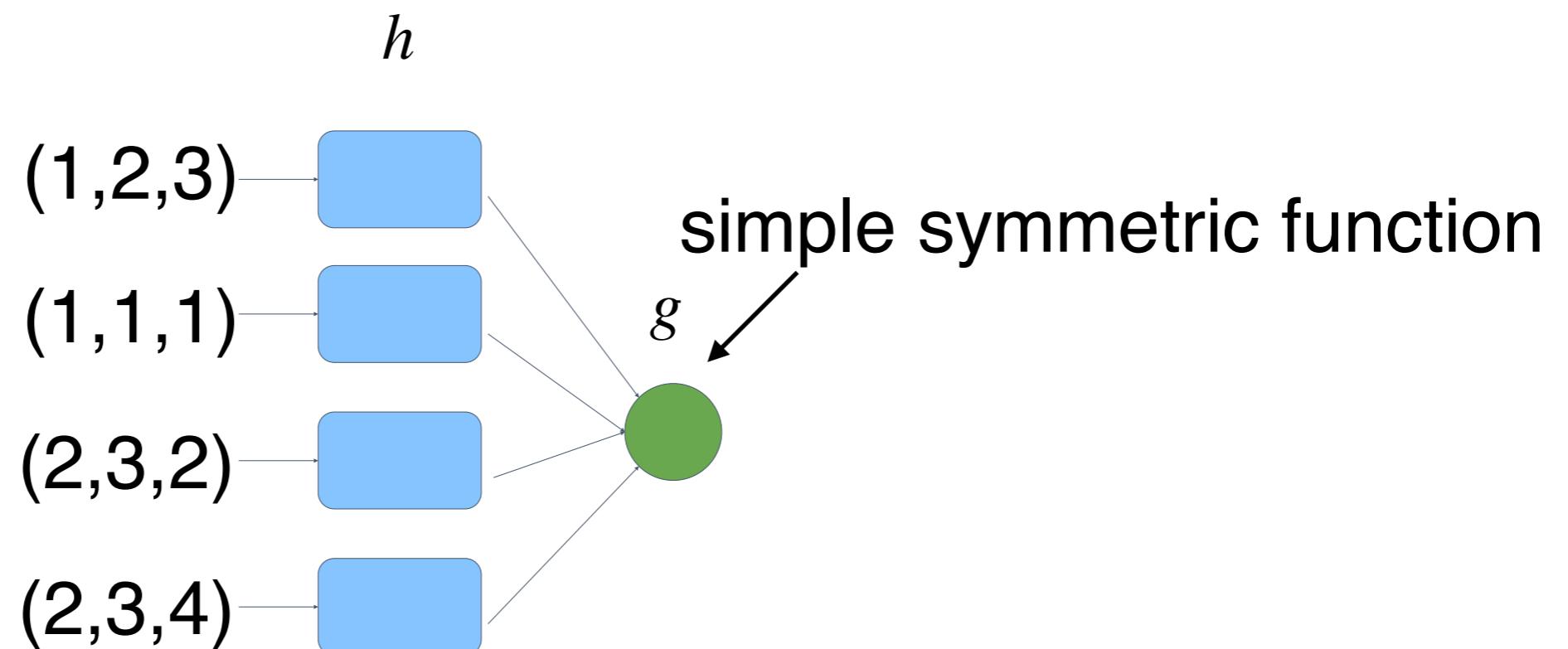
$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric



# Construct a Symmetric Function

Observe:

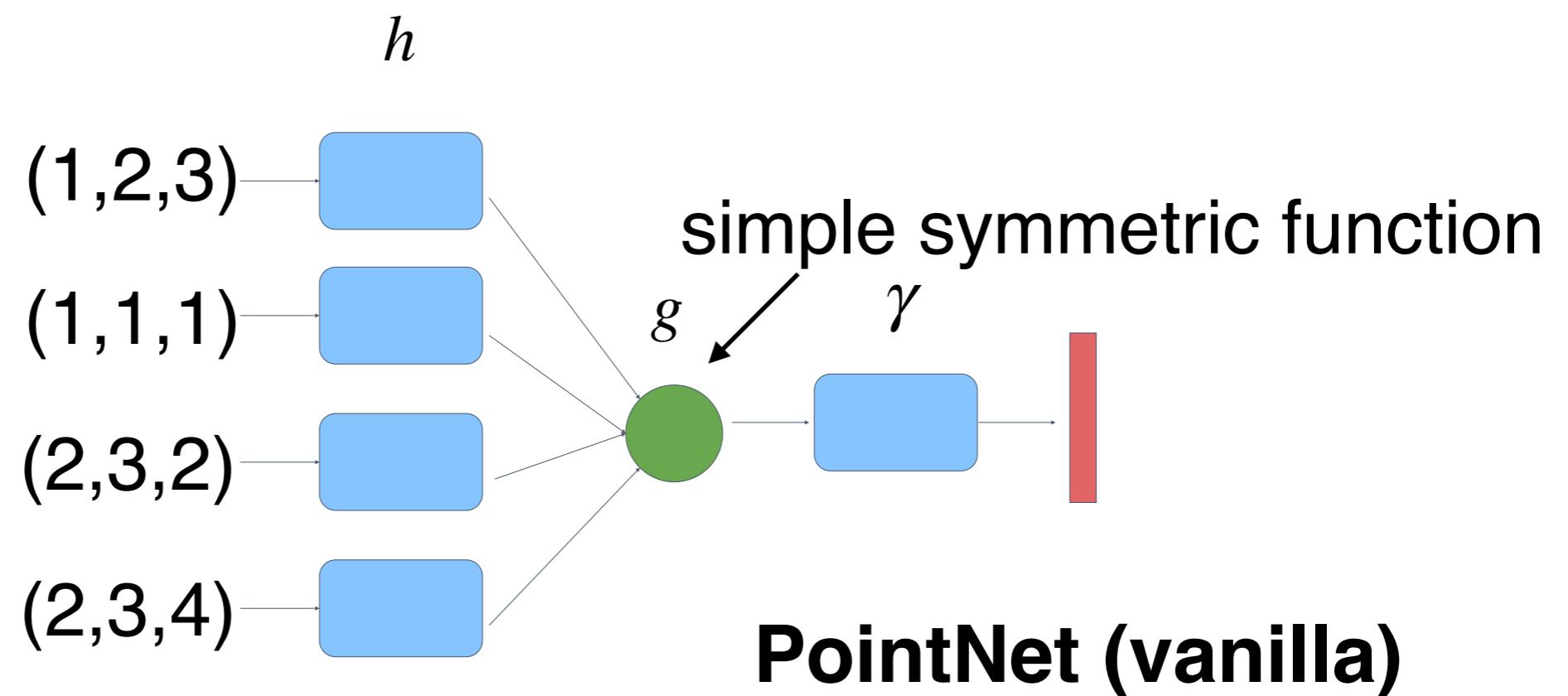
$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric



# Construct a Symmetric Function

Observe:

$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric



# Advanced Topic

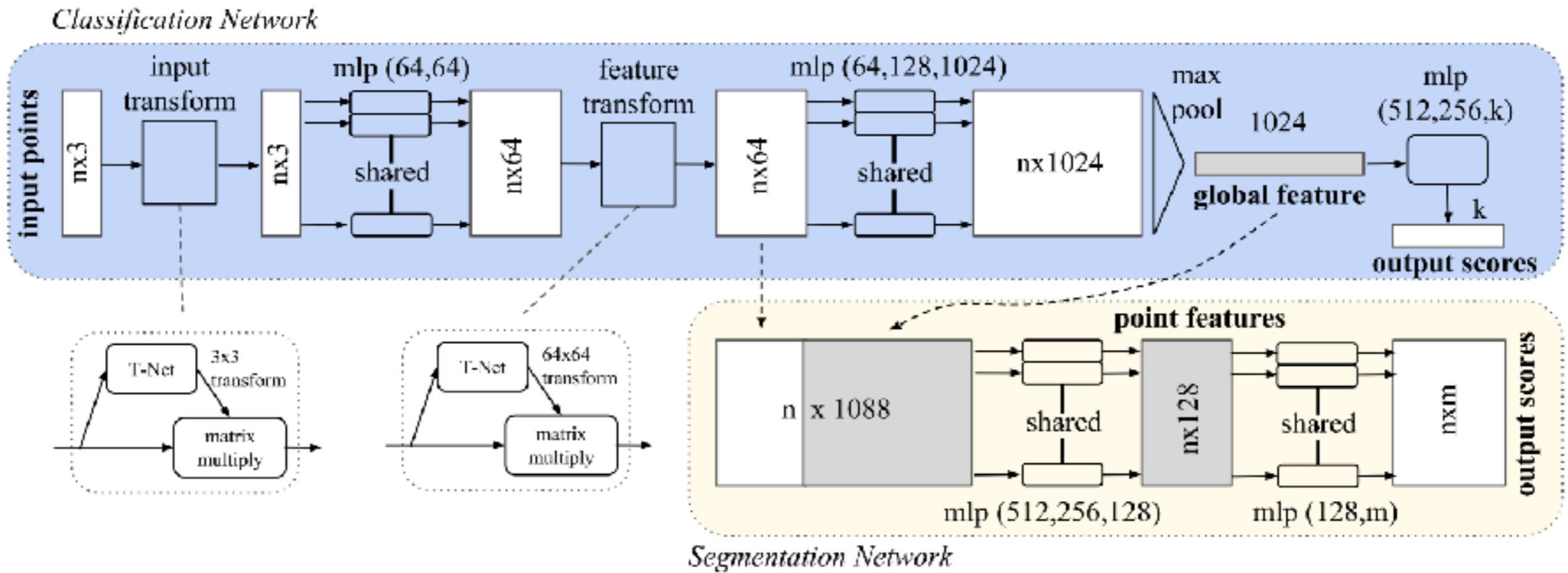
- Is PointNet a universal function approximator of any symmetric function?
- In other words, can we use PointNet to approximate any symmetric function as close as we want?

**Theorem 1.** Suppose  $f : \mathcal{X} \rightarrow \mathbb{R}$  is a continuous set function w.r.t Hausdorff distance  $d_H(\cdot, \cdot)$ .  $\forall \epsilon > 0$ ,  $\exists$  a continuous function  $h$  and a symmetric function  $g(x_1, \dots, x_n) = \gamma \circ \text{MAX}$ , such that for any  $S \in \mathcal{X}$ ,

$$\left| f(S) - \gamma \left( \text{MAX}_{x_i \in S} \{h(x_i)\} \right) \right| < \epsilon$$

where  $x_1, \dots, x_n$  is the full list of elements in  $S$  ordered arbitrarily,  $\gamma$  is a continuous function, and  $\text{MAX}$  is a vector max operator that takes  $n$  vectors as input and returns a new vector of the element-wise maximum.

# Beyond classification



**Concatenate the global feature with each point feature  
Do a point-wise classification = semantic segmentation**

# Robustness

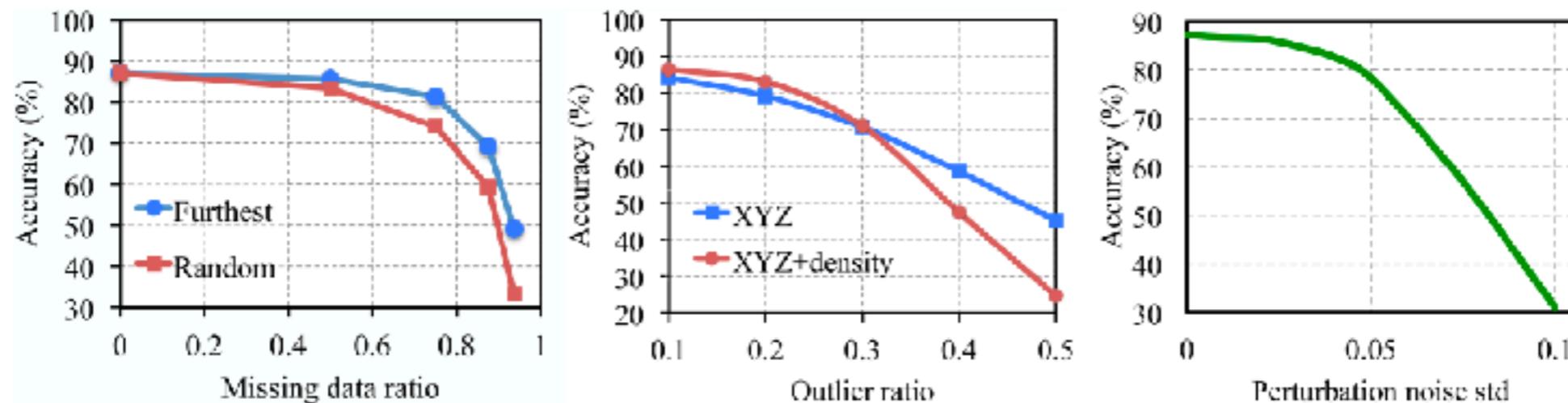
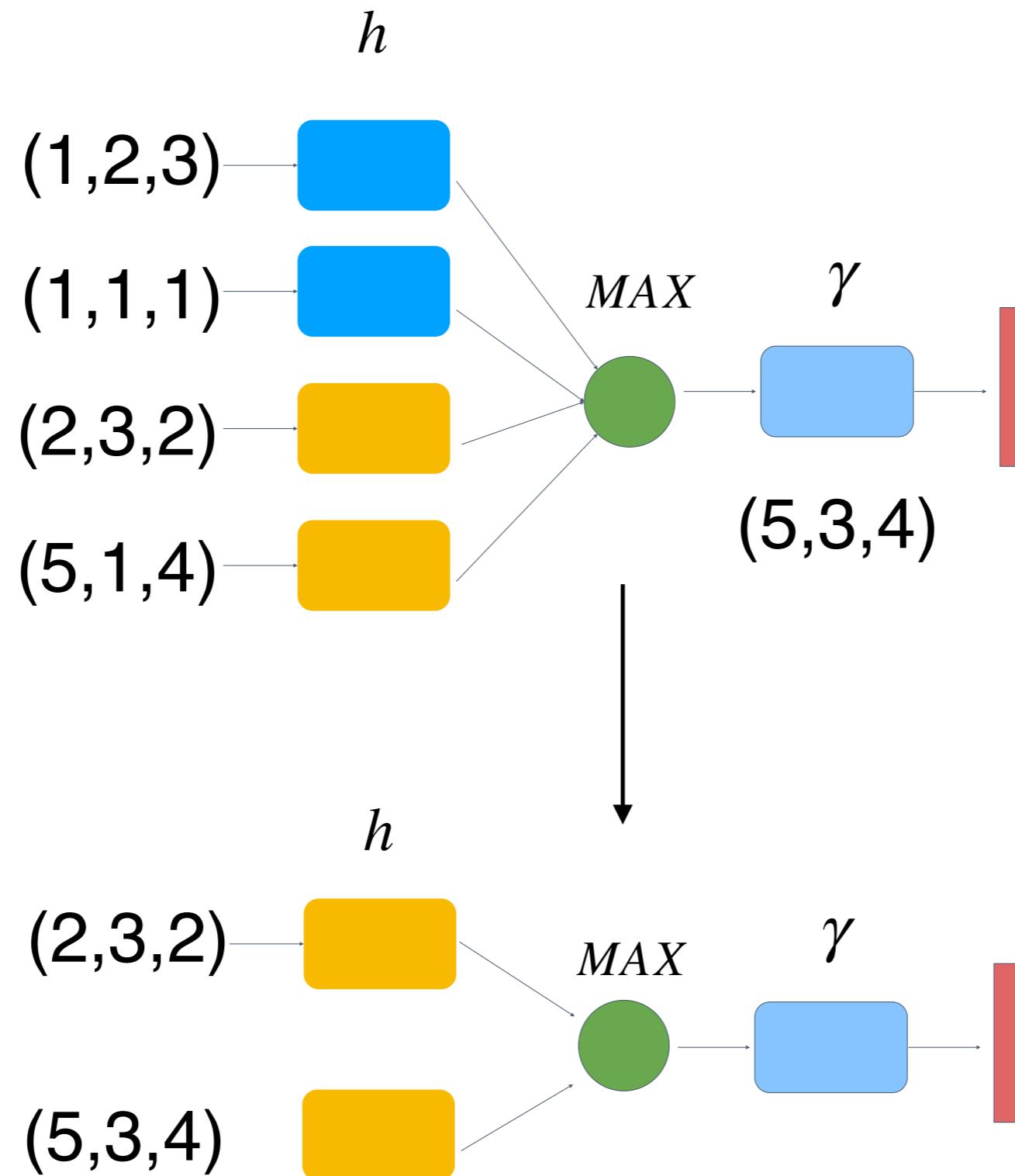


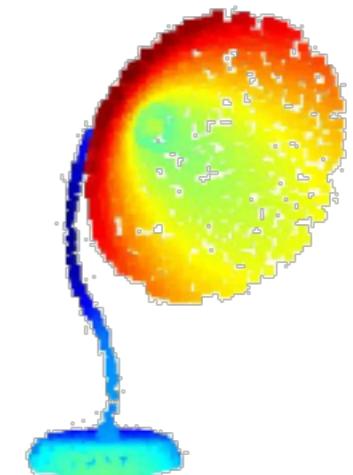
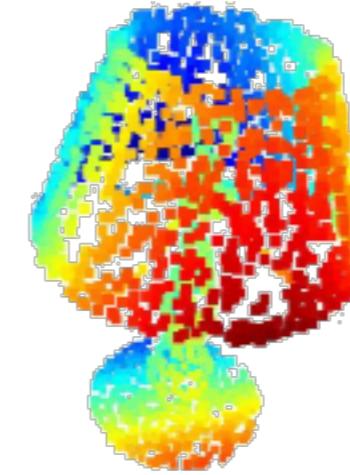
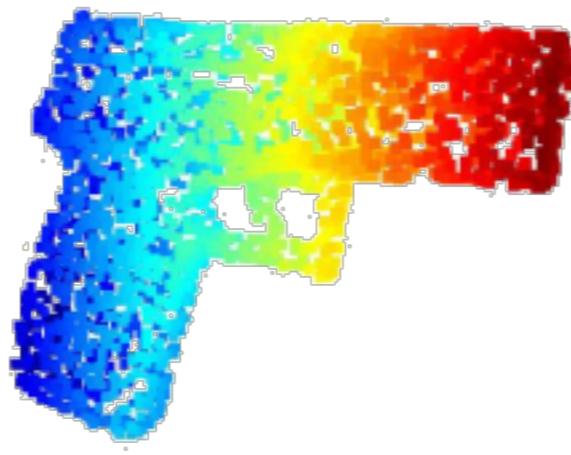
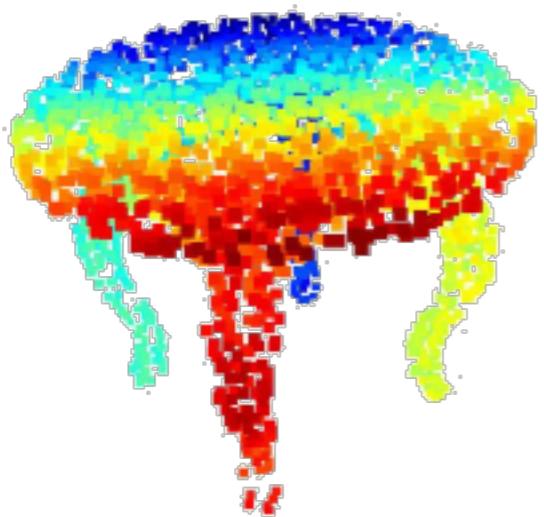
Figure 6. **PointNet robustness test.** The metric is overall classification accuracy on ModelNet40 test set. Left: Delete points. Furthest means the original 1024 points are sampled with furthest sampling. Middle: Insertion. Outliers uniformly scattered in the unit sphere. Right: Perturbation. Add Gaussian noise to each point independently.

# Critical points

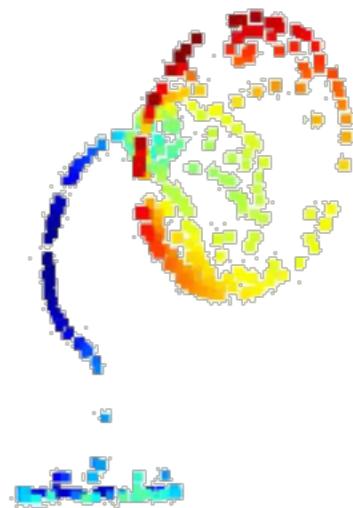
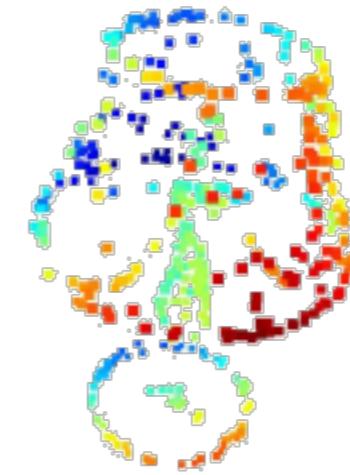
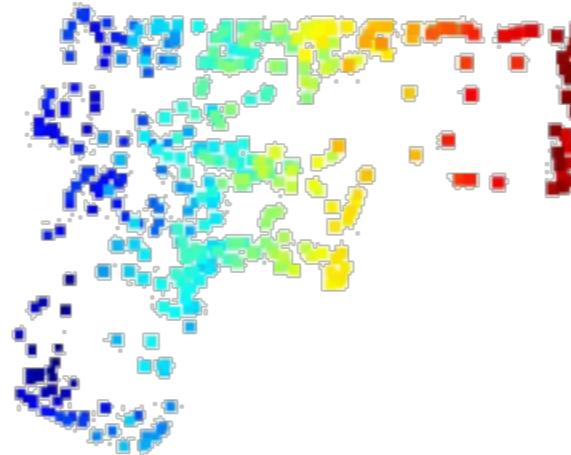
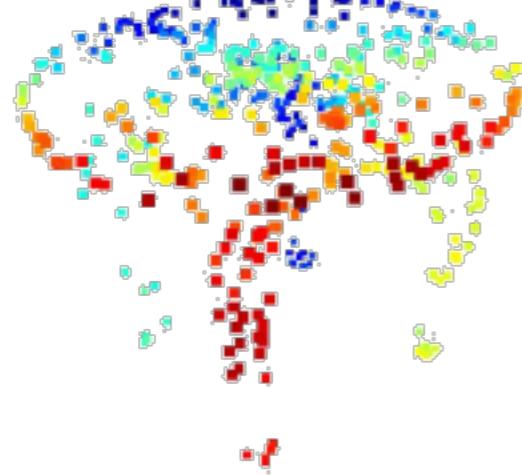


# Visualize What is Learned by Reconstruction

Original Shape

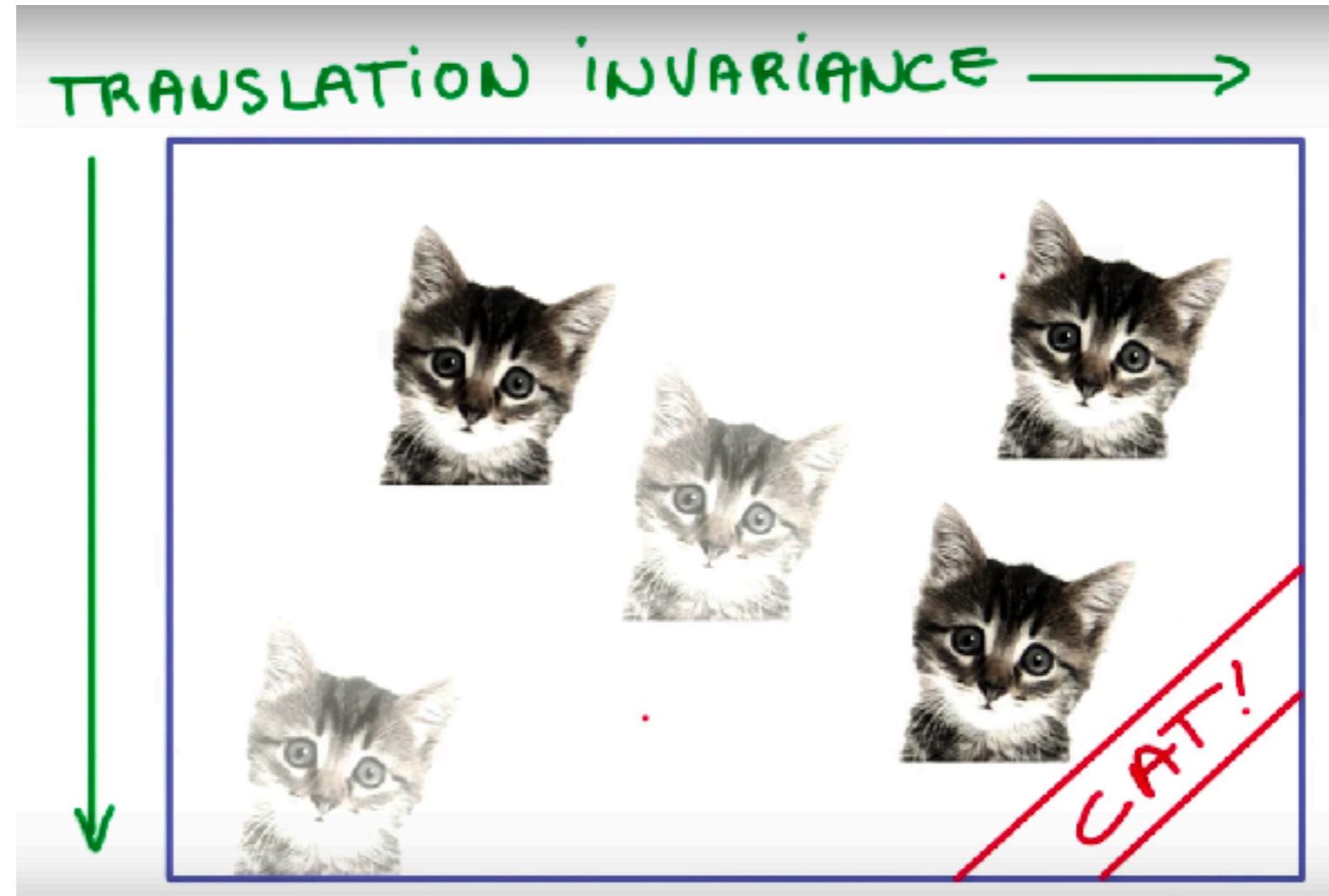


Critical Point Sets



**Salient points are discovered!**

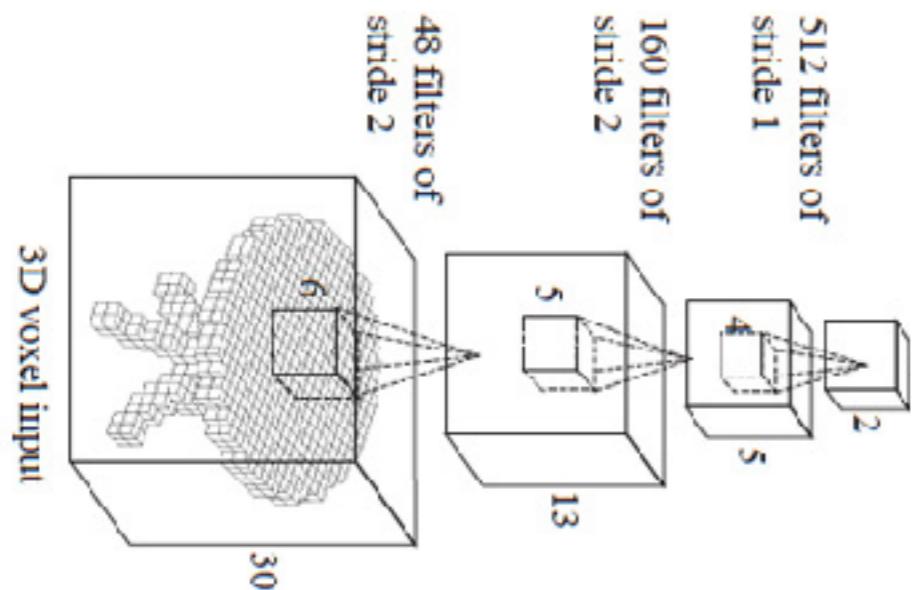
# Translation invariant?



- Global feature depends on absolute coordinate.  
Hard to generalize to unseen scene configurations!

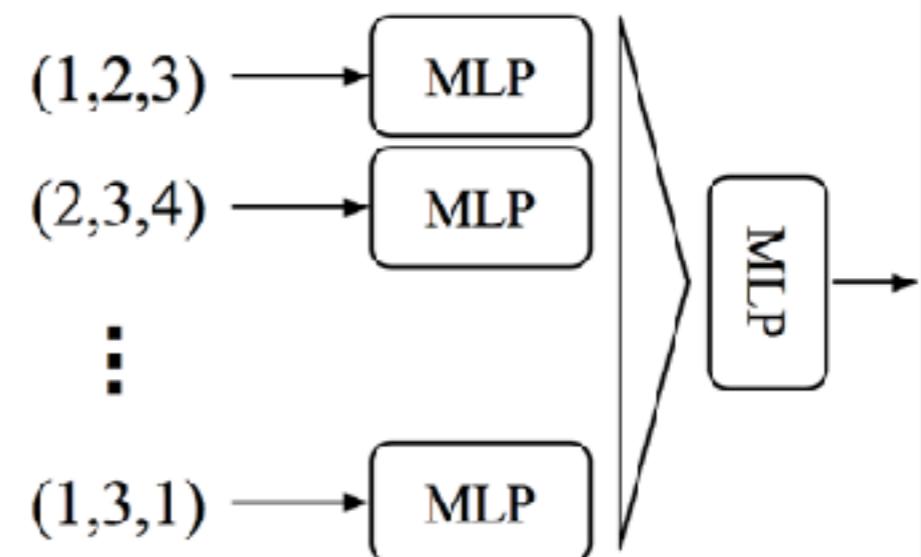
# Limitations of PointNet

Hierarchical feature learning  
Multiple levels of abstraction



3D CNN (Wu et al.)

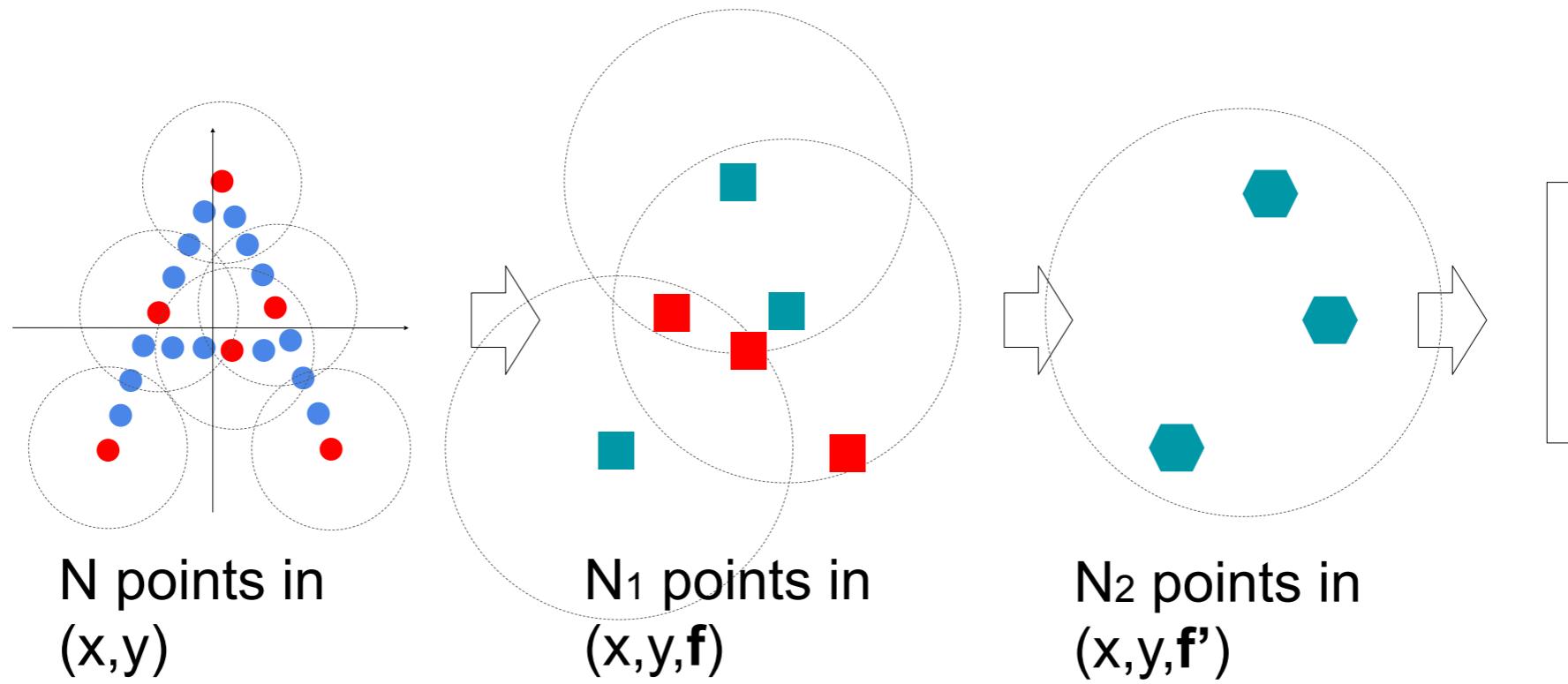
Global feature learning  
Either one point or all points



PointNet (vanilla) (Qi et al.)

- No local context for each point!

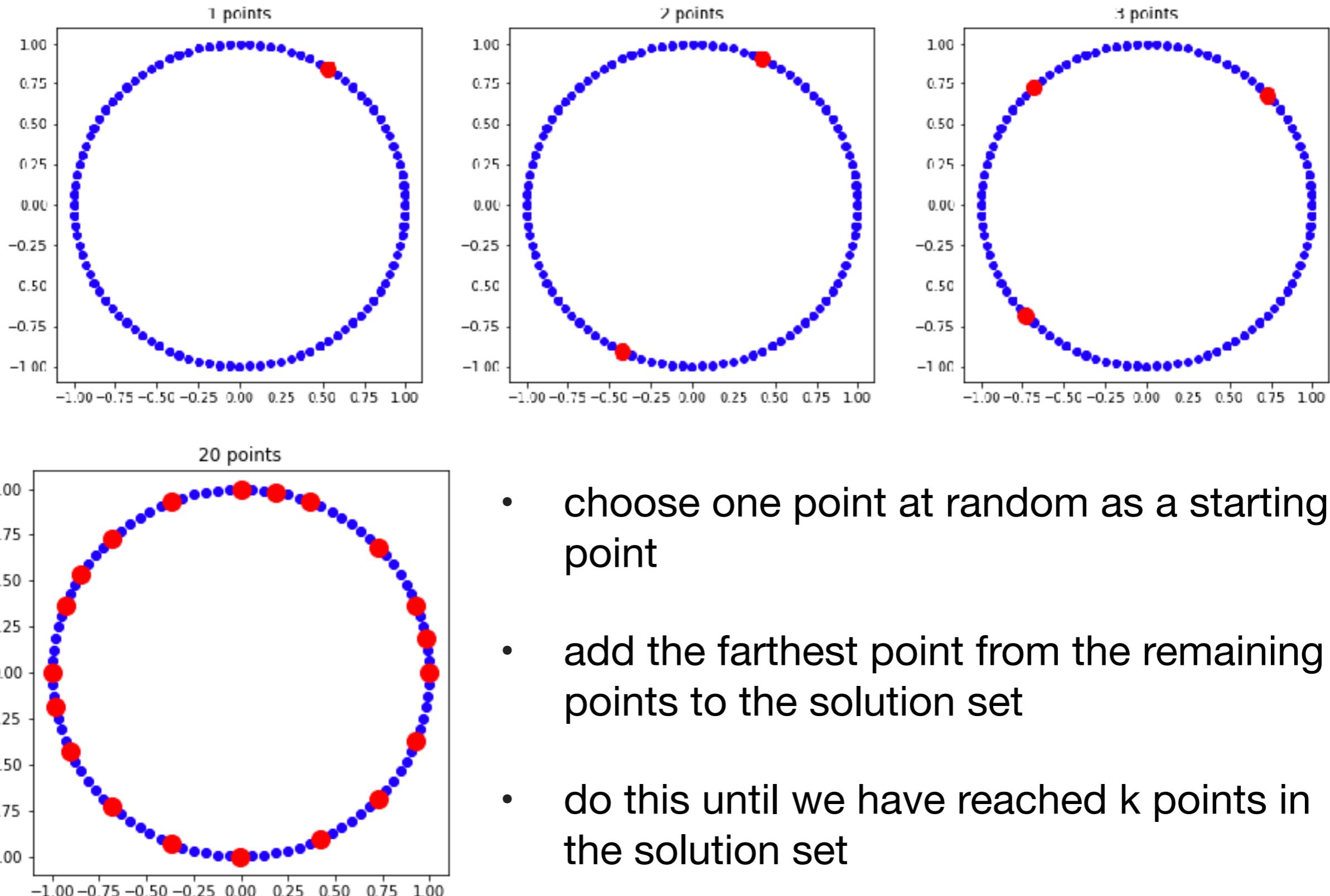
# PointNet++: Multi-Scale PointNet



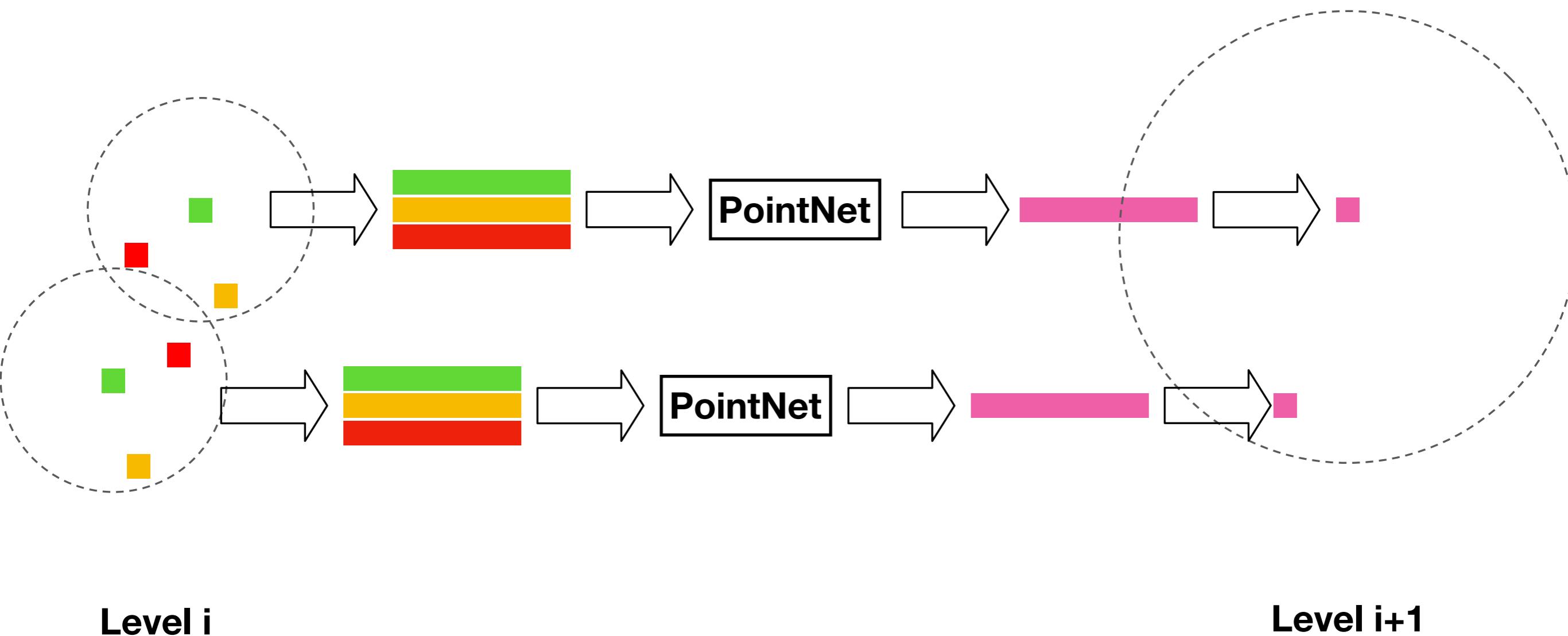
Repeat

- Sample anchor points
- Find neighborhood of anchor points
- Apply PointNet in each neighborhood to mimic convolution

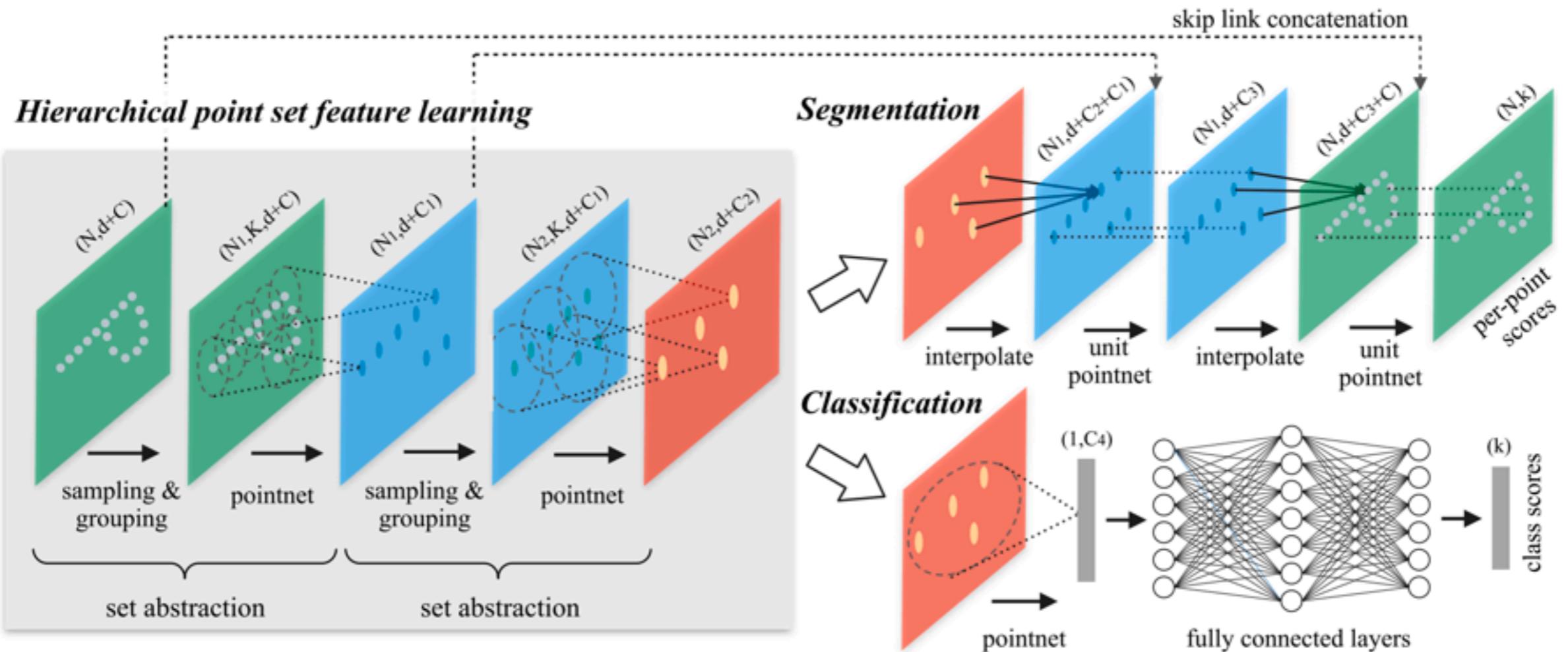
# Farthest point sampling



# Ball query



# Pipeline



# SPARSE-CONV

Graham, Benjamin, Martin Engelcke, and Laurens van der Maaten.  
"3d semantic segmentation with submanifold sparse convolutional  
networks." *Proceedings of the IEEE conference on computer vision  
and pattern recognition*. 2018.

# Strong performance

## 3D Semantic label benchmark

This table lists the benchmark results for the 3D semantic label scenario.

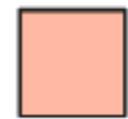
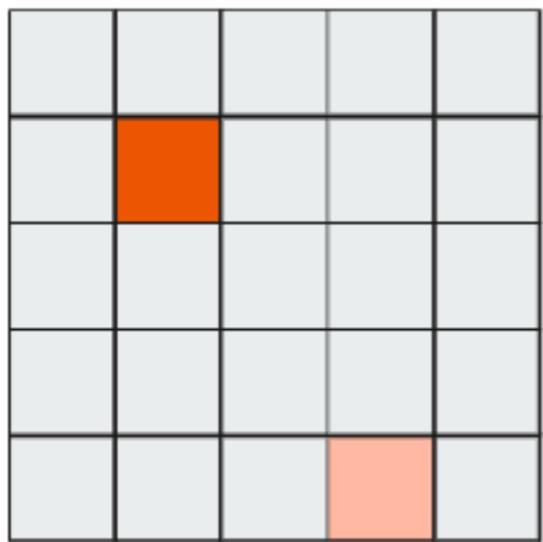
Method	Info	avg iou	bathtub	bed	bookshelf	cabinet	chair	counter	curtain	desk	door	floor	otherfurniture	picture	refrigerator	sho cur
OccuSeg+Semantic		0.764 ±	0.758 ± <sub>12</sub>	0.796 ± <sub>3</sub>	0.839 ± <sub>2</sub>	0.746 ± <sub>1</sub>	0.907 ± <sub>1</sub>	0.562 ± <sub>1</sub>	0.850 ± <sub>2</sub>	0.680 ± <sub>1</sub>	0.672 ± <sub>1</sub>	0.978 ± <sub>1</sub>	0.610 ± <sub>1</sub>	0.335 ± <sub>1</sub>	0.777 ± <sub>1</sub>	0.8
MinkowskiNet	P	0.736 ± <sub>2</sub>	0.859 ± <sub>2</sub>	0.818 ± <sub>2</sub>	0.832 ± <sub>3</sub>	0.709 ± <sub>3</sub>	0.840 ± <sub>3</sub>	0.521 ± <sub>3</sub>	0.853 ± <sub>1</sub>	0.660 ± <sub>2</sub>	0.643 ± <sub>2</sub>	0.951 ± <sub>4</sub>	0.544 ± <sub>3</sub>	0.286 ± <sub>8</sub>	0.731 ± <sub>2</sub>	0.8
SparseConvNet		0.725 ± <sub>3</sub>	0.647 ± <sub>21</sub>	0.821 ± <sub>1</sub>	0.846 ± <sub>1</sub>	0.721 ± <sub>2</sub>	0.869 ± <sub>2</sub>	0.533 ± <sub>2</sub>	0.754 ± <sub>8</sub>	0.603 ± <sub>5</sub>	0.614 ± <sub>3</sub>	0.955 ± <sub>2</sub>	0.572 ± <sub>2</sub>	0.326 ± <sub>2</sub>	0.710 ± <sub>3</sub>	0.8
CU-Hybrid Net		0.693 ± <sub>4</sub>	0.596 ± <sub>24</sub>	0.789 ± <sub>4</sub>	0.803 ± <sub>6</sub>	0.677 ± <sub>4</sub>	0.800 ± <sub>10</sub>	0.469 ± <sub>8</sub>	0.846 ± <sub>3</sub>	0.554 ± <sub>12</sub>	0.591 ± <sub>6</sub>	0.948 ± <sub>10</sub>	0.500 ± <sub>4</sub>	0.316 ± <sub>3</sub>	0.609 ± <sub>5</sub>	0.8
KP-FCNN		0.684 ± <sub>5</sub>	0.847 ± <sub>4</sub>	0.758 ± <sub>10</sub>	0.784 ± <sub>7</sub>	0.647 ± <sub>6</sub>	0.814 ± <sub>7</sub>	0.473 ± <sub>6</sub>	0.772 ± <sub>6</sub>	0.605 ± <sub>4</sub>	0.594 ± <sub>4</sub>	0.935 ± <sub>20</sub>	0.450 ± <sub>10</sub>	0.181 ± <sub>24</sub>	0.587 ± <sub>8</sub>	0.8
		H. Thomas, G. Qi, J. Deschaud, B. Marcotegui, F. Goulette, L. Guibas: KPConv: Flexible and Deformable Convolution for Point Clouds. ICLR 2019														
PointASNL		0.666 ± <sub>6</sub>	0.703 ± <sub>17</sub>	0.781 ± <sub>5</sub>	0.751 ± <sub>12</sub>	0.655 ± <sub>5</sub>	0.830 ± <sub>4</sub>	0.471 ± <sub>7</sub>	0.769 ± <sub>7</sub>	0.474 ± <sub>21</sub>	0.537 ± <sub>8</sub>	0.951 ± <sub>4</sub>	0.475 ± <sub>6</sub>	0.279 ± <sub>9</sub>	0.635 ± <sub>5</sub>	0.68
		Xu Yan, Chaoda Zheng, Zhen Li, Sheng Wang, Shuguang Cui: PointASNL: Robust Point Clouds Processing using Nonlocal Neural Networks with Adaptive Sampling. CVPR 2020														
PointConv	P	0.666 ± <sub>6</sub>	0.781 ± <sub>9</sub>	0.759 ± <sub>9</sub>	0.699 ± <sub>14</sub>	0.644 ± <sub>7</sub>	0.822 ± <sub>6</sub>	0.475 ± <sub>5</sub>	0.779 ± <sub>5</sub>	0.564 ± <sub>11</sub>	0.504 ± <sub>15</sub>	0.953 ± <sub>3</sub>	0.428 ± <sub>16</sub>	0.203 ± <sub>19</sub>	0.586 ± <sub>9</sub>	0.7
		Wenxuan Wu, Zhongang Qi, Li Fuxin: PointConv: Deep Convolutional Networks on 3D Point Clouds. CVPR 2019														
DualMeshNet		0.658 ± <sub>8</sub>	0.778 ± <sub>10</sub>	0.702 ± <sub>14</sub>	0.806 ± <sub>4</sub>	0.619 ± <sub>9</sub>	0.813 ± <sub>8</sub>	0.468 ± <sub>9</sub>	0.693 ± <sub>14</sub>	0.494 ± <sub>18</sub>	0.524 ± <sub>11</sub>	0.941 ± <sub>15</sub>	0.449 ± <sub>11</sub>	0.298 ± <sub>4</sub>	0.510 ± <sub>15</sub>	0.8
		Jonas Schult, Francis Engelmann, Theodora Kontogianni, Bastian Leibe: DualMeshNet: Joint Geodesic and Euclidean Convolutions for 3D Semantic Segmentation. CVPR 2020														
MVPNet	P	0.641 ± <sub>9</sub>	0.831 ± <sub>5</sub>	0.715 ± <sub>13</sub>	0.671 ± <sub>17</sub>	0.590 ± <sub>18</sub>	0.761 ± <sub>13</sub>	0.394 ± <sub>17</sub>	0.679 ± <sub>17</sub>	0.642 ± <sub>3</sub>	0.553 ± <sub>7</sub>	0.937 ± <sub>19</sub>	0.462 ± <sub>8</sub>	0.256 ± <sub>10</sub>	0.649 ± <sub>4</sub>	0.40
		Maximilian Jaritz, Jiayuan Gu, Hao Gu: Multi-view PointNet for 3D Scene Understanding. GM3L Workshop, IC3V 2019														

Top 3 entries are based on SparseConv

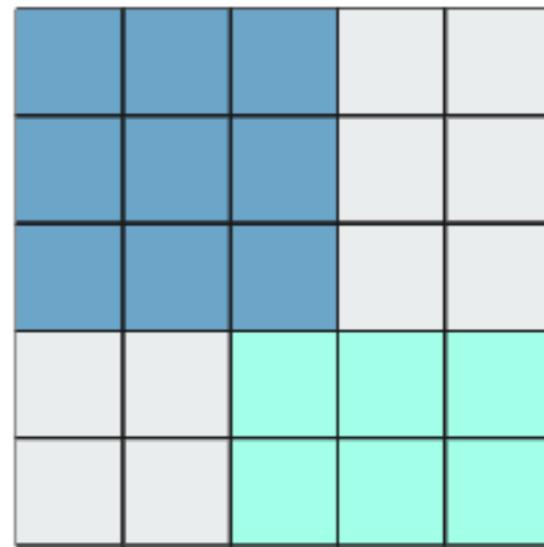
# Terminology

- d-dimension CNN with  $(d+1)$ -dimension input
  - e.g. 2D CNN with  $H \times W \times C$  image
- d-dimension site: associated with a feature vector
- active site: site associated with a non-zero feature
- ground state: zero feature vector

# Sparse convolution (SC)

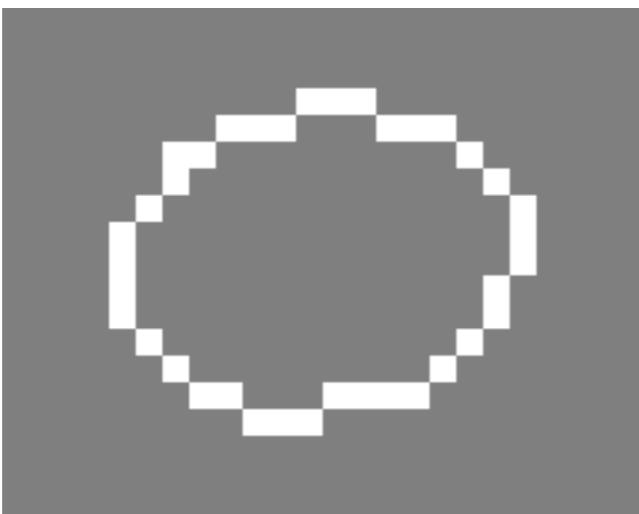


Activate input site



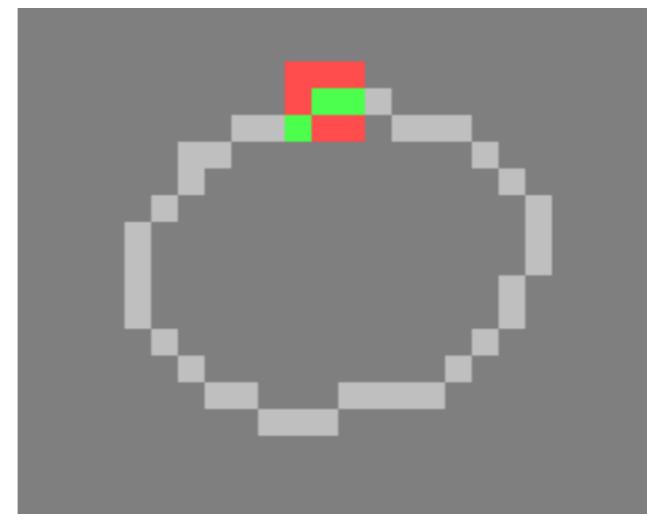
Activate output site

# Dilated issues



SparseConv

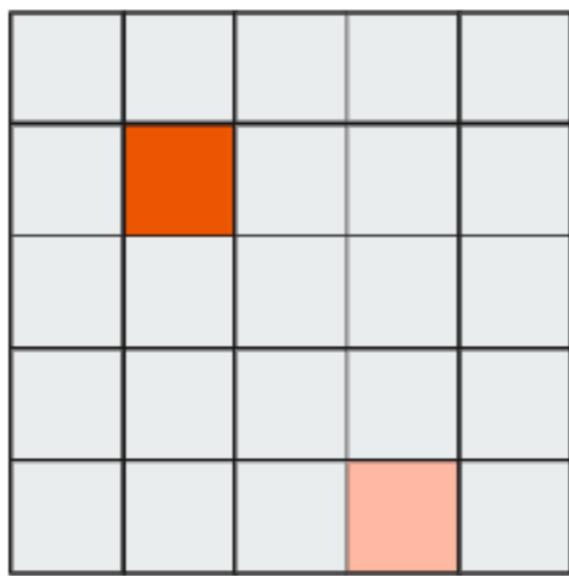
**Sparsity reduce**  
**Computation increase**



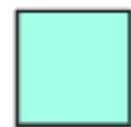
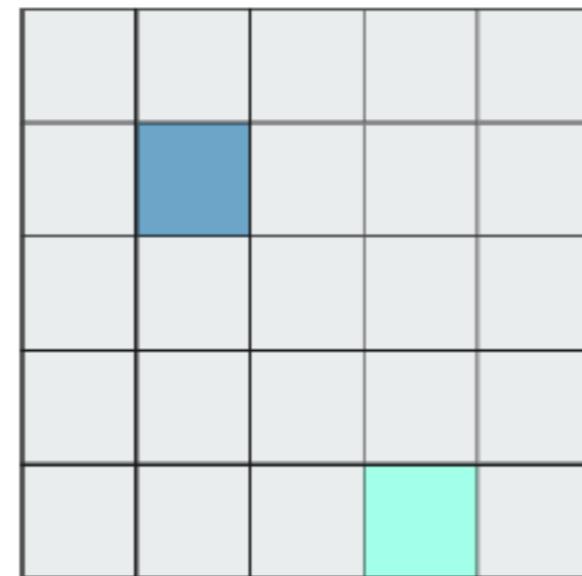
Submanifold SparseConv

**Sparsity keep**  
**Computation keep**

# Submanifold Sparse convolution (SSC)

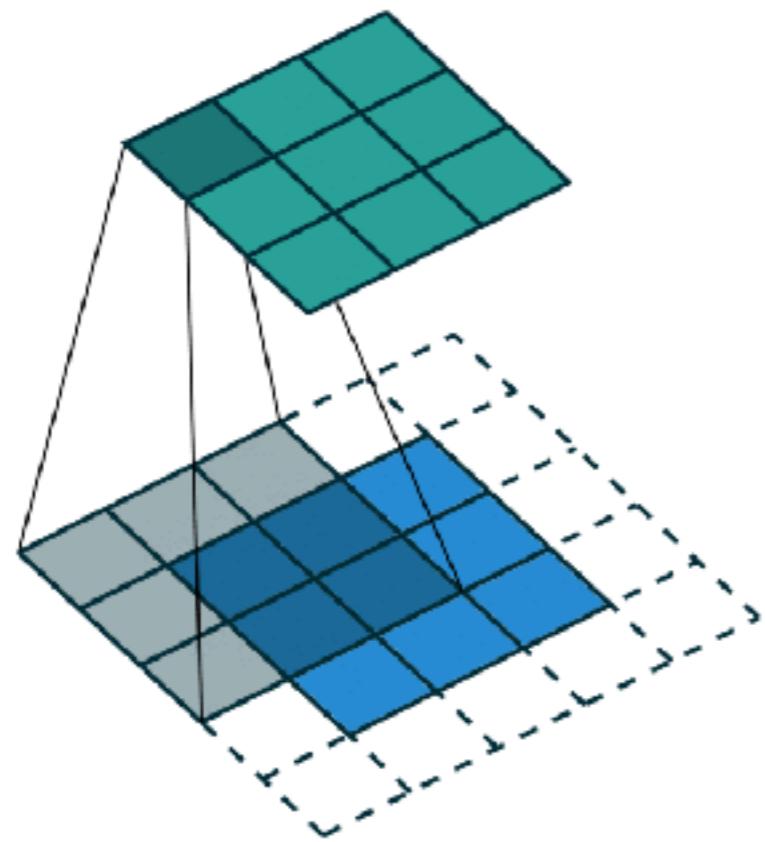


Activate input site

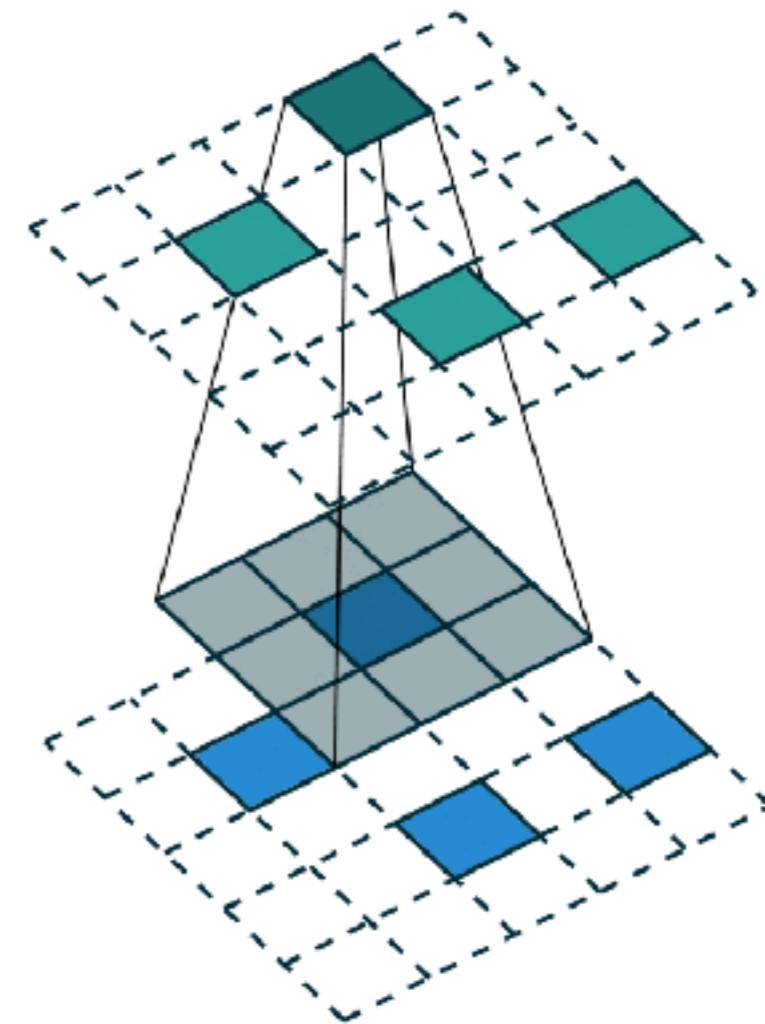


Activate output site

# Dense vs. Sparse conv

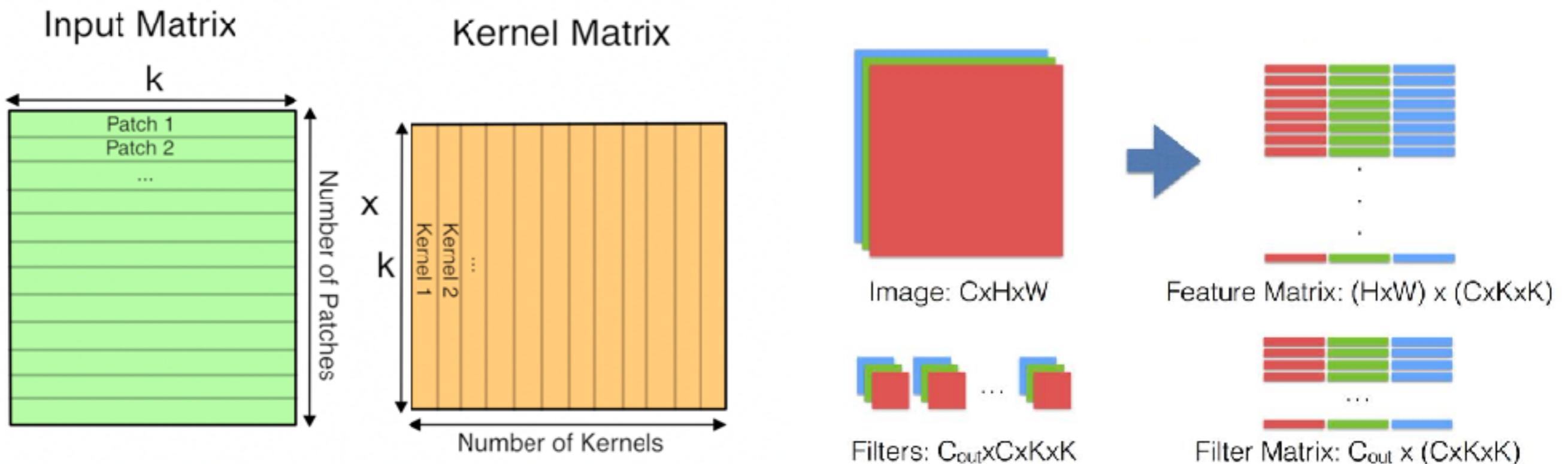


**Dense Convolution**



**Submanifold Sparse Convolution**

# Implementation (dense)

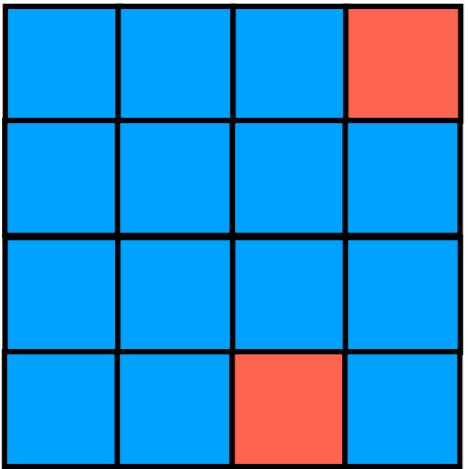


**Convert convolution to matrix multiplication**

<https://petewarden.com/2015/04/20/why-gemm-is-at-the-heart-of-deep-learning/>

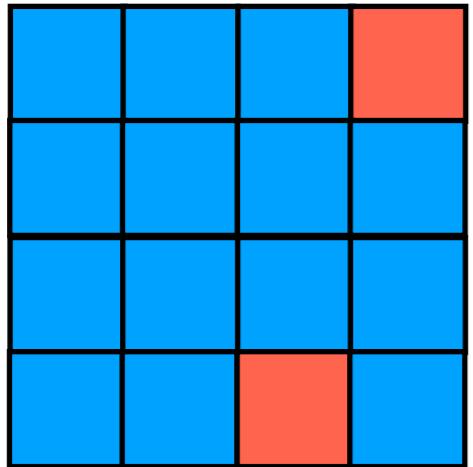
<https://github.com/Yangqing/caffe/wiki/Convolution-in-Caffe:-a-memo>

# Implementation (sparse)



**4x4 input feature map**

# Implementation (sparse)



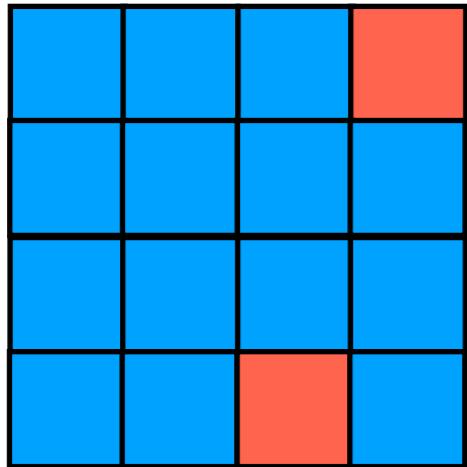
4x4 input feature map



Index	Loc	Feature
0	(0, 3)	
1	(3, 2)	

**Input matrix:  
build input hash table**

# Implementation (sparse)



4x4 input feature map

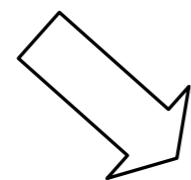


Index	Loc	Feature
0	(0, 3)	
1	(3, 2)	

Input matrix:  
build input hash table

1	2	3
4	5	6
7	8	9

3x3 kernel

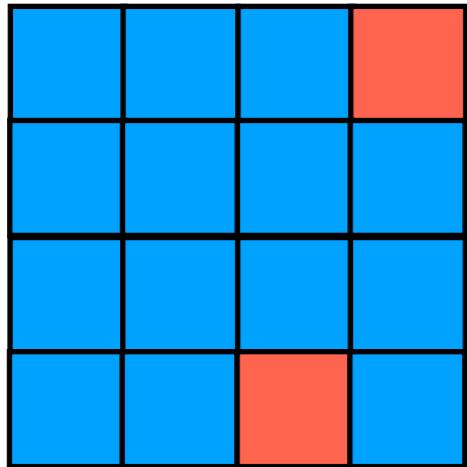


5th rule book

Input	Output
0	0
1	1

Kernel matrix:  
build 9=3x3 rule books

# Implementation (sparse)



4x4 input feature map

Index	Loc	Feature
0	(0, 3)	
1	(3, 2)	

Input matrix:  
build input hash table

Index	Feature
0	
1	

Input matrix:  
gather input features

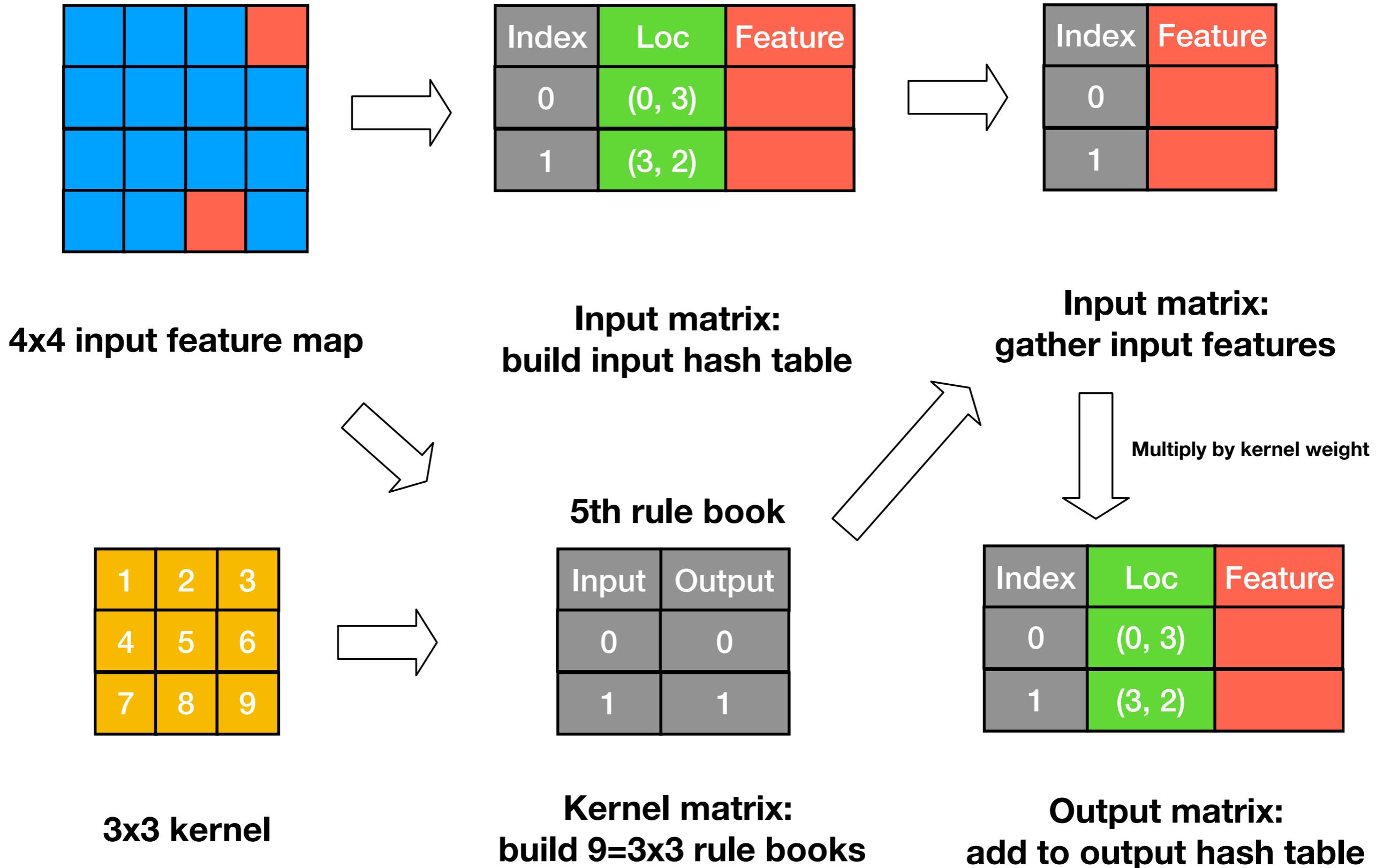
1	2	3
4	5	6
7	8	9

3x3 kernel

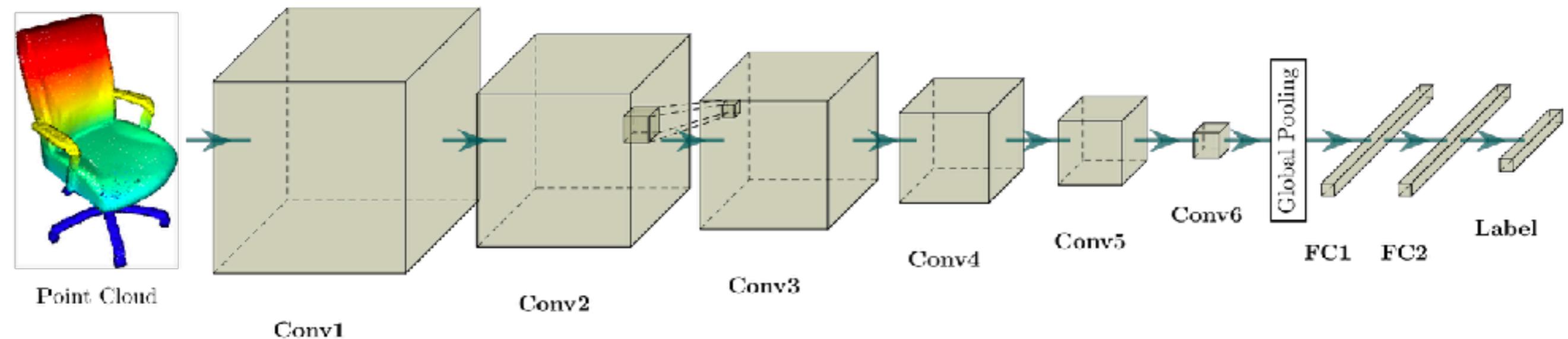
Input	Output
0	0
1	1

Kernel matrix:  
build 9=3x3 rule books

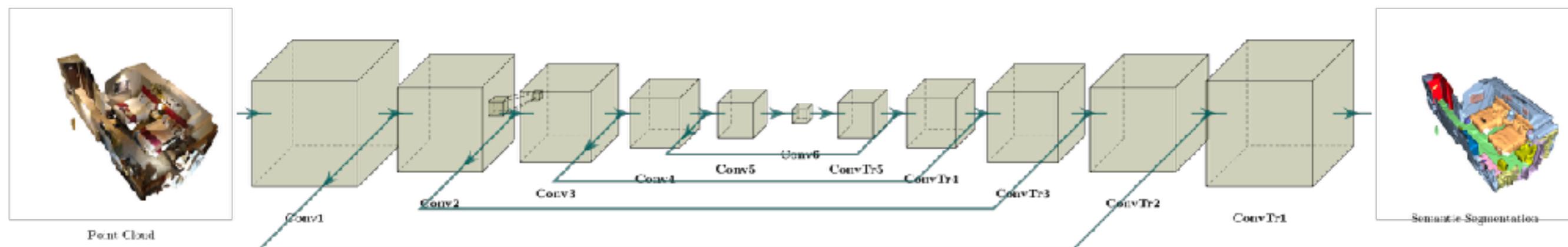
# Implementation (sparse)



# Application



## Classification

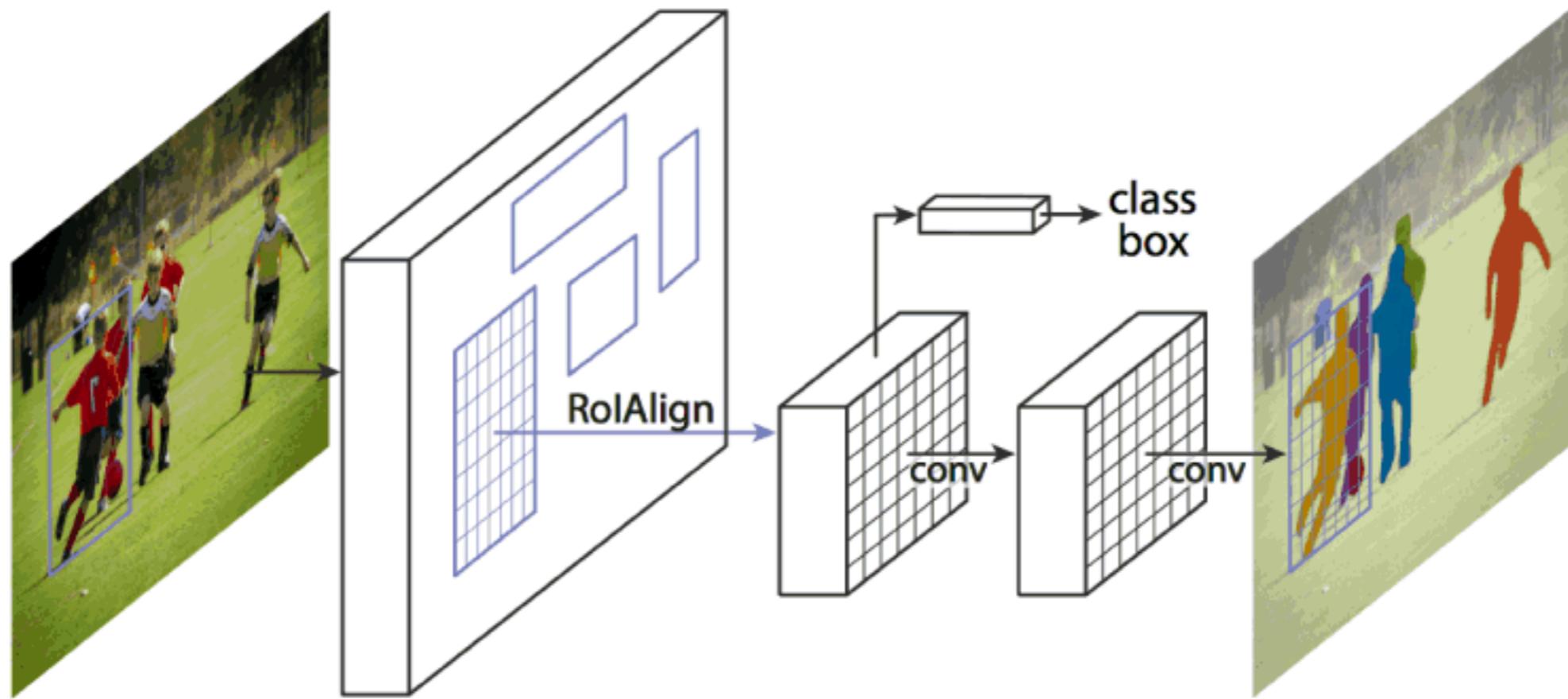


## Semantic Segmentation

# VOTENET

Qi, Charles R., et al. "Deep hough voting for 3d object detection in point clouds." *Proceedings of the IEEE International Conference on Computer Vision*. 2019.

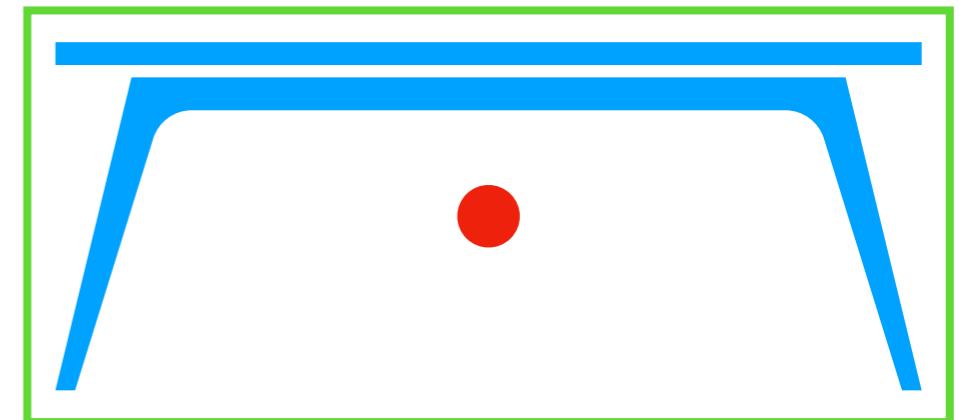
# 3D R-CNN?



The Mask R-CNN framework for instance segmentation

# Challenges for 3D detection

- For 2D, the center of the bounding box of an object is usually a local maximal of the activation.
- However, for 3D, the point cloud is located at the surface. Thus, the center of the 3D bounding box is not necessary to be located on the surface.
- It is still an open question how to represent 3D instances (bounding box or others)?



# Generalized Hough transform

## GENERALIZING THE HOUGH TRANSFORM TO DETECT ARBITRARY SHAPES\*

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(Received 10 October 1979; in revised form 9 September 1980; received for publication 23 September 1980)

**Abstract**—The Hough transform is a method for detecting curves by exploiting the duality between points on a curve and parameters of that curve. The initial work showed how to detect both analytic curves<sup>(1,2)</sup> and non-analytic curves,<sup>(3)</sup> but these methods were restricted to binary edge images. This work was generalized to the detection of some analytic curves in grey level images, specifically lines,<sup>(4)</sup> circles<sup>(5)</sup> and parabolas.<sup>(6)</sup> The line detection case is the best known of these and has been ingeniously exploited in several applications.<sup>(7,8,9)</sup>

We show how the boundaries of an *arbitrary* non-analytic shape can be used to construct a mapping between image space and Hough transform space. Such a mapping can be exploited to detect instances of that particular shape in an image. Furthermore, variations in the shape such as rotations, scale changes or figure-ground reversals correspond to straightforward transformations of this mapping. However, the most remarkable property is that such mappings can be composed to build mappings for complex shapes from the mappings of simpler component shapes. This makes the generalized Hough transform a kind of universal transform which can be used to find arbitrarily complex shapes.

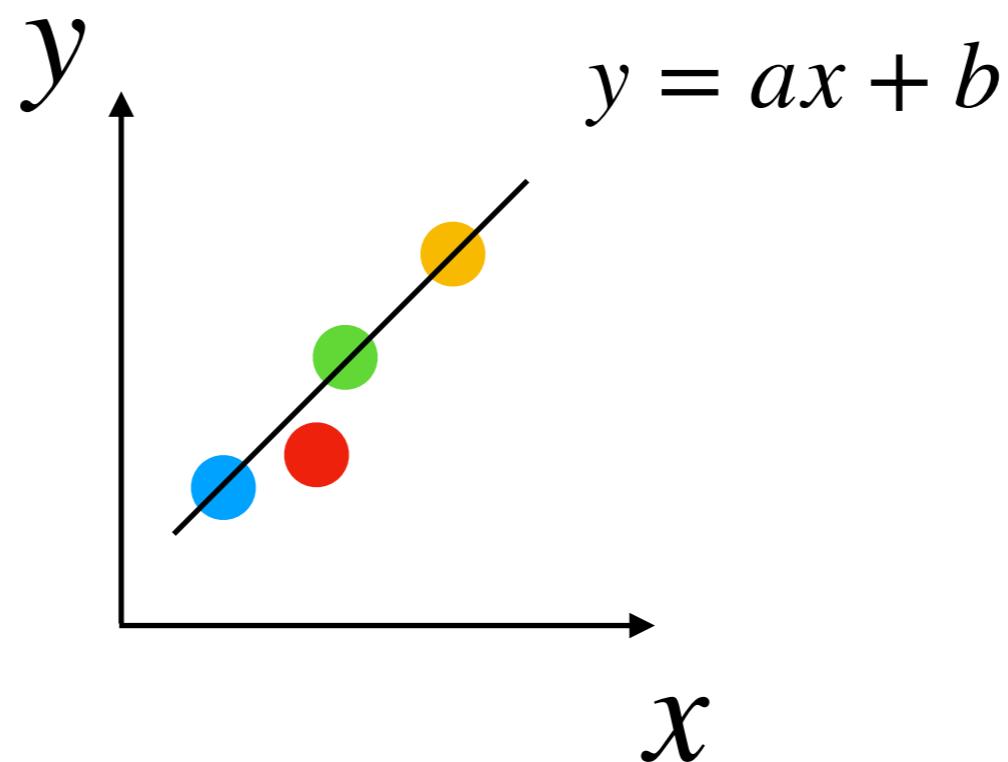
Image processing  
Parallel algorithms

Hough transform

Shape recognition

Pattern recognition

# Example: fit a line



In order to find a line passing the points,  
we can check lines passing each points.

# Example: fit a line

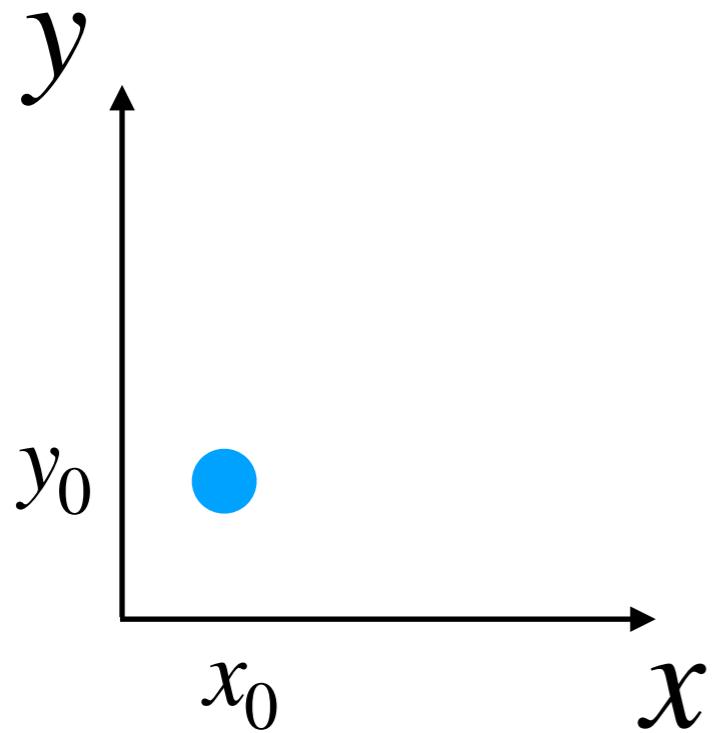
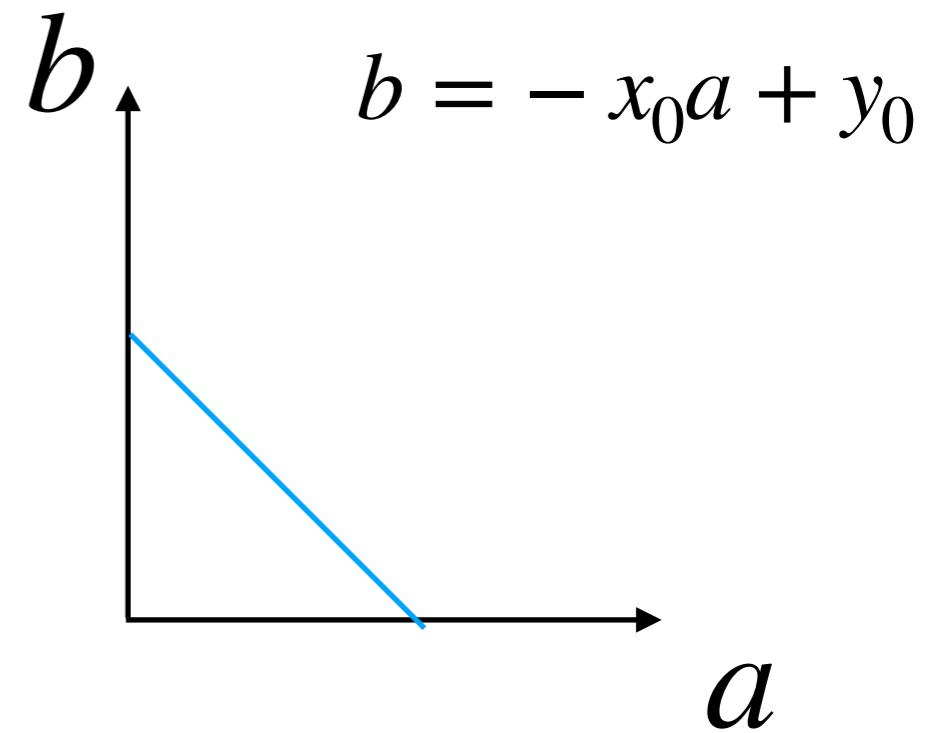
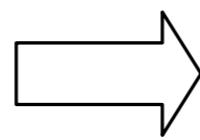


Image space



Parameter (Hough) space

$$b = -x_0 a + y_0$$

# Example: fit a line

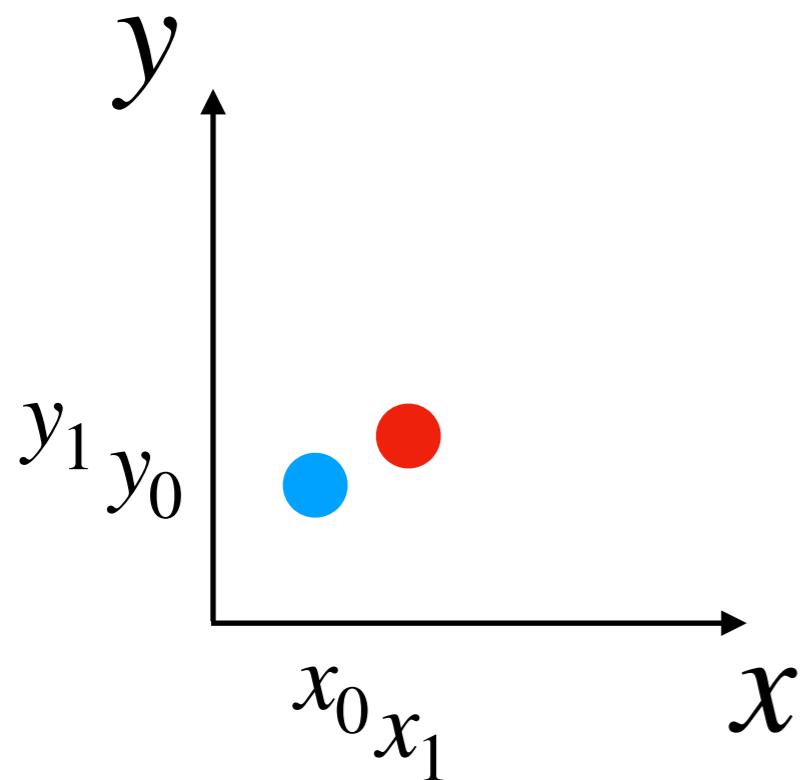
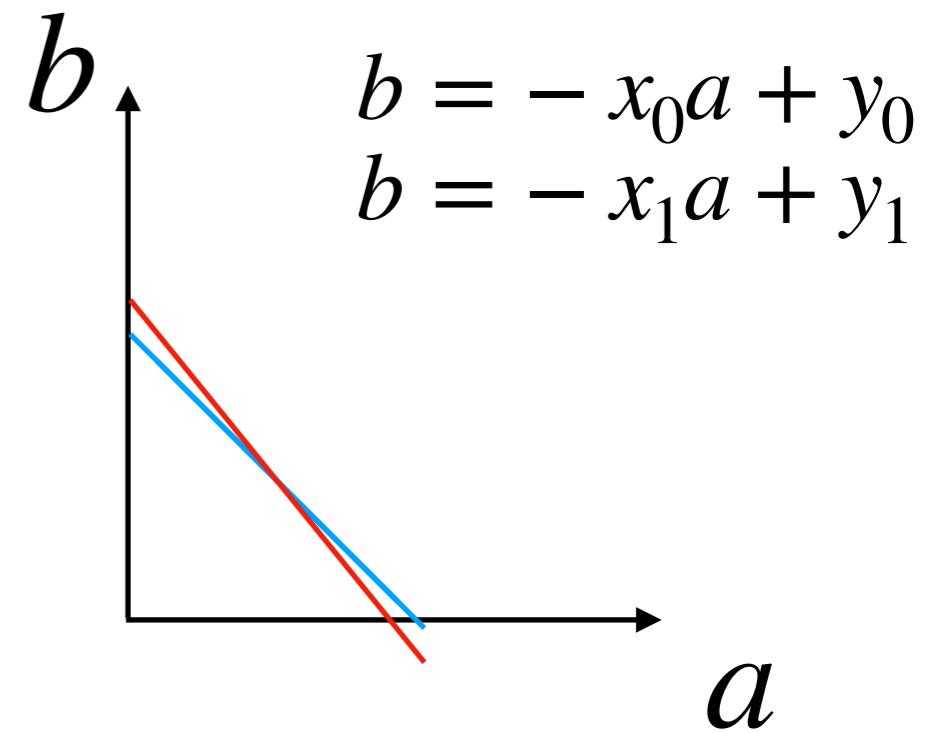


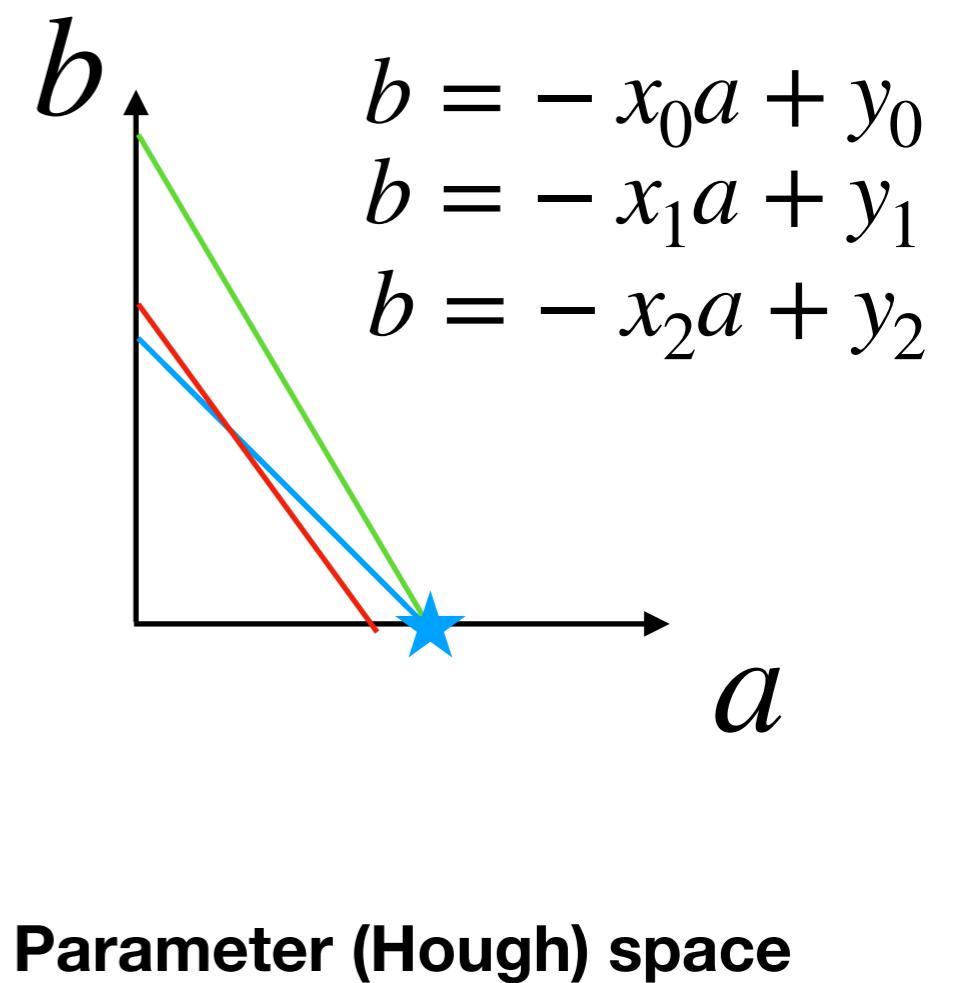
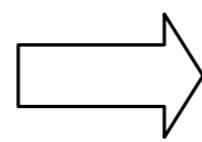
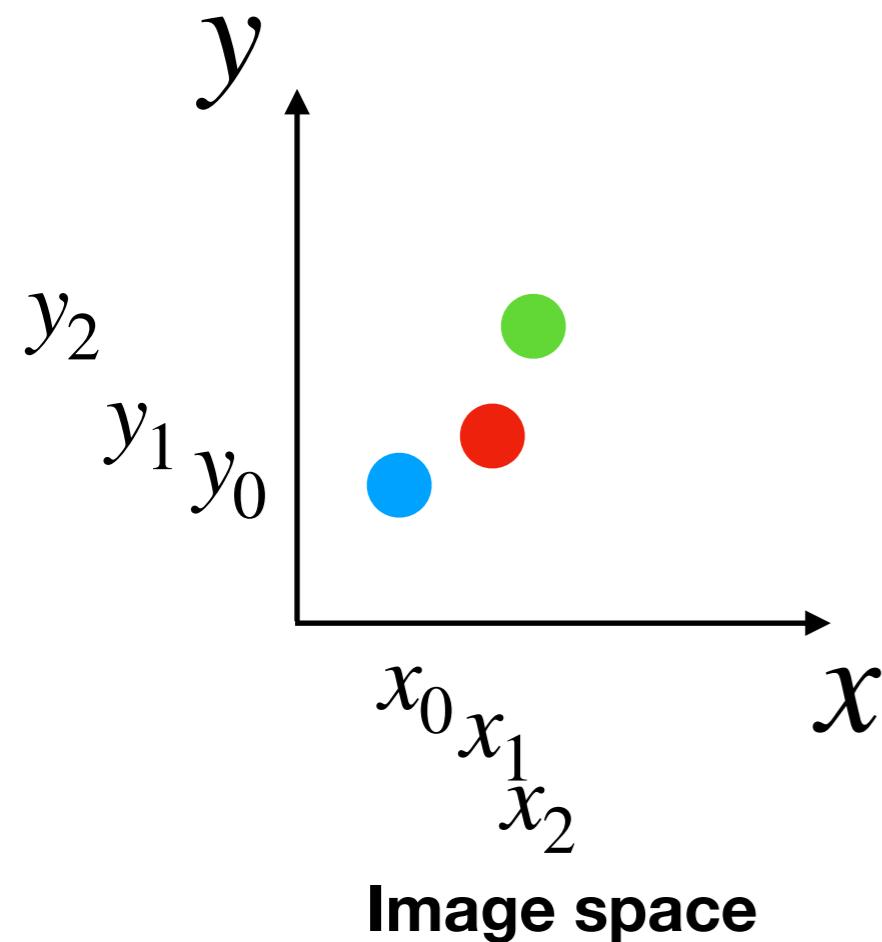
Image space



Parameter (Hough) space

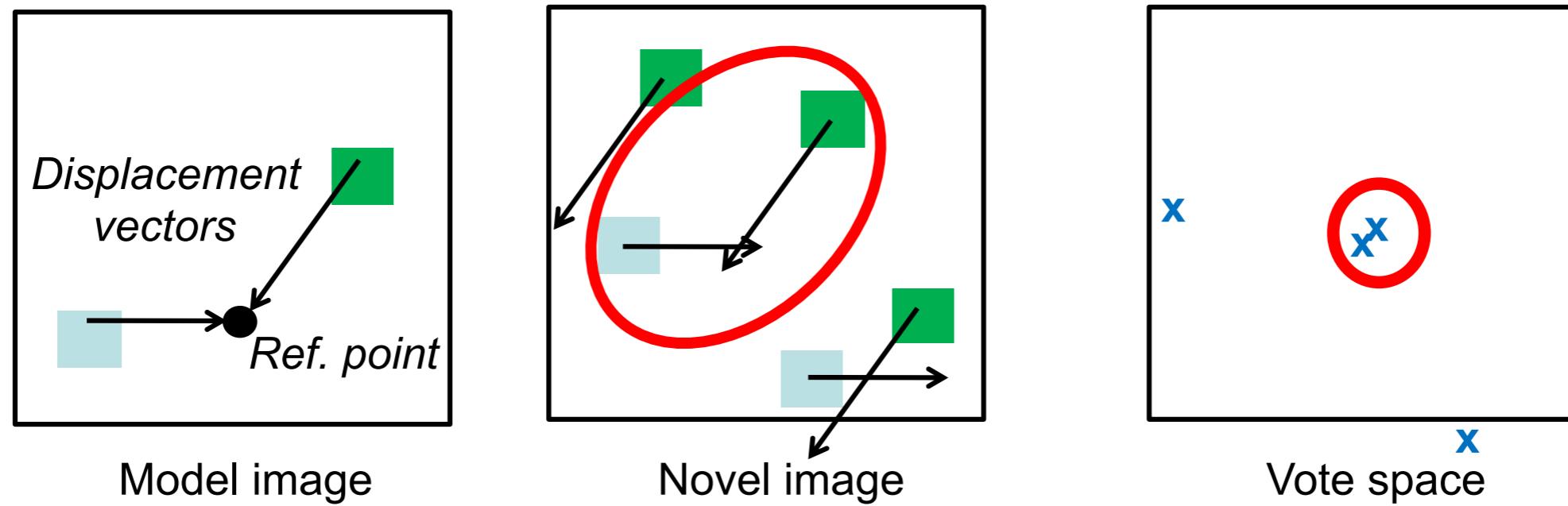
$$b = -x_0a + y_0$$
$$b = -x_1a + y_1$$

# Example: fit a line



coordinate  $\rightarrow$  line parameter

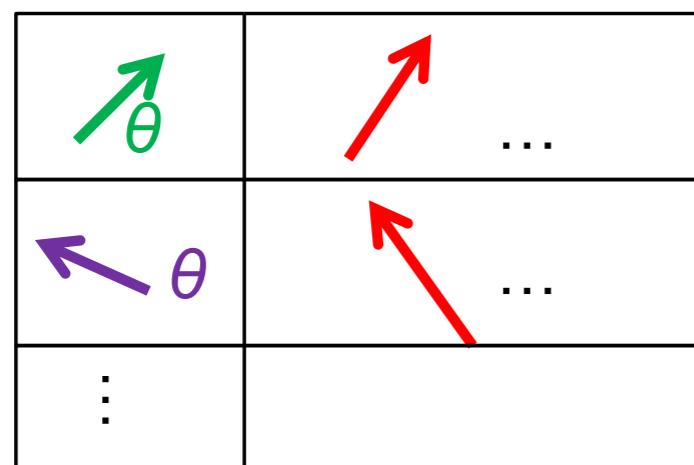
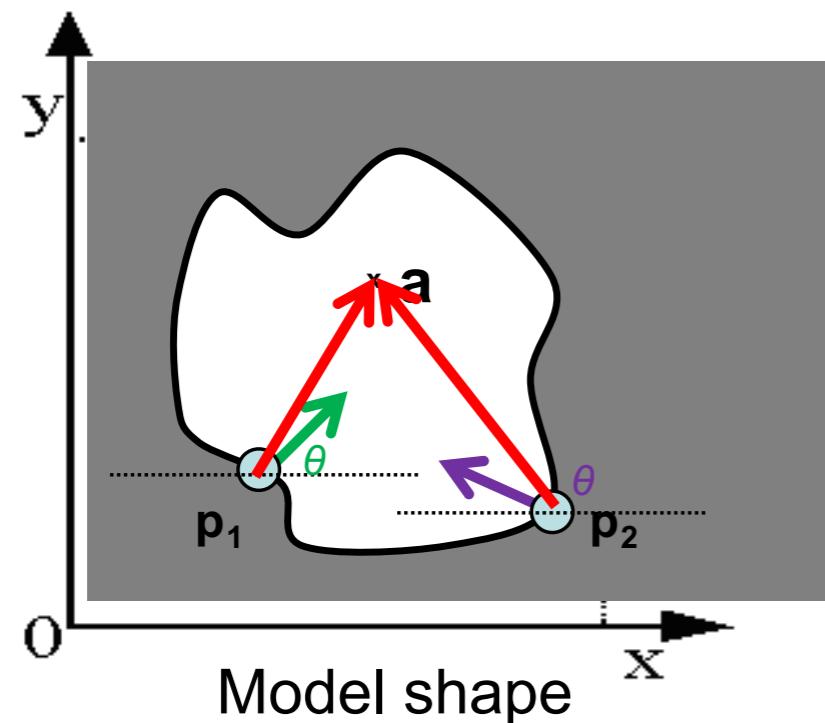
# Generalized hough transformation



**point info —> displacement to the reference point**

# Generalized hough transformation

- Define a model shape by its boundary points and a reference point.



## Offline procedure:

At each boundary point, compute displacement vector:  $\mathbf{r} = \mathbf{a} - \mathbf{p}_i$ .

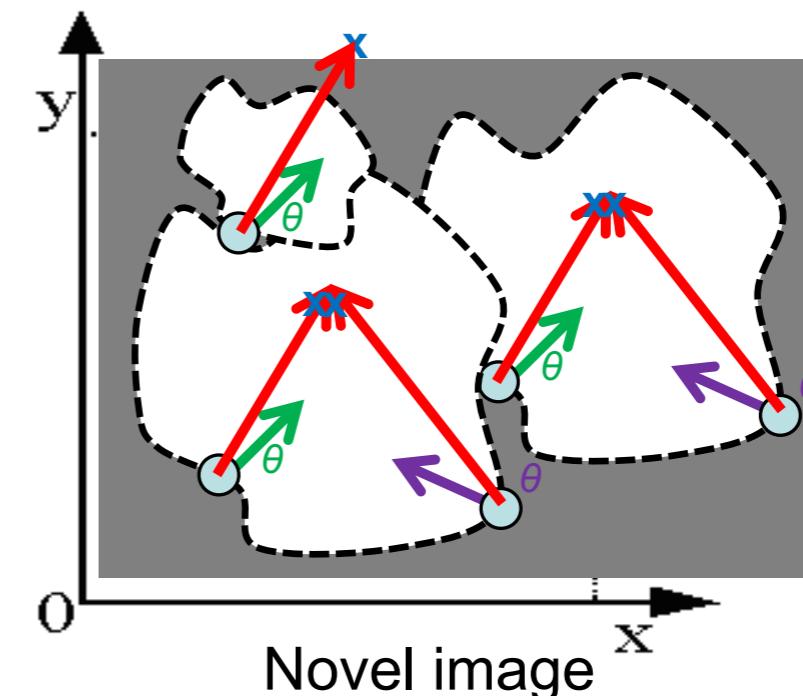
Store these vectors in a table indexed by gradient orientation  $\theta$ .

# Generalized hough transformation

## Detection procedure:

For each edge point:

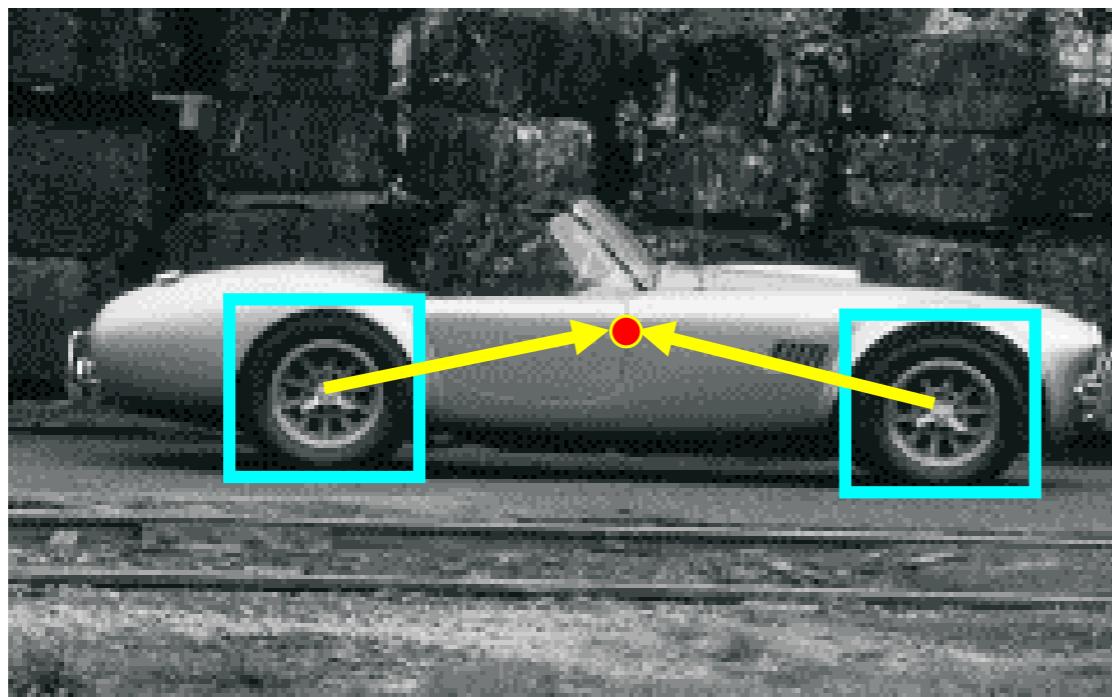
- Use its gradient orientation  $\theta$  to index into stored table
- Use retrieved  $r$  vectors to vote for reference point



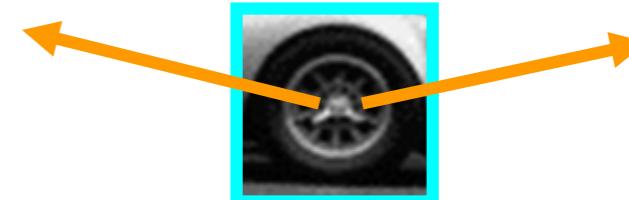
$\nearrow \theta$	$\nearrow \theta$
	...
$\nwarrow \theta$	$\nearrow \theta$
...	

# Learn the distribution of object positions

Instead of indexing displacements by gradient orientation, index by matched local patterns.



training image



“visual codeword” with  
displacement vectors

B. Leibe, A. Leonardis, and B. Schiele, [Combined Object Categorization and Segmentation with an Implicit Shape Model](#), ECCV Workshop on Statistical Learning in Computer Vision 2004

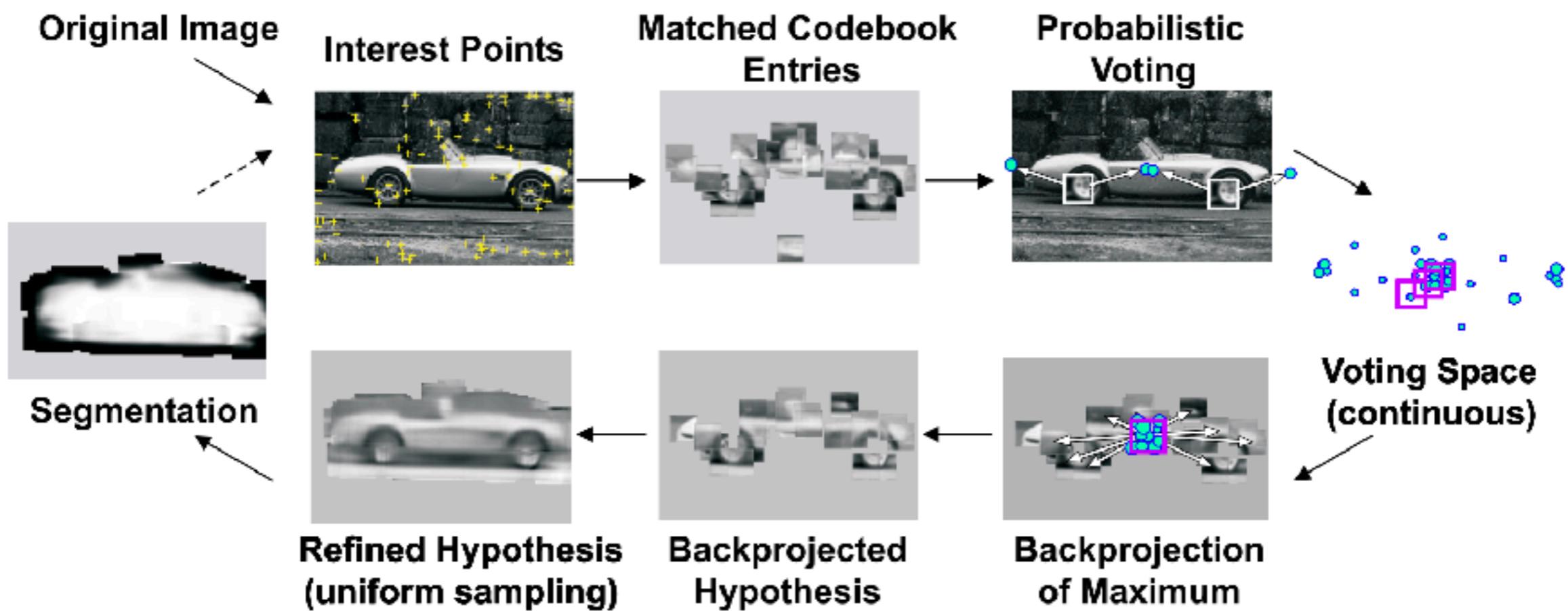
# Vote for objects



test image

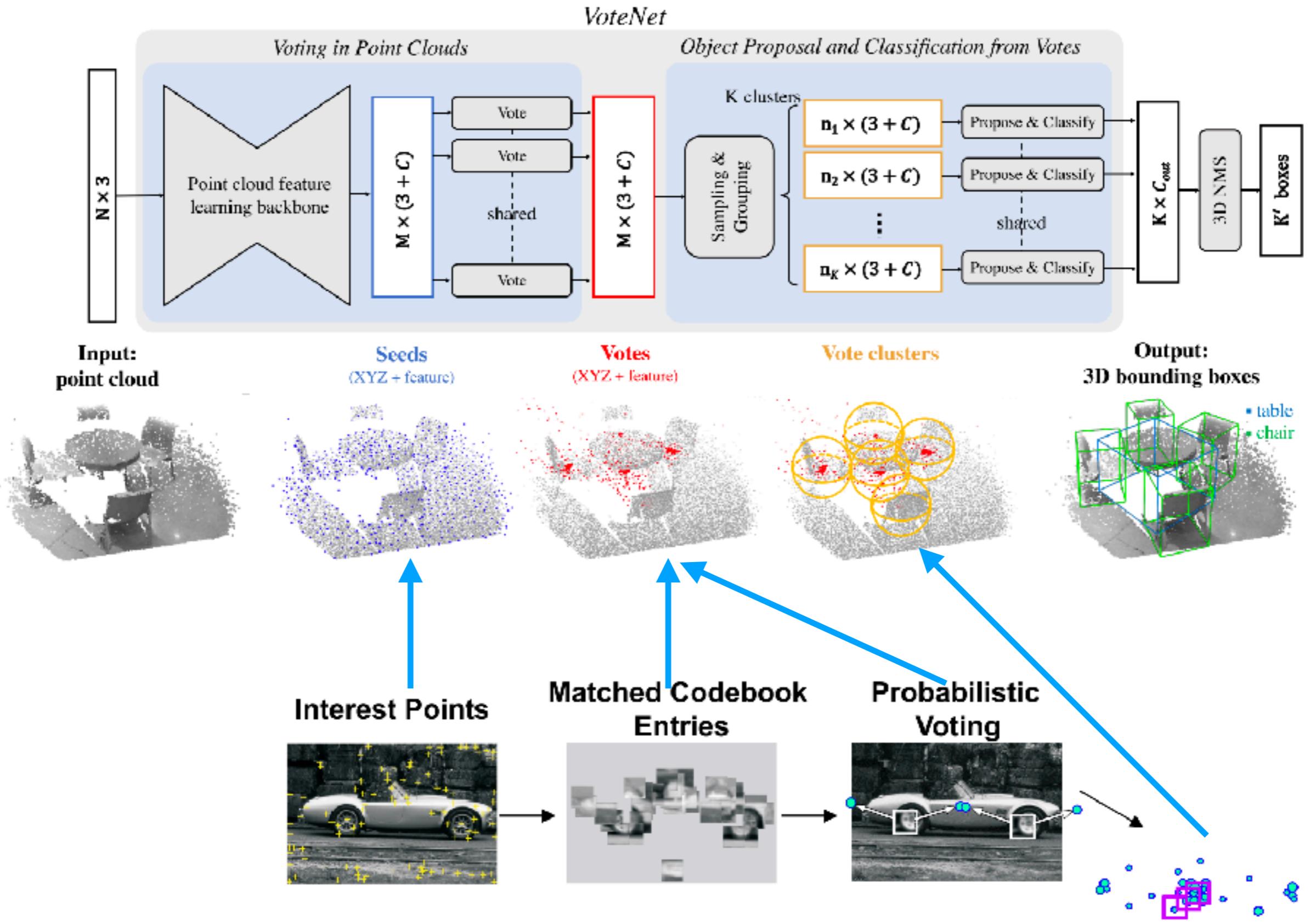
B. Leibe, A. Leonardis, and B. Schiele, [Combined Object Categorization and Segmentation with an Implicit Shape Model](#), ECCV Workshop on Statistical Learning in Computer Vision 2004

# Implicit shape model

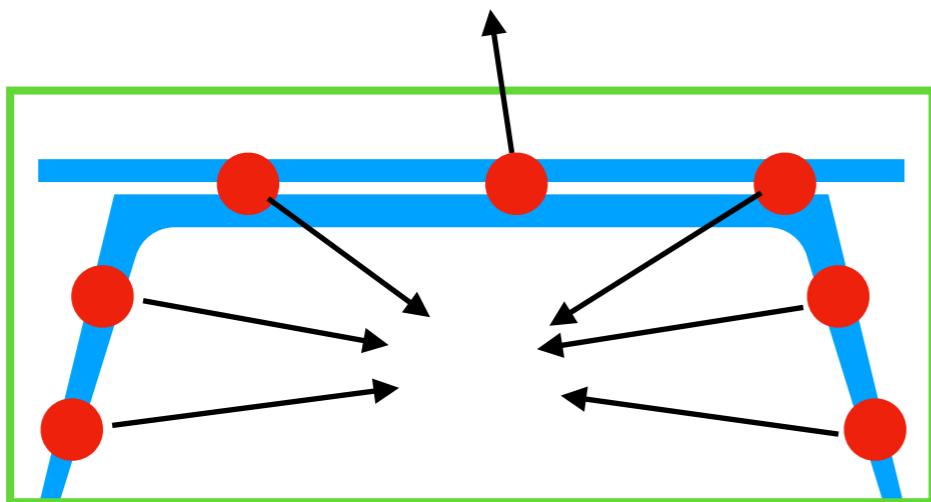


a bottom-up method

# VoteNet

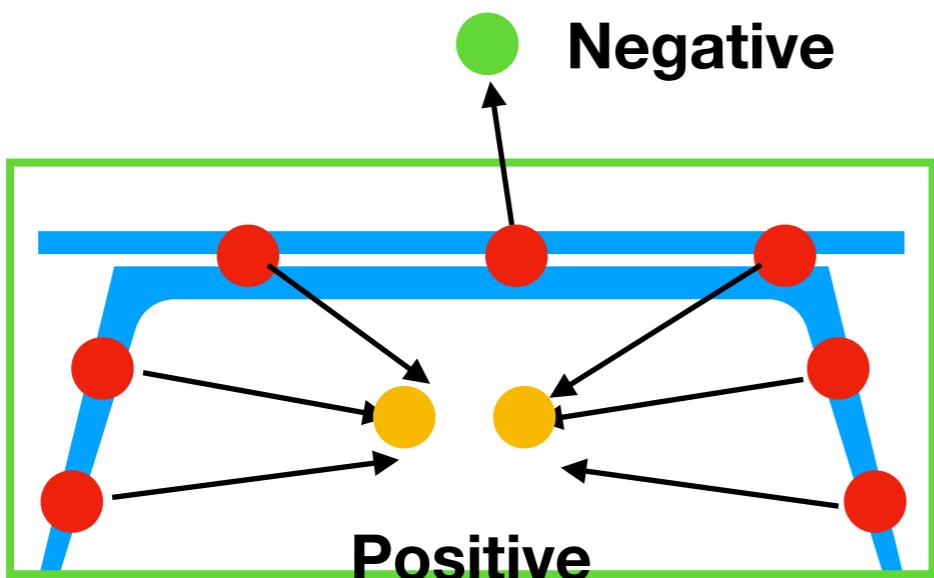


# Learning to vote



**Learn the displacement to  
the bounding boxcenter**

# Cluster vote



**Use farthest point sampling  
to get the cluster**