

```

Vector3 Gravity_force() {
    return new Vector3(0,-g,0);
}

// Air resistance opposing motion
Vector3 Air_force(){
    float vMag = vel.magnitude;
    Vector3 vDir = vel.normalized;
    float airDragMag = dragConst * Mathf.Pow(vMag, 2);
    return airDragMag * -vDir;
}

```

Introduction To Section 2

```

void ResolveForces (Vector3[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaTime = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaTime;
    pos += vel * deltaTime;
    if (isEnabled) transform.position = pos;
}

```

In this section you will learn about...

- Constant acceleration (e.g. local gravity).
- Variable acceleration (drag, Magnus effect).
- Creating methods for linear forces.
- **F = ma** for turning forces into accelerations.
- Calculating velocity & position from acceleration.

Overview Of Pattern

- Unbalanced forces lead to accelerations.
- Accelerations lead to a change in velocity.
- Velocity determines the change in position.

```

Vector3 Gravity_force() {
    return new Vector3(0,-g,0);
}

// Air resistance opposing motion
Vector3 Air_force(){
    float vMag = vel.magnitude;
    Vector3 vDir = vel.normalized;
    float airDragMag = dragConst * Mathf.Pow(vMag, 2);
    return airDragMag * -vDir;
}

```

Newton's First Law

```

void ResolveForces (Vector3[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaTime = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaTime;
    pos += vel * deltaTime;
    if (isEnabled) transform.position = pos;
}

```

In this video...

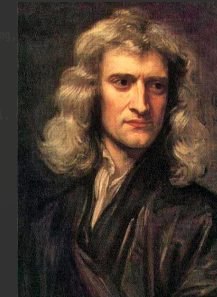
- Introducing Sir Isaac Newton
- Newton's First Law
- About the **FixedUpdate()** loop
- Updating **transform.position**

Isaac Newton

```
float dragMag = vel.magnitude;
Vector3 vdir = vel.normalized;
float airDragMag = dragConst * Math.Pow(dragMag, 2);
return airDragMag * -vdir;

Vector3 MagnusForce() {
    Vector3 x = magnusConst * Vector3.Cross(vel,
    return x;
}

void ApplyForces (Vector[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaT = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaT;
    pos += vel * deltaT;
    transform.position = pos;
}
```



Newton's First Law

- “When viewed in an inertial reference frame, an object either remains at rest or continues to move at a constant velocity, unless acted upon by an external force.”

http://en.wikipedia.org/wiki/Newton%27s_laws_of_motion

Using FixedUpdate()

- Called every 0.02s (20ms) by default.
- That's a **consistent** 50 times a second.
- **Time.deltaTime** returns the current value.

<http://docs.unity3d.com/Manual/ExecutionOrder.html>

Make Your Ball Move

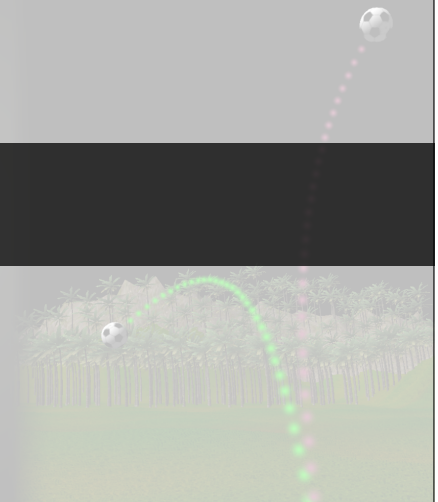
- **transform.position** = displacement from origin
- **v** = average velocity this FixedUpdate()
- **deltaS** = displacement change
- **deltaS = v * Time.deltaTime**
- Set **transform.position** inside **FixedUpdate()**



```
Vector3 Gravity_force() {  
    return new Vector3(0,-g,0);  
}  
  
// Air resistance opposing motion  
Vector3 Air_force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Summing The Forces

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```



Create A Force List

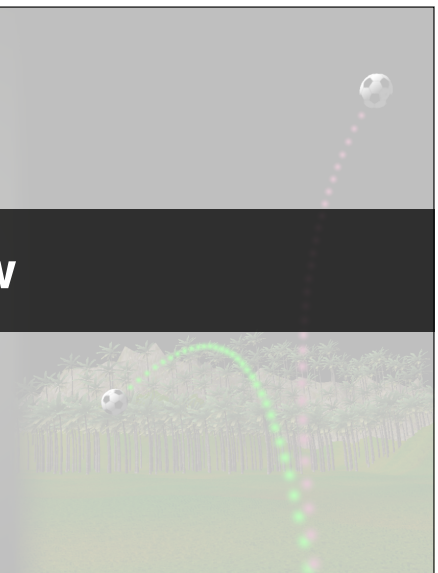
- using **System.Collections.Generic**;
- Create a public list of forces, **forceVectorList**;
- Create **AddForces ()** so sum the forces.
- **Debug.LogError ()** if we have a net force.
- Otherwise continue to update the position.



```
Vector3 Gravity_force() {  
    return new Vector3(0,-g,0);  
}  
  
// Air resistance opposing motion  
Vector3 Air_force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Newton's Second Law

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```



2nd Law Defined

- “The vector sum of the forces **F** on an object is equal to the mass **m** of that object multiplied by the acceleration vector **a** of the object: **F = m a.**”
- **a = F / m**

Write Code For Acceleration

- Publicly expose float **mass**
- Create **UpdateVelocity ()** method
- Modify **velocityVector** every FixedUpdate
- Remove **Debug.LogError()** code



```
Vector3 Gravity_Force() {  
    return new Vector3(0, -g, 0);  
}  
  
// Air resistance: opposing motion  
Vector3 Air_Force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return -vDir * airDragMag;  
}
```

Newton's Third Law

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```

In this video...

- Defining Newton's Third Law.
- Examples of why it's important to consider.
- Introducing our trail drawing code.
- Switching trail direction.
- Recap of Newton's laws

Newton's Third Law

- “When one body exerts a force on a second body, the second body simultaneously exerts a force equal in magnitude and opposite in direction on the first body.”

Modify Your Force Trails

- Turn them round so they face the other way.
- Experiment with particle systems alternative?
- Remember the other force is **always** there.



Recapping Newton's Laws

- **1st Law:** if (**SumForces** == **0**) then **deltaV** = **0**
- **2nd Law:** **acceleration** = **netForce** / mass
- **3rd Law:** **forceAonB** = - **forceBonA**

Valid for a huge range of phenomena. Care below
 10^{-8}m or above 10^8m/s (GPS, superconductors, etc)

```
Vector3 Gravity_force() {  
    return new Vector3(0, -9.8, 0);  
}  
  
// Air resistance, opposing motion  
Vector3 Air_force() {  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Physics Engine Architecture

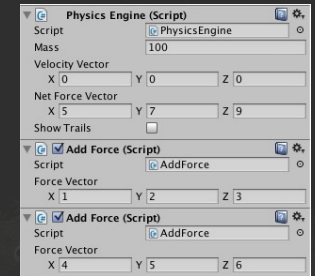
```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```


In this video...

- What we're trying to achieve.
- Why it's important to get this "right".
- Re-organise list iteration for variable forces.
- Bring DrawTrails.cs into PhysicsEngine.cs.
- Move the forces into separate components.

Refactor Your Code

- Move **DrawForces.cs** into **PhysicsEngine.cs**.
- Create **AddForce.cs** script, add two to ball.
- Try applying forces from scripts.



```
Vector3 Gravity_Force() {  
    return new Vector3(0, -9.8, 0);  
}  
  
// Air resistance: opposing motion  
Vector3 Air_Force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2);  
    return -vDir * airDragMag;  
}
```

SI Units & Dimensions

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaTime = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaTime;  
    pos += vel * deltaTime;  
    if (isEnabled) transform.position = pos;  
}
```

In this video...

- About Units and Dimensions.
- Why it's worth thinking about them.
- Where to annotate our units.
- Prepare our **RocketEngine.cs** class.

The 7 Base Units

- One SI base unit for each dimension.
- We're going to use SI base units (or multiples).
- Both sides of any equation must match.
- 1 meter = 4 feet COULD be right
- 1 meter = 4 kilograms couldn't

Where To Annotate Units?

| | Inspector | code readability | IDE pop-up |
|---------------|-----------|------------------|------------|
| // comment | None | Excellent | None |
| /// summary | None | Poor | Excellent |
| [Tooltip...] | Excellent | Poor | None |
| suffix _ms^-1 | Poor | Poor | None |

Annotate All Your Units

- Check all units are annotated neatly.
- Do this for both RocketEngine.cs
- ... and for PhysicsEngine.cs

http://en.wikipedia.org/wiki/SI_base_unit



```
Vector3 Gravity_force() {  
    return new Vector3(0, -9.8, 0);  
}  
  
// Air resistance opposing motion  
Vector3 Air_force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Rocket Science 101

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaTime = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaTime;  
    pos += vel * deltaTime;  
    if (isEnabled) transform.position = pos;  
}
```

In this video...

- The thrust of a rocket engine.
- Modelling rocket engines and fuel burn.
- An introduction to “delta V”.

http://en.wikipedia.org/wiki/Rocket_engine

Write float FuelThisUpdate()

- Return fuel used during this Time.deltaTime in kg
- Annotate private variables with units.
- Burn 1 metric tonne of fuel in virtual shuttle.
- Check that “delta V” is 2.23 m s^{-1} .
- Check same delta V at lower thrustPercent



```
Vector3 Gravity_force() {  
    return new Vector3(0, g, 0);  
}  
  
// Air resistance: opposing motion  
Vector3 Air_force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Improving Code Architecture

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```

```
Vector3 Gravity_force() {  
    return new Vector3(0, g, 0);  
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// Air resistance: opposing motion  
Vector3 Air_force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Modelling Gravity

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```


In this video...

- Review the universal gravitation equation*
- Create a method for it in Unity.
- Check we get realistic force values.

*http://en.wikipedia.org/wiki/Gravitational_constant

Write the equation into Unity

- No simple power operator like ****** or **^** I'm afraid.
- Use **Mathf.pow(distance, 2f)**; for square.
- Test you get a **force** of around 9.8 Newtons.



```
Vector3 Gravity_Force() {  
    return new Vector3(0, 9, 0);  
}  
  
// Air resistance: opposing motion  
Vector3 Air_Force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Back Down To Earth

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaTime = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaTime;  
    pos += vel * deltaTime;  
    if (isEnabled) transform.position = pos;  
}
```

In this video...

- Setup a football field “on Earth”.
- Test gravitation matches real values.
- Explore parabolic flight.
- Set scene for air resistance.

Score A Goal

- Start in the centre of the pitch.
- Use a single rocket engine to land in goal box.
- Burn for no more than 2 seconds.
- Burn only in one direction.



```
Vector3 Gravity_Force() {  
    return new Vector3(0,-9,0);  
}  
  
// Air resistance opposing motion  
Vector3 Air_Force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Modelling Simple Air Resistance

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```



In this video...

- Design a simple formula for air resistance.
- Create an Air Drag component.
- Test flight against reference ball.
- Tweak to get similar results to Unity's engine.

[http://en.wikipedia.org/wiki/Drag_\(physics\)](http://en.wikipedia.org/wiki/Drag_(physics))

Create The Fluid Drag Component

- Remember **Mathf.Pow()**
- Test against Unity's reference ball

```
Vector3 x = magnitude * Vector3.Cross(vel, angular)  
return x;  
  
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```



```

Vector3 Gravity_Force() {
    return new Vector3(0,-g,0);
}

// Air resistance opposing motion
Vector3 Air_force(){
    float vMag = vel.magnitude;
    Vector3 vDir = vel.normalized;
    float airDragMag = dragConst * Mathf.Pow(vMag, 2);
    return airDragMag * -vDir;
}

void ResolveForces (Vector3[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaTime = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaTime;
    pos += vel * deltaTime;
    if (isEnabled) transform.position = pos;
}

```

Script Execution Order

In this video...

- Expand on Unity's script execution order*
- Demonstrate our bug at “high” speeds.
- Show how this relates to fixed update time.
- Move Universal Gravity to separate object.

* <http://docs.unity3d.com/Manual/ExecutionOrder.html>

Script Execution Order

| Script Instance | Script Instance | Script Instance |
|--------------------------------|--------------------------------|-----------------------------|
| PhysicsEngine on ball 3 | PhysicsEngine on ball 1 | UniversalGravitation |
| Awake () | - | - |
| - | Awake () | - |
| - | - | Awake () |
| Start () | - | - |
| - | Start () | - |
| - | - | Start () |
| FixedUpdate() | - | - |
| - | FixedUpdate() | - |
| - | - | FixedUpdate() |



Create UniversalGravitation.cs

- Create a game object called Universal Gravitation
- Move gravitation code to UniversalGravitation.cs
- Make it work and test at high speeds



```

Vector3 Gravity_force() {
    return new Vector3(0,-g,0);
}

// Air resistance opposing motion
Vector3 Air_force(){
    float vMag = vel.magnitude;
    Vector3 vDir = vel.normalized;
    float airDragMag = dragConst * Mathf.Pow(vMag, 2);
    return airDragMag * -vDir;
}

```

Making A Simple Game

```

void ResolveForces (Vector3[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaTime = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaTime;
    pos += vel * deltaTime;
    if (isEnabled) transform.position = pos;
}

```



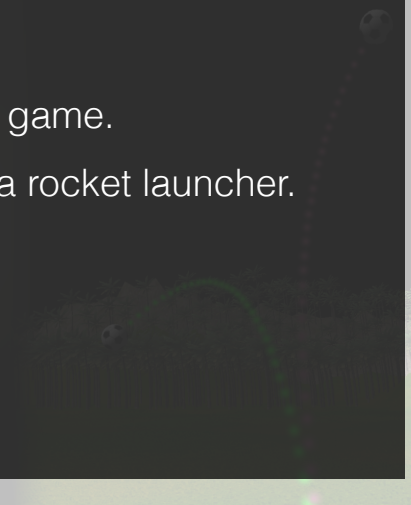
In this video...

- Make a simple hit-the-target game.
- Add a cylinder to represent a rocket launcher.
- Write **Launcher.cs** class.

```

// Resolve forces (Vector3[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaTime = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaTime;
    pos += vel * deltaTime;
    if (isEnabled) transform.position = pos;
}

```



Write Launcher.cs class

- Take **maxLaunchSpeed** as a parameter.
- Drag-in two sounds, for wind-up and launch.
- Drag-in the ball to be instantiated & launched.
- Launch speed increases while launcher clicked.



```

Vector3 Gravity_force() {
    return new Vector3(0,-g,0);
}

// Air resistance opposing motion
Vector3 Air_force(){
    float vMag = vel.magnitude;
    Vector3 vDir = vel.normalized;
    float airDragMag = dragConst * Mathf.Pow(vMag, 2);
    return airDragMag * -vDir;
}

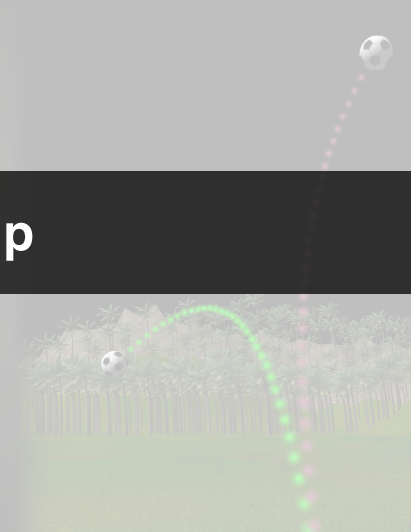
```

Finishing & Tidying Up

```

void ResolveForces (Vector3[] forces) {
    Vector3 combinedForce = Vector3.zero;
    foreach (Vector3 force in forces) {
        combinedForce += force;
    }
    float deltaTime = Time.fixedDeltaTime;
    acc = combinedForce / mass;
    vel += acc * deltaTime;
    pos += vel * deltaTime;
    if (isEnabled) transform.position = pos;
}

```



In this video...

- Re-introduce Universal Gravitation.
- Review the overall structure of what we've done.

```
Vector3 Gravity_Force() {  
    return new Vector3(0,-g,0);  
}  
  
// Air resistance opposing motion  
Vector3 Air_Force(){  
    float vMag = vel.magnitude;  
    Vector3 vDir = vel.normalized;  
    float airDragMag = dragConst * Mathf.Pow(vMag, 2f);  
    return airDragMag * -vDir;  
}
```

Section Wrap-Up

```
void ResolveForces (Vector3[] forces) {  
    Vector3 combinedForce = Vector3.zero;  
    foreach (Vector3 force in forces) {  
        combinedForce += force;  
    }  
    float deltaT = Time.fixedDeltaTime;  
    acc = combinedForce / mass;  
    vel += acc * deltaT;  
    pos += vel * deltaT;  
    if (isEnabled) transform.position = pos;  
}
```

What You've Learnt

- Basic physics engine architecture / trade-offs.
- A foundation in Newton's Laws of Motion.
- Dimensional checking as a tool.
- How to distill information from Wikipedia etc.
- How to create components for various forces.

Create & Share Rocket Lander

- Give keyboard control over thrust.
- Display fuel, velocity and height to player.
- Challenge to "land" below 5 m s⁻¹.
- Score is fuel kg remaining.
- Share with us via [GameBucket.io.g](https://gamebucket.io/g)

