June 3, 2022

The results below are generated from an R script.

```
## Install a package manager and packages
if (!require("pacman")) {
  install.packages("pacman")
}
pacman::p_load(Rfast, foreach, doParallel, mvnfast, rstudioapi)
current_path = rstudioapi::getActiveDocumentContext()$path
setwd(dirname(current_path))
## Error in setwd(dirname(current_path)): cannot change working directory
pacman::p_load_gh("pkimes/sigclust2")
shc = get("shc", env = environment(shc))
source("sequential_function.R")
\# k = 3 \# number of clusters (3 or 10)
# uneven = FALSE #whether or not to have uneven weights
# distribution = 't' # t distribution or normal distribution?
# iterations = 50 # number of iterations
n = 500 \# total number of samples
alpha = 0.05
if (distribution=='t'){
  distribution_name = 'True distribution components: t-distribution (df=3) mixture distribution'
  samplefunc <- function(n, mu, sigma, w){</pre>
    rmixt(n = n,mu = mus,sigma = sigmas,w = w,df = 3)
  }
}else{
  distribution_name = 'True distribution: Normal mixture distribution'
  samplefunc <- function(n, mu, sigma, w){</pre>
 rmixn(n=n, mu=mus, sigma=sigmas, w=w)
}
}
# formulating d, delta (dimension and distance between clusters)
if (k == 10){
  a = c(2, 1, 2, 2, 2, 3, 2, 4, 2, 5, 2, 6, 2, 7, 2, 8, 2, 9) # dim2
 b = c(8, 1, 8, 2, 8, 3, 8, 4, 8, 5, 8, 6, 8, 7, 8, 8, 8, 9) # dim8
  d_delta = matrix(c(a, b) , ncol = 2, byrow = T)
} else if (k == 3){
```

```
a = c(2, 1, 2, 2, 2, 3, 2, 4, 2, 5, 2, 6, 2, 7, 2, 8, 2, 9) # dim2
  b = c(8, 1, 8, 2, 8, 3, 8, 4, 8, 5, 8, 6, 8, 7, 8, 8, 8, 9) # dim8
  d_delta = matrix(c(a, b) , ncol = 2, byrow = T)
} else {
  stop("k != 3 or 10")
#weights
w = rep.int(1, k)
if (uneven){
 w[1] = 1 / 4
 w[2] = 1 / 2
w = w / sum(w)
K = floor(sqrt(n / 2)) #num clusters to test
K = min(K, 14L) # to ensure not estimating too many clusters
coresToUse = floor(detectCores() / 2) # cores to use
# function which creates data and performs one iteration
simulation <- function(iteration) {</pre>
  # simulate data
  set.seed(18 + iteration)
  data = samplefunc(n=n, mu=mus, sigma=sigmas, w=w)
  D1 = data[1:floor(n / 2), ]
  D2 = data[(floor(n / 2) + 1):n,]
  # Estimate no.clusters
  Cluster_numbers = estimate.cluster.all(D1, D2, alpha, K)
  sigclust_splits = sum(shc(data, alpha = alpha)$nd_type == "sig")
 return(c(unlist(Cluster_numbers, use.names = F), sigclust_splits + 1L))
meanEstimate = matrix(nrow = nrow(d_delta), ncol = iterations)
medianEstimate = meanEstimate
meanEstimate12 = meanEstimate
medianEstimate12 = meanEstimate
AICEstimate = meanEstimate
BICEstimate = meanEstimate
sigclustEstimate = meanEstimate
RIFThierEstimate = meanEstimate
# For parallel computing
cl <- makeCluster(coresToUse) #not to overload computer</pre>
registerDoParallel(cl)
```

```
for (j in 1:nrow(d_delta)) {
  d = d_delta[j, 1]
  delta = d_delta[j, 2]
  \#sigmas = lapply(c(3,1,1), function(x) diag(x, nrow=d))
  sigmas = lapply(rep.int(1, k), function(x)
   diag(x, nrow = d))
  \#mus = zeros(k, d)
  \#mus[1,1] = delta
  \#mus[2,2] = -delta
  \#mus[3,2] = delta
  mus = outer(rep.int(1L, k), seq.int(d)) + delta * seq.int(0, k - 1L)
  estimates <-
   foreach(
     i = 1:iterations,
      .combine = cbind,
      .inorder = F,
      .packages = c("mclust", "Rfast", "mvnfast", "MASS"),
      .verbose = F
    ) %dopar% {
     simulation(i)
   }
  # format data into table
  meanEstimate[j, ] = estimates[1, ]
  medianEstimate[j, ] = estimates[2, ]
 meanEstimatel2[j, ] = estimates[3, ]
  medianEstimatel2[j, ] = estimates[4, ]
  BICEstimate[j, ] = estimates[5, ]
  AICEstimate[j,] = estimates[6,]
  RIFThierEstimate[j, ] = estimates[7, ]
  sigclustEstimate[j, ] = estimates[8, ]
  df = stack(data.frame(
   cbind(
      "Mean" = meanEstimate[j, ],
      "Mean12" = meanEstimate12[j, ],
      "Median" = medianEstimate[j, ],
      "Median12" = medianEstimatel2[j, ],
      "AIC" = AICEstimate[j, ],
      "BIC" = BICEstimate[j, ],
      "RIFT.hc" = RIFThierEstimate[j, ],
      "shc" = sigclustEstimate[j, ]
   )
  print(paste0("(dimension, delta) = (", d, ",", delta, ")"))
  colnames(df) = c("ESTIMATE" , "METHOD")
  tableEstimates = with(df, table(METHOD, ESTIMATE))
  print(tableEstimates)
```

```
## [1] "(dimension, delta) = (2,1)"
          ESTIMATE
##
           1 2 3 4 5 6 7 8 14
## METHOD
           68 25 6 1
##
    Mean
                      0
                         0
                            0
                              0 0
##
    Mean12
           68 25 6
                    1
                      0
                         0
                            0
    Median 4 40 44
                      2
                         2 0 0 0
##
                   8
    Medianl2 4 40 44 8 2 2 0 0 0
##
           10 37 36 12 4 1 0 0 0
##
    AIC
           34 40 23 1
                      2 0 0 0
##
    BIC
##
    RIFT.hc 15 51 21 9 4 0 0 0 0
##
            0 13 40 22 8 8 6 2 1
    shc
  [1] "(dimension, delta) = (2,2)"
##
##
          ESTIMATE
## METHOD
           1 2 3 4 5 6 7 8 9 10 11
##
    Mean
           61 24 14 1 0 0 0 0 0 0
##
    Meanl2 62 23 14 1
                      0
                         0
                            0
                              0
                                0
##
            3 26 50 14
                      5
                         2 0
                              0
                                0
    Median
##
    Medianl2 3 26 50 14
                      5 2
                            0 0
##
            2 17 49 25
                              0 0
    AIC
                      6 0 1
##
    BIC
           33 35 25 5
                      2
                         0 0
                              0
                                0
##
    RIFT.hc 16 28 32 15 9 0 0 0 0 0
           0 0 0 2 16 22 30 12 12 5 1
    shc
  [1] "(dimension, delta) = (2,3)"
##
         ESTIMATE
##
## METHOD
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
##
    Mean
          53 23 18 6 0 0 0 0 0 0 0
    Meanl2 53 23 18 6
##
                      0
                         0
                            0
                              0
                                0
                                   0
                                      0
                                        0
##
    Median 1 15 27 17
                      5
                         3
                            2
                              1
                                 2
                                   4
                                      3
                                        7
    Medianl2 1 15 27 18 6 2 2 1 3 3 3
##
##
            3 12 45 27 8 4 0 0 0 0 0
    ATC
                                        1
##
    BIC
           26 39 29 5 1 0 0 0 0 0
                                        0
##
    RIFT.hc 17 22 35 14 10 1 1 0 0 0 0
                                        0
                                           0
##
          0 0 0 0 0 1 5 10 34 33 14 2 1
##
  [1] "(dimension, delta) = (2,4)"
##
          ESTIMATE
## METHOD
            1 2 3 4 5 6 7 8 9 10 11 12 13 14
##
           33 17 19 7 5 2 2 2 3 4 2 2 0 2
    Mean
    Meanl2 33 17 19 7 5
                         2 2 2 3 4 2
##
            0 3 3
                    0
                      1
                         2
                            2
                             5 12 23 15 16
##
    Median
                         2 2 5 13 25 11 17
##
    Median12 0 3 3 0
                      1
                                           1 17
            1 6 23 14 5 5 2 2 4 9 9
##
##
    BIC
           25 33 30 10 1 0 1
                              0 0 0
                                     0
                                        0
                                           0
                                              0
    RIFT.hc 20 19 37 12 11 0 0 0 1 0 0
##
                                        0
          0 0 0 0 0 0 0 3 19 62 14 2 0 0
##
  [1] "(dimension, delta) = (2,5)"
##
         ESTIMATE
##
## METHOD
            1 2 3 4 5 6 7 8 9 10 11 12 13 14
            8 9 10 10 6 7 6 6 9 8 10 6 4 1
##
##
    Meanl2
            8 10 10 8
                      6 7 7 7 9 8 9 6 4 1
##
    Median
            0 0 0
                    0
                      1
                         0 3 11 11 23 18 14
                                           5 14
##
    Medianl2 0 0 0 0 1 0 3 11 14 23 17 14 4 13
## AIC 0 2 5 3 6 1 2 2 5 16 13 22 16 7
```

```
##
    BIC 19 28 26 8 5 1 1 0 1 3 3 3 2 0
    RIFT.hc 20 24 25 20 7 4 0 0 0 0 0 0 0
           0 0 0 0 0 0 0 2 11 73 12 2 0 0
##
##
  [1] "(dimension, delta) = (2,6)"
         ESTIMATE
##
## METHOD
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
##
    Mean
            4 3 3 5
                     7 5 8 11 17 16 11 5 2 3
##
    Meanl2
            5 2 3 5
                     7 5 8 11 17 16 11
                                       5
                                         2 3
##
    Median
            0 0 0 0 0 0 0 7 28 24 19
                                      7 3 12
##
    Medianl2 0 0 0 0 0 0 1 7 30 26 19 5 1 11
                     0 0 0 4 7 21 24 13 14 15
##
    AIC
            0 1 1
                   0
           9 14 12 7
                     2 1 1 0 6 18 9 8 5 8
##
    BTC
##
    RIFT.hc 20 28 26 15 4 6 1 0 0 0 0 0 0
##
         0 0 0 0 0 0 0 0 8 83 9 0 0 0
  [1] "(dimension, delta) = (2,7)"
##
          ESTIMATE
##
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
##
    Mean
           4 1 2 3 0 4 6 13 30 17 8 5 5 2
##
    Meanl2
           4 1 2
                   3
                     0
                        4 6 13 30 17
                                    8
                                       5
            0 0 0 0 0 0 0 11 28 27 19 8 6 1
##
    Median
##
    Median12 0 0 0 0
                     0 0 0 12 28 28 19 8 4 1
##
            0 0 0 0
                     0
                        0 0 3 7 14 25 18 17 16
    AIC
##
    BIC
           4 5 2 4
                     0
                        0 0 1 7 17 21 13 11 15
##
    RIFT.hc 19 28 27 17 4 5 0 0 0 0 0 0 0
##
          0 0 0 0 0 0 0 0 4 85 11 0 0 0
  [1] "(dimension, delta) = (2,8)"
##
##
         ESTIMATE
## METHOD
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
##
           3 0 1 0 0 4 3 9 23 29 15 5 3
    Mean
##
            3 0 1
                   0
                     0
                        4 3 9 23 29 15
    Meanl2
            0 0 0 0 1 0 0 9 35 28 10
##
    Median
                                       6
    Medianl2 0 0 0 0 1 0 0 10 38 28 7
##
            0 0 0 0 0 0 0 3 6 32 12 18 11 18
##
    AIC
##
    BIC
            1 1 2 0 0 0 0 3 11 32 16 13 7 14
##
    RIFT.hc 16 26 30 18 5 3 1 0 1 0 0 0 0
           0 0 0 0 0 0 0 0 4 88 7 1 0 0
  [1] "(dimension, delta) = (2,9)"
##
          ESTIMATE
##
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
##
            3 0 0 0 0 1 2 7 25 44 9 4 2 3
    Mean
##
    Meanl2
            3 0 0 0 0 1 2 7 25 44 9
                                       4
##
            0 0 0 0
                     0
                        0 1 5 36 37 13
                                       3
    Median
    Medianl2 0 0 0 0 0 0 1 5 38 38 10 3 3 2
##
##
    AIC
            0 0 0 0
                     0 0 0 0 9 34 17 10 15 15
##
    BIC
            0 0 0 0
                     0
                        0 0 1 9 37 19 8 13 13
##
    RIFT.hc 21 31 21 18 8 1 0 0 0 0 0 0 0
           0 0 0 0 0 0 0 0 2 91 6 1 0 0
## [1] "(dimension, delta) = (8,1)"
         ESTIMATE
##
## METHOD
           1 2 3 4 5 6 7 8 9 10 11 12 14 15 16 17 18 19 20 21 22 23 24 25 26
##
    Mean
           21 58 7 7
                     6 1
                           0 0 0 0 0 0 0
                                              0
                                                0
                                                  0
                                                     0
    Meanl2 21 58 7 7
                           0
                             0 0 0 0
                                       0
                                         0 0
                                                     0
                                                        0 0 0 0
                                                                  0
##
                     6 1
                                              0
                                                 0
                                                   0
##
    Median 1 62 22 12 3 0 0 0 0 0
                                      0 0 0 0 0 0 0 0 0 0
                                                                  0
## Medianl2 1 62 22 12 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
```

```
0 5 21 25 36 6 3 2 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0
##
    AIC
             0 20 42 15 16 3 1 1 1
                                     0
                                       1
                                          0
                                             0
                                                0
                                                  0
                                                     0
                                                       0
                                                          0
                                                             0
##
             2 36 39 21 1 1 0 0 0 0 0
                                          0
                                             0 0 0 0 0 0 0
                                                                  0
                                                                    0
                                                                       0
    RIFT.hc
             0 0 0 0 0 0 0 0 2 4 0
                                          6
                                             6
                                               8 7 8 10 6 12 9
##
                                                                  8 5
  [1] "(dimension, delta) = (8,2)"
##
##
           ESTIMATE
## METHOD
            1 2 3 4 5 6 7 8 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27
##
    Mean
            22 53 11
                     9
                       5
                          0
                            0
                               0 0
                                    0
                                       0
                                          0
                                             0
                                               0
                                                  0
                                                    0
                                                       0
                                                          0
                                                             0
                                                               0
                                                                 0
                                                                    0
##
    Mean12
           22 53 11
                       5
                          0
                             0
                                0
                                  0
                                     0
                                       0
                                          0
                                             0
                                                0
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
##
            0 62 23
                     9
                      4
                          1
                             0
                               0
                                  0
                                     0
                                       0
                                          1
                                             0
                                                0
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
    Median
##
    Medianl2 0 62 23 9 4
                          1
                             0
                               0
                                  0
                                     0
                                       0
                                          1
                                             0
                                                0
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
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                                                                     0
                                                                       0
             0 6 23 23 29
                          9
                             1
                               4
                                  1
                                             1
                                                0
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                                                     0
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                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
                                                                          0
##
    ATC
                                     1
                                       1
                                          1
##
             0 19 43 17 13
                          4
                             2
                               0
                                  1
                                     0
                                       0
                                          1
                                             0
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                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
##
             1 55 41 2 0 1 0 0 0
                                     0
                                       0
                                          0
                                             0
                                               0
                                                 0
                                                     0 0
                                                         0
                                                            0
                                                               0
                                                                 0 0
                                                                       \cap
                                                                          0
                                                                             \cap
    RIFT.hc
                                                                                0
             ##
##
           ESTIMATE
## METHOD
           28
##
    Mean
            0
##
    Mean12
             0
##
    Median
             0
##
    Medianl2 0
##
    AIC
             0
##
    BIC
             0
##
    RIFT.hc
             0
##
    shc
            1
  [1] "(dimension, delta) = (8,3)"
##
##
          ESTIMATE
## METHOD
            1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 27
##
            21 52 12 7 5 0 0 0 0 0 1 1 0 1 0 0
                                                       0
                                                         0
                                                            0
                                                               0
                                                                 0 0 0 0
    Mean
##
            21 52 12
                     7
                       5
                          0
                             0
                               0
                                  0 0
                                       1
                                          1
                                             0
                                               1
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
                                                                          0
    Meanl2
                       5
                          3
                             2 0 1 10 10 18 11
                                               5
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
##
    Median
             0 17 14
                    4
                                                  \cap
                                                     \cap
                                                        \cap
                                                                          \cap
                                                                             \cap
    Medianl2 0 17 14 4 5 3 2 0 1 9 15 16 10
                                                4
                                                  0
                                                     0
                                                        0
                                                             0
             0 6 20 22 29 6 2 2
                                       2
                                     0
                                          3
                                             2
                                                5
                                                  0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
##
    ATC
                                 1
                                                     0
##
    BIC
             0 23 40 12 16
                          3
                             2
                               0
                                  0
                                     1
                                       1
                                          2
                                             0
                                                0
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
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                                                                  0
                                                                     0
    RIFT.hc
             3 49 46 2 0 0 0 0 0 0 0
                                             0
                                               0
                                                  0
                                                    \cap
                                                       0 0 0 0 0
                                                                    Ω
                                                                       0
##
             0 0 0 0 0 0 0
                                  0
                                    0
                                       0
                                          0
                                             1
                                               1
                                                  3
                                                    4 8 16 14 14 21 7
   [1] "(dimension, delta) = (8,4)"
##
##
           ESTIMATE
            1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 27
## METHOD
##
            18 50 11 10 6
                         1 0
                               0 0 1 0 1 1 1 0
                                                    0
                                                       0
                                                         0
                                                            0
                                                               0
                                                                 0
    Mean
##
    Meanl2 18 50 11 10
                       6
                          1
                             0
                               0 0 1
                                       0
                                          1
                                             1
                                               1
                                                  0
                                                     0
                                                       0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
##
             0 7
                 4
                    3
                       0
                          1
                            0 0
                                 0 9 19 33 18
                                                6
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
    Median
    Median12 0 7 4 3 0
                         1 0 0 1 15 19 30 17
                                                3
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     \cap
##
                                                  0
                                                     0
                                                        0
##
             0 6 26 16 20 3 3 1
                                  0
                                    0
                                       3
                                          8
                                             6
                                                8
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
    ATC
##
    BIC
             0 20 40 14 14
                          1
                            1
                               2
                                  0
                                     1
                                       2
                                          3
                                             1
                                                1
                                                  0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
##
    RIFT.hc
             3 59 35 3 0 0 0 0 0 0
                                          0
                                            0
                                               0
                                                  0 0 0
                                                          0
                                                            0
                                                               0 0
                                                                    0
                                                                       0
                                                                             0
             0 0 0 0 0 0 0 0 0 0 0 1 1 6 8 10 11 13 19 18 6 4
  [1] "(dimension, delta) = (8,5)"
##
          ESTIMATE
##
## METHOD
            1 2 3 4 5 6 7 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 26 27
            20 48 12 5 2
                          0 0 2 0 1 1 3
##
    Mean
                                             6
                                               0
                                                  0
                                                     0
                                                        0
                                                          0
                          0 0 2 0 1 1 3
    Meanl2
            20 48 12 5
                       2
                                             6
                                               0
                                                        0
                                                          0
                                                             0
                                                               0
                                                                  0
                                                                     0
                                                                       0
##
                                                  0
                                                     0
##
    Median
            0 5 0 1 1
                          0 0 1 13 25 25 19 10 0 0 0
                                                       0
                                                          0
                                                             0
                                                               0
                                                                  0
                                                                     0
                                                                       \cap
## Medianl2 0 5 0 1 1 0 0 2 19 24 25 16 7 0 0 0 0 0 0 0 0 0 0 0
```

```
4 9 16 0 0 0 0 0
##
     AIC
                0 7 17 20 15 5
                                   1 0 1
                                              5
                                                                          0 0 0 0
                                                                                         0
                                 3
                                    0
                                                 2
                                                    3
                                                                        0
                                                                            0
                                                                               0
##
     BTC.
                0 24 36 15 11
                                       0
                                          1
                                              4
                                                        1
                                                           0
                                                               0
                                                                  0
                                                                     0
##
                3 51 40
                         6
                             0
                                0
                                    0
                                       0
                                          0
                                              0
                                                 0
                                                    0
                                                        0
                                                           0
                                                              0 0
                                                                    0
                                                                        0
                                                                           0
                                                                               0
                                                                                  0
                                                                                      0
                                                                                         0
     RIFT.hc
                             0 0
                                   0
                                          0
                                             0
                                                 0
                                                        2
##
                0
                   0 0 0
                                       0
                                                    1
                                                           6
                                                              6 11 21 10 15 10
                                                                                  8
   [1] "(dimension, delta) = (8,6)"
##
##
              ESTIMATE
##
   METHOD
                1 2 3
                          4
                             5
                                6
                                   7
                                       9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 27
##
     Mean
               20 41
                       6
                          9
                             6
                                 1
                                    0
                                       1
                                          4
                                              2
                                                 2
                                                     3
                                                        5
                                                           0
                                                              0
                                                                  0
                                                                     0
                                                                        0
                                                                            0
                                                                               0
                                                                                   0
                                                                                      0
##
     Mean12
               20 41
                          9
                             6
                                 1
                                    0
                                       1
                                           4
                                              2
                                                 2
                                                     3
                                                        5
                                                           0
                                                               0
                                                                  0
                                                                     0
                                                                         0
                                                                            0
                                                                               0
                                                                                   0
##
                             0
                                 0
                                       4 18 29 20 16
                                                        9
                                                           0
                                                                     0
                                                                        0
                                                                            0
                                                                               0
                                                                                  0
     Median
                0
                   2
                       1
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   [1] "(dimension, delta) = (8,7)"
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##
   [1] "(dimension, delta) = (8,8)"
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   [1] "(dimension, delta) = (8,9)"
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##
                0 0
#stop cluster (parallel computing)
stopCluster(cl)
print(distribution name )
## [1] "True distribution components: t-distrbution (df=3) mixture distribution"
```

```
print(paste(k, 'true clusters:'))
## [1] "10 true clusters:"

print('Cluster weights:')
## [1] "Cluster weights:"

print(w)
## [1] 0.02857143 0.05714286 0.11428571 0.11428571 0.11428571 0.11428571 0.11428571 0.11428571
```

The R session information (including the OS info, R version and all packages used):

```
sessionInfo()
## R version 4.1.2 (2021-11-01)
## Platform: x86_64-apple-darwin17.0 (64-bit)
## Running under: macOS Monterey 12.0.1
## Matrix products: default
## LAPACK: /Library/Frameworks/R.framework/Versions/4.1/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_GB.UTF-8/en_GB.UTF-8/en_GB.UTF-8/C/en_GB.UTF-8/en_GB.UTF-8
## attached base packages:
## [1] grid
                                   graphics grDevices utils
                 parallel stats
                                                                   datasets methods
## [9] base
##
## other attached packages:
## [1] arm_1.12-2
                                              Matrix_1.3-4
                                                                 knitr_1.37
                           lme4_1.1-27.1
## [5] sigclust_1.1.0
                                              gridExtra_2.3
                           mixtools_1.2.0
                                                                 ggplot2_3.3.5
## [9] MASS_7.3-54
                           pracma_2.3.6
                                              mclust 5.4.9
                                                                 sigclust2_1.2.4
## [13] rstudioapi_0.13
                           mvnfast_0.2.7
                                              doParallel_1.0.16 iterators_1.0.13
## [17] foreach_1.5.1
                           Rfast_2.0.6
                                              RcppZiggurat_0.1.6 Rcpp_1.0.8
## [21] pacman_0.5.1
##
## loaded via a namespace (and not attached):
## [1] minqa_1.2.4
                               colorspace_2.0-2
                                                      ellipsis_0.3.2
## [4] dynamicTreeCut_1.63-1 htmlTable_2.4.0
                                                      XVector_0.34.0
## [7] base64enc_0.1-3
                               ggdendro_0.1.23
                                                      bit64_4.0.5
## [10] AnnotationDbi_1.56.2
                              fansi_0.5.0
                                                      codetools_0.2-18
## [13] splines_4.1.2
                               cachem_1.0.6
                                                      impute_1.68.0
## [16] Formula_1.2-4
                               nloptr_1.2.2.3
                                                      broom_0.7.12
## [19] WGCNA 1.70-3
                               cluster 2.1.2
                                                      kernlab 0.9-29
## [22] GO.db 3.14.0
                               png_0.1-7
                                                      compiler_4.1.2
## [25] httr 1.4.2
                               backports 1.4.1
                                                      fastmap 1.1.0
## [28] htmltools_0.5.2
                               tools_4.1.2
                                                      coda_0.19-4
## [31] gtable_0.3.0
                               glue_1.6.1
                                                      GenomeInfoDbData 1.2.7
## [34] dplyr_1.0.7
                               ggthemes_4.2.4
                                                      Biobase_2.54.0
## [37] vctrs_0.4.1
                               Biostrings_2.62.0
                                                      preprocessCore_1.56.0
## [40] nlme_3.1-153
                                                      fastcluster_1.2.3
                               xfun_0.30
                                                    zlibbioc_1.40.0
## [43] stringr_1.4.0
                              lifecycle_1.0.1
```

```
## [46] scales_1.1.1
                                                      yaml_2.3.4
                               RColorBrewer_1.1-2
## [49] memoise_2.0.1
                               rpart_4.1-15
                                                      segmented_1.3-4
## [52] latticeExtra 0.6-29
                               stringi_1.7.6
                                                      RSQLite 2.2.10
## [55] highr_0.9
                               S4Vectors_0.32.3
                                                      blme_1.0-5
## [58] checkmate_2.0.0
                               BiocGenerics_0.40.0
                                                      boot 1.3-28
## [61] GenomeInfoDb_1.30.1
                               rlang_1.0.2
                                                      pkgconfig_2.0.3
## [64] matrixStats_0.61.0
                               bitops_1.0-7
                                                      evaluate_0.15
## [67] lattice_0.20-45
                               purrr_0.3.4
                                                      htmlwidgets_1.5.4
## [70] bit_4.0.4
                               tidyselect_1.1.1
                                                      magrittr_2.0.2
## [73] R6_2.5.1
                                                      generics_0.1.1
                               IRanges_2.28.0
## [76] Hmisc_4.6-0
                               DBI_1.1.2
                                                      pillar_1.6.4
## [79] foreign_0.8-81
                               withr_2.4.3
                                                      survival_3.2-13
## [82] KEGGREST_1.34.0
                               abind_1.4-5
                                                      RCurl_1.98-1.6
## [85] nnet_7.3-16
                               tibble_3.1.6
                                                      crayon_1.4.2
## [88] utf8_1.2.2
                               rmarkdown_2.13
                                                      jpeg_0.1-9
## [91] data.table 1.14.2
                               blob 1.2.2
                                                      forcats 0.5.1
## [94] digest_0.6.29
                               tidyr_1.1.4
                                                      stats4_4.1.2
## [97] munsell_0.5.0
Sys.time()
## [1] "2022-06-03 05:01:13 BST"
```