## June 10, 2022

The results below are generated from an R script.

```
## Install a package manager and packages
if (!require("pacman")) {
  install.packages("pacman")
}
pacman::p_load(Rfast, foreach, doParallel, mvnfast, rstudioapi)
current_path = rstudioapi::getActiveDocumentContext()$path
setwd(dirname(current_path))
## Error in setwd(dirname(current_path)): cannot change working directory
pacman::p_load_gh("pkimes/sigclust2")
shc = get("shc", env = environment(shc))
source("sequential_function.R")
\# k = 3 \# number of clusters (3 or 10)
# uneven = FALSE #whether or not to have uneven weights
# distribution = 't' # t distribution or normal distribution?
# iterations = 50 # number of iterations
n = 500 \# total number of samples
alpha = 0.05
if (distribution=='t'){
  distribution_name = 'True distribution components: t-distribution (df=3) mixture distribution'
  samplefunc <- function(n, mu, sigma, w){</pre>
    rmixt(n = n,mu = mu,sigma = sigma,w = w,df = 3)
  }
}else{
  distribution_name = 'True distribution: Normal mixture distribution'
  samplefunc <- function(n, mu, sigma, w){</pre>
 rmixn(n=n, mu=mu, sigma=sigma, w=w)
}
}
# formulating d, delta (dimension and distance between clusters)
if (k == 10){
  a = c(2, 20, 2, 40, 2, 60, 2, 80, 2, 100, 2, 150, 2, 200) # dim2
 b =c(8, 20, 8, 40, 8, 60, 8, 80, 8, 100, 8, 150, 8, 200) # dim8
  d_delta = matrix(c(a, b) , ncol = 2, byrow = T)
} else if (k == 3){
```

```
a = c(2, 1, 2, 2, 2, 3, 2, 4, 2, 5, 2, 6, 2, 7, 2, 8, 2, 9) # dim2
  b = c(8, 1, 8, 2, 8, 3, 8, 4, 8, 5, 8, 6, 8, 7, 8, 8, 8, 9) # dim8
  d \ delta = matrix(c(a, b), ncol = 2, byrow = T)
} else {
  stop("k != 3 or 10")
#weights
w = rep.int(1, k)
if (uneven){
 w[1] = 1 / 4
 w[2] = 1 / 2
w = w / sum(w)
K = floor(sqrt(n / 2)) #num clusters to test
K = min(K, 14L) # to ensure not estimating too many clusters
coresToUse = floor(detectCores() / 2) # cores to use
# function which creates data and performs one iteration
simulation <- function(iteration) {</pre>
  mu = matrix(runif(k*d, min = 0, max = delta), nrow = k)
  # simulate data
  set.seed(18 + iteration)
  data = samplefunc(n=n, mu=mu, sigma=sigma, w=w)
  D1 = data[1:floor(n / 2),]
  D2 = data[(floor(n / 2) + 1):n,]
  # Estimate no.clusters
  Cluster_numbers = estimate.cluster.all(D1, D2, alpha, K)
  sigclust_splits = sum(shc(data, alpha = alpha)$nd_type == "sig")
 return(c(unlist(Cluster_numbers, use.names = F), sigclust_splits + 1L))
}
meanEstimate = matrix(nrow = nrow(d_delta), ncol = iterations)
medianEstimate = meanEstimate
meanEstimate12 = meanEstimate
medianEstimate12 = meanEstimate
AICEstimate = meanEstimate
BICEstimate = meanEstimate
sigclustEstimate = meanEstimate
RIFThierEstimate = meanEstimate
# For parallel computing
cl <- makeCluster(coresToUse) #not to overload computer</pre>
```

```
registerDoParallel(cl)
for (j in 1:nrow(d_delta)) {
  d = d_delta[j, 1]
  delta = d_delta[j, 2]
  \#sigma = lapply(c(3,1,1), function(x) diag(x, nrow=d))
  sigma = lapply(rep.int(1, k), function(x)
   diag(x, nrow = d))
  estimates <-
   foreach(
     i = 1:iterations,
     .combine = cbind,
     .inorder = F,
     .packages = c("mclust", "Rfast", "mvnfast", "MASS"),
      .verbose = F
    ) %dopar% {
     simulation(i)
  # format data into table
  meanEstimate[j, ] = estimates[1, ]
  medianEstimate[j, ] = estimates[2, ]
  meanEstimatel2[j, ] = estimates[3, ]
 medianEstimatel2[j, ] = estimates[4, ]
  BICEstimate[j, ] = estimates[5, ]
  AICEstimate[j,] = estimates[6,]
  RIFThierEstimate[j, ] = estimates[7, ]
  sigclustEstimate[j, ] = estimates[8, ]
  df = stack(data.frame(
    cbind(
      "Mean" = meanEstimate[j, ],
      "Mean12" = meanEstimate12[j, ],
      "Median" = medianEstimate[j, ],
      "Median12" = medianEstimatel2[j, ],
      "AIC" = AICEstimate[j, ],
      "BIC" = BICEstimate[j, ],
      "RIFT.hc" = RIFThierEstimate[j, ],
     "shc" = sigclustEstimate[j, ]
   )
  ))
  print(paste0("(dimension, delta) = (", d, ",", delta, ")"))
  colnames(df) = c("ESTIMATE" , "METHOD")
 tableEstimates = with(df, table(METHOD, ESTIMATE))
 print(tableEstimates)
```

```
## [1] "(dimension, delta) = (2,20)"
##
          ESTIMATE
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
            5 7 19 18 17 11 2 13 3 4 1 0 0 0
##
    Mean
##
    Meanl2
          5 7 19 18 17 11 2 13 3 4 1 0 0 0
##
    Median
           0 0 1 4 14 10 12 19 12 10 5 1
                                           2 10
##
    Medianl2 0 0 1 4 14 11 11 19 12 11
                                     4
                                        1
##
            0 1 3 5 12 5 17 26 14 8 7 1 0
    AIC
##
    BIC
            0 3 16 12 14 10 17 15 4 5 4 0 0 0
##
            8 6 14 26 30 10 6 0 0 0 0 0 0
    RIFT.hc
##
    shc
            2 1 1 4 3 10 11 17 19 14 8 5 4 1
##
  [1] "(dimension, delta) = (2,40)"
##
          ESTIMATE
           -1 1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
##
            0 0 1 1 4 6 9 17 21 18 14 4 3 2 0
    Mean
##
    Meanl2
            0 0 1 1 4 6 9 17 21 18 14 4 3 2 0
##
    Median
            0 0 0 0 0 0 4 7 21 15 13 12 3 0 25
##
    Medianl2 0 0 0 0 0 0 5 7 22 16 12 10 3 0 25
            0 0 0 0 0 0 2 3 20 18 16 18 12 10
##
    ATC
            0 0 0 0 0 1 2 6 19 20 21 16 7 6 2
##
           1 4 2 4 9 17 15 20 15 9 4 0 0 0 0
##
    RIFT.hc
##
    shc
            0 1 0 0 0 2 2 1 5 22 37 21 8 1 0
##
  [1] "(dimension, delta) = (2,60)"
          ESTIMATE
            1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
            0 0 1 1 2 9 23 16 16 21 5 3 0
##
    Mean
##
    Meanl2
            0 0 1 1 2 9 23 16 16 21 5 3 0 3
##
    Median
            0 0 0 0 1 2 10 16 16 13 4 2 2 34
    Medianl2 0 0 0 0 1 3 9 17 16 13 4 1
##
                                           3 33
##
            0 0 0 0 0 2 3 14 20 21 17 12
    AIC
            0 0 0 0 0 2 3 9 27 26 13 12 5 3
##
    BIC
##
    RIFT.hc 9 1 2 3 7 10 11 24 22 10 1 0 0 0
##
            0 0 0 1 0 0 1 0 11 40 31 14 1 1
##
  [1] "(dimension, delta) = (2,80)"
##
         ESTIMATE
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
            0 0 0 2 0 11 20 20 17 22 6 1 0 1
##
    Mean
##
    Meanl2
            0 0 0 2 0 11 20 20 17 22 6 1 0 1
            0 0 0 0 2 7 15 22 9 11 1 1 6 26
##
    Median
    Medianl2 0 0 0 0 2 7 15 23 10 9 1 1 7 25
##
            0 0 0 0 0 0 7 10 15 31 24
##
    AIC
                                        5
##
            0 0 0 0 0 3 5 11 17 31 25 4 2 2
    BIC
##
    RIFT.hc 11 2 6 4 4 5 9 24 18 14 3 0 0 0
##
        0 0 0 0 0 0 0 1 14 40 30 12 3 0
##
   [1] "(dimension, delta) = (2,100)"
##
          ESTIMATE
## METHOD
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
            0 1 0 2 2 7 16 23 28 15 3 2 1 0
##
    Mean
##
    Meanl2
            0 1 0 2 2 7 16 23 28 15 3 2 1 0
##
    Median
            0 0 0 0 2 7 18 27 12 9 1 1 3 20
##
    Median12 0 0 0 0 3 8 17 27 11 9 0 1 5 19
##
    AIC
            0 0 0 0 0 1 7 15 19 33 11 10
##
            0 0 0 0 0 1 8 13 25 30 13 7 2 1
    BTC
```

```
RIFT.hc 11 3 6 5 5 6 2 11 23 27 1 0 0 0
##
        1 0 0 0 0 0 0 1 10 42 26 11 7 2
## [1] "(dimension, delta) = (2,150)"
          ESTIMATE
           1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
##
            0 1 1 3 2 4 16 21 28 15 8 1 0
    Mean
##
    Meanl2
             0 1
                 1
                    3 2 4 16 21 28 15
                                      8
                                        1
##
    Median
             0
              0 0 0 3 10 24 25 19 6
                                      4
                                         2
                                           1
##
    Medianl2 0 0 0 0 4 13 20 26 18 6 4
##
             0 0 0 0 0 0 5 20 32 19 15
    ATC
            0 0 0 0 0 0 4 20 30 21 17
##
    BIC
##
    RIFT.hc 19 3 4 3 1 4 6 2 19 36 3 0 0
            0 0 0 0 0 0 0 0 1 36 45 10 7 1
##
  [1] "(dimension, delta) = (2,200)"
          ESTIMATE
##
            1 2 3 4 5 6 7 8 9 10 11 12 13 14
## METHOD
             0 0 0 1 2 8 17 24 25 17 6 0
    Mean
             0 0 0 1 2 7 18 24 25 17
##
    Meanl2
##
    Median
             0 0 0 0
                      2 16 23 20 20 9
                                      0
    Medianl2 0 0 0 0 2 16 25 18 20 9 0
##
                                        1
##
    AIC
            0 0 0 0 0 0 11 19 31 22 14
                                        1
             0 0 0 0 0 10 20 32 22 13
##
    BIC
                                           1
##
    RIFT.hc 16 1 5 2 6 7 6 4 12 40 1 0 0
           0 0 0 0 0 0 0 0 0 41 36 14 8 1
##
  [1] "(dimension, delta) = (8,20)"
##
          ESTIMATE
## METHOD
            1 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27
            1 1 1 2 0 2 1 0 1 78 7
                                        6 0 0
                                                       0
                                                          0 0 0 0 0 0 0
##
                                                0
                                                  0
                                                     0
##
    Meanl2
            1 1 1
                    2
                      0
                         2 1 0 1 78
                                      7
                                         6
                                           0
                                              0
                                                0
                                                   0
                                                     0
                                                        0
                                                           0
                                                             0
                                                               0
                                                                  0
                                                                     0
##
    Median
             0 0 0
                    0
                       0
                         0
                            1
                              9 26 56
                                      7
                                         1
                                           0
                                              0
                                                0
                                                   0
                                                     0
                                                        0
                                                           0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
    Median12 0 0 0 0
                      0 0 1 9 27 58
                                      4
                                           0
                                              0
                                                        0
                                                           0
                                                             0
                                                                0
                                                                  0
                                                                     0
                                                                       0
##
                                         1
                                                0
                                                   0
                                                     0
             0 0 0 0 0 0 0 0 66 22
                                        8
                                           4
                                              0
                                                0
                                                   0
                                                     0
                                                        0
                                                           0
##
             0 0 0 0 0 0 0 0 0 92 7
                                        0
                                          1
                                             0
                                                0
                                                   0 0 0
                                                          0 0
                                                               0 0
                                                                    0
##
    BTC
##
    RIFT.hc 0 0 1 1 3 17 28 33 15 2 0 0 0 0 0 0 0 0 0
                                                               0
                                                                  0
##
            0 0 0 0 0 0 0 0 0 0 1 2 6 9 4 10 13 18 17 8 5 2
           ESTIMATE
##
## METHOD
          28
##
    Mean
            0
##
    Meanl2
##
    Median
             0
##
    Medianl2 0
##
    AIC
             0
##
    BIC
             0
##
    RIFT.hc
            0
##
    shc
            1
  [1] "(dimension, delta) = (8,40)"
##
          ESTIMATE
           -1 1 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 27
## METHOD
            0 1 1
                    1
                      3
                         3 6 19 49 7 4 6 0 0 0
                                                  0
                                                     0 0 0 0
##
    Mean
                      3 3 6 19 49 7
                                      4
                                        6 0
                                                           0 0
##
    Meanl2
            0 1
                 1
                    1
                                              0
                                                0
                                                   0
                                                     0
                                                        0
                                                               0
            0
                 0
                    0
                      0
                         0 0 10 74 8 4
                                        4
                                           0
##
    Median
                                              0
                                                0
                                                   0
                                                     0
##
    Medianl2 0 0
                    0
                       0
                         0 0 13 76 4 3 4
                                           0
                                              0
                                                     0
                                                        0
                                                           0
                                                             0
                                                                0
                                                                  0
                 0
                                                0
                                                   0
##
    AIC
            0 0 0 0
                      0
                         0 0 3 37 21 21 18 0 0 0
                                                   0
                                                     0
                                                        0
                                                          0
                                                             0
                                                                0
                                                                  0
    BIC 0 0 0 0 0 0 6 83 7 3 1 0 0 0 0 0 0 0 0 0
##
```

```
RIFT.hc 1 0 0 0 3 11 25 48 12 0 0 0 0 0 0 0 0 0 0 0 0 0
##
          0 0 0 0 0 0 0 0 0 0 0 0 7 11 5 10 9 18 13 13 9 2 3
## [1] "(dimension, delta) = (8,60)"
          ESTIMATE
## METHOD
            -1 2 3 4 5 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27
##
             0 1 1
                      1
                        1
                           4 1 5 35 34 8 6 3 0 0 0
                                                         0
                                                            0
                                                               0
                                                                    0
    Mean
##
    Mean12
             0
                1
                   1
                      1
                        1
                           4
                              1
                                5 35 34
                                         8
                                            6
                                              3
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
                                                                             0
##
    Median
             0
                0
                   0
                      0
                        0
                           0
                              0 0 23 62
                                         9
                                            1
                                              5
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
                                                                             0
                                        3
##
    Medianl2 0
                0 0
                        0
                           0
                              0 0 29 63
                                           1
                                              4
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                     0
                                                                       0
##
             0
               0 0 0
                        0
                           0
                              0 0 2 33 24 17 24
                                                 0
                                                    0
                                                       0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
    ATC
                           0 0 0 9 64 18 7
##
    BIC
             0 0 0 0
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                                                    0
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                                                          0
                                                            0
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             5 0 0 0
                        0 0 4 26 49 16 0 0
                                              0
                                                 0
                                                    0
                                                      0 0
                                                            0
                                                              0
                                                                 0
                                                                    0
                                                                       0
                                                                          0
##
    RTFT.hc
             0 0 0 0 0 0 0 0 0 0 0
                                              0
                                                 7
                                                    9 7 11 5 15 20 15 5
##
   [1] "(dimension, delta) = (8,80)"
           ESTIMATE
##
            -1 1 2 5 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 26 27
## METHOD
             0 1 1 1 2 3 9 33 35 7 1 7 0 0 0
                                                      0
    Mean
                                                         0 0
                           3 9 33 35 7
                                            7
##
    Mean12
             0 1
                  1
                      1
                        2
                                         1
                                              0
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               \cap
                                                                  0
                                                                    0
                                                                       0
    Median
             \cap
                0
                   0
                      0
                        0
                           0
                             0 21 56 14
                                         3
                                            6
                                              0
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                        0
                           0 0 25 66 4
                                        0
                                            5
                                              0
                                                 0
                                                          0
                                                            0
                                                               \cap
                                                                  \cap
                                                                    0
                                                                       \cap
##
    Medianl2 0
               0
                   \cap
                      0
                                                    \cap
                                                       0
                             0 3 39 26 13 19
##
    AIC
             \cap
                0
                   0
                      0
                        0
                           0
                                               0
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                                                    0
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                                                          0
                                                            0
                                                               \cap
                           0 0 9 63 16 5
                                           7
##
             0 0
                     0
                        0
                                               0
                                                 0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                     0
                                                                       \cap
                                                                          0
    BIC
                   0
                                                    0
                                                       0
                        1 1 22 59 15 0 0
##
    RIFT.hc
             2 0 0 0
                                           0
                                              0 0
                                                    0 0
                                                         0
                                                            0
                                                               0
                                                                 0
                                                                    0
                                                                       0
                                                                          0
##
             0 0 0 0 0 0 0 0 0 0 0 0 5 10 9 10 8 20 14 12 7
   [1] "(dimension, delta) = (8,100)"
##
##
          ESTIMATE
## METHOD
            -1 1 3 4 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 28
             0 1 1 1 1 1 4 6 43 31 7 3 1 0
                                                              0 0 0 0 0 0
##
                                                   0
                                                      0
                                                         0
                                                            0
##
    Meanl2
             0
               1
                   1
                        1
                           1
                             4 6 43 31 7
                                            3
                                              1
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
                      1
##
    Median
             0
                0
                  0
                      0
                        0
                           0
                              0 2 20 56
                                         9
                                            3 10
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                     0
                                                                       0
                                                                          0
                                                                             0
                        0
                           0 0 2 24 57
                                         7
                                              9
                                                 0
                                                            0
                                                               0
                                                                  0
                                                                     0
                                                                       0
                                                                          0
##
    Medianl2 0
                0 0 0
                                            1
                                                    0
                                                       \cap
                                                          0
                                                                             \cap
                        0
                           0 0 0 11 45 28
                                            9
                                              7
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
##
             ()
                      0
             0 0 0 0 0 0 0 16 58 20
                                            4
                                              2
                                                 0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
##
    BTC
                                                    0
                                                       0
##
    RIFT.hc
             4
               0 0 0
                        0
                           0 0 20 61 15 0
                                            0
                                              0
                                                 0
                                                    0 0
                                                         0
                                                            0
                                                               0
                                                                 0
                                                                    0
                                                                       0
                                                                          0
             0 0 0 0 0 0 0 0 0 0 0 1 5 6 10 9 9 20 15 11 6
##
   [1] "(dimension, delta) = (8,150)"
##
           ESTIMATE
                        6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 26 27
## METHOD
            -1 1 2 3
                                                0 0 0
             0 3 0 1
                        2 1 3 8 41 33 4
                                           4 0
                                                         0
                                                            0 0 0 0 0
                                                                         0
##
    Mean
##
             0 3 0
                     1
                        2
                          1
                             3 8 41 33
                                        4
                                           4 0
                                                 0
                                                    0
                                                       0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
    Mean12
##
    Median
             0
               0 0
                     0
                        0
                           0
                              0 0 22 35
                                        5
                                            0 38
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
##
    Medianl2 0
                0
                  0
                     0
                        0
                           0
                              0 0 24 36
                                        2
                                            0 38
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                        0
                           0 0 0 11 61 17
                                            6
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       \cap
##
    ATC
             0 0 1
                      0
                                             4
                                                 0
                                                    0
                                                       0
                                                          0
##
    BIC
             0 0
                      0
                        0
                           0 0 0 11 66 14
                                            7
                                              1
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                  1
##
    RIFT.hc
             1 0 0
                     0
                        0
                           0 0 13 66 20 0
                                           0
                                              0
                                                 0 0
                                                      0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       0
                                                                          0
             0 0 0 0 0 0 0 0 0 0 0 0 0 4 10 9 9 11 15 16 13 5 6
##
   [1] "(dimension, delta) = (8,200)"
           ESTIMATE
##
            -1 1 2 4 7 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 28
## METHOD
##
             0 5 1 1 1 4 55 29 2 1 1 0 0 0 0
                                                      0
                                                         0
                                                           0
                                                              0
                                                                 0
                                                                    0
                                                                      0
    Mean
                        1 4 55 29 2 1 1
                                            0
                                              0
##
    Meanl2
                5
                  1
                                                 0
                                                    0
                                                       0
                                                          0
                                                            0
                           2 27 17 3 0 51
                0 0
                     0
                        0
                                            0
                                              0
                                                 0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       \cap
##
    Median
             0
                                                    0
                                                       0
                                                          0
##
    Median12 0 0 0 0
                        0
                           2 27 18 2 0 51
                                            0
                                              0
                                                 0
                                                    0
                                                       0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                    0
                                                                       \cap
    AIC 0 0 1 0 0 0 13 63 17 6 0 0 0 0 0 0 0 0 0 0 0 0 0
##
```

```
BIC 0 0 1 0 0 0 13 68 16 2 0 0 0 0 0 0 0 0 0 0 0 0
##
            1 0 0 0 0 9 76 14 0 0 0 0 0 0 0 0 0 0
##
    RIFT.hc
            0 0 0 0 0 0 0 0 0 0 5 10 7 13 9 11 18 13 8 4 1 1
##
#stop cluster (parallel computing)
stopCluster(cl)
print(distribution_name )
## [1] "True distribution components: t-distribution (df=3) mixture distribution"
print(paste(k, 'true clusters:'))
## [1] "10 true clusters:"
print('Cluster weights:')
## [1] "Cluster weights:"
print(W)
```

The R session information (including the OS info, R version and all packages used):

```
sessionInfo()
## R version 4.1.2 (2021-11-01)
## Platform: x86_64-apple-darwin17.0 (64-bit)
## Running under: macOS Monterey 12.0.1
## Matrix products: default
## LAPACK: /Library/Frameworks/R.framework/Versions/4.1/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_GB.UTF-8/en_GB.UTF-8/en_GB.UTF-8/C/en_GB.UTF-8/en_GB.UTF-8
##
## attached base packages:
## [1] grid
                parallel stats
                                    graphics grDevices utils
                                                                   datasets methods
## [9] base
##
## other attached packages:
## [1] knitr_1.37
                          sigclust_1.1.0
                                              mixtools_1.2.0
                                                                 gridExtra_2.3
## [5] ggplot2 3.3.5
                          MASS 7.3-54
                                              pracma 2.3.6
                                                                 mclust 5.4.9
## [9] sigclust2_1.2.4
                          rstudioapi_0.13
                                              mvnfast_0.2.7
                                                                 doParallel_1.0.16
## [13] iterators_1.0.13 foreach_1.5.1
                                              Rfast_2.0.6
                                                                 RcppZiggurat_0.1.6
                          pacman_0.5.1
## [17] Rcpp_1.0.8
##
## loaded via a namespace (and not attached):
     [1] colorspace_2.0-2
                              ellipsis_0.3.2
                                                       dynamicTreeCut_1.63-1
     [4] rprojroot_2.0.3
                                                       XVector_0.34.0
##
                               htmlTable_2.4.0
    [7] base64enc_0.1-3
##
                                ggdendro_0.1.23
                                                       fs_1.5.2
## [10] remotes_2.4.2
                               bit64_4.0.5
                                                       AnnotationDbi_1.56.2
## [13] fansi_0.5.0
                                codetools_0.2-18
                                                       splines_4.1.2
## [16] cachem_1.0.6
                                impute_1.68.0
                                                       pkgload_1.2.4
                                                       cluster_2.1.2
## [19] Formula_1.2-4
                               WGCNA_1.70-3
```

```
## [22] kernlab 0.9-29
                                GO.db 3.14.0
                                                       png_0.1-7
   [25] compiler_4.1.2
                                httr_1.4.2
                                                       backports_1.4.1
##
   [28] Matrix 1.3-4
                                fastmap 1.1.0
                                                        cli 3.3.0
##
                                prettyunits_1.1.1
## [31] htmltools 0.5.2
                                                        tools_4.1.2
   [34] gtable 0.3.0
                                                        GenomeInfoDbData 1.2.7
##
                                glue_1.6.1
##
   [37] dplyr_1.0.7
                                ggthemes_4.2.4
                                                        Biobase_2.54.0
##
    [40] vctrs_0.4.1
                                Biostrings_2.62.0
                                                       preprocessCore_1.56.0
##
   [43] xfun_0.30
                                fastcluster_1.2.3
                                                        stringr_1.4.0
##
   [46] ps_1.7.0
                                brio_1.1.3
                                                       testthat_3.1.4
                                                       zlibbioc_1.40.0
   [49] lifecycle_1.0.1
                                devtools_2.4.3
##
##
   [52] scales_1.1.1
                                RColorBrewer_1.1-2
                                                       memoise_2.0.1
   [55] rpart_4.1-15
                                segmented_1.3-4
                                                       latticeExtra_0.6-29
   [58] stringi_1.7.6
                                RSQLite_2.2.10
                                                       highr_0.9
##
    [61] S4Vectors_0.32.3
                                desc_1.4.1
                                                        checkmate_2.0.0
##
   [64] BiocGenerics_0.40.0
                                pkgbuild_1.3.1
                                                       GenomeInfoDb 1.30.1
   [67] rlang 1.0.2
                                pkgconfig_2.0.3
                                                       matrixStats 0.61.0
##
   [70] bitops_1.0-7
                                evaluate_0.15
                                                       lattice_0.20-45
##
   [73] purrr 0.3.4
                                htmlwidgets_1.5.4
                                                       bit 4.0.4
##
   [76] tidyselect_1.1.1
                                processx_3.5.3
                                                       magrittr_2.0.2
  [79] R6_2.5.1
                                IRanges_2.28.0
                                                       generics_0.1.1
##
   [82] Hmisc 4.6-0
                                DBI 1.1.2
                                                       pillar_1.6.4
##
   [85] foreign_0.8-81
##
                                withr_2.4.3
                                                       survival_3.2-13
   [88] KEGGREST_1.34.0
                                RCurl_1.98-1.6
                                                       nnet_7.3-16
   [91] tibble_3.1.6
##
                                crayon_1.4.2
                                                       utf8_1.2.2
   [94] jpeg_0.1-9
                                usethis_2.1.6
                                                       data.table_1.14.2
##
                                callr_3.7.0
                                                       digest_0.6.29
   [97] blob_1.2.2
## [100] stats4_4.1.2
                                munsell_0.5.0
                                                        sessioninfo_1.2.2
Sys.time()
## [1] "2022-06-09 00:51:32 BST"
```