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Purpose

Model the distribution of observables \mathbf{x} in terms of

- Physical parameters of interest p
- Other parameters **q** to describe detector effects (resolution, efficiency,...)



Probability density function F(x;p,q)

 normalized over allowed range of the observables x w.r.t the parameters p and q

Implementation

- Add-on package to ROOT
 - ROOT is an object-oriented analysis environment
 - C++ command line interface & macros
 - Graphics interface
 - I/O support ('persisted objects')

- RooFit is collection of classes that augment the ROOT environment
 - Object-oriented data modeling
 - Integration in existing analysis environment
 - · Interfaces with existing data formats
 - No need to learn new language



RooFit @ BaBar

- Successor of RooFitTools
 - RooFitTools no longer maintained
 - RooFit is a nearly complete rewrite (~95%) of RooFitTools
 - Class structure redesigned from scratch, having learned from RooFitTools evolution
 - Key class names and functionality identical to enhance macro portability
- Code split in two SRT packages
 - RooFitCore
 - Core code, base classes, interface to MINUIT, plotting logic, integrators, PDF operator classes, ...
 - Everything except the PDFs
 - · Maintained exclusively by Wouter & David for code stability and design overview
 - RooFitModels
 - PDF implementations (Gauss, Argus etc)
 - · Contributed by BaBar users
- No code dependence on other BaBar software
 - Uses SoftRelTools for BaBar builds, but standalone Makefile provided
 - Some work still in progress...
 - Compiles clean & tested on Linux, Solaris, OSF
 - You can run it on your laptop, at home,...

The basics



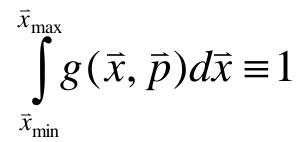
Probability density functions & likelihoods

The basics of OO data modeling

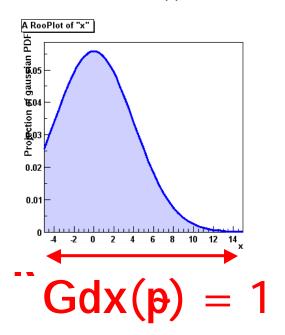
The essential ingredients: PDFS, datasets, functions

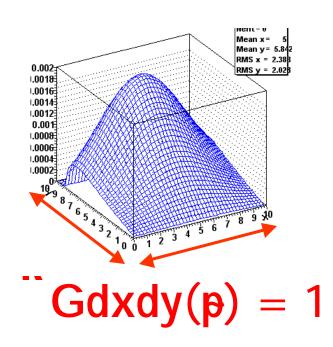
Probability density functions

- Fundamental property of any probability density function g(x,p):
 - Easy to construct for 1-dim. PDF much more effort for >1 dim.



- RooFit automatically takes care of this
 - User supplied function need not be normalized





Likelihood fits & ToyMC generation

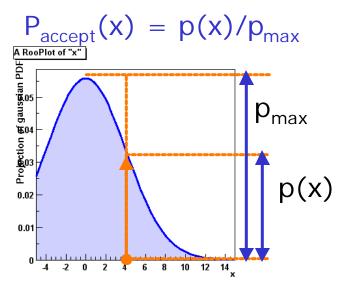
- Likelihood fit
 - Likelihood is product of probabilities given by g(x) for all data points in a given dataset D[x]

$$L(\vec{p}) = \prod_{D} g(\vec{x}_i, \vec{p})$$

- Fit find \vec{p} for which $-\log(L(\vec{p}))$ is smallest

$$-\log(L(\vec{p})) = -\sum_{D}\log(g(\vec{x}_i, \vec{p}))$$

- ToyMC generation
 - Accept/reject method ------
 - 'Direct' method (e.g. gauss)



Object-oriented data modeling

- In RooFit every variable, data point, function, PDF represented in a C++ object
 - Objects classified by data/function type they represent, not by their role in a particular setup
 - All objects are self documenting
- Objects
 representing a 'real' value.

 RooRealVar mb0("mb0","B0 mass",5.2794,"GeV");

 RooRealVar mb0("mb0","B0 mass",5.2794,"GeV");

 RooRealVar mb0("mb0","B0 mass",5.2794,"GeV");

 RooRealVar mb0("mb0","B0 mass",5.2794,"GeV");

References to variables

Object-oriented data modeling

Elementary operations on value holder objects

```
mass.Print()
     Print value and attributes
                               RooRealVar::mass: 5.2500 L(5.2 - 5.3)
                               mass = 5.27;
                                                             Error: new value
                               mass.setVal(5.27);
            Assign new value
                                                             out of allowed range
                               mass = 9.0
                               RooAbsRealLValue::inFitRange(mass):
                                    value 9 rounded down to max limit 5.3
            Retrieve contents
                               Double_t massVal = mass.getVal();
                               b0sig.Print()
Print works for all RooFit objects
                               RooGaussian::b0sig(mass,mb0,width) = 0
getVal() works for all real-valued
                               Double_t val = b0sig.getVal()
objects (variables and functions)
```

Elementary operations with a PDF

Setup gaussian PDF and plot

```
// Build Gaussian PDF
RooRealVar x("x","x",-10,10);
RooRealVar mean("mean", "mean of gaussian", 0, -10, 10);
RooRealVar sigma("sigma", "width of gaussian", 3);
RooGaussian gauss("gauss", "gaussian PDF", x, mean, sigma);
// Plot PDF
                                     A RooPlot of "x"
                                    gaussian PDF
0.00
0.00
0.00
RooPlot* xframe = x.frame()
gauss.plotOn(xframe);
xframe->Draw();
                                    Jo uoi 6.015
      Axis label from gauss title-
                                     0.01
                                                           Unit
A RooPlot is an empty frame
                                                       normalization
                                     0.005
capable of holding anything
plotted versus it variable
                                                                            8
                                       -10
                                                                2
                                                                        6
                        Plot range taken from limits of x
                                                                Wouter Verkerke, UCSB
```

Correct axis label for data

Events / (0.2)

200

A RooPlot of "x"

- 1) Generate 10K events from PDF
- 2) Fit PDF to event sample
- 3) Plot PDF on data

```
150
                                                      PDF
// Generate a toy MC set
                                      100
                                                   automatical
RooDataSet* data =
                                                    normalized
         gauss.generate(x,10000)
                                                    to dataset
// Fit pdf to toy
gauss.fitTo(*data);
// Plot PDF and toy data overlaid Once the model is built,
                                     Generating ToyMC, fitting, plotting
RooPlot* xframe2 = x.frame();
data->plotOn(xframe2) ;
                                     are mostly one-line operations!
gauss.plotOn(xframe2,"L");
xframe2->Draw();
                                                         Wouter Verkerke, UCSB
```

 PDF objects have no intrinsic notion of a variable begin a parameter or observable

```
RooGaussian b0sig("b0sig","B0 sig PDF", mass, mb0, width);
```

But, PDF normalization depends on parameter/observable interpretation of variables

$$\int_{x_{\min}}^{x_{\max}} g(x, p) dx \equiv 1 \qquad \begin{array}{l} x = \text{observable} \\ p = \text{parameter} \end{array}$$

- Parameter/observable interpretation is automatic and implicit when a PDF is used together with a dataset
 - All PDF variables that are member of the dataset are observables
 - All other PDF variables are parameters
 - Limits are normalization range if variable is observable Limits are MINUIT bounds if variable is parameter

Variables → Parameter or observable?

- Example of dynamic variable interpretation
 - BMixingPDF(dt,mixState,...) + data(dt)
 - mixState is parameter.
 - Data is fitted with pure mixed or unmixed PDF depending on value of mixState
 - BMixingPDF(dt,mixState,...) + data(dt,mixState)
 - mixState is observable.
 - PDF is normalized explicitly over the 2 states of mixState and behaves like a 2-dimensional PDF
- Determining the parameters/observables of a given PDF

```
getDependents:
Make list of common variables
between data and gauss
```

getParameters:

Make list of variables of gauss
that do not occur in data

```
RooArgSet* paramSet = gauss.getDependents(data);
paramSet.Print("v");
RooArgSet::dependents:
    1) RooRealVar::x : 0 L(-10 - 10)

RooArgSet* paramSet = gauss.getParameters(data);
paramSet.Print("v");
RooArgSet::parameters:
    1) RooRealVar::mean : -0.940910 +/- 0.0304
    2) RooRealVar::sigma : 3.0158 +/- 0.0222
```

Lists and sets

 RooFit has two collection classes that are frequently passed as arguments or returned as argument

- **RooArgSet** Set semantics
 - Each element may appear only once
 - No ordering of elements
- RooArgList List semantics
 - Elements may be inserted multiple times
 - Insertion order is preserved

```
RooArgSet s1(x,y,z);
RooArgSet s2(x,x,y); //ERROR!
```

```
RooArgList l1(z,y,x);
RooArgList l2(x,x,y);
l2.Print();
RooArgList:::
   1) RooRealVar::x: "x"
   2) RooRealVar::x: "x"
   3) RooRealVar::y: "y"
```



Basic PDFs

Combining building blocks via addition, multiplication

Generic real-valued functions

Plug-and-play parameters

The building blocks

RooFitModels provides a collection of 'building block' PDFs

- Argus background shape RooArgusBG **ROOBCPEffDecay** - BO decay with CP violation RoobmixDecay - B0 decay with mixing RooBifurGauss - Bifurcated Gaussian RooBreitWigner - Breit-Wigner shape - Crystal Ball function RooCBShape - Chebychev polynomial RooChebychev - Simple decay function RooDecay RooDircPdf - DIRC resolution description - D* background description RooDstD0BG RooExponential - Exponential function - Gaussian function RooGaussian

RooKeysPdfNon-parametric data descriptionNon-parametric data description

RooPolynomial - Generic polynomial PDFRooVoigtian - Breit-Wigner (X) Gaussian

- More will PDFs will follow
 - Easy to for users to write/contribute new PDFs

Generic expression-based PDFs

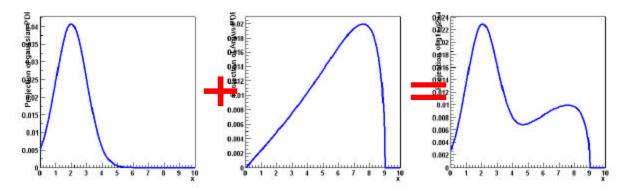
If your favorite PDF isn't there
 and you don't want to code a PDF class right away
 → USE RooGenericPdf

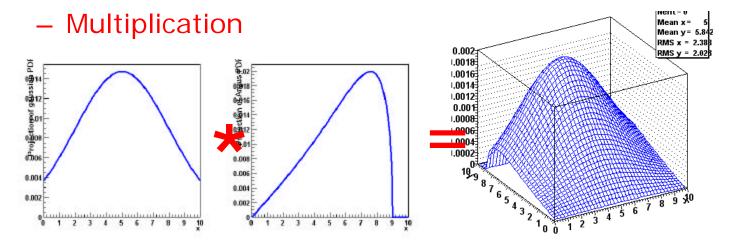
Just write down the PDFs expression as a C++ formula

- Automatic normalization
 - Expression divided by numerical integral of expression

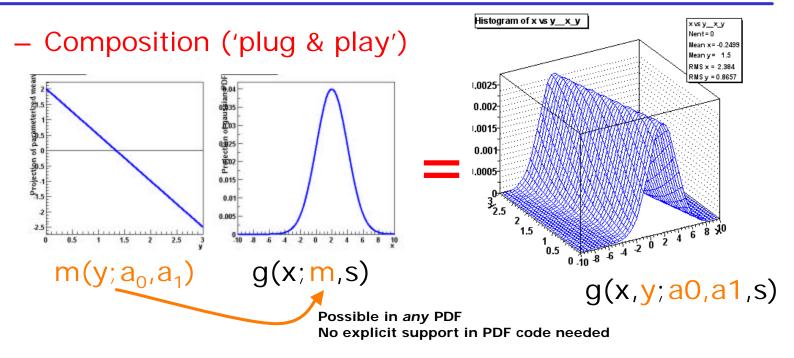
Building realistic models

- Complex PDFs be can be trivially composed using operator classes
 - Addition

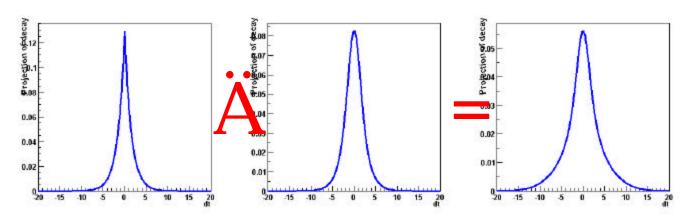




Building realistic models



Convolution

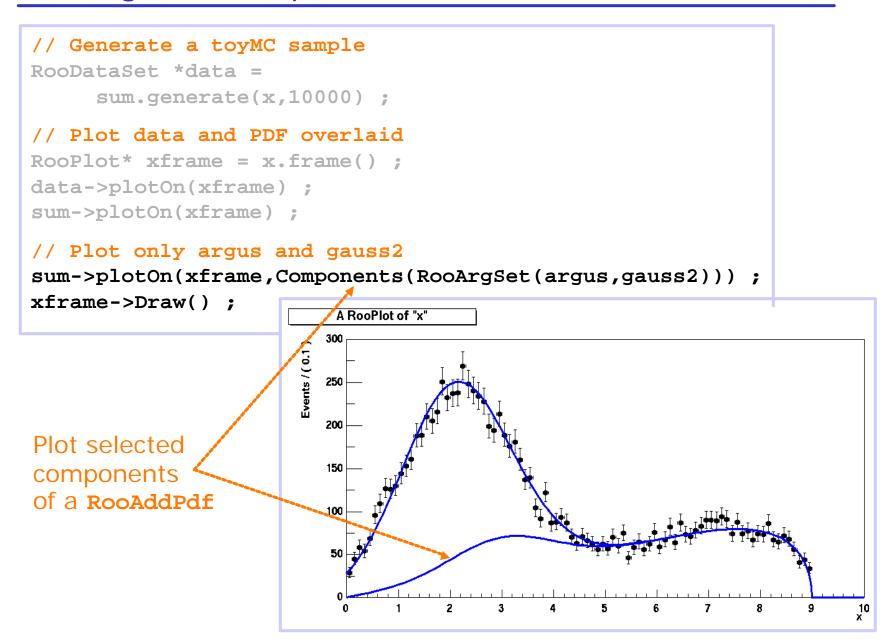


RooAddPdf constructs the sum of N PDFs with N-1 coefficients:

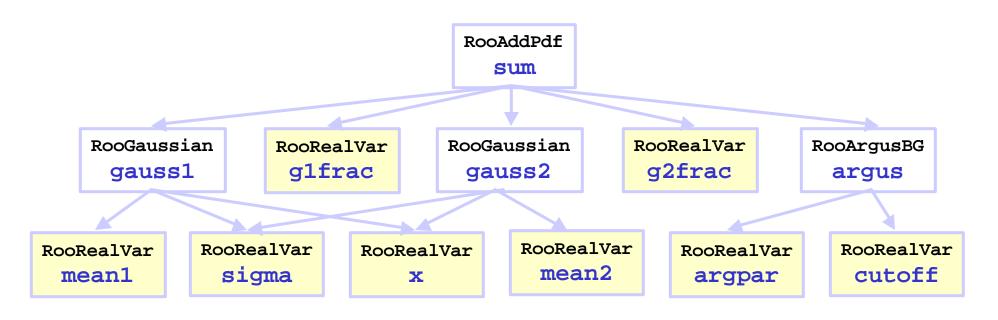
$$S = c_0 P_0 + c_1 P_1 + c_2 P_2 + \dots + c_{n-1} P_{n-1} + \left(1 - \sum_{i=0, n-1} c_i\right) P_n$$

```
// Build two Gaussian PDFs
             RooRealVar x("x","x",0,10);
             RooRealVar mean1("mean1", "mean of gaussian 1", 2);
Build 2
             RooRealVar mean2("mean2", "mean of gaussian 2", 3);
Gaussian
             RooRealVar sigma("sigma", "width of gaussians", 1);
 PDFs
             RooGaussian gauss1("gauss1", "gaussian PDF", x, mean1, sigma);
             RooGaussian gauss2("gauss2", "gaussian PDF", x, mean2, sigma);
             // Build Argus background PDF
  Build
             RooRealVar argpar("argpar", "argus shape parameter", -1.0);
ArgusBG
             RooRealVar cutoff("cutoff", "argus cutoff", 9.0);
  PDF
             RooArgusBG argus("argus","Argus PDF",x,cutoff,argpar);
             // Add the components
             RooRealVar glfrac("glfrac", "fraction of gauss1", 0.5); List of PDFs
             RooRealVar g2frac("g2frac", "fraction of gauss2", 0.1);
             RooAddPdf sum("sum", "g1+g2+a", RooArgList(gauss1, gauss2, argus),
                                             RooArgList(glfrac,g2frac));
```

Adding PDF components



Parameters of composite PDF objects



```
RooArgSet *paramList = sum.getParameters(data) ;
paramList->Print("v") ;
RooArgSet::parameters:
  1) RooRealVar::argpar : -1.00000 C
  2) RooRealVar::cutoff: 9.0000 C
                                        The parameters of sum
  3) RooRealVar::glfrac: 0.50000 C
                                        are the combined
  4) RooRealVar::g2frac : 0.10000 C
  5) RooRealVar::mean1 : 2.0000 C
                                        parameters
  6) RooRealVar::mean2 : 3.0000 C
                                        of its components
  7) RooRealVar::sigma
                        : 1.0000 C
                                                     Wouter Verkerke, UCSB
```

RooProdPdf constructs the product of N PDFs:

$$P = P_0(x_1, x_2) \cdot P_1(y_1, y_2,...) \cdot P_2(z_1, z_2,...) \cdot ... P_n(w_1, w_2,...)$$

Build 2 Gaussian PDFs

Component PDFs may not share dependents e.g. $pdf_1(\mathbf{x}, \mathbf{y}) * pdf_2(\mathbf{x}, \mathbf{z})$ not allowed

Such forms are not very common, but can be performed with RooGenericPdf Shared parameters no problem

Normalization more complicated

Plotting multi-dimensional PDFs

```
RooPlot* xframe = x.frame();

data->plotOn(xframe);

prod->plotOn(xframe);

xframe->Draw();

f(x) = \int pdf(x,y)dy
c->cd(2);

RooPlot* yframe = y.frame();

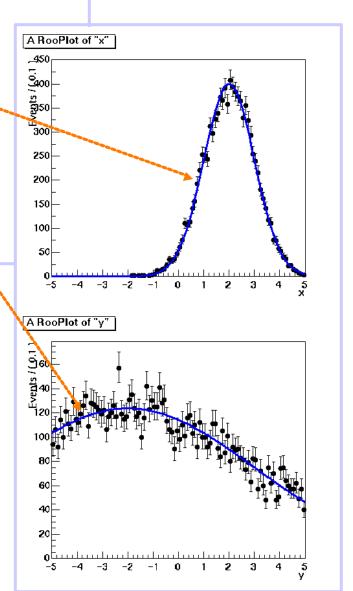
data->plotOn(yframe);

prod->plotOn(yframe);

yframe->Draw();

f(y) = \int pdf(x,y)dx
```

- -Plotting a dataset D(x,y) versus x represents a *projection over y*
- -To overlay PDF(x,y), you must plot Int(dy)PDF(x,y)
- -RooFit automatically takes care of this!
 - •RooPlot remembers dimensions of plotted datasets



Suppose you want to build a PDF like this

```
PDF(x,y) = gauss(x,m(y),s)

m(y) = m_0 + m_1 \cdot sqrt(y)
```

How do you do that? Just like that:

```
RooRealVar x("x","x",-10,10);
RooRealVar y("y","y",0,3);

**Muild a parameterized mean variable for gauss**
RooRealVar mean0("mean0", "mean offset",0.5);
RooRealVar mean1("mean1", "mean slope",3.0);
RooFormulaVar mean("mean", "mean0+mean1*y",

**RooArgList(mean0,mean1,y));
RooRealVar sigma("sigma", "width of gaussian",3);
RooGaussian gauss("gauss", "gaussian", x, mean, sigma);
```

Plug-and-play parameters!

PDF expects a real-valued object as input, not necessarily a variable

Generic real-valued functions

- RooFormulaVar makes use of the ROOT TFormula technology to build interpreted functions
 - Understands generic C++ expressions, operators etc
 - Two ways to reference RooFit objects
 By name:

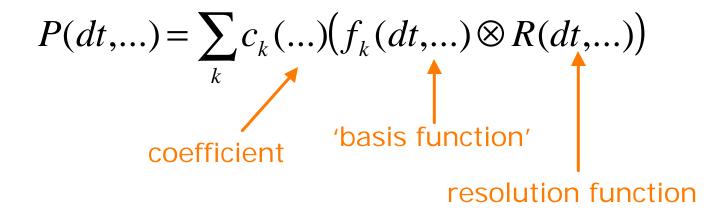
```
RooFormulaVar f("f","exp(foo)*sqrt(bar)", RooArgList(foo,bar));

By position:
RooFormulaVar f("f","exp(@0)*sqrt(@1)",RooArgList(foo,bar));
```

- You can use RooFormulaVar where ever a 'real' variable is requested
- RooPolyVar is a compiled polynomial function

```
RooRealVar x("x","x",0.,1.);
RooRealVar p0("p0","p0",5.0);
RooRealVar p1("p1","p1",-2.0);
RooRealVar p2("p2","p2",3.0);
RooFormulaVar f("f","polynomial",x,RooArgList(p0,p1,p2));
```

 Convoluted PDFs that can be written if the following form can be used in a very modular way in RooFit



Example: Bo decay with mixing

$$c_0 = 1 \pm \Delta w,$$
 $f_0 = e^{-|t|/t}$ $c_1 = \pm (1 - 2w),$ $f_1 = e^{-|t|/t} \cos(\Delta m \cdot t)$

Convoluted PDFs

Physics model and resolution model are implemented separately in RooFit

Implements $f_i(dt,...) \otimes R(dt,...)$ Also a PDF by itself

RooResolutionModel

$$P(dt,...) = \sum_{k} c_{k}(...) (f_{k}(dt,...) \otimes R(dt,...))$$

RooConvolutedPdf (physics model)

Implements c_k Declares list of f_k needed



User can choose combination of physics model and resolution model at run time

(Provided resolution model implements all f_k declared by physics model)

Convoluted PDFs

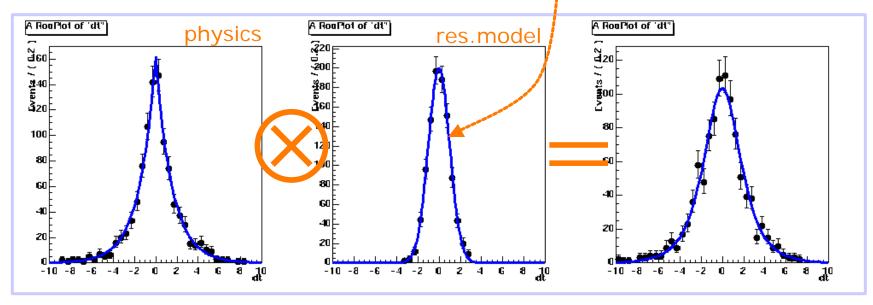
```
RooRealVar dt("dt", "dt", -10,10);
RooRealVar tau("tau","tau",1.548);
                                               A RouPlot of 'dt"
                                                                    decay
                                               30.6
// Truth resolution model
RooTruthModel tm("tm","truth model 1,dt)
                                               .05
8.05
                                               0.04
// Unsmeared decay PDF
                                                0.03
RooDecay decay tm("decay tm", "decay",
   dt,tau,tm,RooDecay::DoubleSided);
                                                0.02
                                                0.01
// Gaussian resolution model
                                                     -6 -4 -2 0 2 4 G 8 10
RooRealVar bias1("bias1","bias1",0);
RooRealVar sigma1("sigma1","sigma1",1);
                                               A RoaPlot of "dt"
                                                              decay ⊗ gm1
RooGaussModel gm1("gm1", "gauss model",
                                               9.04
                        dt,bias1,sigma1)/;
                                               02035
                                               9.03
// Construct a decay (x) gauss PDF
                                               0-025
RooDecay decay_gm1("decay_gm1", "decay",
                                               0.02
    dt,tau,gm1,RooDecay::DoubleSided);
                                               0.015
                                                0.01
                                               0.005
```

Composite Resolution Models: RooAddModel

```
//... (continued from last page)
// Wide gaussian resolution model
                                              A RouPlot of 'dt"
                                                            decay ⊗ gm1
                                              20.04
RooRealVar bias2("bias2","bias2",0);
RooRealVar sigma2("sigma2","sigma2",5);
                                              RooGaussModel gm2("gm2", "gauss model 2"
                                              9.03
                                              0.025
                    ,dt,bias2,sigma2);
                                              0.02
                                              0.015
// Build a composite resolution model
                                               0.01
RooRealVar f("f", "fraction of gm1", 0.5)
                                              0.005
RooAddModel gmsum("gmsum", "gm1+gm2",
                                                RooArgList(gm1,gm2),f);
                                                 decay \otimes (f \cdot gm1 + (1-f) \cdot gm2)
// decay (x) (gm1 + gm2)
                                              29.03 F
RooDecay decay_gmsum("decay_gmsum",
                                              07025
                "decay", dt, tau, gmsum,
                                              ≨.02
                RooDecay::DoubleSided) ;
                                              0.015
                                               0.01
                                              0.005
 →RooAddModel works like RooAddPdf
```

Resolution models

- Currently available resolution models
 - RooGaussModel Gaussian with bias and sigma
 - RooGExpModel Gaussian (X) Exp with sigma and lifetime
 - RooTruthModel Delta function
- A RooResolutionModel is also a PDF
 - You can use the same resolution model you use to convolve your physics PDFs to ft to MC residuals



Extended PDFs add extra term to global likelihood

$$-\log(L(\vec{p})) = -\sum_{D}\log(g(\vec{x}_i, \vec{p})) + N_{\exp} - N_{obs}\log(N_{\exp})$$

- Building extended PDFs
 - Any PDF can be turned into an extended PDF by wrapping it in a RooExtendPdf object

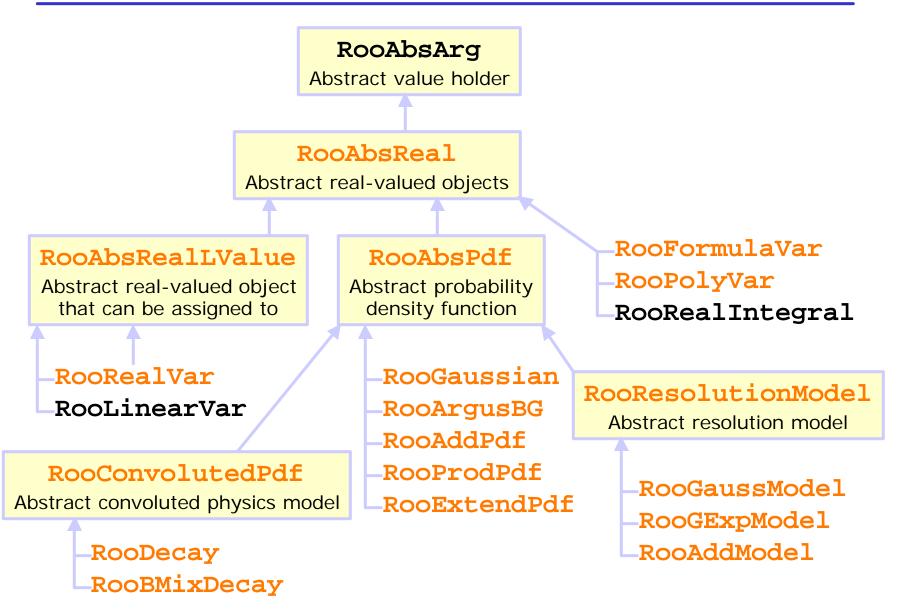
```
RooGaussian gauss("gauss","Gaussian",x,mean,sigma);
RooRealVar nsig("nsig","number of signal events",5,0,100);
RooExtendPdf gausse("gausse","Extended Gauss",gauss,nsig);
```

nsig is now a parameter of gausse -----and represents the number of expected events

Extended likelihood PDFs

- Composition rules for extended PDFs
 - A ROOAddPdf of all extendable PDFs is extendable
 - No coefficients needed (fractions calculated from components Nexpected)
 - A ROOProdPdf with a single extendable component is extendable
 - A RooSimultaneous with any extendable component is extendable
 - Can do mixed extended/regular MLL fits in various data subsets
- RooAddPdf short-hand form for branching fraction fits
 - If RooAddPdf is given N coefficients instead of N-1 fractions
 - → RooAddPdf is automatically extended
 - → coefficients represent the expected #events for each PDF comp.

Class tree for real-valued objects



Discrete variables



Organizing and classifying your data with discrete functions

Discrete-valued functions

Tabulating discrete data

- So far we have expressed all models purely in terms of real-valued variables
 - RooFit also has extensive support for discrete variables
 - Discrete variables are called categories
- Properties of RooFit categories
 - Finite set of named states → self documenting
 - Optional integer code associated with each state

```
At creation.
                      // Define a cat. with explicitly numbered states
        a category
                      RooCategory b0flav("b0flav", "B0 flavour");
      has no states
                      b0flav.defineType("B0",-1);
                      b0flav.defineType("B0bar",1);
        Add states
with a label and index
                      // Define a category with labels only
                      RooCategory tagCat("tagCat", "Tagging category") ;
       Add states
                      tagCat.defineType("Lepton");
   with a label only.
                      tagCat.defineType("Kaon");
     Indices will be
                      tagCat.defineType("NetTagger-1");
      automatically
                      tagCat.defineType("NetTagger-2");
          assigned
```

When to use discrete variables

- Discrete valued observables
 - B0 flavour
 - Rec/tag mixing state
- Event classification
 - tagging category
 - run block
 - B0 reconstruction mode
- Cuts
 - Mass window / sideband window
- In general, anything that you would use integer codes for in FORTRAN
 - RooFit makes your life easier:
 all states are labeled by name → no codes to memorize
 - Optional integer code associated with category states allows to import existing integer encoded data
 - Self-documenting: category state definitions provide single and easily understandable integer—state name conversion point

Managing data subsets / RooSimultaneous

- Simultaneous fit to multiple data samples
 - E.g. to fit PDF_A to dataset D_A and PDF_B to dataset D_B simultaneously, the NLL is

$$NLL = \sum_{i=1,n} -\log(PDF_{A}(D_{A}^{i})) + \sum_{i=1,m} -\log(PDF_{B}(D_{B}^{i}))$$

 Use categories to split a master dataset D into subsets D_A, D_B etc

Dataset A	4				
5.0			Dataset A+B		
3.7			5.0	Α	
1.2			3.7	Α	
4.3			1.2	А	
			4.3	А	
Dataset F	3		5.0	В	
5.0			3.7	В	
3.7			1.2	В	
1.2					

Using categories: RooSimultaneous

RooSimultaneous implements 'switch' PDF:

```
case (indexCat) {
   A: return pdfA;
   B: return pdfB;
}
Effectively fitting
pdfA to dataA
pdfB to dataB
```

```
Create dataset indexing category  

Create dataset indexing category  

Associate created  
   PDFs with appropriate index  
   category state  

// Define a category with labels only  
RooCategory tagCat("tagCat", "Tagging category");  
tagCat.defineType("Lepton");  

// Build PDFs for Lepton and Kaon data subsets

// Construct simultaneous PDF for lep and kao  
RooSimultaneous simPdf("simPdf", "simPdf", tagCat);  
simPdf.addPdf(pdfLep, "Lepton");  
simPdf.addPdf(pdfKao, "Kaon");
```

Sig Sideband

You can use discrete variables to describe cuts, e.g.

~800 ⊏

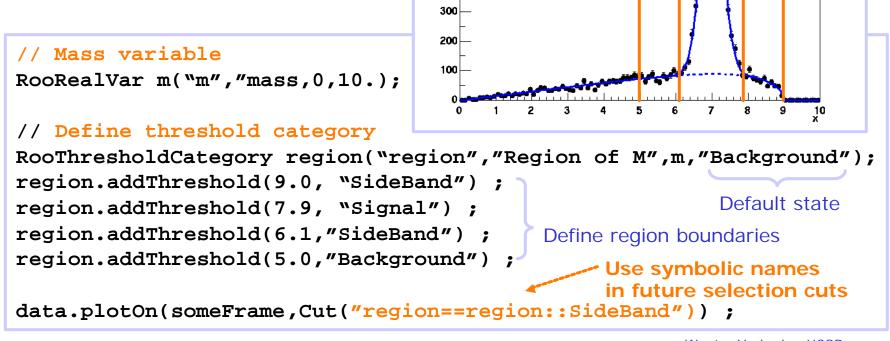
Events / (0

500

400

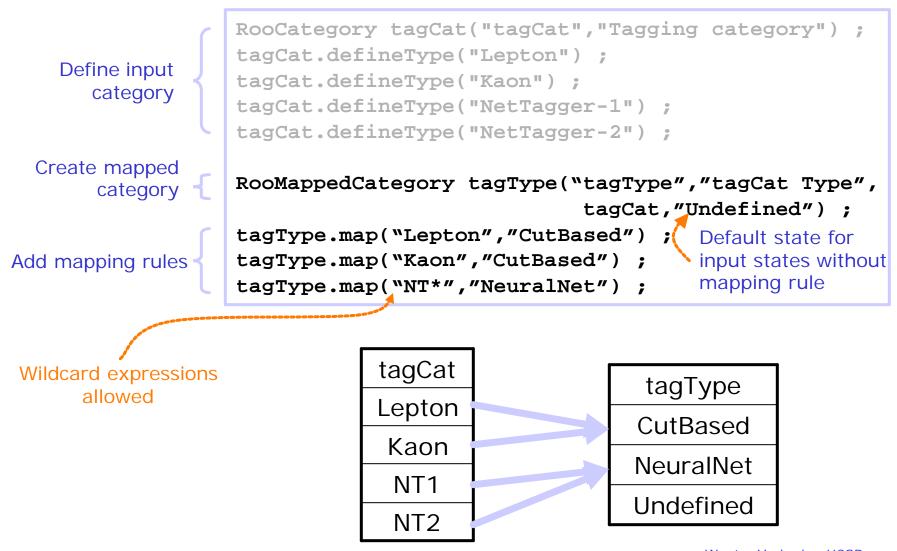
background

- Signal, sideband mass windows
- RooThresholdCategory
 - Defines regions of a real variable



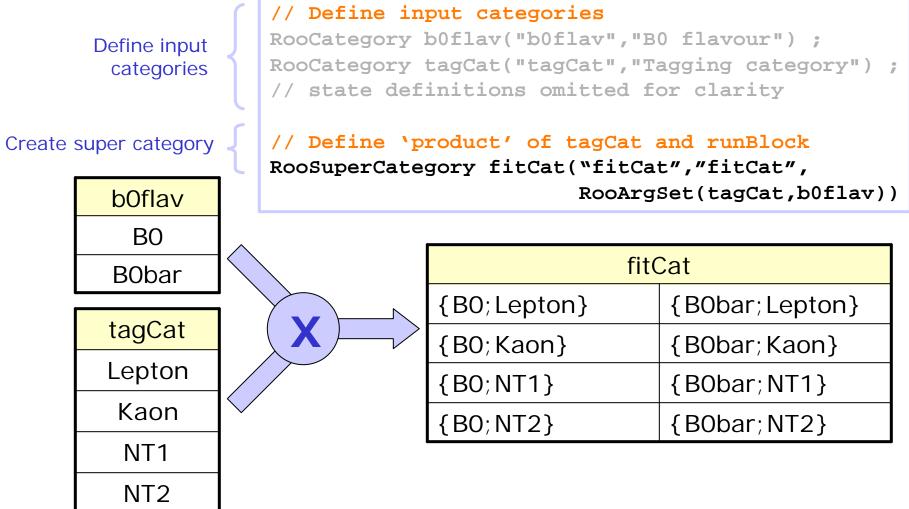
Discrete functions

RooMappedCategory provides cat → cat mapping



Discrete functions

 RooSuperCategory/RooMultiCategory provides category multiplication



Exploring discrete data

 Like real variables of a dataset can be plotted, discrete variables can be tabulated

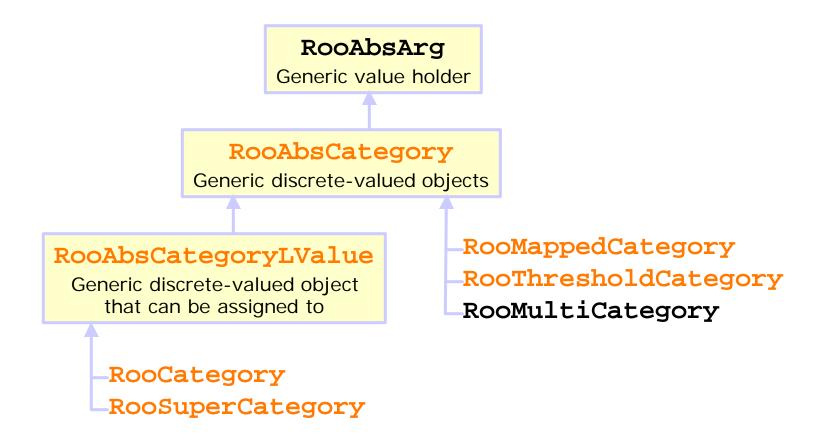
```
RooTable* table=data->table(b0flav) ;
                               table->Print();
  Tabulate contents of dataset
                               Table b0flav : aData
           by category state
                                    B0bar
      Extract contents by label
                               Double_t nB0 = table->get("B0");
                               Double_t b0Frac = table->getFrac("B0");
Extract contents fraction by label
                               data->table(tagCat, "x>8.23")->Print();
                                  Table tagCat : aData(x>8.23)
         Tabulate contents of
                                          Lepton
                                                    668
       selected part of dataset
                                            Kaon
                                                    717
                                    NetTagger-1
                                                    632
                                    NetTagger-2
```

Exploring discrete data

 Discrete functions, built from categories in a dataset can be tabulated likewise

data->table(b0Xtcat)->Print(); Table b0Xtcat : aData {B0;Lepton} {B0bar;Lepton} Tabulate RooSuperCategory states {B0;Kaon} {B0bar; Kaon} {B0; NetTagger-1} {B0bar; NetTagger-1} {B0; NetTagger-2 1223 {B0bar; NetTagger-2 data->table(tcatType)->Print(); Table tcatType : aData Tabulate **RooMappedCategory** states Unknown Cut based Neural Network

Class tree for discrete-valued objects



Datasets

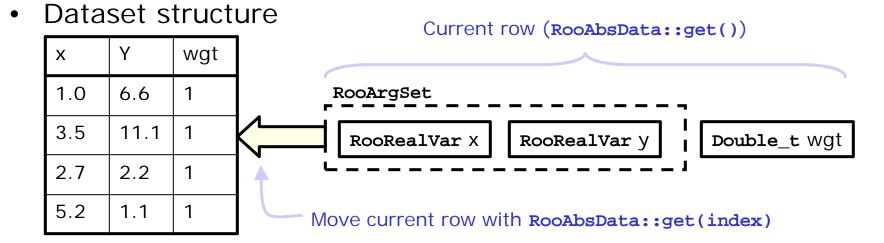


Binned vs unbinned datasets

Importing data from outside sources

Operations on datasets

- A dataset is a collection of points in N-dimensional space
 - Dimensions can be either real or discrete
 - Two dataset implementations:
 - RooDataSet unbinned (weighted & unweighted)
 - RooDataHist binned
 - Common abstract base class RooAbsData
 - Nearly all RooFit classes/functions (including fitting)
 take RooAbsData objects
 - Operations universally supported for binned and unbinned data



Unbinned dataset basics

Create empty dataset with fields x,y,c.
Dataset row representation will be a **clone** of (x,y,c).
Original (x,y,c) will no longer be referenced after ctor.

To add a datapoint value holders x,y,c must be passed

```
// Create dataset variables
RooRealVar x("x","x",-10,10);
RooRealVar y("y", "y", 0, 40);
RooCategory c("c", "c");
c.defineType("Plus",+1);
c.defineType("Minus",-1);
RooDataSet
data("data","data",RooArgSet(x,y,c));
// Fill d with dummy values
Int t i;
for (i=0; i<1000; i++) {
 x = i/50 - 10;
 y = sqrt(1.0*i);
  c = (i\%2)?"Plus":"Minus";
 d.add(RooArgSet(x,y,c));
d.Print("v") ;
RooDataSet::d: "d"
  Contains 1000 entries
  Defines RooArgSet::Dataset Variables:
    1) RooRealVar::x:
    2) RooRealVar::y:
    3) RooCategory::c: "c"
  Caches RooArgSet::Cached Variables:
```

Unbinned dataset basics

Access the pointer to the RooArgSet holding the current row

Load row #900 in the RooArgSet holding the current row

Find value holder for x in the current row

```
// Retrieve the 'current' row
RooArgSet* row = data.get() ;
row->Print("v");
RooArgSet::Dataset Variables: (Owning contents)
  1) RooRealVar::x : 9.0000 L(-10 - 10)
  2) RooRealVar::y: 31.607 L(0 - 40)
  3) RooCategory::c : Plus
// Retrieve a specific row
row = data.get(900);
row->Print("v");
RooArgSet::Dataset Variables: (Owning contents)
  1) RooRealVar::x: 8.0000 L(-10 - 10)
  2) RooRealVar::y: 30.000 L(0 - 40)
  3) RooCategory::c: Minus
// Retrieve a specific field of the row
RooRealVar* xrow = (RooRealVar*) row->find("x") ;
cout << xrow->getVal() << endl ;</pre>
8.0000
```

Weighting unbinned datasets

```
// Print current row and weight of dataset
                     row->Print("v");
                     RooArgSet::Dataset Variables: (Owning contents)
                        1) RooRealVar::x : 8.0000 L(-10 - 10)
                        2) RooRealVar::y: 30.000 L(0 - 40)
                        3) RooCategory::c : Minus
                     cout << data.weight() << endl ;</pre>
                      1.0000
  Instruct dataset
                      // Designate variable y as the event weight
  to interpret y as
                     data.setWeightVar(y)
  the event weight
                      // Retrieve same row again
                     row = data.get(900);
                     row->Print("v");
                     RooArgSet::Dataset Variables: (Owning contents)
   Variable y is
                        1) RooRealVar::x: 8.0000 L(-10 - 10)
   no longer in the
                        2) RooCategory::c : Minus
   current row
    Current value
                     cout << data.weight() << endl ;</pre>
   of y is returned
                      30.0000
as the event weight
```

Importing data

- Unbinned datasets (RooDataSet) can be constructed from
 - ROOT TTree objects
 - RooRealVar dataset rows are taken /D /F /I tree branches with equal names
 - RooCategory dataset rows are taken from /I /b tree branches with equal names

```
Ttree* tree = <someTFile>.Get("<someTTree>");
RooDataSet data("data","data",tree,RooArgSet(x,c));
```

- ASCII data data files
 - ASCII file fields are interpreted in order of supplied RooArgList

```
RooDataSet* data =
   RooDataSet::read("ascii.file",RooArgList(x,c));
```

Implicit selection: External data may contain entries that exceed limits set on RooFit value holder objects

- If a loaded value of a **RooRealVar** exceeds the RRVs limits, the entire tree row is not loaded
- If a loaded index of a RooCategory is not defined,
 the entire tree row is not loaded

Importing data

- Binned dataset (RooDataHist) can be constructed from
 - ROOT TH1/2/3 objects
 - TH dimensions are matched in order to supplied list of RooFit value holders

```
TH2* histo = <yourTHistogram> ;
RooDataHist bdata("bdata","bdata",RooArgList(x,y),histo);
```

- RooDataSet unbinned datasets
 - Binning for each dimension is specified by setFitRange(lo,hi),setFitBins(nbins)
 - The unbinned dataset may have more dimensions than the binned dataset.

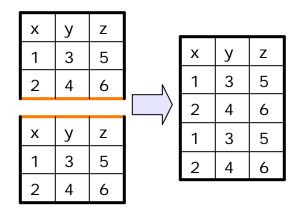
Dimensions not specified are automatically projected

```
RooDataSet* data = <yourUnbinnedData> ;
RooDataHist bdata("bdata","bdata",RooArgList(x,y),data) ;
```

Extending and reducing unbinned datasets

Appending

```
RooDataSet d1("d1","d1",RooArgSet(x,y,z));
RooDataSet d2("d2","d2",RooArgSet(x,y,z));
d1.append(d2);
```



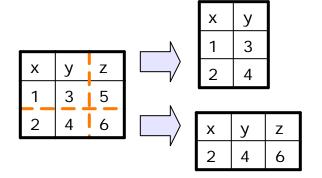
Merging

```
RooDataSet d1("d1","d1",RooArgSet(x,y);
RooDataSet d2("d2","d2",RooArgSet(z));
d1.merge(d2);
```

х	у	Z	,	х	У	Z
1	3	5		1	3	5
2	4	6	V	2	4	6

Reducing

```
RooDataSet d1("d1","d1",RooArgSet(x,y,z);
RooDataSet* d2 = d1.reduce(RooArgSet(x,y));
RooDataSet* d3 = d1.reduce("x>1");
```

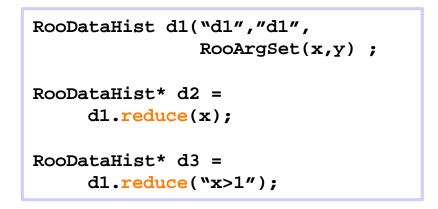


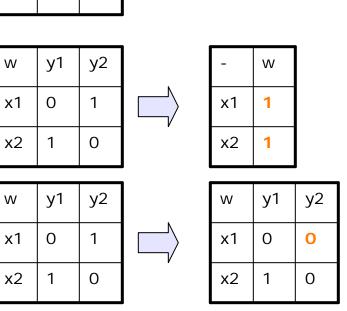
Adding and reducing binned datasets

Adding

w y1 y2 x1 0 1 x2 1 0 w y1 y2 x1 1 1 x2 1 0

Reducing





Fitting & Generating

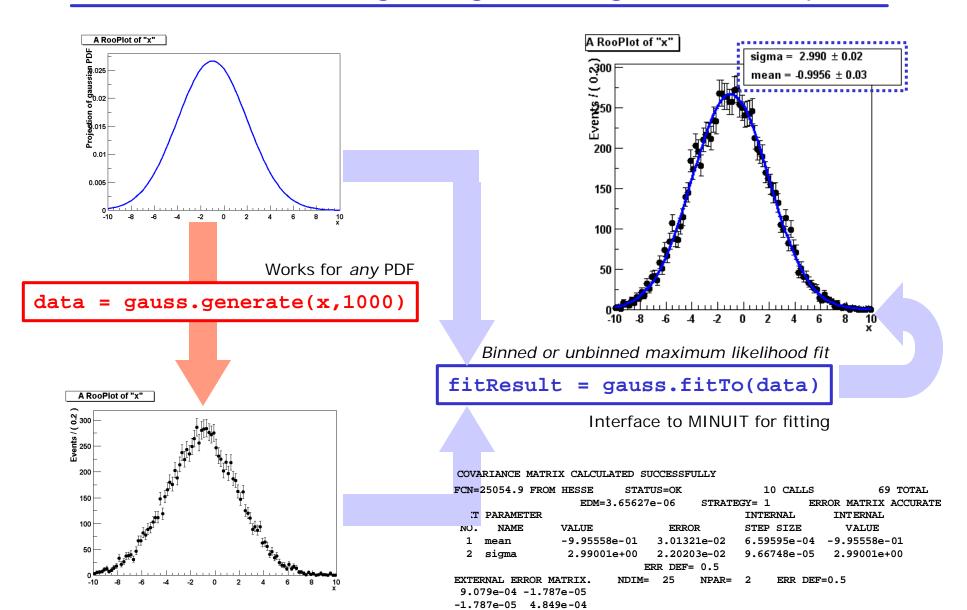


Fitting

Browsing your fit results
Generating toy MC

Putting it all together

Given a model, fitting and generating are 1-line operations



Wouter Verkerke, UCSB

Fitting

```
RooAbsData* data ;
RooAbsPdf* pdf ;
RooFitResult* fitres = pdf->fitTo(*data,"<options>") ;
```

- Binned/unbinned fit performed depending on type of dataset (RooDataHist/RooDataSet)
- Fitting options:

```
"m" = MIGRAD only, i.e. no MINOS
MINUIT
           "s" = estimate step size with HESSE before starting MIGRAD
control •
           "h" = run HESSE after MIGRAD
           "e" = Perform extended MLL fit
options
           "0" = Run MIGRAD with strategy MINUIT 0 (faster, but no corr. matrix at end)
                 Does not apply to HESSE or MINOS, if run afterwards.
            "q" = Switch off verbose mode
           "1" = Save log file with parameter values at each MINUIT step
output
           "v" = Show changed parameters at each MINUIT step
options
           "t" = Time fit
           "r" = Save fit output in RooFitResult object (return value is object RFR pointer)
```

Automatic fit optimization

- RooFit analyzes PDF objects prior to fit and applies several optimizations
 - Actual fit performed on copy of PDF and dataset
 - · Allows case-specific non-reversible optimizations
 - Components that have all constant parameters are pre-calculated
 - Dataset variables not used by the PDF are dropped
 - Simultaneous fits: When a parameters changes only parts of the total likelihood that depend on that parameter are recalculated
 - PDF normalization integrals are only recalculated when the ranges of their observables or the value of their parameters are changed
 - · Lazy evaluation: calculation only done when intergral value is requested
- Little or no need for 'hand-tuning' of user PDF code
 - Easier to code and code is more readable
- 'Typical' large-scale fits see significant speed increase
 - Factor of 3x 10x not uncommon.

Browsing fit results with RooFitResult

- As fits grow in complexity (e.g. 45 floating parameters), number of output variables increases
 - Need better way to navigate output that MINUIT screen dump
- RooFitResult holds complete snapshot of fit results
 - Constant parameters
 - Initial and final values of floating parameters
 - Global correlations & full correlation matrix
 - Returned from RooAbsPdf::fitTo() when "r" option is supplied
- Compact & verbose printing mode

Compact Mode

```
Constant
                fitres->Print();
 parameters
                  RooFitResult: min. NLL value: 1.6e+04, est. distance to min: 1.2e-05
 omitted in
compact mode
                                       FinalValue +/- Error
                    Floating Parameter
                               argpar -4.6855e-01 +/- 7.11e-02
 Alphabetical
                               g2frac 3.0652e-01 +/- 5.10e-03
  parameter
                                       7.0022e+00 +/- 7.11e-03
                                mean1
    listing
                                mean2
                                        1.9971e+00 +/- 6.27e-03
                                        2.9803e-01 +/- 4.00e-03
                                sigma
```

Browsing fit results with RooFitResult

Verbose printing mode

```
fitres->Print("v");
 RooFitResult: min. NLL value: 1.6e+04, est. distance to min: 1.2e-05
 Constant Parameter
                      Value
                                     Constant parameters
              cutoff 9.0000e+00
                                     listed separately
              glfrac 3.0000e-01
                                     FinalValue +/- Error
   Floating Parameter
                      InitialValue
                                                             GblCorr.
              argpar -5.0000e-01 -4.6855e-01 +/- 7.11e-02 0.191895
              g2frac 3.0000e-01 3.0652e-01 +/- 5.10e-03 0.293455
               mean1 7.0000e+00 7.0022e+00 +/- 7.11e-03 0.113253
               mean2 2.0000e+00
                                     1.9971e+00 +/- 6.27e-03 0.100026
               sigma 3.0000e-01
                                     2.9803e-01 +/- 4.00e-03 0.276640
```

Initial, final value and global corr. listed side-by-side

Correlation matrix accessed separately

Browsing fit results with RooFitResult

- Easy navigation of correlation matrix
 - Select single element or complete row by parameter name

```
r->correlation("argpar","sigma")
(const Double_t)(-9.25606412005910845e-02)

r->correlation("mean1")->Print("v")
RooArgList::C[mean1,*]: (Owning contents)
   1) RooRealVar::C[mean1,argpar]: 0.11064 C
   2) RooRealVar::C[mean1,g2frac]: -0.0262487 C
   3) RooRealVar::C[mean1,mean1]: 1.0000 C
   4) RooRealVar::C[mean1,mean2]: -0.00632847 C
   5) RooRealVar::C[mean1,sigma]: -0.0339814 C
```

- RooFitResult persistable with ROOT I/O
 - Save your batch fit results in a ROOT file and navigate your results just as easy afterwards

Visualize errors and correlation matrix elements

```
RooFitResult* r = pdf->fitTo(data,"mhvr") ;
     RooPlot* f = new RooPlot(tau, sigma1, 1.35, 1.6, 0.85, 1.20);
      r->plotOn(f,tau,sigma1,"ME12VHB");
      f->Draw();
                               1.2
E 1.2
1.15
Works on any RooFitResult,
                                 1.1
Also after persistence
                                1.05
                                0.95
                                 0.9
 MINUIT contour scan
                                0.85
1.35
 is also possible with
                                          1.4
                                                  1.45
                                                          1.5
                                                                  1.55
                                                                           1.6
                                                                         tau
 a separate interface
```

Generating ToyMC

- Normal generator run
 - Just specify set of observables to generate and #events

```
RooAbsPdf* pdf ;
RooDataSet* toyMCdata = pdf->generate(RooArgSet(dt,mixState),10000);

#events
Observables to generate
```

- Generator run with prototype data
 - Specify set of observables to generate and a prototype dataset

```
RooDataSet* protoData
RooAbsPdf* pdf ;
RooDataSet* toyMCdata = pdf->generate(RooArgSet(dt,mixState),*protoData);
```

Observables to generate

Prototype dataset

- Generated dataset will replicate exactly the prototype dataset except for observables generated by the PDF
- Ideal for per-event errors, tagging breakdown, ...

Automatic generator optimizations

- Most efficient generator technique automatically selected
 - PDF components can advertise a smarter generation technique (direct generation, e.g. gauss) which is used when appropriate
 - RooProdPdf delegates generation of observables to component PDFs (1 x N-dim generation → N x 1-dim generation)
 - RooAddPdf components generated separately
 Accept/reject method very inefficient when broad and narrow distributions are summed
 - RooConvolutedPdf generates physicsPDF and smearing model separately if both support 'direct' generation (convolution integrals not evaluated during generation)

Putting it all together: generating and fitting a decay PDF

```
// Build a simple decay PDF
RooRealVar dt("dt", "dt", -20,20);
RooRealVar tau("tau","tau",1.548,-10,10);
// Build a gaussian resolution model
RooRealVar bias("bias","bias",0,-5,5);
RooRealVar sigma("sigma","sigma",1,0.1,2.0);
RooGaussModel gm("gm", "gauss model", dt, bias, sigma) ;
// Construct a decay (x) gm
RooDecay decay("decay", "decay", dt, tau, gm, RooDecay::DoubleSided);
// Generate BMixing data with above set of event errors
RooDataSet *data = decay.generate(dt,2000) ;
// Fit the generated data to the model
                                                A RooPlot of "dt"
                                                                       tau = 1.561 ± 0.06
RooFitResult* r = decay.fitTo(*data,"mhr")
                                                                        sigma1 = 0.98 ± 0.1
r->correlation(sigma,tau);
                                                                       bias1 = 0.007 \pm 0.05
                                               ≃ 250
-0.818443
// Make a plot of the data and PDF
                                                150
RooPlot* dtframe = dt.frame(-10,10,30);
data->plotOn(dtframe) ;
                                                 100
pdf.plotOn(dtframe) ;
                                                 50
pdf.paramOn(dtframe) ;
dtframe->Draw();
```

Plotting & Saving



Adding statistics, parameter boxes

Changing colors and styles

Plotting in 2 and 3 dimensions

Persisting plots & fit results

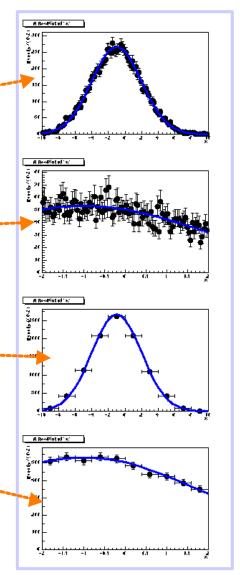
Changing the plot range / histogram binning

By default a Rooplot frame takes the limits and the

number of bins from its plot variable

Can be overridden by frame() arguments

```
data->plotOn(frame1);
pdf->plotOn(frame1);
frame1->Draw();
RooPlot* frame2 = x.frame(-2,2);
data->plotOn(frame1) ;
pdf->plotOn(frame1);
frame2->Draw();
RooPlot* frame3 = x.frame(10) ---
data->plotOn(frame1) ;
pdf->plotOn(frame1);
frame3->Draw();
RooPlot* frame3 = x.frame(-2,2,10)
data->plotOn(frame1) ;
pdf->plotOn(frame1);
frame3->Draw() :
```



Decoration

- A RooPlot is an empty frame that can contain
 - RooDataSet projections
 - PDF and generic real-valued function projections
 - Any ROOT drawable object (arrows, text boxes etc)
- Adding a dataset statistics box / PDF parameter box

```
RooPlot* frame = x.frame() ;
data.plotOn(xframe);
                                             A RooPlot of "x"
pdf.plotOn(xframe) ;
                                                                               sigma = 3.043 \pm 0.02
                                            300
pdf.paramOn(xframe,data)
                                                                               mean = -1.0112 \pm 0.03
                                            Events / (
data.statOn(xframe)
                                                                               N = 10000
                                                                               \langle x \rangle = -0.9975 \pm 0.03
xframe->Draw();
                                                                               x_{RMS} = 3.017 \pm 0.02
                                              150
                                              100
```

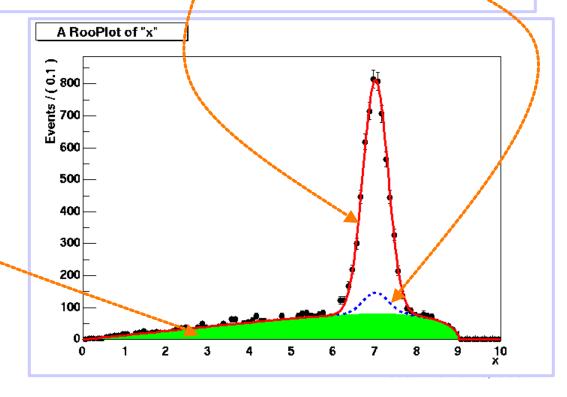
Decoration

Adding generic ROOT text boxes, arrows etc.

```
TPaveText* tbox = new TPaveText(0.3,0.1,0.6,0.2,"BRNDC");
tbox->AddText("This is a generic text box") ;
TArrow* arr = new TArrow(0,40,3,100);
xframe2->addObject(arr);
xframe2->addObject(tbox);
                               A RooPlot of "x"
                                                                      sigma = 3.043 \pm 0.02
                              Events / ( 0.2 )
                                                                      mean = -1.0112 \pm 0.03
                                                                      N = 10000
                                                                      \langle x \rangle = -0.9975 \pm 0.03
                                                                     x_{RMS} = 3.017 \pm 0.02
                                200
                                150
                                100
                                 50
                                               This is a generic text box
                                                      -2
```

Customization

Changing colors and styles of histograms and curves



Plotting in more than 2,3 dimensions

- No equivalent of RooPlot for >1 dimensions
 - Usually >1D plots are not overlaid anyway
 - Methods provided to produce 2/3D ROOT histograms from datasets and PDFs/functions

```
TH2* ph2 = x.createHistogram("x vs y pdf",y,0,0,0,bins);
prod.fillHistogram(ph2,RooArgList(x,y));
ph2->Draw("SURF") ;
TH2* dh2 = x.createHistogram("x vs y data",y,0,0,0,bins);
data->fillHistogram(dh2,RooArgList(x,y));
dh2->Draw("LEGO") ;
                 Histogram of x vs y data | x y
                                                          Histogram of x vs y pdf x y
                                                x va y dete x y
                                                                                        x va y pdf x
                                                RMS y - 2.632
                                                                                        RMS y - 2.664
                                                          0.008
                                                          0.007
                   70
                                                          0.006
                                                          0.005
                                                          0.004
                                                          0.003
                   30
                                                          0.002
                                                          0.001
```

Persisting and reviving Rooplots

Persisting ROOT Object Browser File View Options <u>H</u>elp RooFitResult* r : a demo2.root RooPlot* xframe ; All Folders Contents of "/ROOT Files/demo2.root" Iroot Tfile f("demo2.root" /afs/slac.stanford.edu/u/ec/verk "RECREATE" ROOT Files fit(sum,sumData);1 frame(089da940);1 r->Write(); all demo2.root xframe->Write(); f.Close(); 2 Objects. Reviving A Roo lot of "x" 2 800 Throwswer the 설 700 600 E RooFitResult* r = f.Get("fit(data,sum)"); 500 r->Print("v"); 300 RooFitResult: min. NLL value: 1.6e+04, ... 200 -Floating Parameter FinalValue +/- Error argpar -4.6855e-01 +/- 7.11e-0Wouter Verkerke, UCSB

Storing configuration data in ASCII files

- RooArgLists can be written to and read from ASCII file
 - Convenient to load initial values of fit parameters

```
set.Print("v");
RooArgSet::parameters:
    1) RooRealVar::argpar : -0.468507 +/- 0.0711 (-0.0713, 0.0710) L(-2 - 0)
    2) RooRealVar::cutoff : 9.0000 C
    3) RooRealVar::g1frac : 0.30000 C
    4) RooRealVar::g2frac : 0.30652 +/- 0.00510 (-0.00509, 0.00511)
    5) RooRealVar::mean1 : 7.0022 +/- 0.00711 (-0.00712, 0.00710) L(0 - 10)
    6) RooRealVar::mean2 : 1.9971 +/- 0.00627 (-0.00628, 0.00626) L(0 - 10)
    7) RooRealVar::sigma : 0.29803 +/- 0.00400 (-0.00396, 0.00403)
set.writeToFile("config.txt");
```

config.txt

```
argpar = -0.468507 +/- 0.0711 (-0.0713, 0.0710) L(-2 - 0)
cutoff = 9.0000 C
g1frac = 0.30000 C
g2frac = 0.30652 +/- 0.00510 (-0.00509, 0.00511)
mean1 = 7.0022 +/- 0.00711 (-0.00712, 0.00710) L(0 - 10)
mean2 = 1.9971 +/- 0.00627 (-0.00628, 0.00626) L(0 - 10)
sigma = 0.29803 +/- 0.00400 (-0.00396, 0.00403)
```

```
set.readFromFile("config.txt") ;
```

Documentation



RooFit home page
Tutorial macros
Inline code documentation

How to get started / documentation

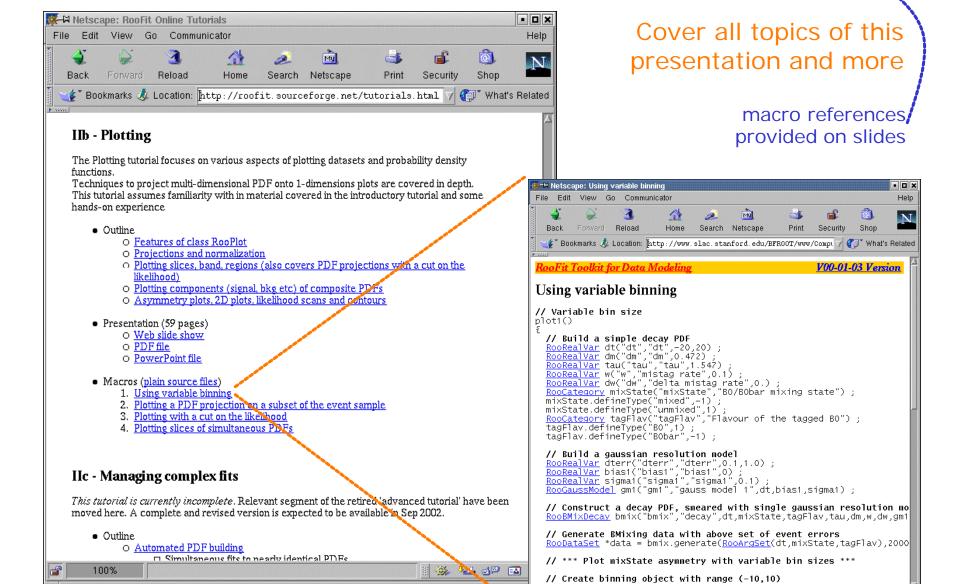
Starting point for all documentation is the RooFit homepage

http://roofit.sourceforge.net

Online tutorials



🔆 🛂 🔞 🖼 🤣



Rinning abins(-10.10)

HTML class documentation

