

Spin measurements in top-quark events at the LHC

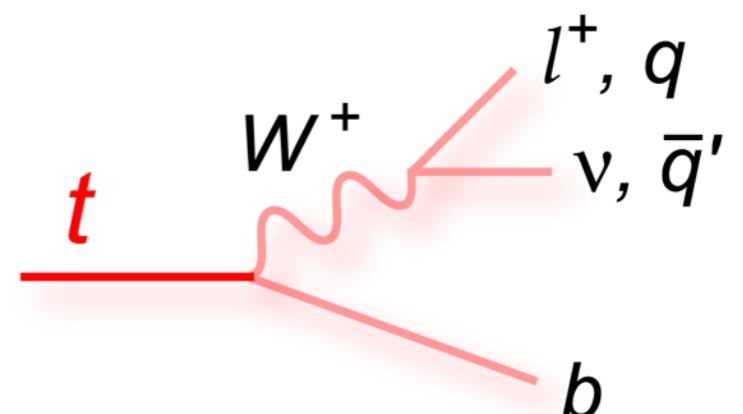
Jacob Linacre (FNAL)
on behalf of the ATLAS and CMS collaborations

TOP2015
15th September 2015

- ▶ Today I'll show recent top quark spin measurements from ATLAS and CMS
- ▶ top quark polarisation
 - ▶ in $t\bar{t}$ and single top (t-channel) events
- ▶ $t\bar{t}$ spin correlations

- Top decays before QCD interactions can affect its spin

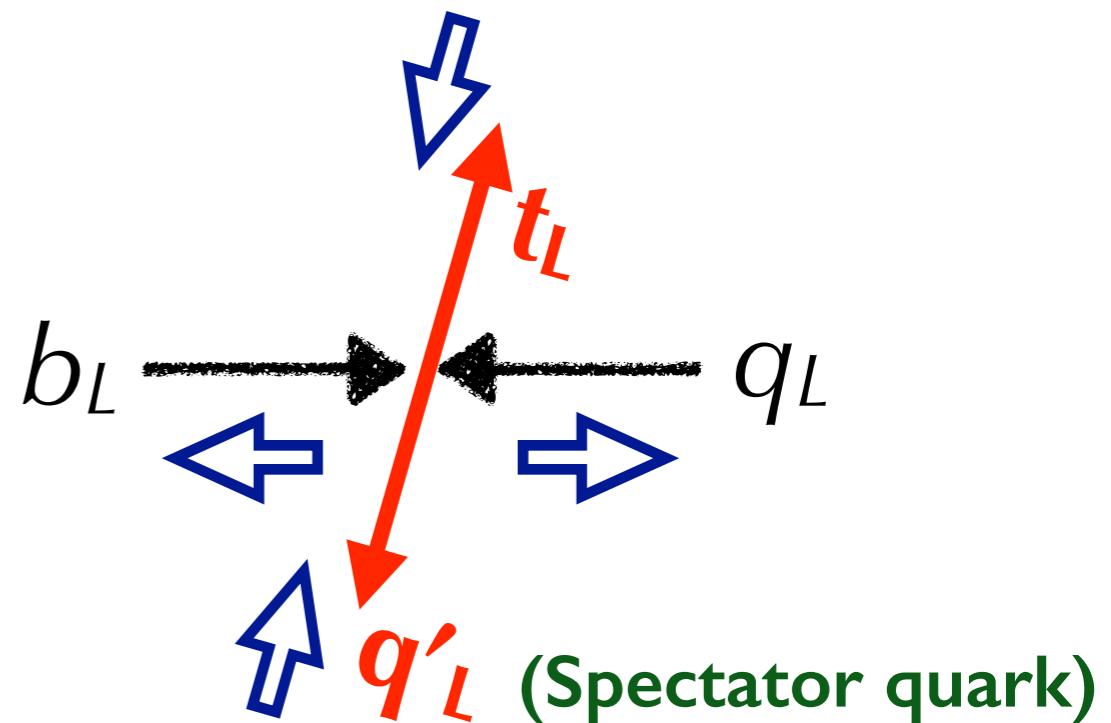
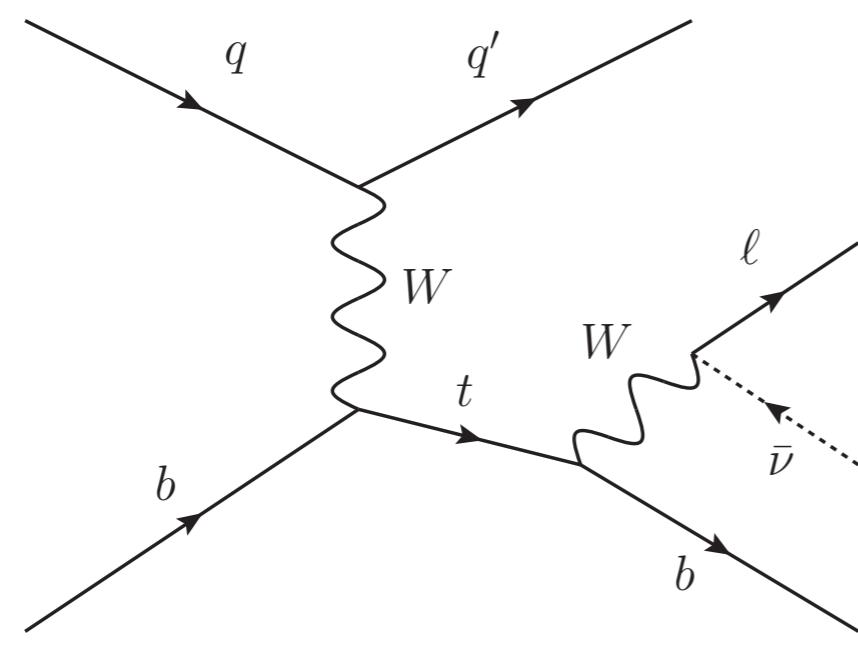
$$\text{top lifetime} < \frac{\text{QCD timescale}}{\text{timescale}} \ll \frac{\text{spin-flip timescale}}{\text{timescale}}$$
$$10^{-25} \text{ s} < 10^{-24} \text{ s} \ll 10^{-21} \text{ s}$$



- top decay products give us **direct access to its spin**
- expect top spin variables to be **well predicted by perturbative QCD**
- excellent test of SM
- Spin variables can be significantly **modified by new physics**
- already being used to set limits

Top polarisation

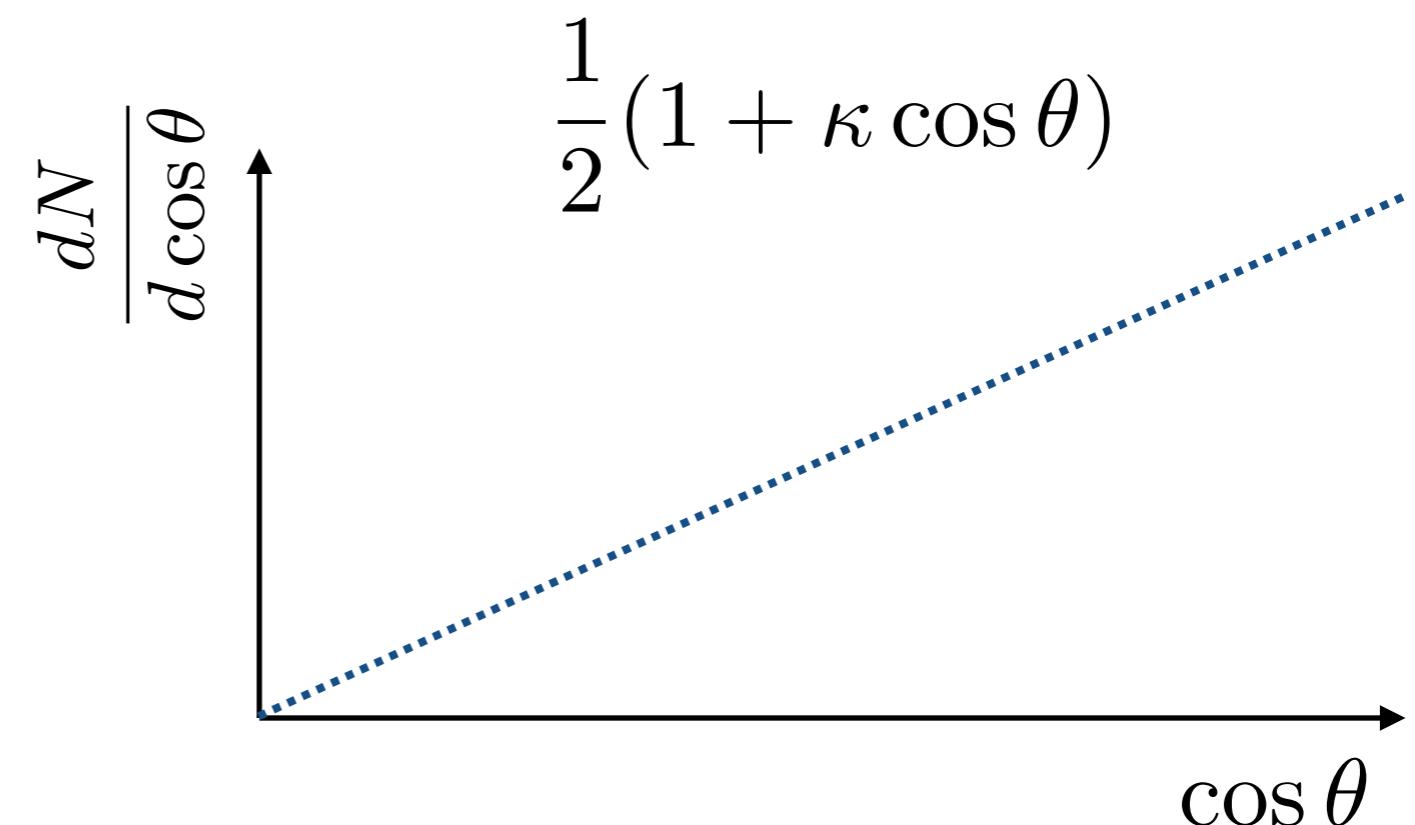
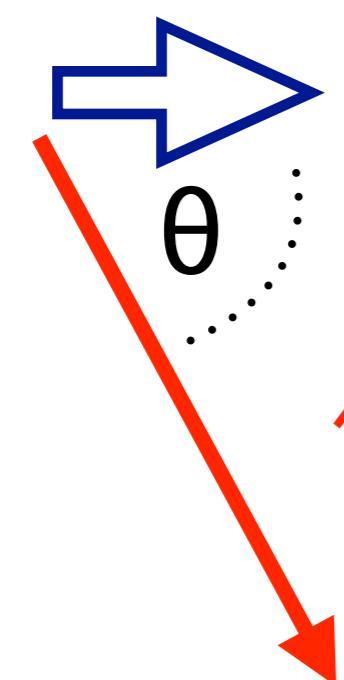
- ▶ Top spin **depends on production process** and on the basis (direction) for spin measurement
- ▶ Single top t-channel:
 - ▶ tops **100% L chirality** (because they have to couple to the W)
 - ▶ translates to **~95% spin up** in **spectator basis**



- ▶ $t\bar{t}$ production via strong interaction with **unpolarised incoming partons**
 - ▶ R and L tops equally likely
 - ▶ **no net polarisation at LO QCD** (usually measured in **helicity basis**)

- ▶ The top quark's spin determines the angular distribution of its daughters when it decays
- ▶ spin analysing powers: $\kappa_\ell = 1, \kappa_{\bar{d}} = 0.97, \kappa_u = -0.31, \kappa_b = -0.39$
[A. Brandenburg, Z. G. Si, P. Uwer \(2002\)](#)
- ▶ **lepton preferentially produced in top spin direction**

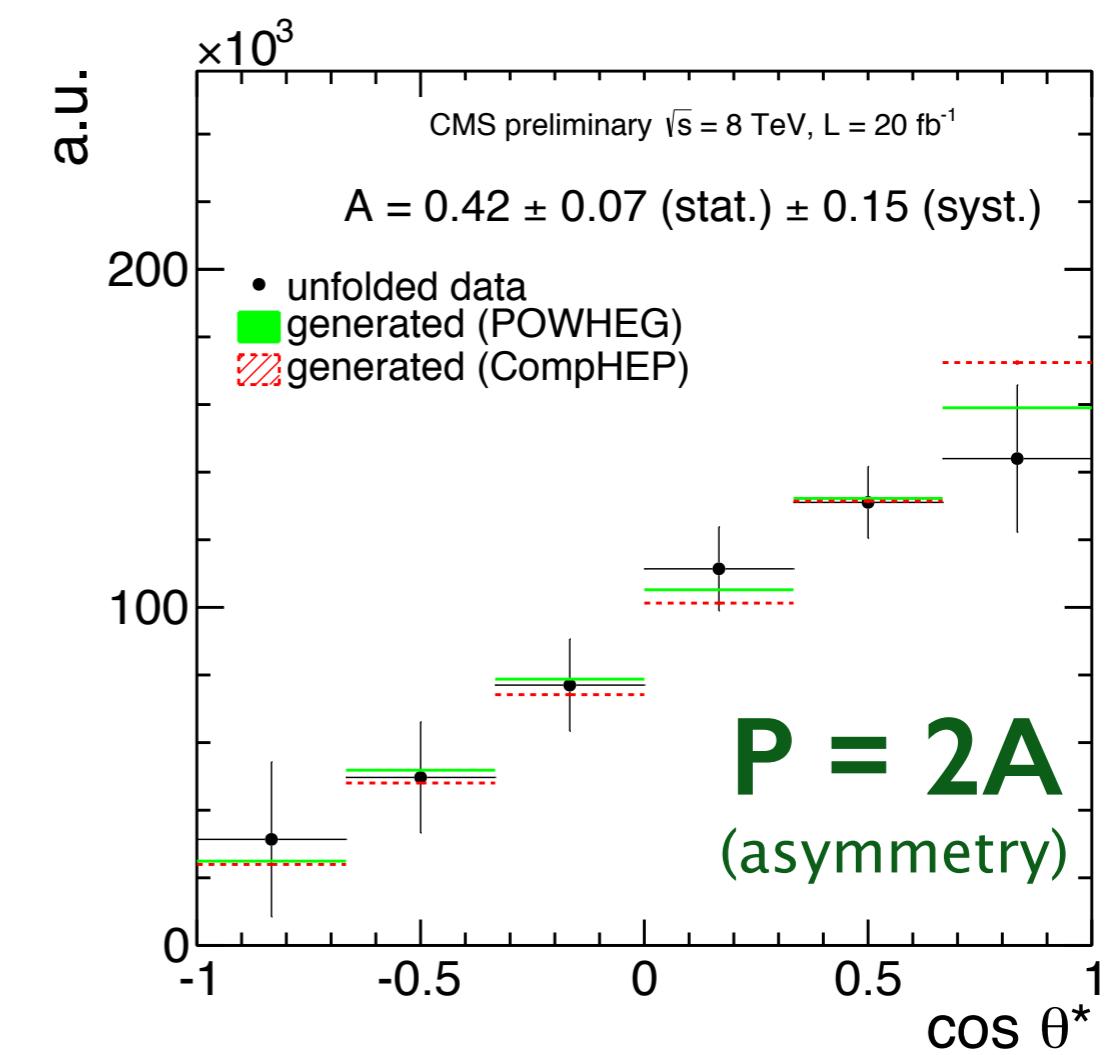
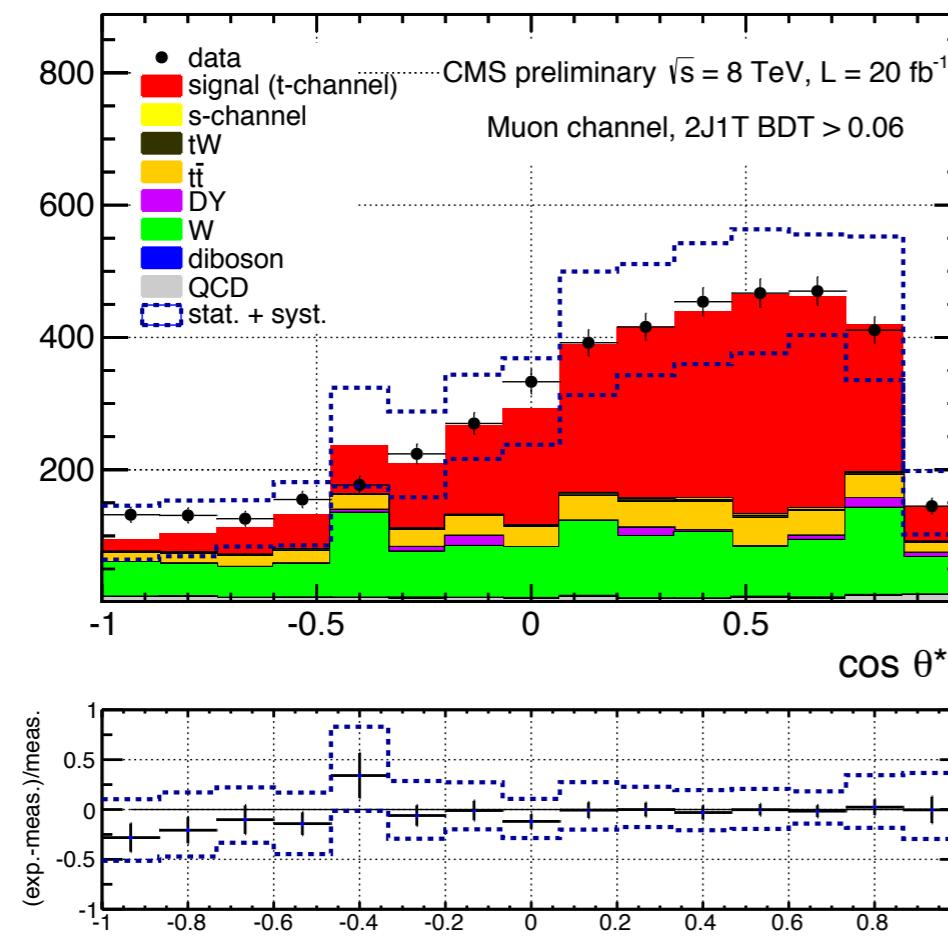
top rest frame



- ▶ Polarisation measures average spin:

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta} = \frac{1}{2}(1 + \kappa P \cos \theta)$$

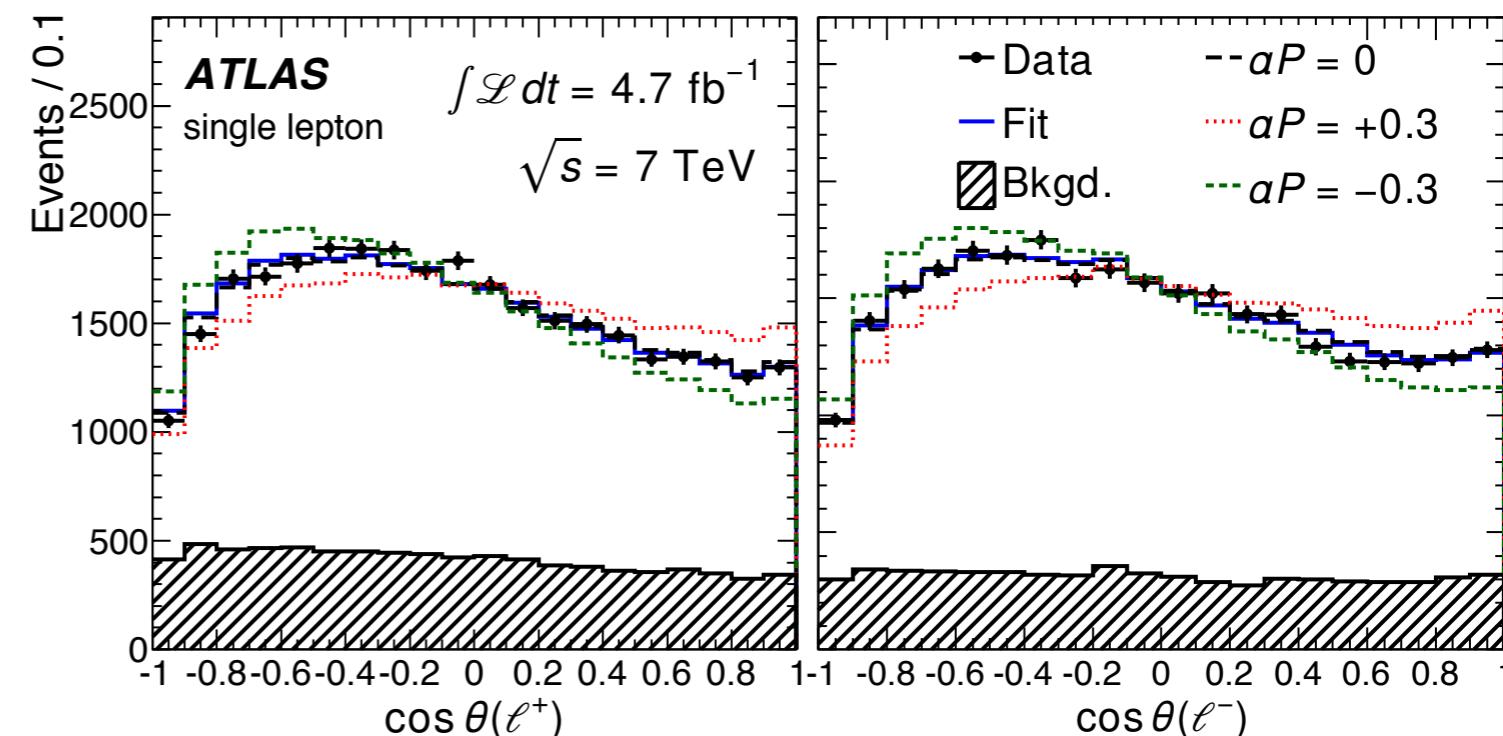
- ▶ BDT selects **~50% pure t-channel sample** [CMS-PAS-TOP-13-001](#)
- ▶ Reconstruct $\cos \theta^*$, subtract background ($W+jets$ largest), unfold to parton level, and combine e and μ channels
- ▶ Dominant systematics from JES and background subtraction



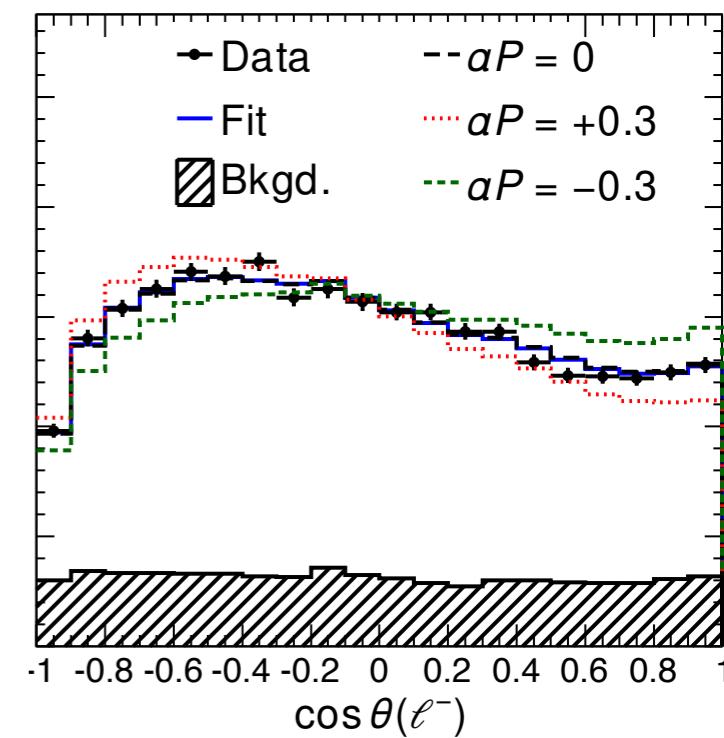
- ▶ Polarisation from distribution **asymmetry**: $P = (82 \pm 12 \pm 32)\%$

- ▶ Template fit to $\cos \theta^*$ at reco-level using templates with **+30%** and **-30%** polarisation
- ▶ $1\ell, 2\ell$ channels and t, \bar{t} distributions (ℓ^+ and ℓ^-) fitted separately
- ▶ Two scenarios
- ▶ **CP-conservation:**
 $P(t) = P(\bar{t})$
- ▶ **Maximal CP violation:**
 $P(t) = -P(\bar{t})$
- ▶ Jet reconstruction dominant systematic

[PRL 111, 232002 \(2013\)](#)

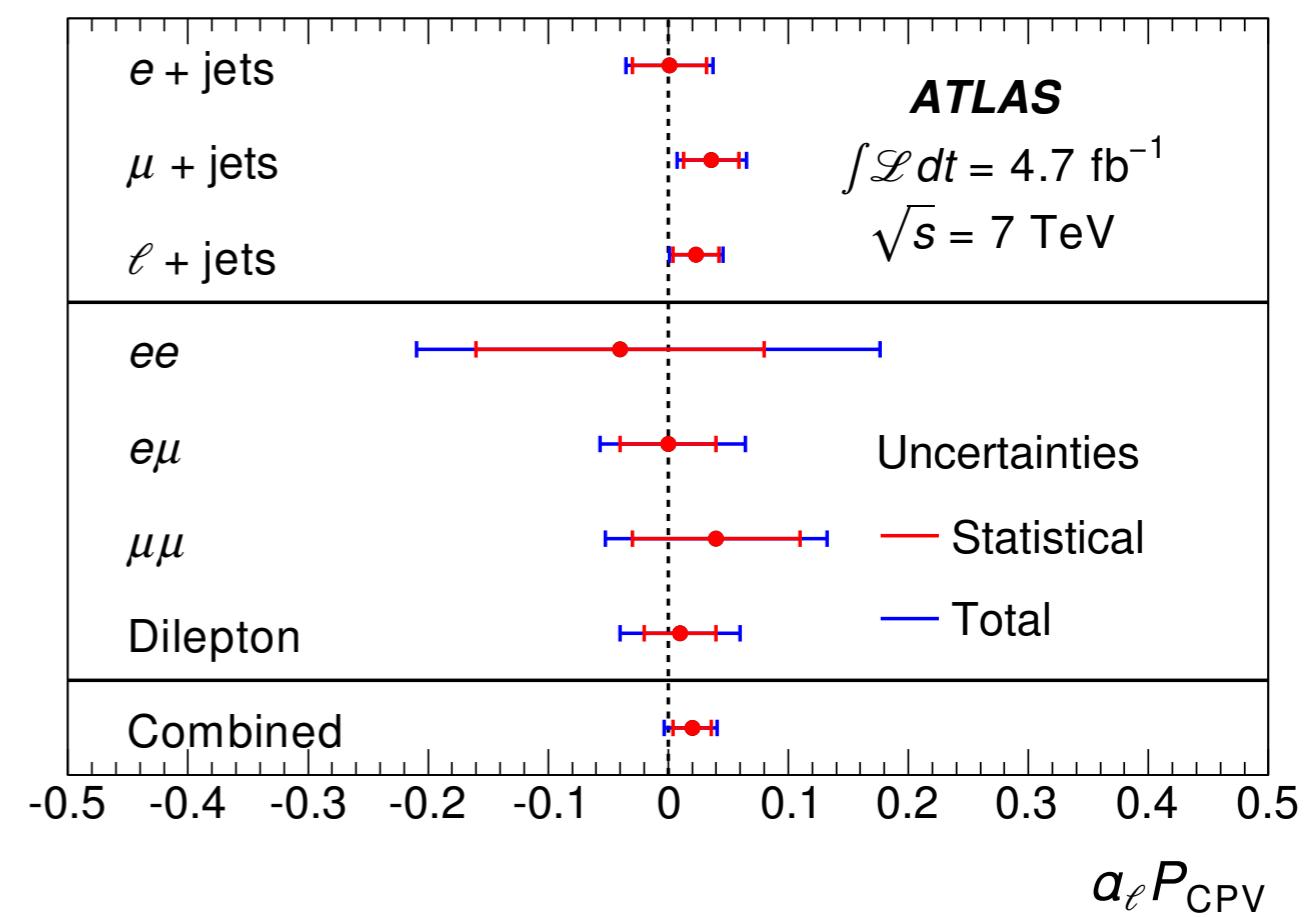
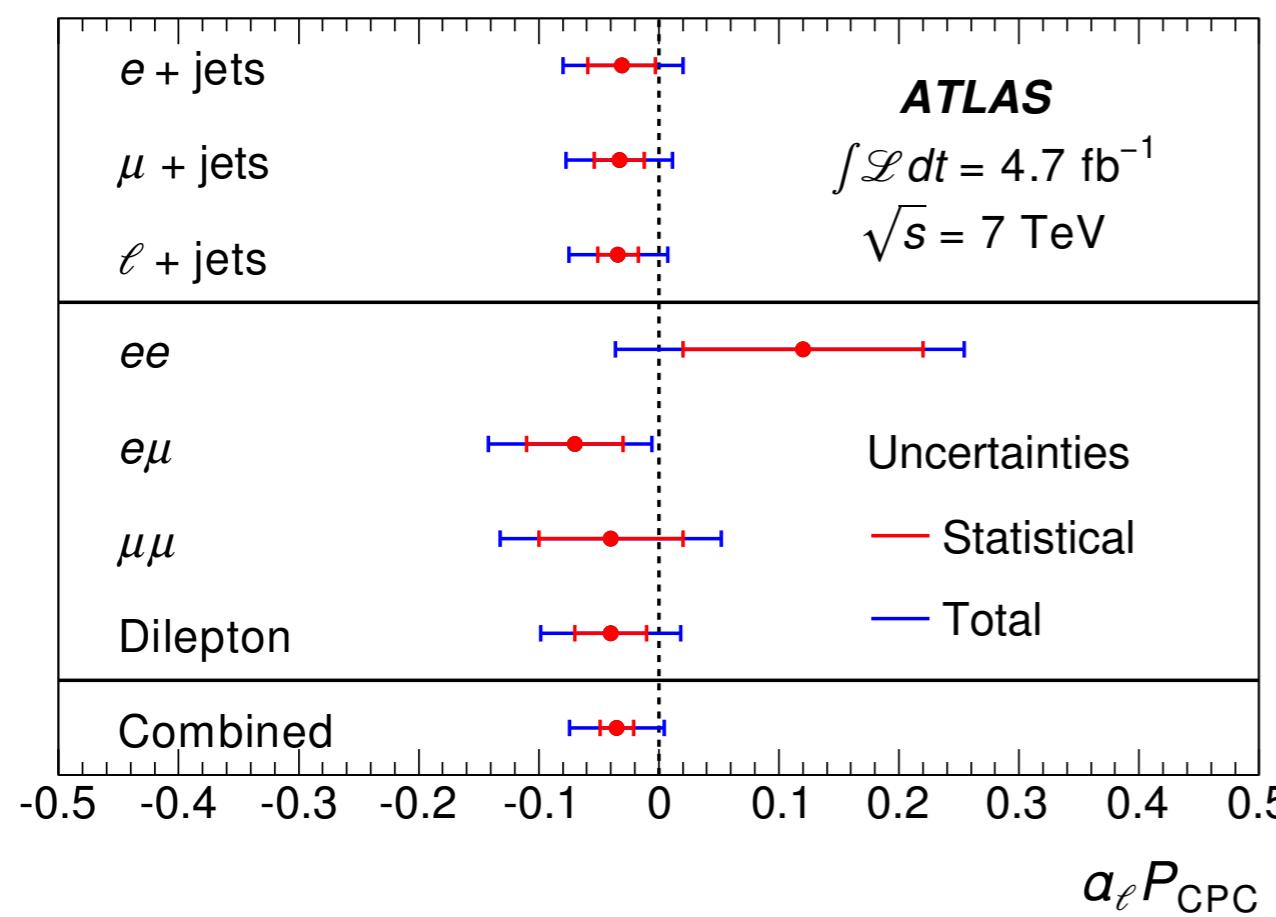


CP violating hypothesis:
 ℓ^+ templates unchanged
and ℓ^- templates flipped
so benefits from
maximal cancellation of
systematics



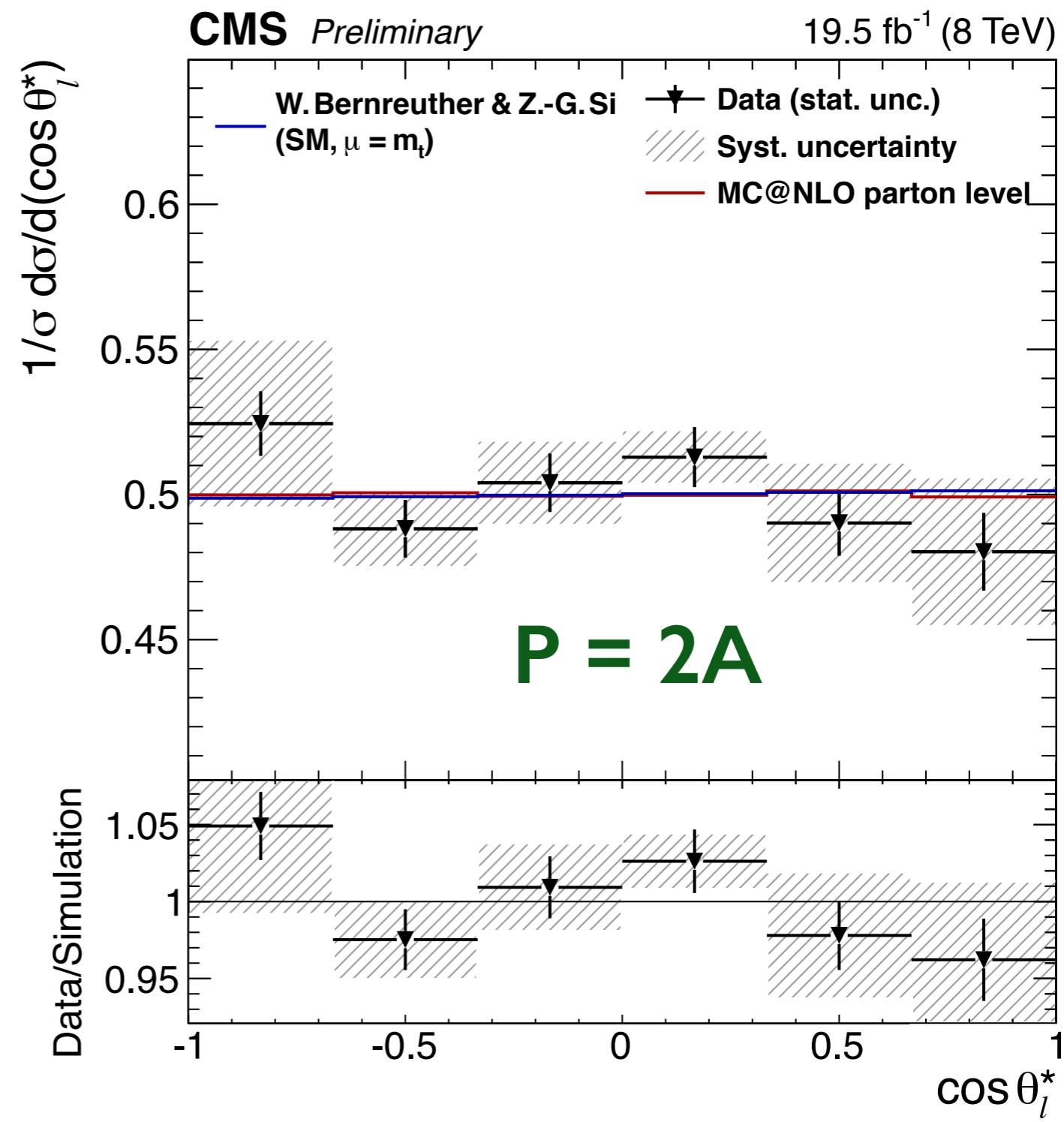
[PRL 111, 232002 \(2013\)](#)

- ▶ Results (assuming $\kappa_\ell = 1$):
- ▶ $P_{CP\text{C}} = (-3.5 \pm 1.4 \pm 3.7)\%$
- ▶ $P_{CP\text{V}} = (2.0 \pm 1.6 {}^{+1.3}_{-1.7})\%$


 $\alpha = \kappa = \text{spin analysing power}$

[CMS TOP-14-023](#)

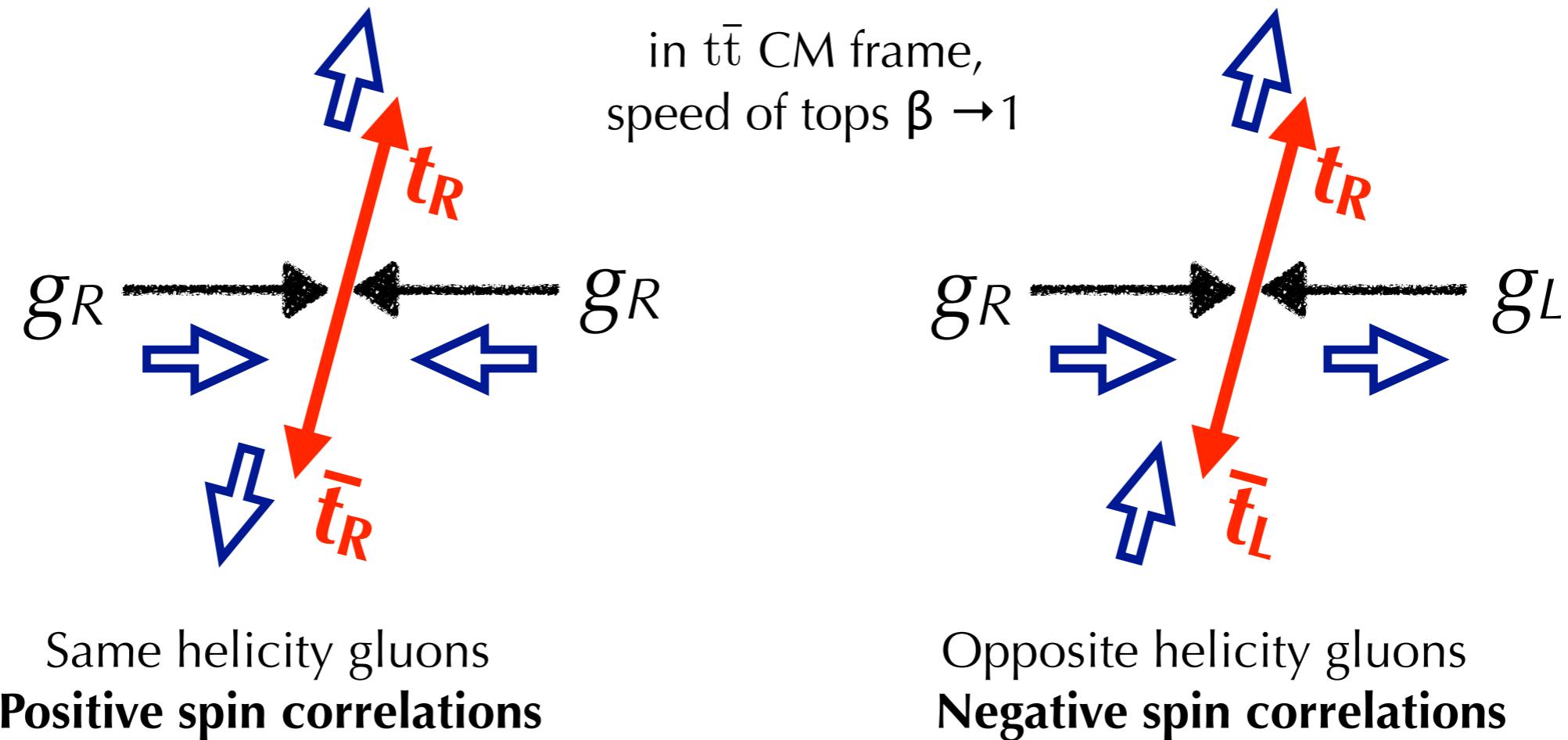
- ▶ $\cos \theta^*$ distribution **unfolded to parton level**
(dilepton channel)
- ▶ P measured from
asymmetry of distribution
- ▶ Two measurements per event (ℓ^+ and ℓ^-)
- ▶ Combined assuming CP conservation and violation
- ▶ $P_{CP} = (-2.2 \pm 5.9)\%$
 - ▶ JES dominant systematic
- ▶ $P_{CPV} = (-0.0 \pm 1.7)\%$
 - ▶ cancellation of systematics



$t\bar{t}$ spin correlations

Introduction to spin correlations

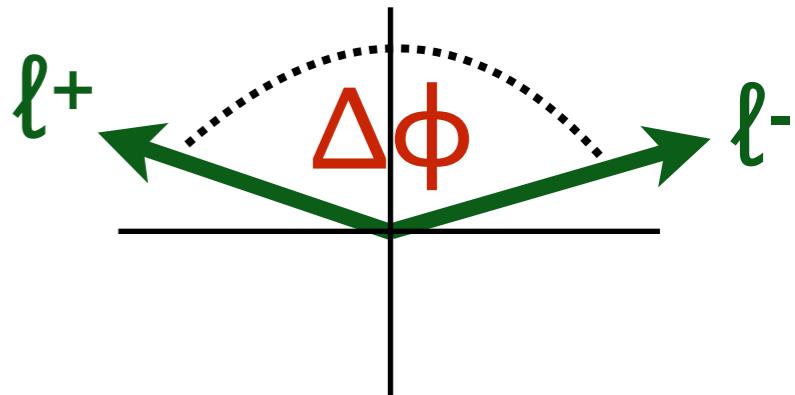
- ▶ Same and opposite helicity gluon fusion contributions impart different spin correlations to the top quark pairs



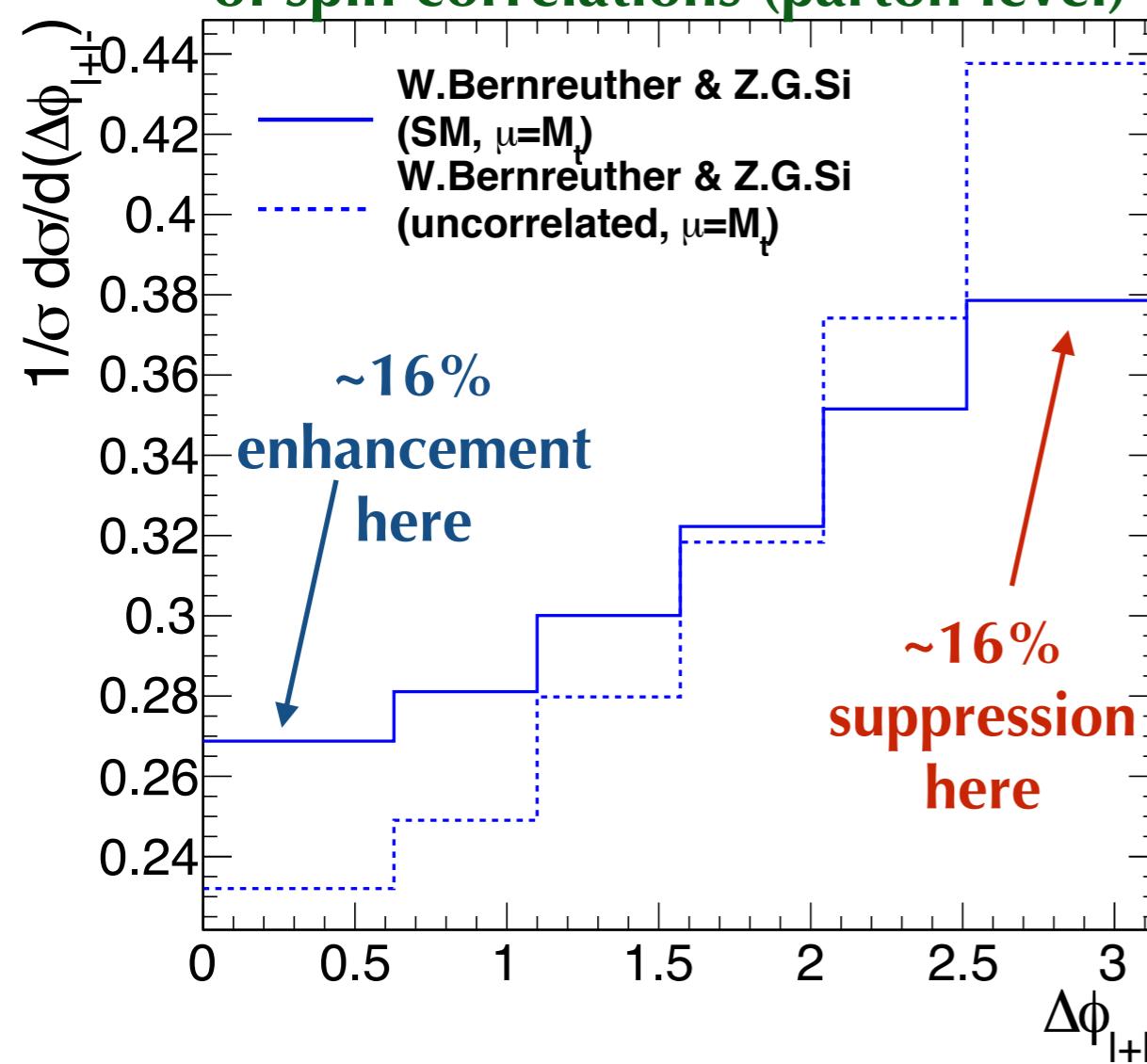
- ▶ Same helicity contribution is dominant near threshold
- ▶ Opposite helicity dominant when $E_t \gg m_t$ (helicity conservation)
- ▶ Expected net spin correlation strength of about +30% at the LHC
- ▶ modified in many new physics scenarios

Dilepton $\Delta\phi$ distribution

- ▶ Spin correlations in same-helicity gluon fusion result in aligned lepton decays
- ▶ alignment **strongest in $\Delta\phi$** (lab frame azimuthal angle between two leptons)

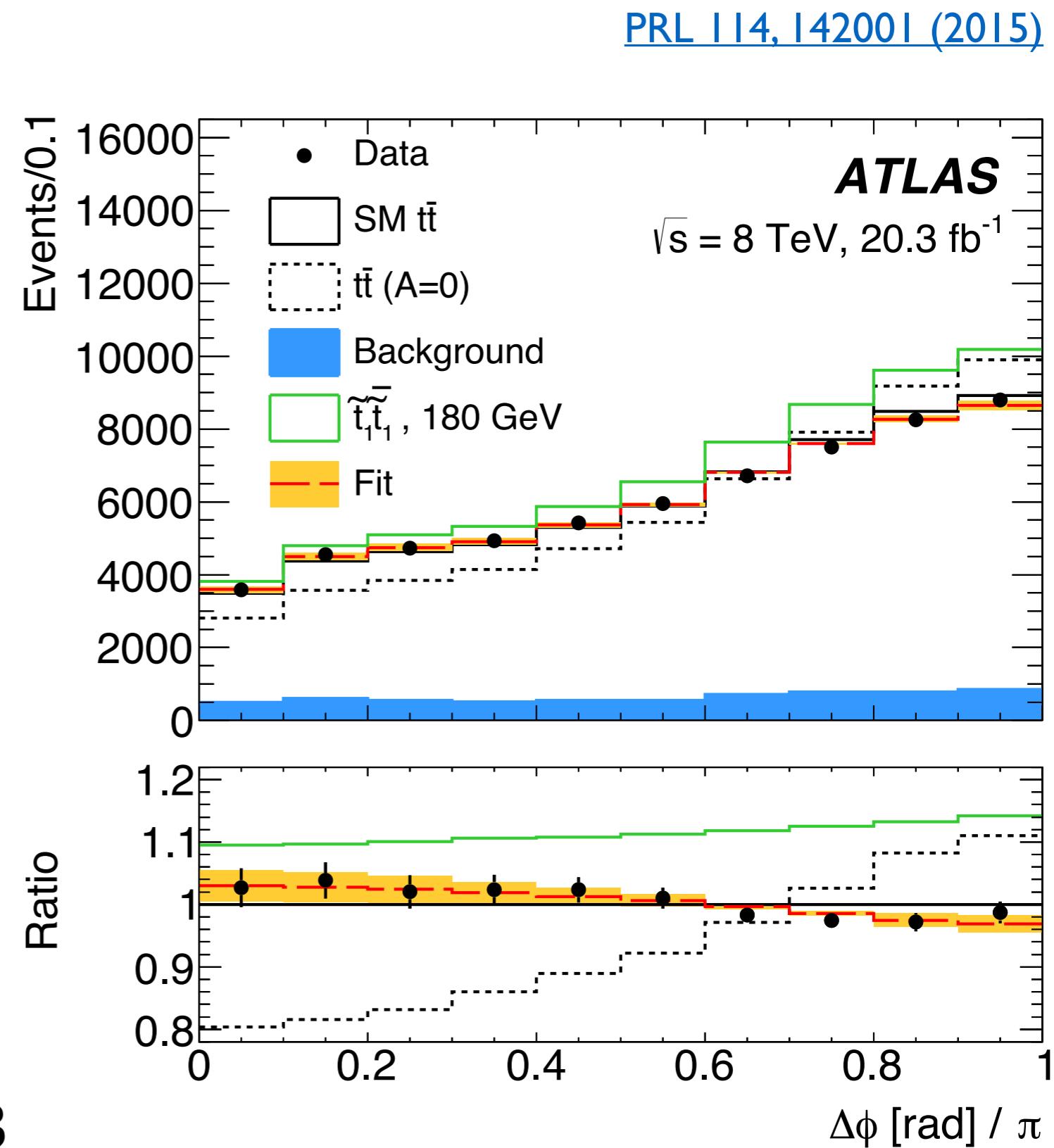


Δϕ distribution in presence and absence of spin correlations (parton level)



- ▶ Kinematically, large $\Delta\phi$ is preferred because tops are produced back to back
- ▶ **relative enhancement at low $\Delta\phi$ due to spin correlations**
- ▶ Lepton angles have excellent experimental resolution
- ▶ $\Delta\phi$ most precise probe of spin correlations (unique to LHC)

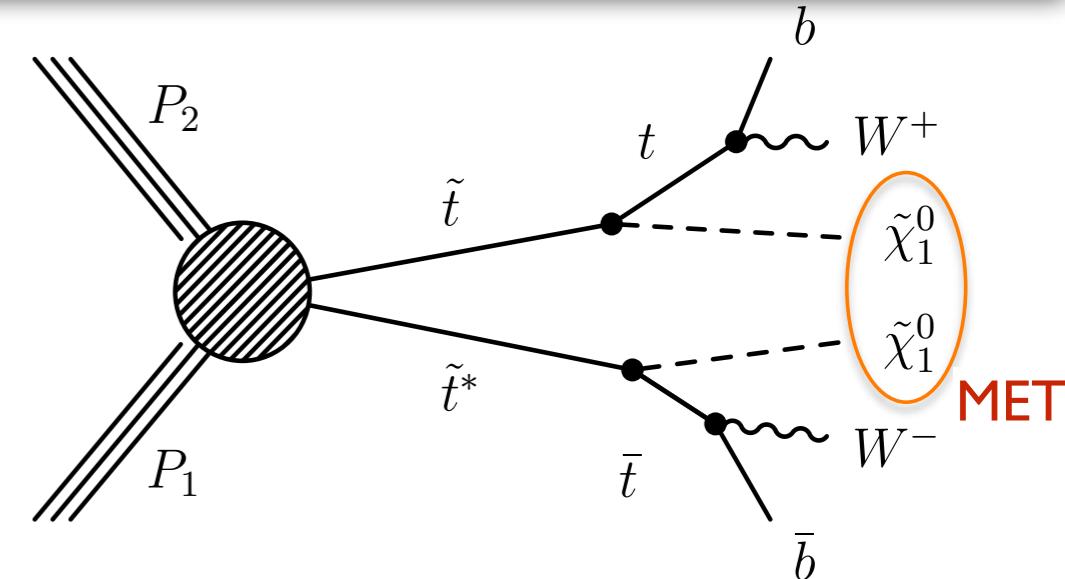
- ▶ Select $t\bar{t}$ events in dilepton final state
- ▶ data-driven prediction for dominant $Z/\gamma^* + \text{jets}$ background
- ▶ Quantify spin correlation strength as **fraction “f_{SM}” of SM expectation**
- ▶ template fit using simulated correlated and uncorrelated $t\bar{t}$
- ▶ $f_{\text{SM}} = 1.20 \pm 0.05 \pm 0.13$



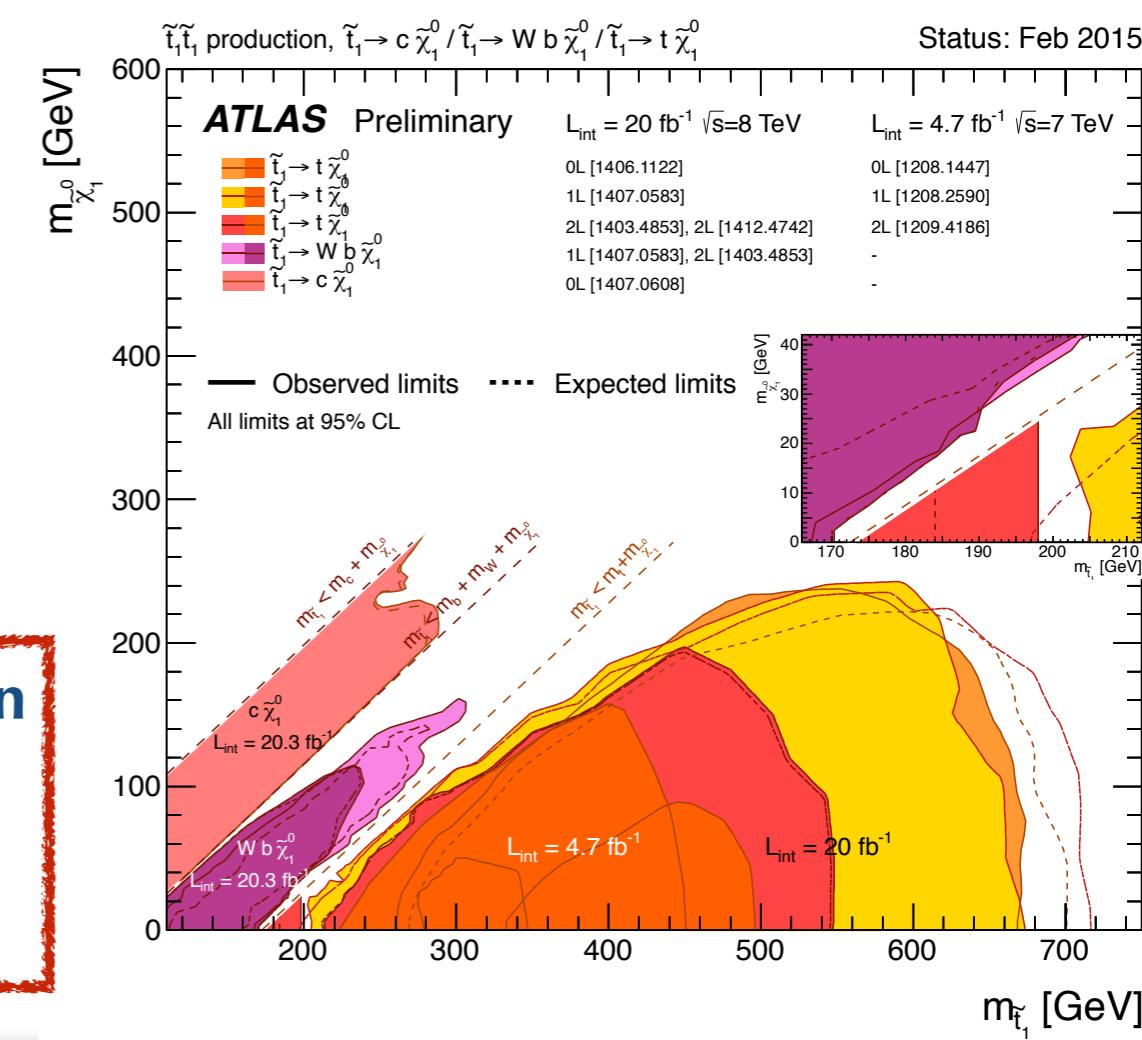
Probing SUSY with spin correlations

- ▶ Supersymmetric top squark pair production looks like $t\bar{t} + \text{MET}$
- ▶ Squarks have spin-zero
- ▶ daughter top quarks look similar to **uncorrelated $t\bar{t}$** events
- ▶ but only $\sim 1/6$ of the $t\bar{t}$ cross section for $m_{\text{stop}} = m_t$
- ▶ **Total cross section measurement**
also sensitive to stops
- ▶ Combining the two,
ATLAS excludes
 $m_t < m_{\text{stop}} < 191 \text{ GeV}$

Important region
to probe based
on naturalness
considerations

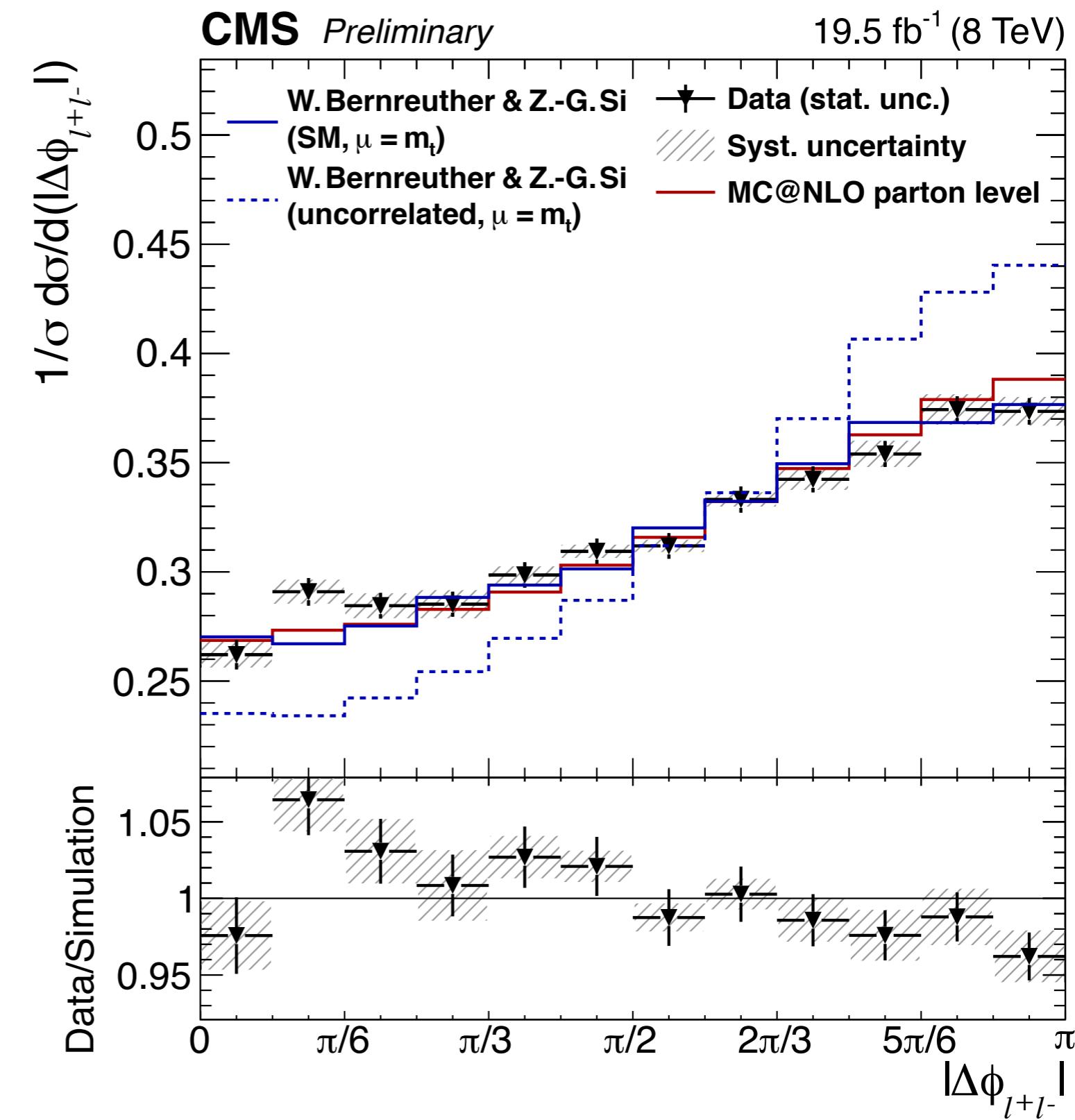


Direct searches insensitive when $\tilde{\chi}_1^0$ soft

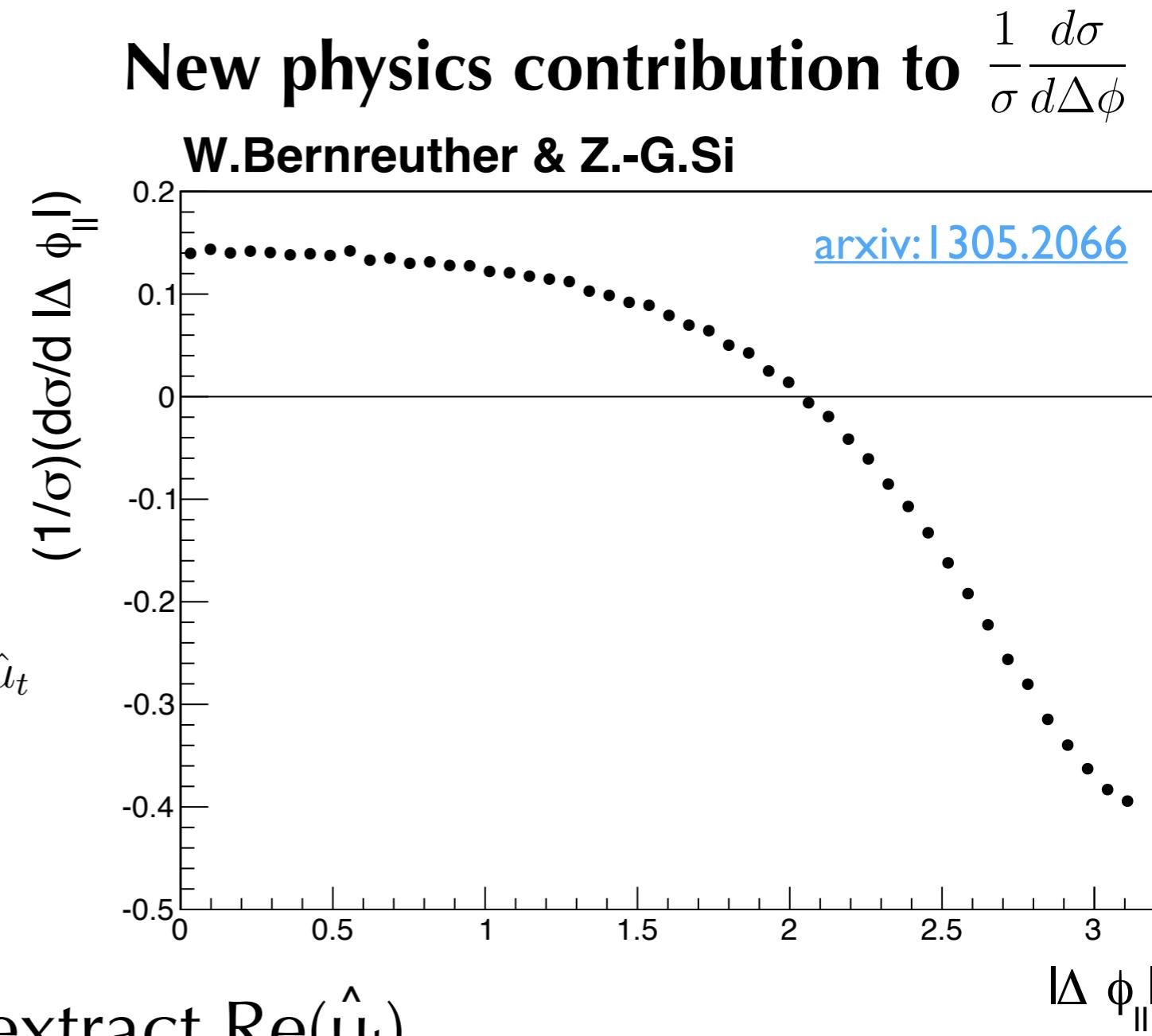


[CMS TOP-14-023](#)

- ▶ $\Delta\phi$ distribution **unfolded to parton level**
- ▶ Compared to theoretical predictions at NLO with and without spin correlations
- ▶ The data agree with the SM prediction
- ▶ **top p_T modelling** dominant experimental systematic
- ▶ $f_{SM} = 1.18 \pm 0.18$
- ▶ dominant uncertainty from **scale uncertainties in the NLO predictions**

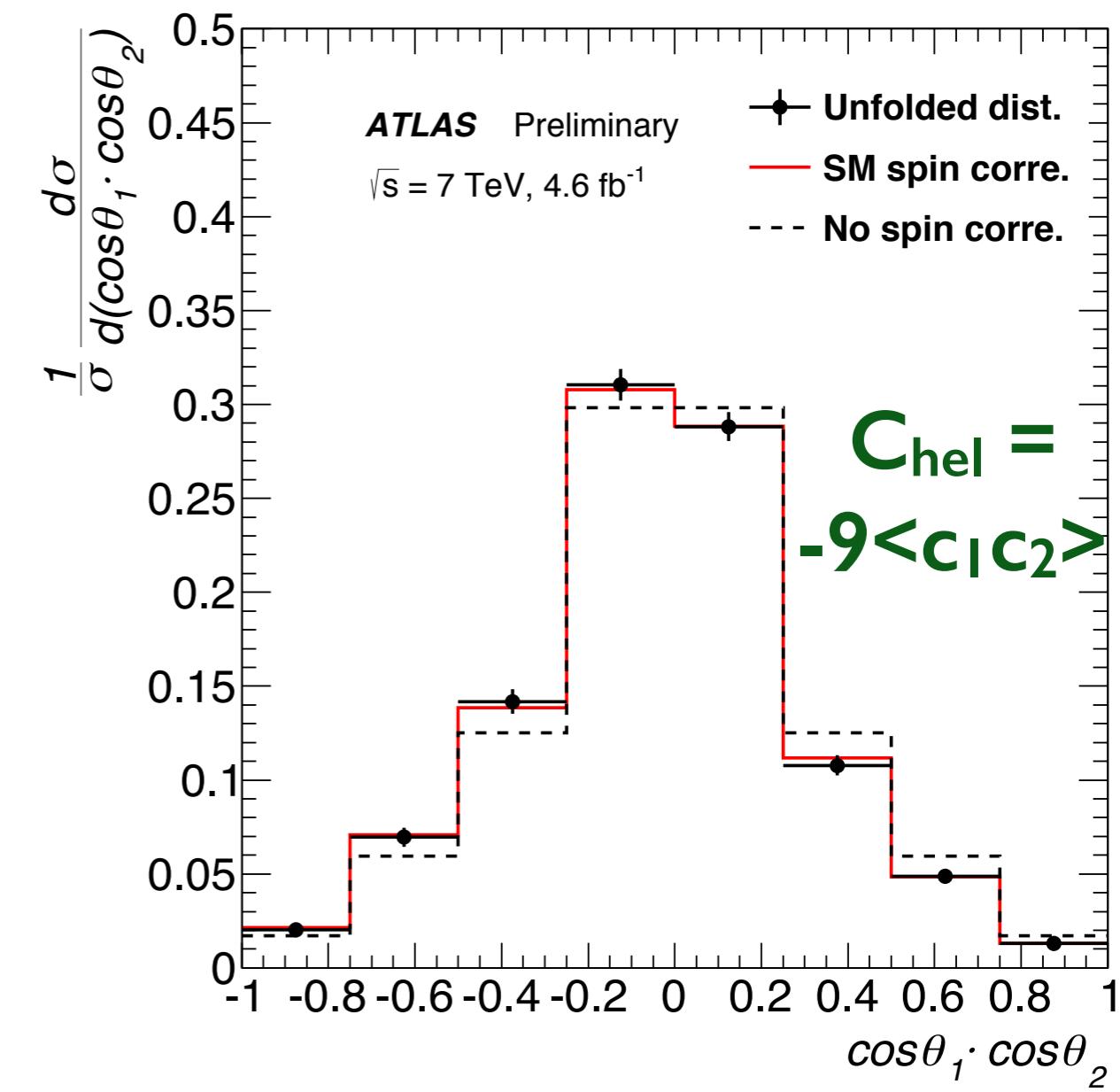
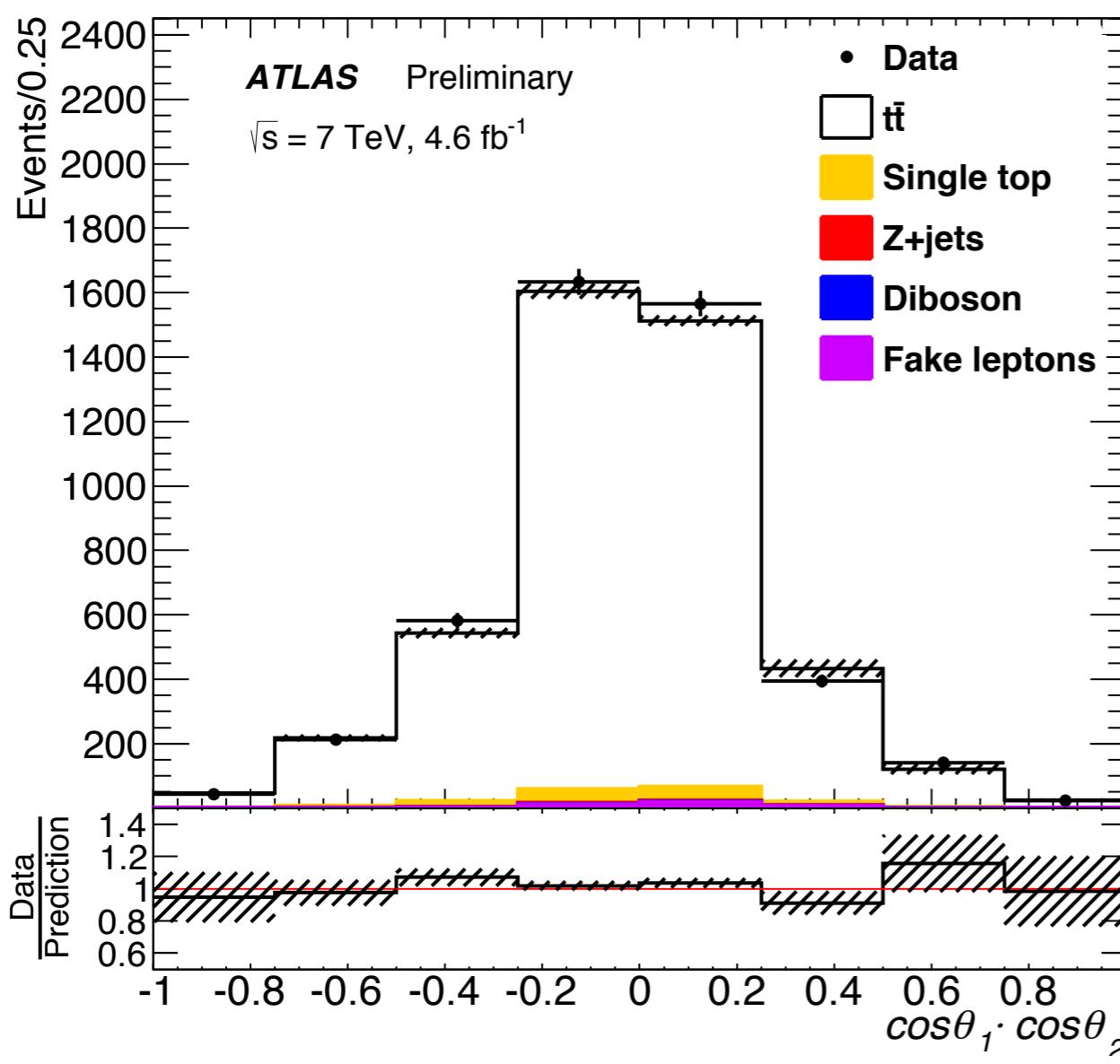


- ▶ Heavy particle exchange in $t\bar{t}$ production can modify spin correlations by introducing colour dipole ttg couplings
- ▶ Model-independent effective Lagrangian:
 - ▶ $\mathcal{L}_{eff} = \mathcal{L}_{SM} - \frac{\tilde{\mu}_t}{2} \bar{t} \sigma^{\mu\nu} T^a t G_{\mu\nu}^a$
 - ▶ $\tilde{\mu}_t$ = anomalous CMMDM
 - ▶ For small $\tilde{\mu}_t$:
$$\frac{1}{\sigma} \frac{d\sigma}{d\Delta\phi} = \left(\frac{1}{\sigma} \frac{d\sigma}{d\Delta\phi} \right)_{SM} + \left(\frac{1}{\sigma} \frac{d\sigma}{d\Delta\phi} \right)_{NP} \text{Re}(\hat{\mu}_t)$$
 - ▶ $d\sigma$ only sensitive to $\text{Re}(\tilde{\mu}_t)$
 - ▶ Template fit to SM+NP to extract $\text{Re}(\hat{\mu}_t)$
 - ▶ **-0.050 < Re($\hat{\mu}_t$) < 0.076 (95% CL)**



[\(CMS TOP-14-023\)](#)

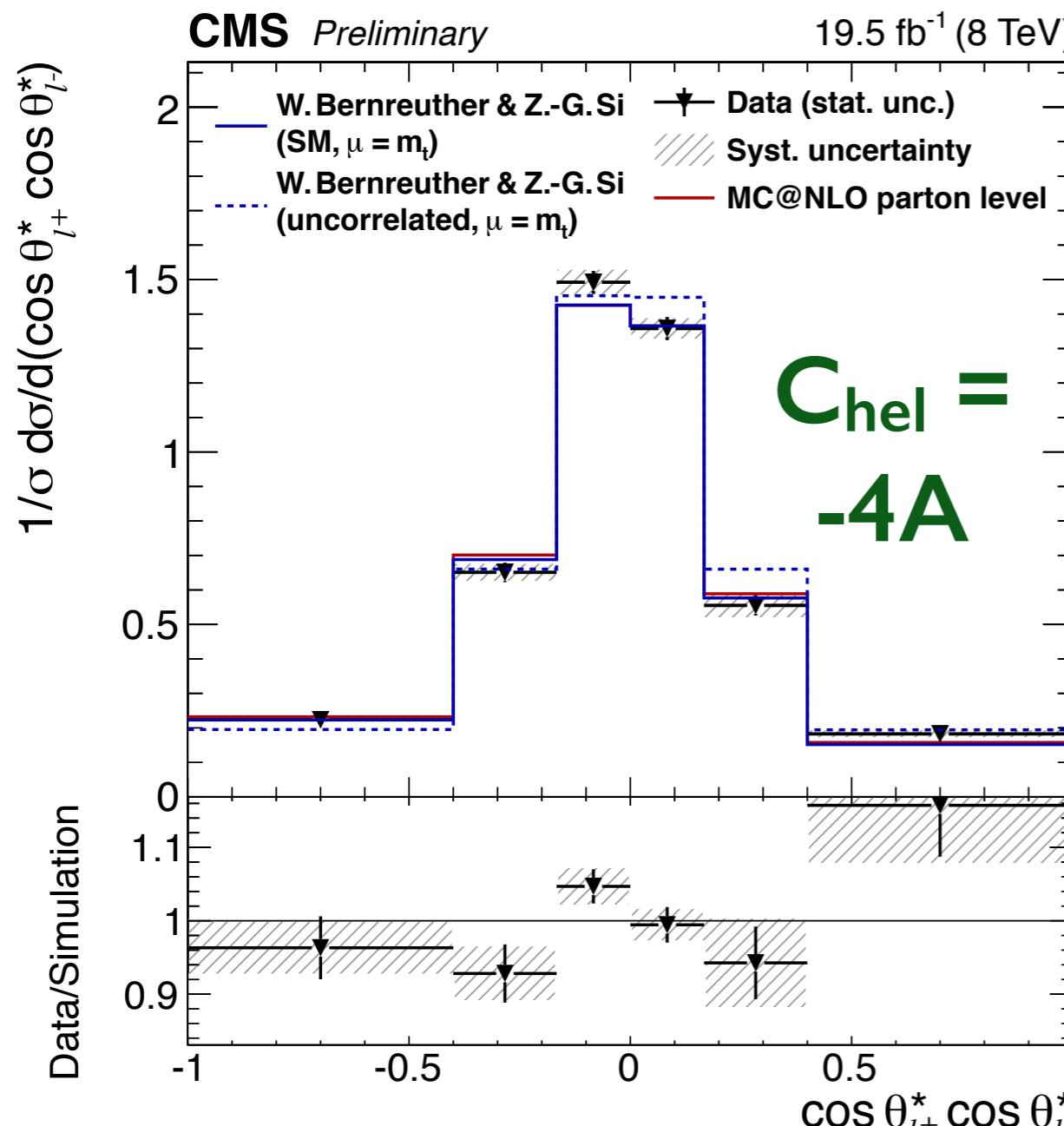
- ▶ Direct measurement requires **full t, \bar{t} reconstruction** Paper in preparation
- ▶ **Lepton directions** in parent top CMs used as a **proxies for the top spins**
- ▶ C_{hel} coefficient from distribution of product of top spins: $\cos \theta_{\ell+}^* \cos \theta_{\ell-}^*$



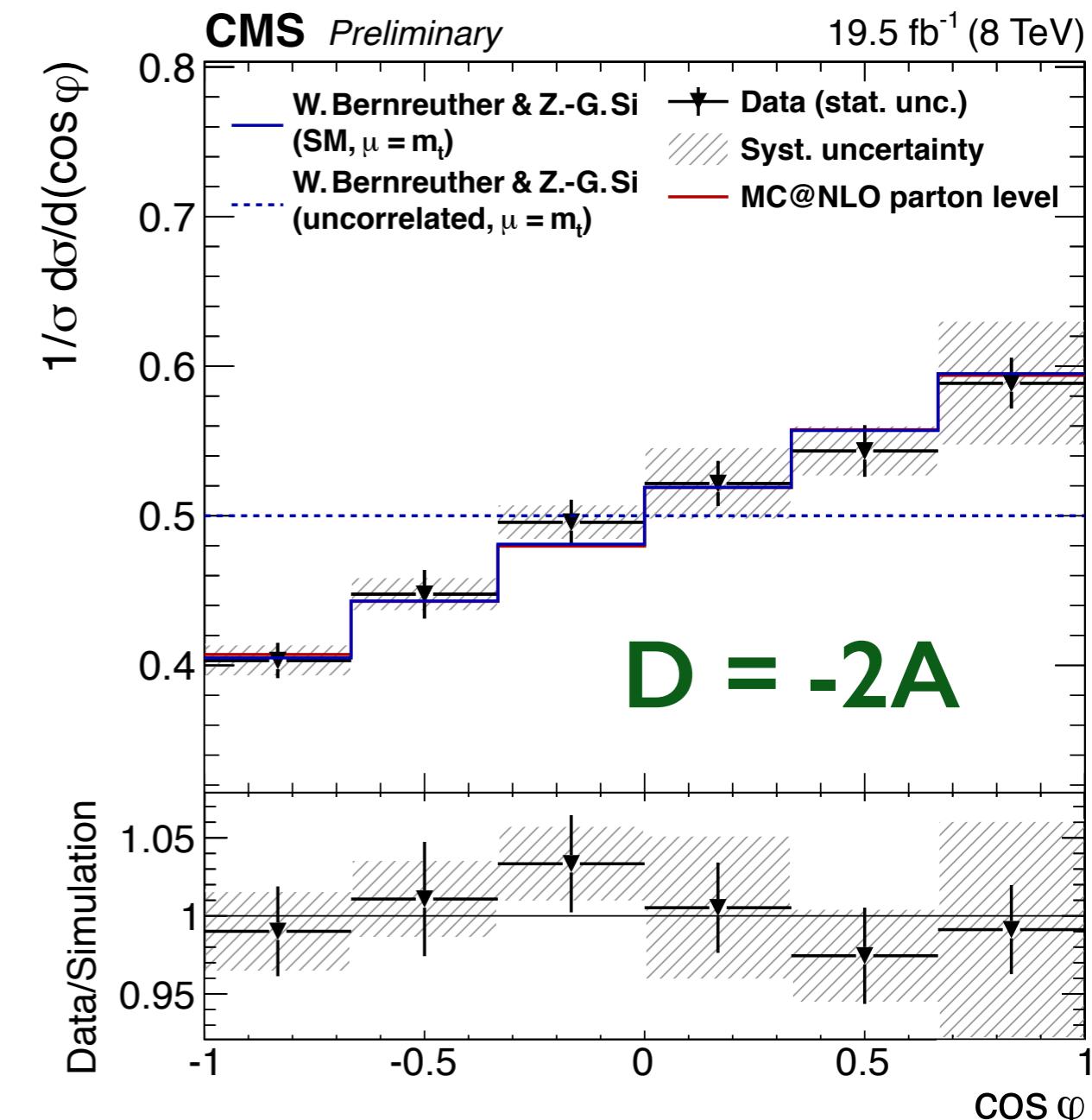
▶ $C_{hel} = 0.315 \pm 0.061 \pm 0.049$

▶ $f_{SM} = 1.02 \pm 0.26$ (unofficial)

- ▶ Direct measurement requires **full t, \bar{t} reconstruction** [CMS TOP-14-023](#)
- ▶ **Lepton directions** in parent top CMs used as a **proxies for the top spin**
- ▶ D coefficient from distribution of angle between the spins: $\varphi = \angle(\hat{\ell^+}, \hat{\ell^-})$

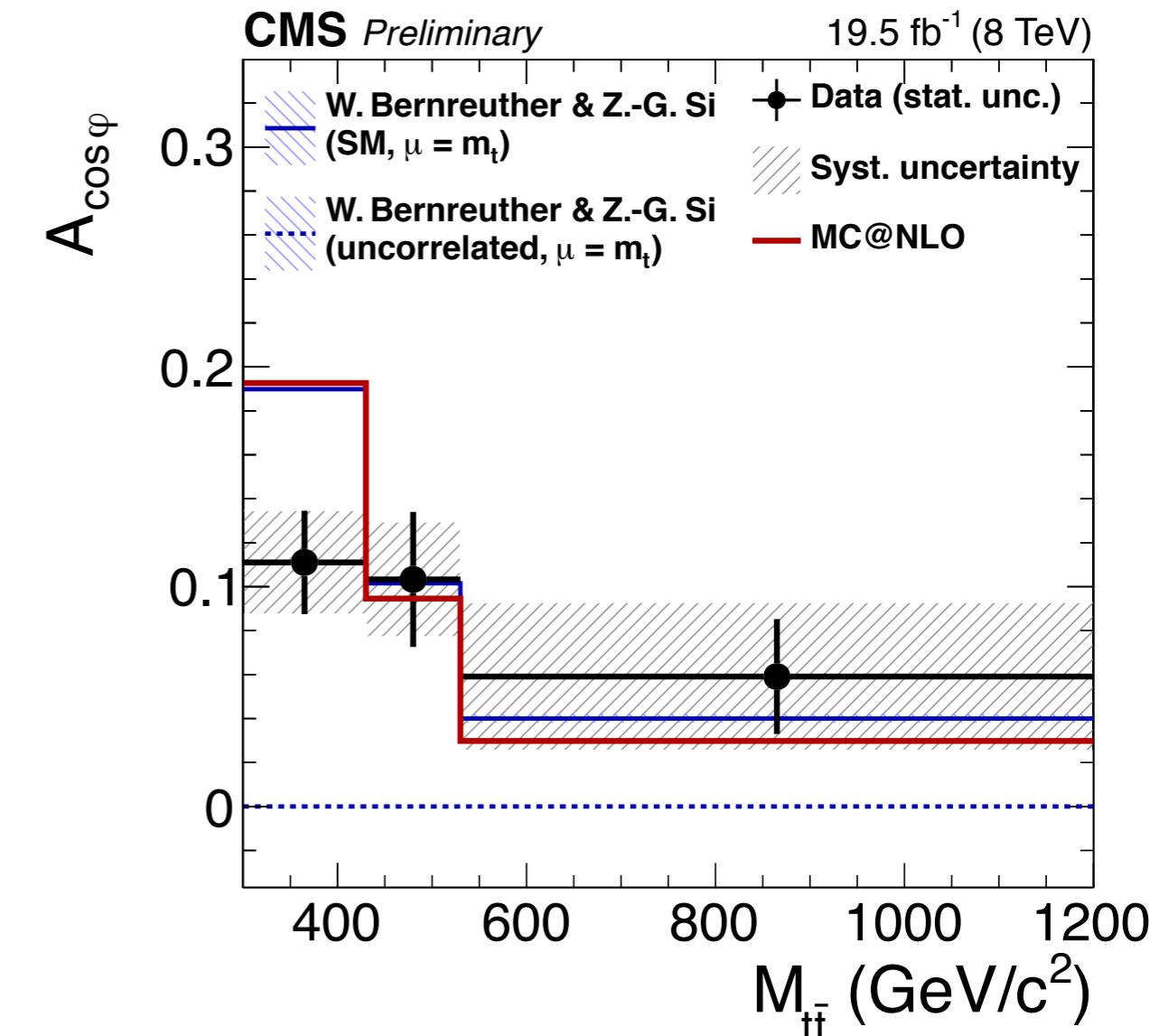
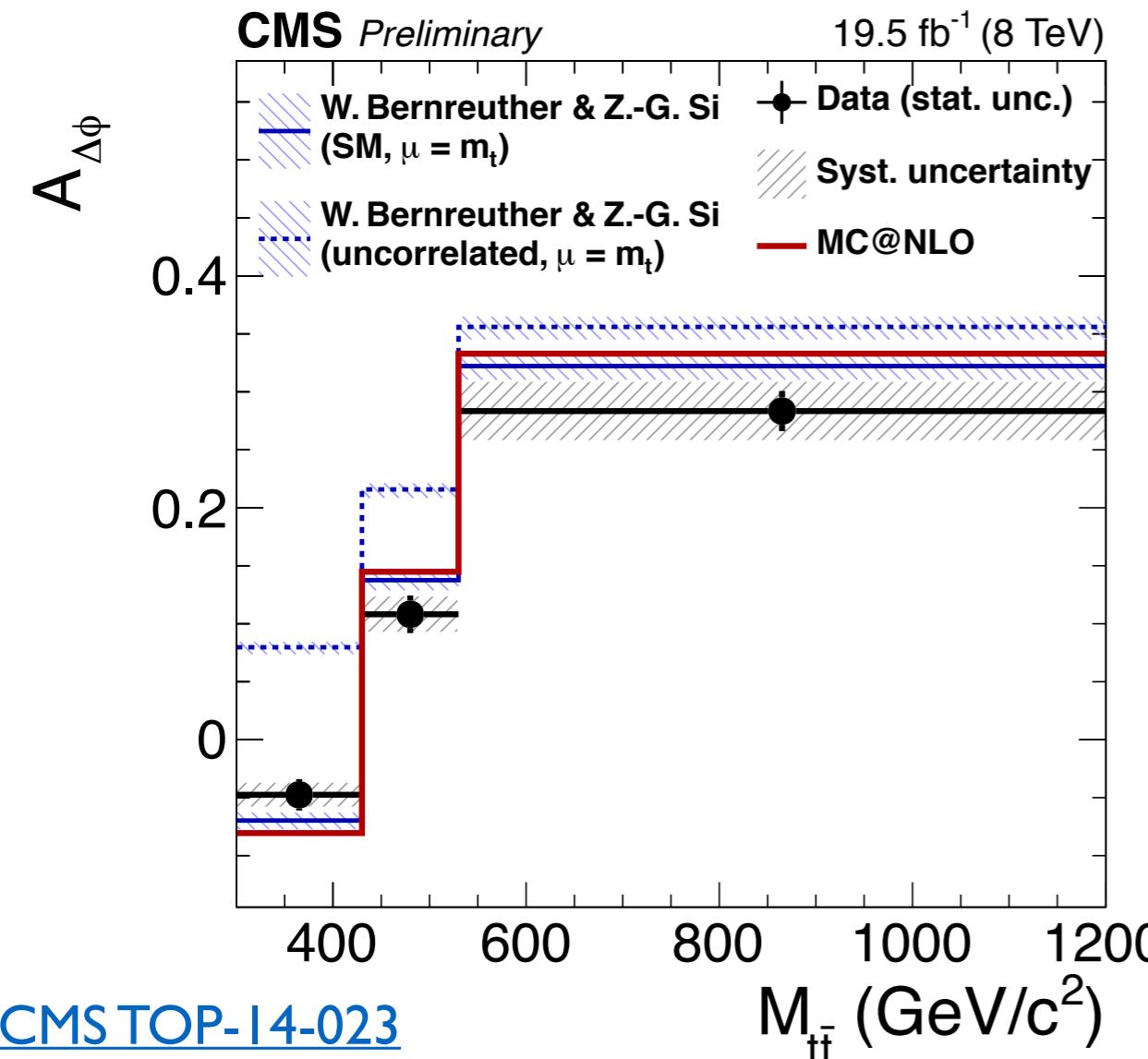


▶ $f_{SM} = 0.87 \pm 0.27$



▶ $f_{SM} = 0.90 \pm 0.16$

- Asymmetry variables measured **differentially** wrt $M_{t\bar{t}}$, $|y_{t\bar{t}}|$, $p_T^{t\bar{t}}$



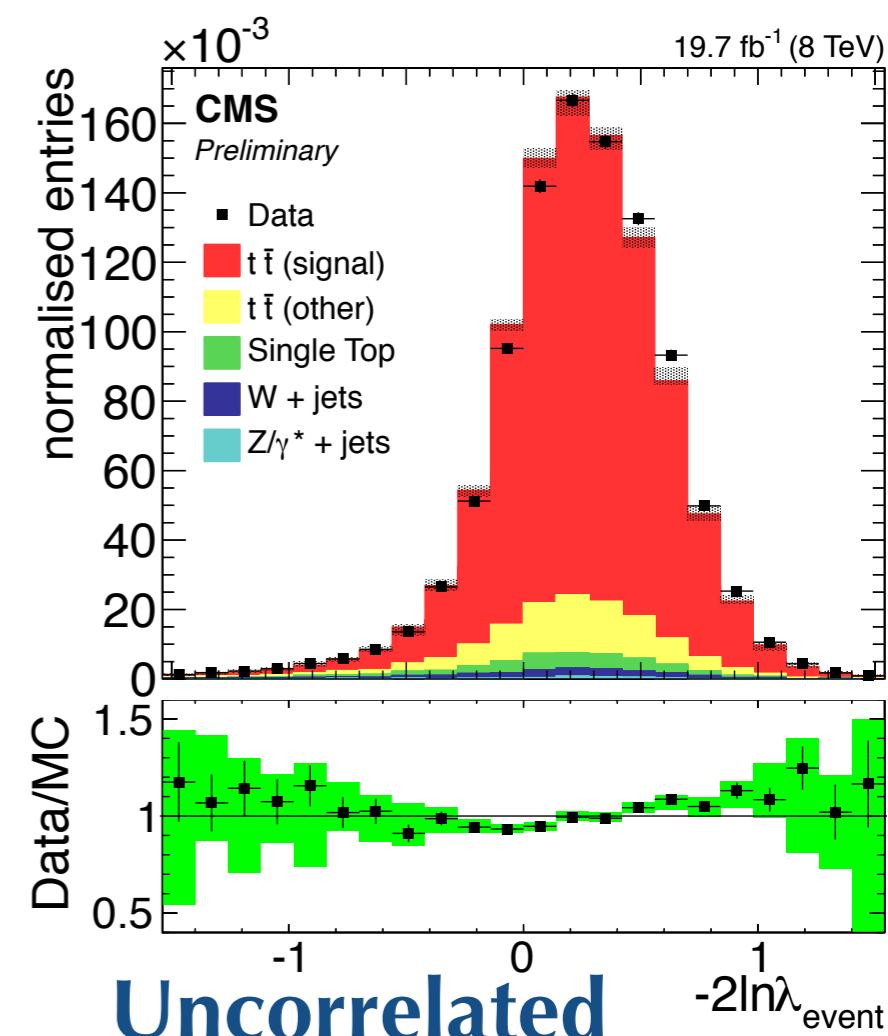
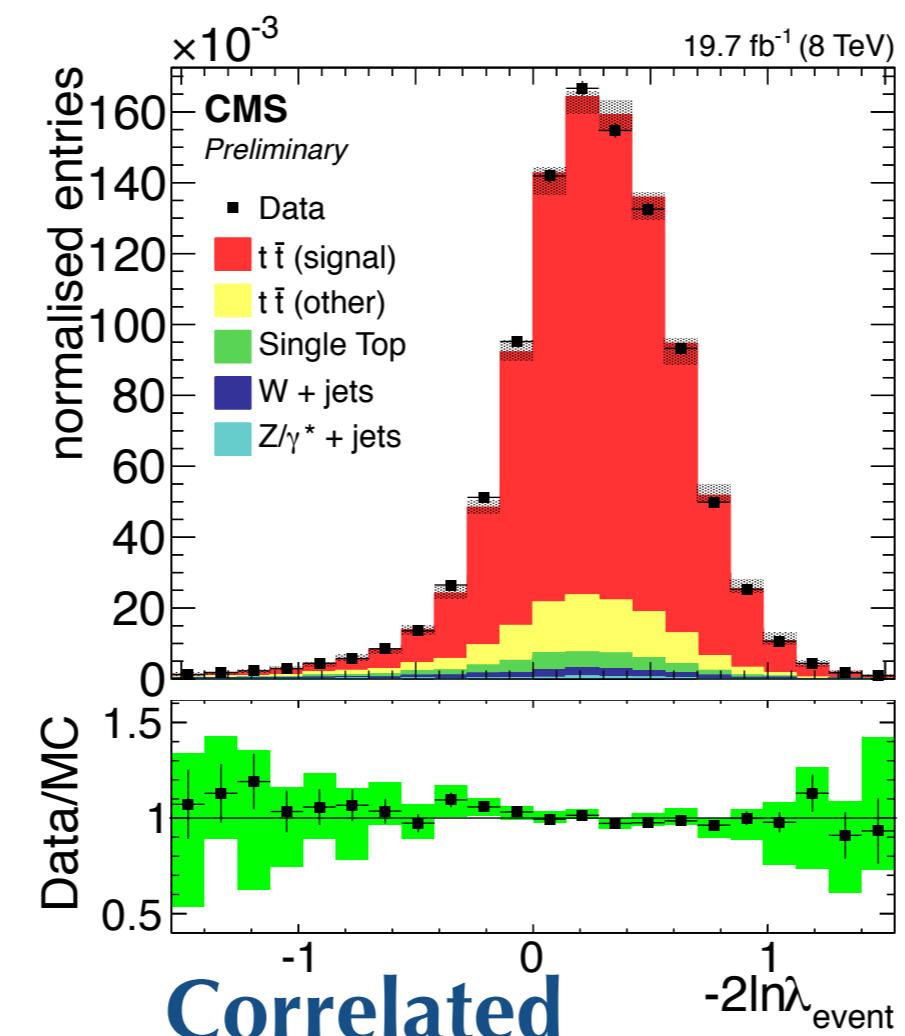
- SM spin correlations have most structure wrt $M_{t\bar{t}}$
- Unfolding wrt $M_{t\bar{t}}$ **minimises the $\Delta\phi$ top p_T systematic:**
- $f_{\text{SM}} = 1.16 \pm 0.15$ (but still limited by NLO scale uncertainties)

- ▶ In 1 ℓ events, $\Delta\phi$ distribution is not as sensitive
- ▶ don't know whether light jet is u ($\kappa = -0.31$) or d ($\kappa = 0.97$)
- ▶ b-jet also has small spin analysing power ($\kappa = -0.39$)
- ▶ Use **matrix element method** to extract more information from each event

[CMS-PAS-TOP-13-015](#)

$$\lambda_{event} = \frac{P_{uncor}}{P_{cor}} = \frac{\text{Event probability using LO uncorrelated ME}}{\text{Event probability using LO correlated ME}}$$

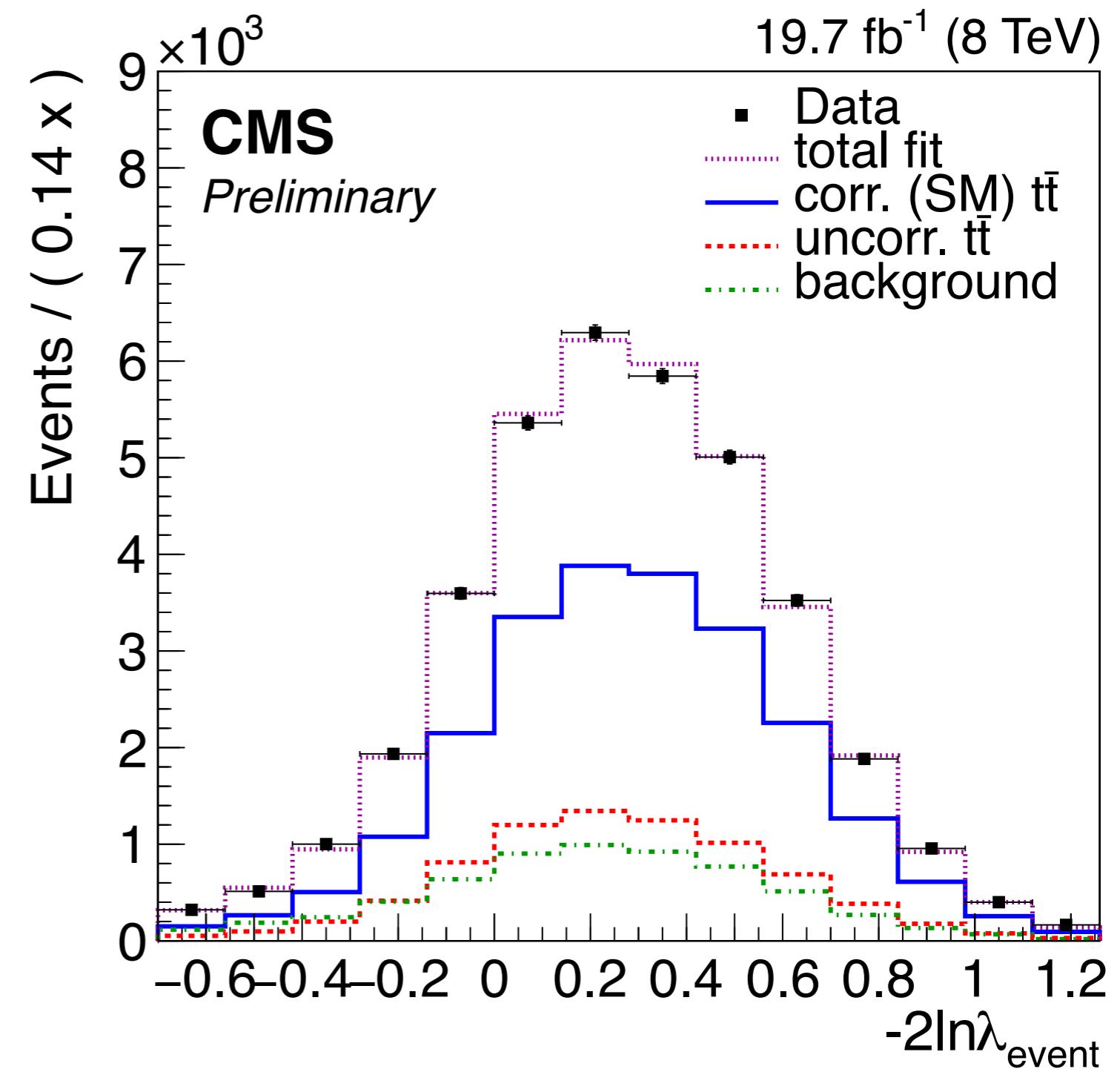
- ▶ Create templates using simulated correlated and uncorrelated t \bar{t}



[CMS-PAS-TOP-13-015](#)

- ▶ Fit $-2 \ln \lambda_{event}$ distribution using **correlated** and **uncorrelated** templates
- ▶ Q^2 and JES dominant systematics

$$\lambda_{event} = \frac{P_{uncor}}{P_{cor}}$$



$$f_{SM} = 0.72 \pm 0.09 \text{ (stat)} ^{+0.15}_{-0.13} \text{ (syst)}$$

Spin correlations summary

- ▶ Summary of most precise f_{SM} measurements

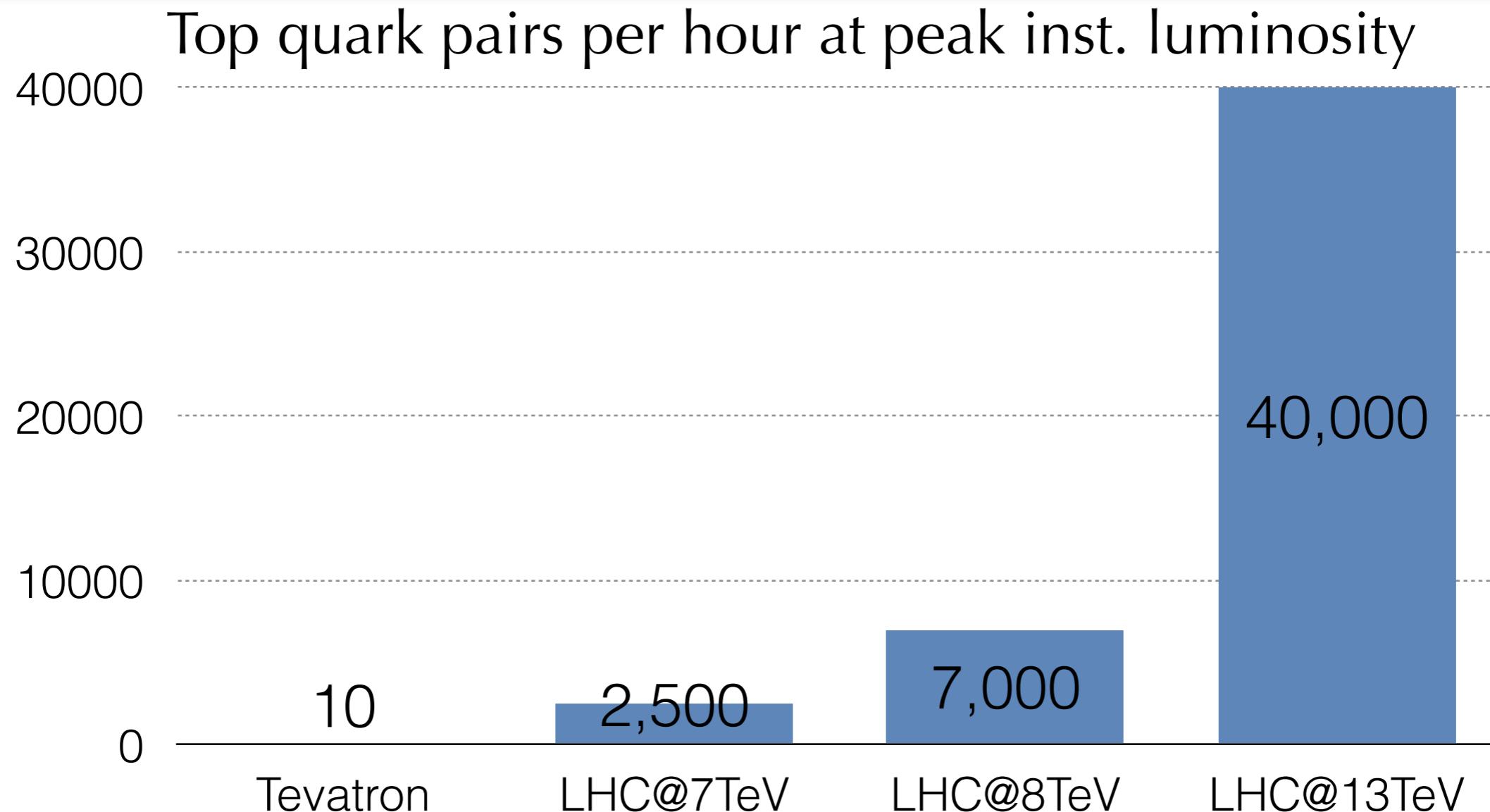
Variable	Channel	Collaboration	f_{SM}
$\Delta\phi$	dilepton	ATLAS (8 TeV)	1.20 ± 0.14
ME-based (S-ratio)	dilepton	ATLAS (7 TeV)	$0.87 \pm 0.18^*$
$\Delta\phi$	lepton+jets	ATLAS (7 TeV)	1.12 ± 0.25
$\Delta\phi$	dilepton	CMS (8 TeV)	1.16 ± 0.15
D	dilepton	CMS (8 TeV)	0.90 ± 0.16
ME-based	lepton+jets	CMS (8 TeV)	0.72 ± 0.17

* ATLAS 7 TeV dilepton $\Delta\phi$ measurement has lower relative uncertainty ($f_{SM}=1.19\pm0.20$), improved on by 8 TeV result (above)

- ▶ All consistent with $f_{SM} = 1$
- ▶ $f_{SM} = 0$ strongly disfavoured
- ▶ Proof top really behaves like a bare quark!

Summary and Outlook

- ▶ Top quark spin variables are an excellent test of the SM and probe for NP
- ▶ So far the results are very consistent with SM expectations
- ▶ Inclusive measurements systematics limited
 - ▶ both experimental and theory systematics
- ▶ Differential results mostly still statistics limited

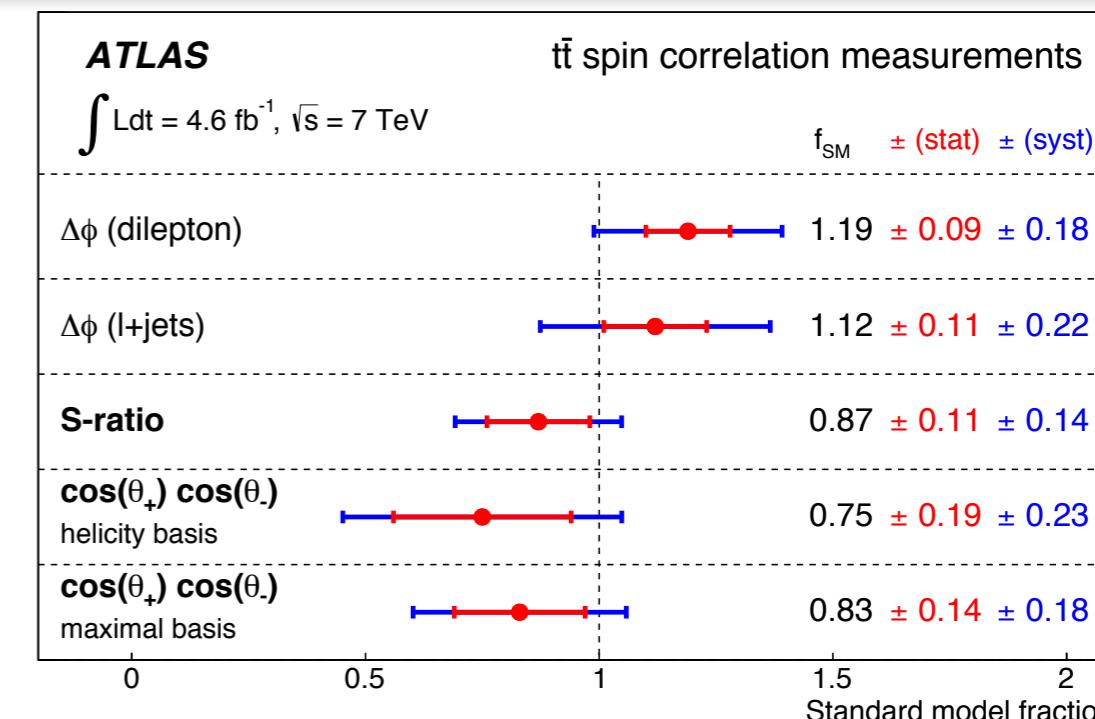
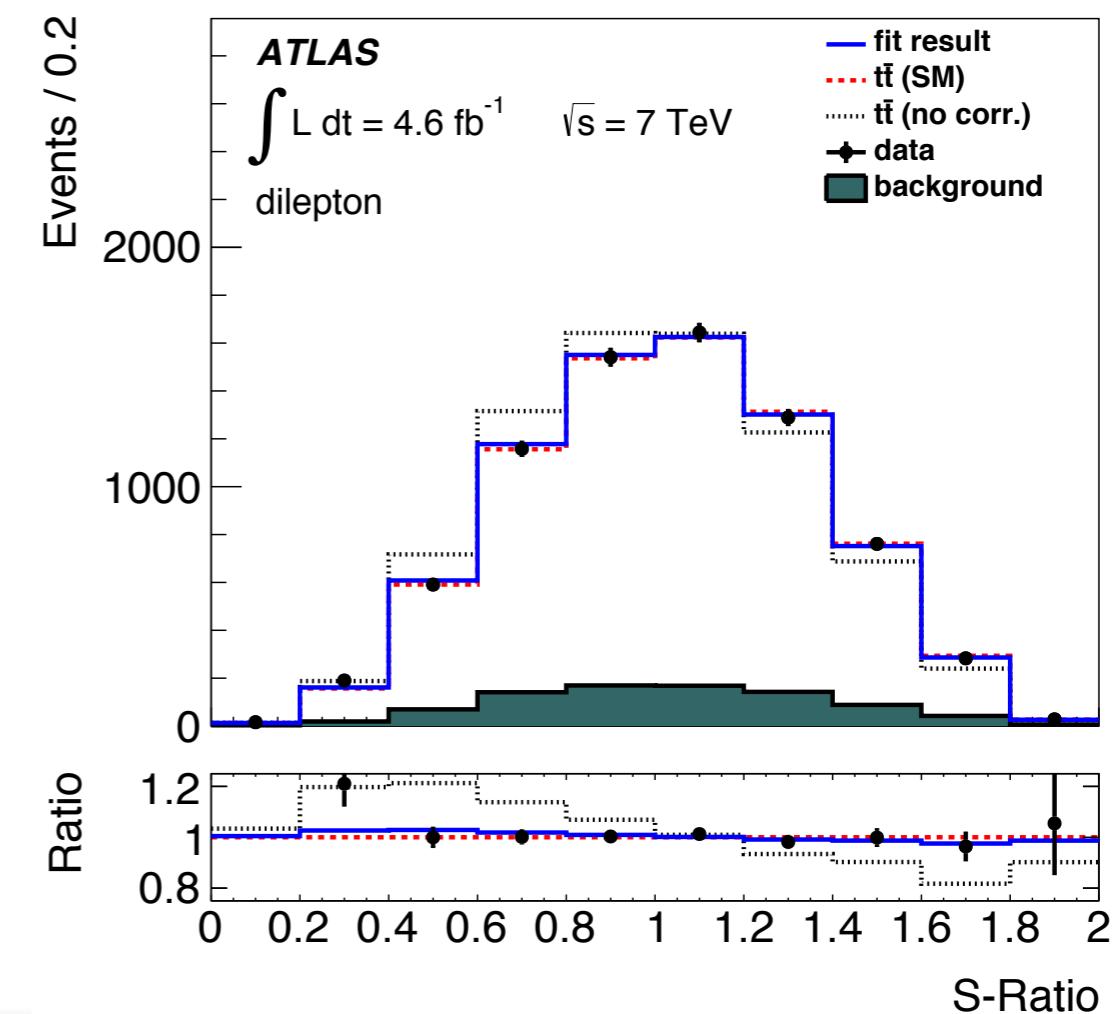
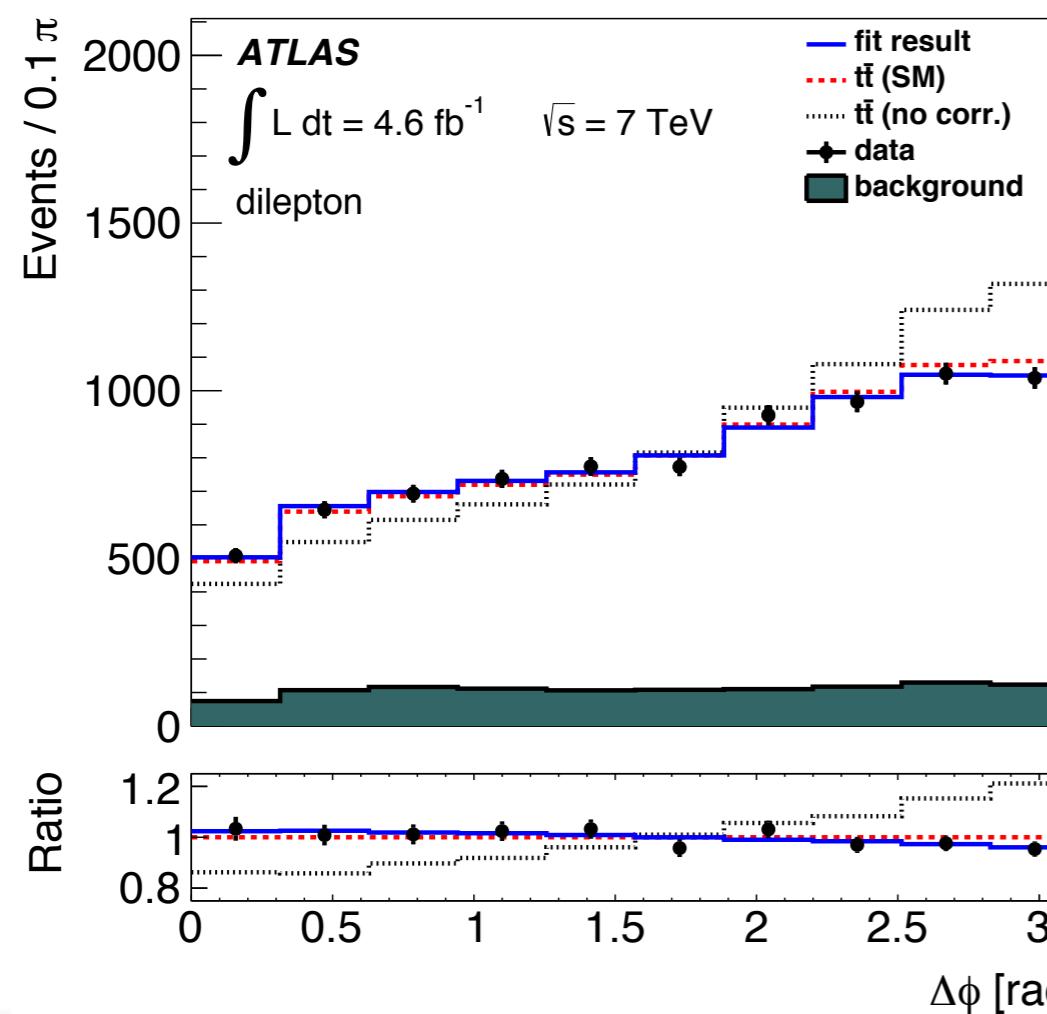


cross sections from [arXiv:1303.6254](https://arxiv.org/abs/1303.6254): Tevatron $\sim 7\text{pb}$, LHC@7TeV $\sim 172\text{pb}$, LHC@8TeV $\sim 246\text{pb}$, LHC@13TeV $\sim 806\text{pb}$
peak inst. luminosity: Tevatron: $\sim 4 \times 10^{32}\text{cm}^{-2}\text{s}^{-1}$, LHC@7TeV: $\sim 4 \times 10^{33}\text{cm}^{-2}\text{s}^{-1}$, LHC@8TeV: $\sim 8 \times 10^{33}\text{cm}^{-2}\text{s}^{-1}$, LHC@13TeV: $\sim 1.3 \times 10^{34}\text{cm}^{-2}\text{s}^{-1}$

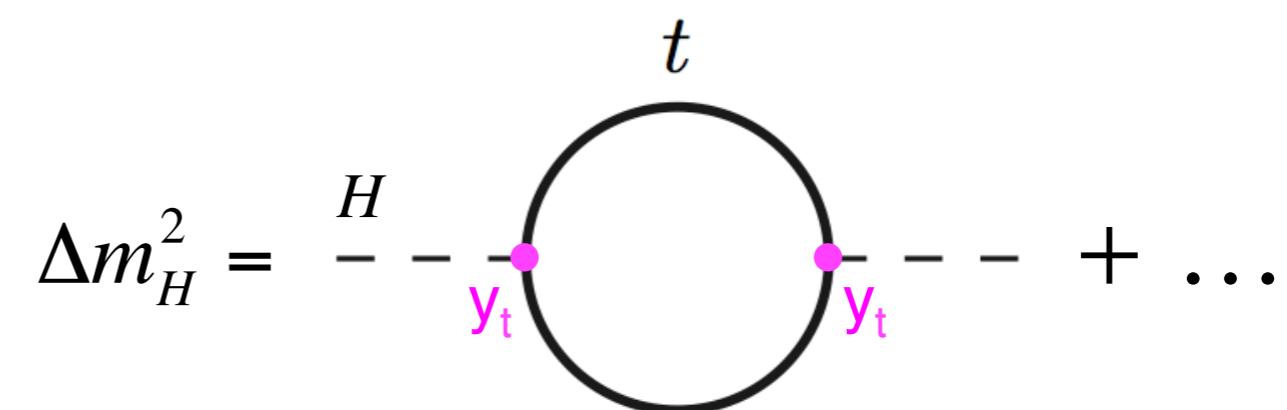
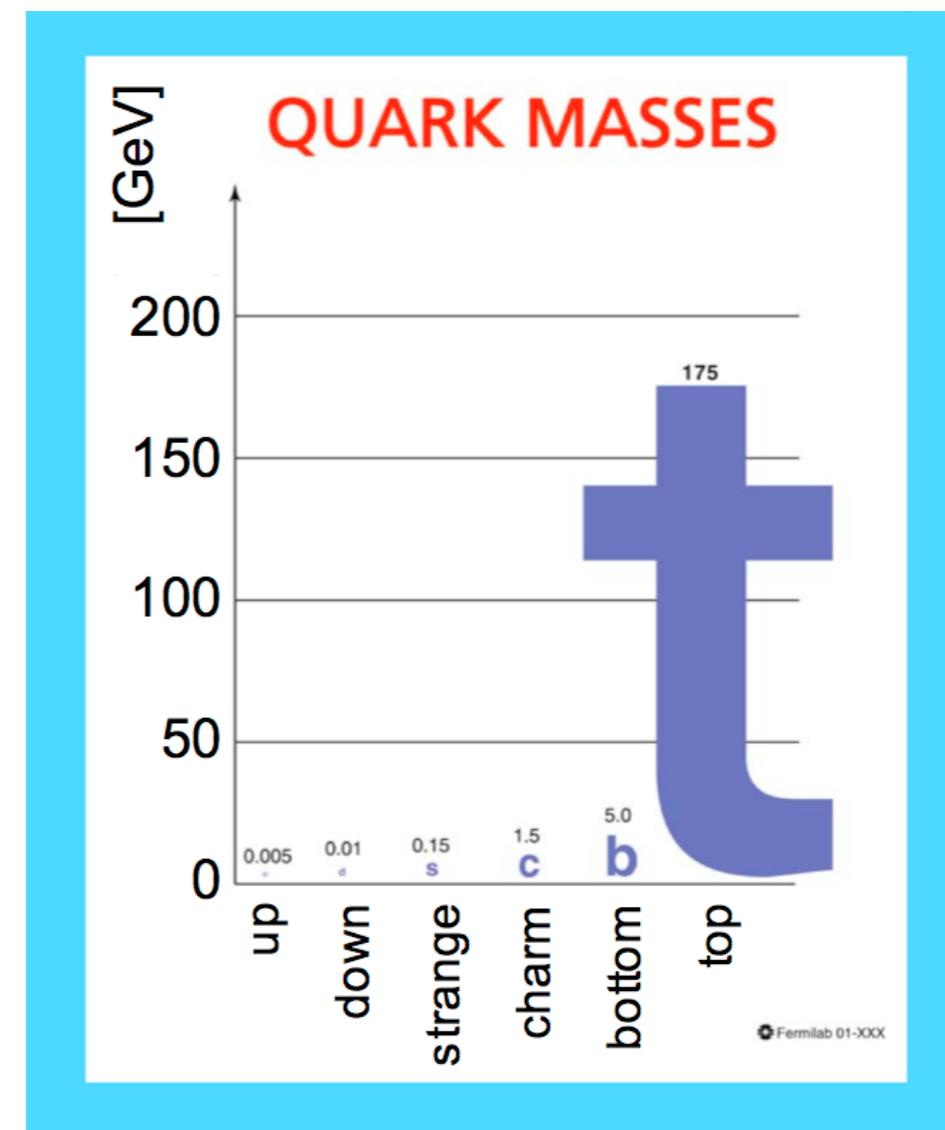
- ▶ In Run 2 we have another order of magnitude increase for $t\bar{t}$ pair production
- ▶ Improvements in systematic and theoretical uncertainties essential to keep pace
- ▶ Could new physics show up first in top spin variables in Run 2?

[Phys. Rev. D. 90, 112016 \(2014\)](#)

- ▶ ATLAS 7 TeV analysis measured large suite of variables in 1ℓ and 2ℓ channels
- ▶ template fit using simulated correlated and uncorrelated $t\bar{t}$
- ▶ dilepton $\Delta\phi$ and S-ratio most precise

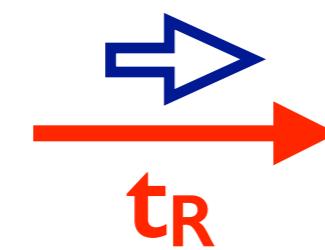


- ▶ Why are **top properties** interesting?
- ▶ top quark **decays before it can form bound states**
- ▶ unique opportunity to study a “bare” quark (using the decay products)
- ▶ **heaviest elementary particle known**
($m_t \sim 173$ GeV)
- ▶ large coupling to Higgs boson suggests special role in EWSB
- ▶ top properties measurements test SM and **probe new physics**

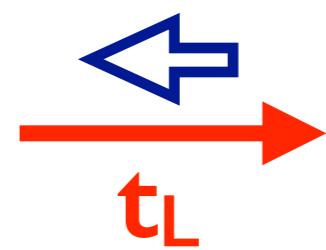


- ▶ The measurements rely on an understanding of the helicities of the top quarks we produce
- ▶ reminder: helicity is the particle's spin component along its momentum direction
- ▶ I'll denote particle momenta and spin directions with solid and open arrows:

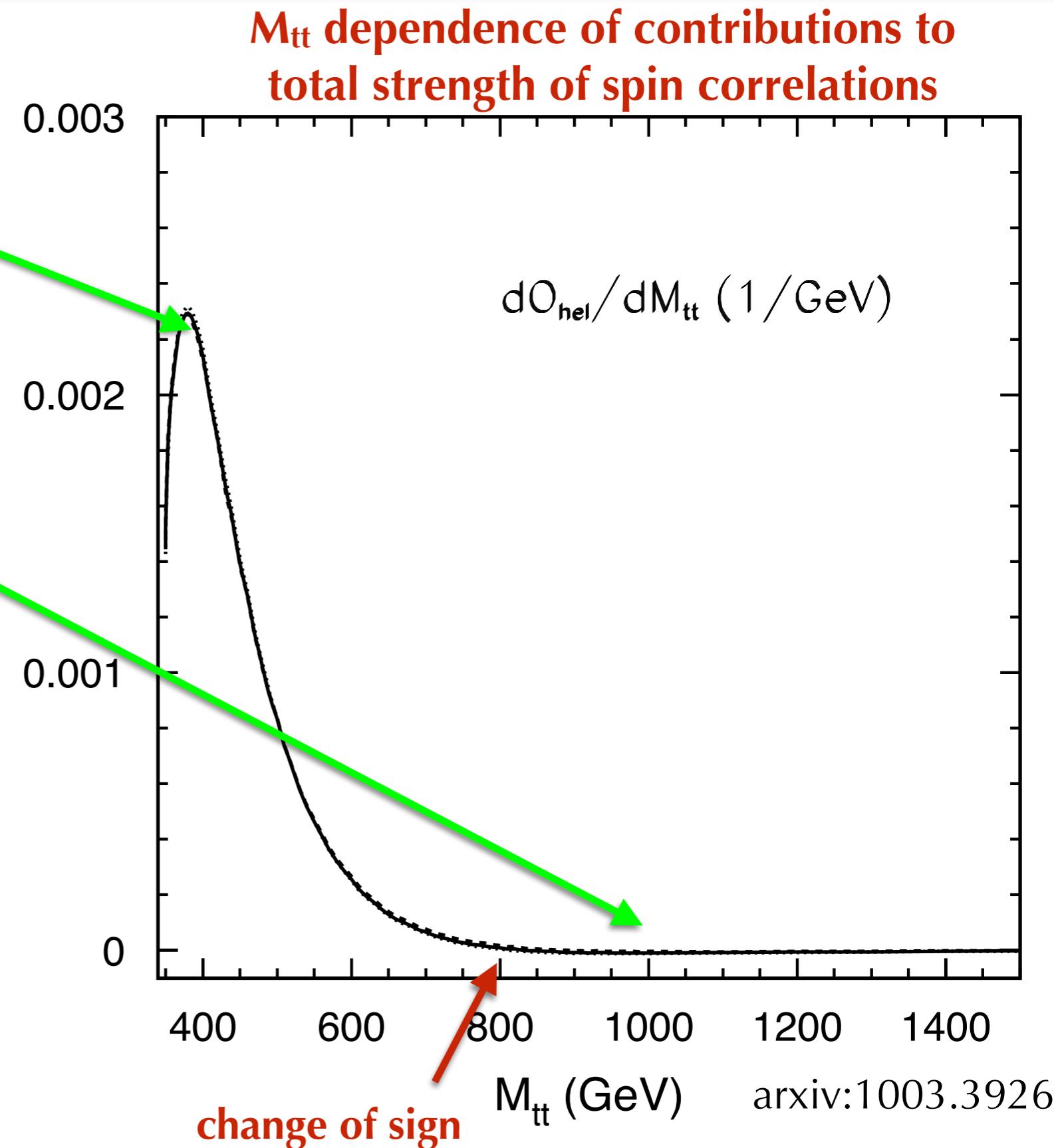
Right-handed top quark



Left-handed top quark

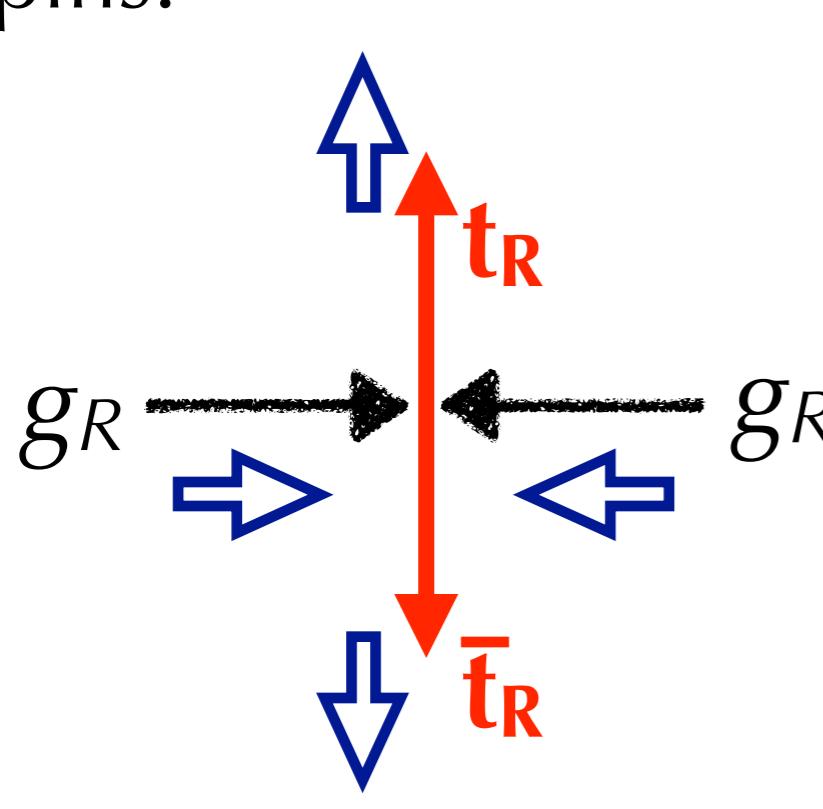


- ▶ Same helicity contribution is dominant near threshold
- ▶ Opposite helicity becomes dominant when $E_t \gg m_t$
- ▶ helicity conservation
- ▶ Net spin correlation strength of ~30% (LHC)

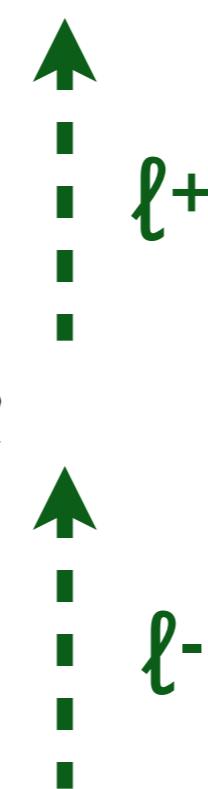


- ▶ Initial state and invariant mass dependence of spin correlations makes them a **rich process to test our understanding of perturbative QCD**
- ▶ future very high precision measurements sensitive to proton quark and gluon content

- ▶ Direct measurement of spin correlations requires **full reconstruction of t and \bar{t}**
- ▶ Can we try something more simple?
- ▶ Choose dilepton final state (charged leptons best spin analysers)
- ▶ Preferred lepton directions in the top rest frames given by top spins:

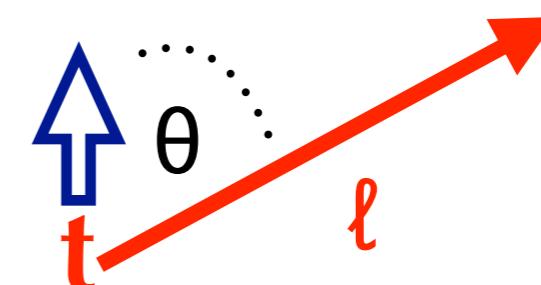


Same helicity gluons
Positive spin correlations

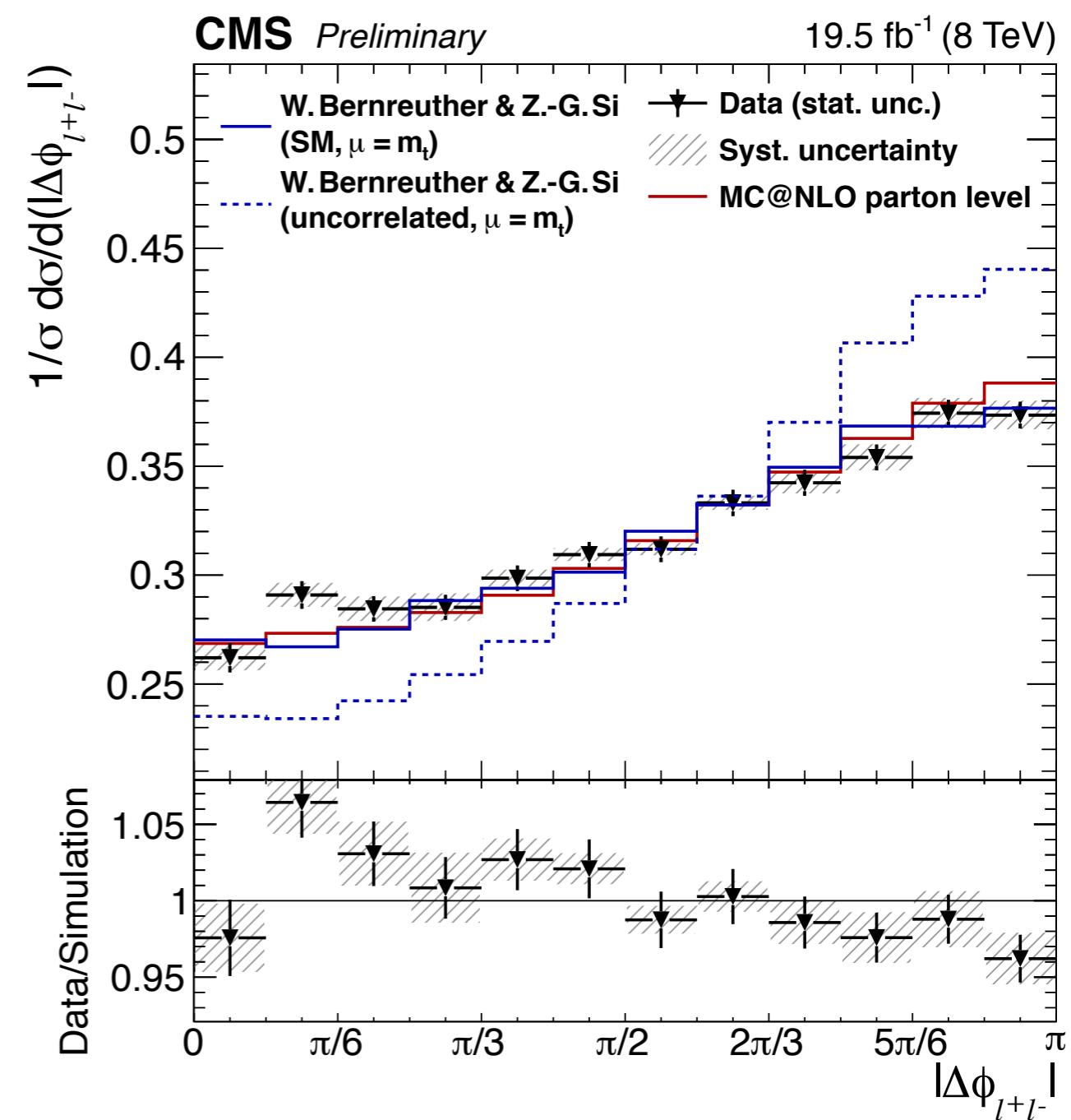


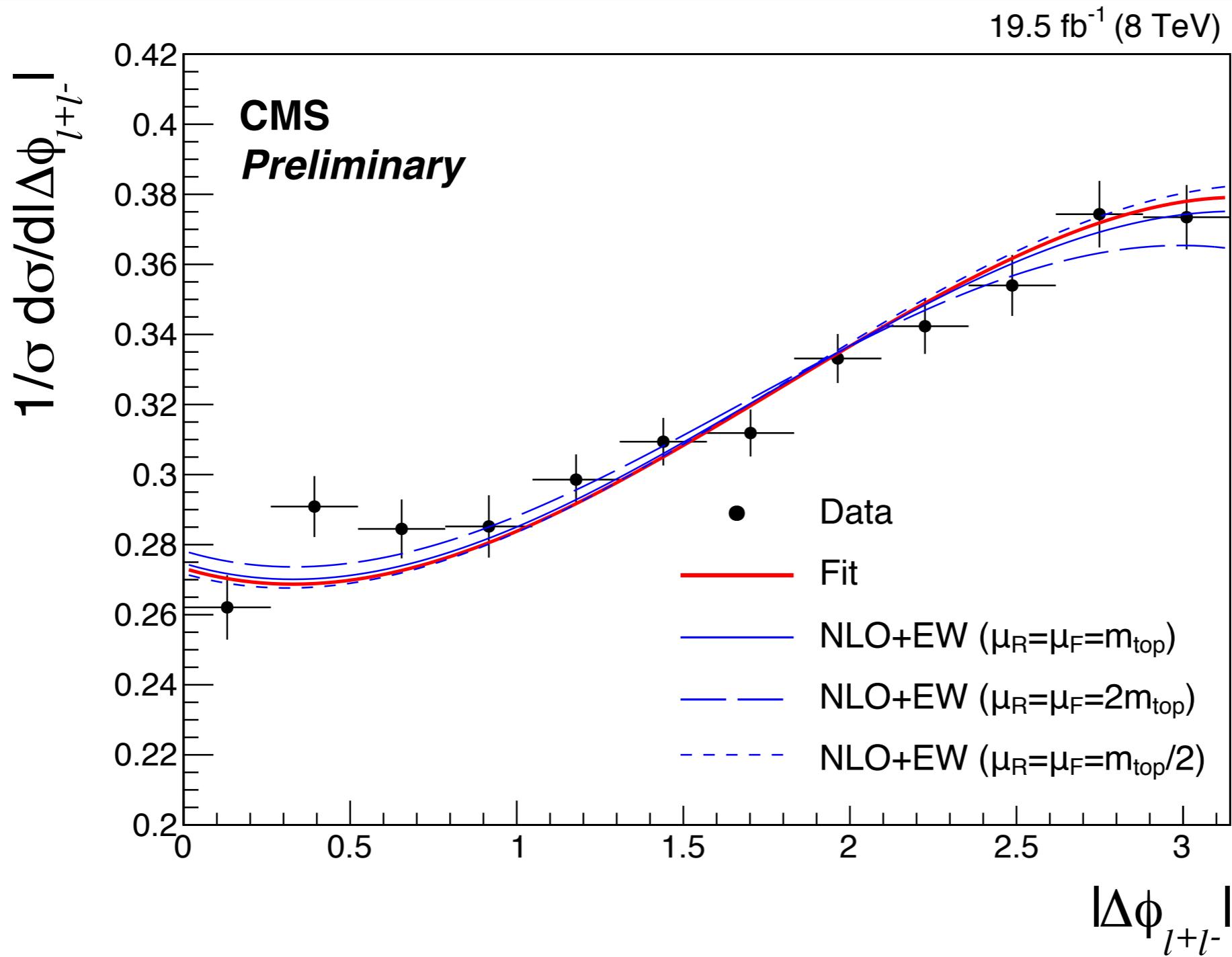
ℓ^\pm angular distributions:
$$(1 \pm \cos \theta)/2$$

(parity violating weak decay)



- ▶ Can reinterpret measured $\Delta\phi$ distribution in terms of new physics that affects spin correlations
- ▶ In general, new physics in $t\bar{t}$ production **due to heavy particle exchange** manifests as a **colour dipole coupling of top to gluons**
 - ▶ **modifies the expected spin correlations**
- ▶ Supersymmetry
 - ▶ top quarks and antiquarks produced from **decay of scalar (spin0) particles** have **no way of being correlated**





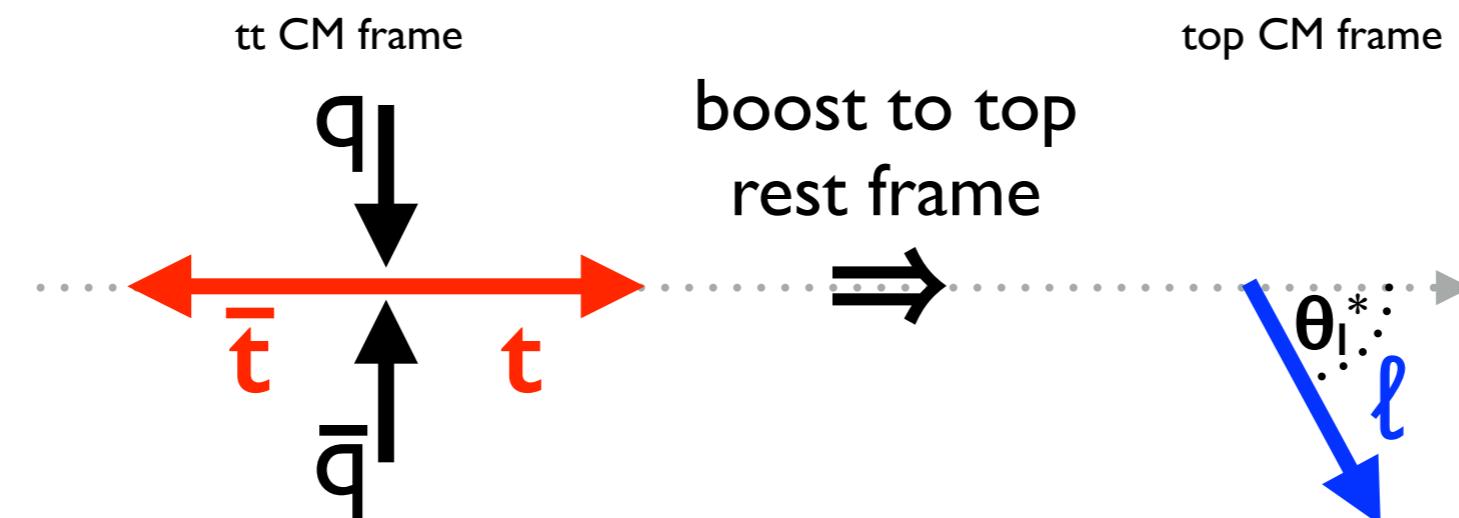
- ▶ A value of $\text{Re}(\hat{\mu}_t)$ outside the range $-0.050 < \text{Re}(\hat{\mu}_t) < 0.076$ is excluded at 95% CL $\left(\tilde{\mu}_t = \frac{g_s}{m_t} \hat{\mu}_t \right)$
- ▶ competitive with existing limits
- ▶ uncertainty dominated by scale variations in the theoretical predictions

- ▶ Spin correlation quantified by relative numbers of same and opposite helicity $t\bar{t}$ pairs:

$$C \equiv \frac{\sigma(t_R\bar{t}_R + t_L\bar{t}_L) - \sigma(t_R\bar{t}_L + t_L\bar{t}_R)}{\sigma(t_R\bar{t}_R + t_L\bar{t}_L) + \sigma(t_R\bar{t}_L + t_L\bar{t}_R)}$$

“spin correlation coefficient”

- ▶ Lepton direction favours top spin direction, with distribution $(1 \pm \cos \theta_\ell^*)/2$
- ▶ the measured $\cos \theta_\ell^*$ is a proxy for the top helicity (diluted by a factor of 2)



- ▶ Measure $\cos \theta_\ell^*$ for **both tops** in each event, and take the product (“ $c_1 c_2$ ”)
- ▶
$$A_{c_1 c_2} = \frac{N(c_1 \cdot c_2 > 0) - N(c_1 \cdot c_2 < 0)}{N(c_1 \cdot c_2 > 0) + N(c_1 \cdot c_2 < 0)} = -C/4$$
- ▶ factor 1/4 because our helicity measurement is diluted by a factor of 2 for each top