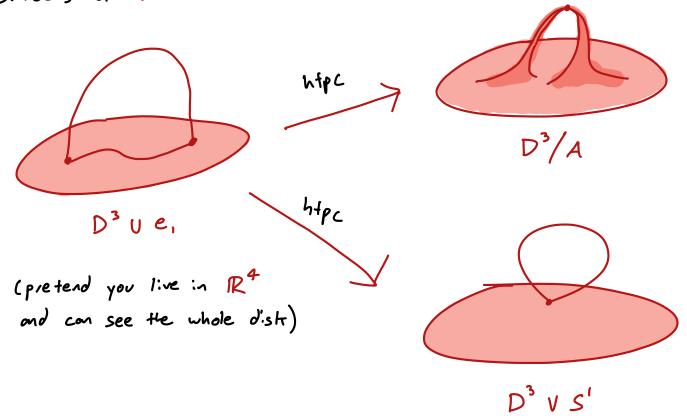
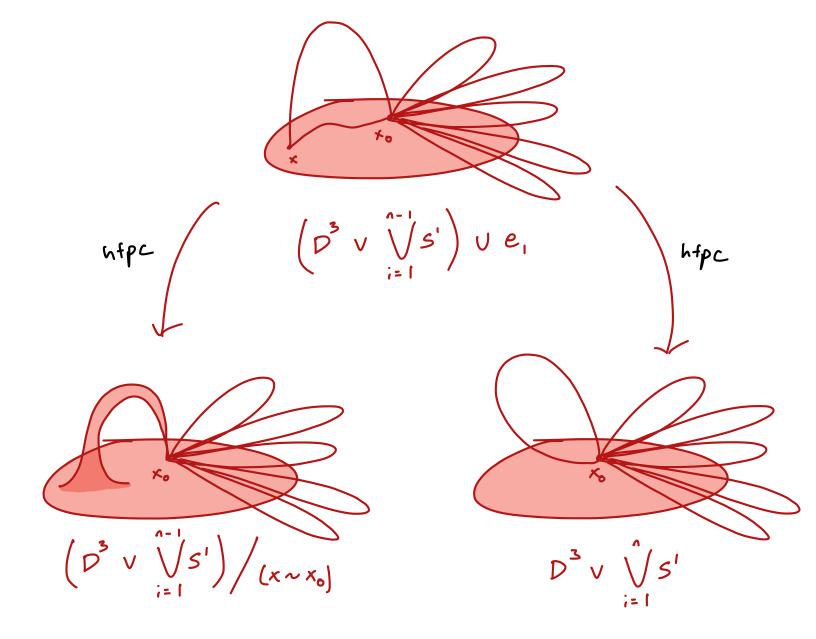
First assume |A|=2. Consider the space made by attaching a 1-cell to the points of A; it is homotopic to both  $D^3/A$  via contracting the added 1-cell, and it is also homotopic to  $D^3 \vee S^1$ , contracting along a path between the two members of A.



Thus  $\pi_i(D^3/A) \cong \pi_i(D^3 \vee S') = \mathbb{Z}$ .

Inductively assume  $D^3/A$  is homotopic to  $D^3 \vee \bigvee_{i=1}^3 S^i$  for some N. Now add one  $X \in D^3$  to A. As before, consider the space obtained by attaching a 1-cell to X and the weake point  $X_0$ . Then we can confinct along this 1-cell or a path connecting X and  $X_0$  to get the desired homotopy equivalence:



Thus  $D^3/A$  is homotopic to  $D^3 \vee \bigvee_{i=1}^{|A|-1}$ , and therefore  $\prod_i (D^3/A)$  is isomorphic to the free group on |A|-1 generators (i.e., the (|A|-1) - fold free product of  $\mathbb{Z}$ ).