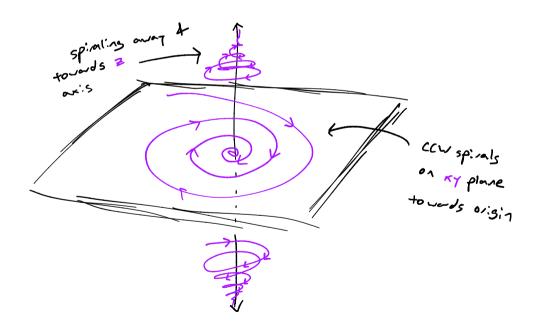
**Problem 1.1** (Exam 1, Fall 2019). Find the general solution for  $\dot{X} = AX$  where

$$A = \begin{bmatrix} -2 & 1 & 0 \\ -1 & -2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

Sketch the phase portrait and determine the stable and unstable subspaces.

We see upon inspection that A is in comonical form, If we conread off its eigenvalues:  $\lambda = -2 = i$ , 3. Thus our general solution is

$$X(t) = e^{-2t} \begin{bmatrix} \cos t \\ -\sin t \end{bmatrix} + e^{-2t} \begin{bmatrix} \sin t \\ \cos t \end{bmatrix} + e^{-2t} \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$



stable subspace: 0
unstable subspace: Z - axis