Suppose the poles of f have a limit point a. Because a is a pole, f is analytic in a punctured neighborhood about a. But because a is a limit point of poles, all of its neighborhoods contain poles, so f is not analytic in any of them &

