

8. (*Javier and Zhihua*) Apply three steps of Newton's method to $e^x + x^2 - 4 = 0$ with starting point $x = 1$.

Newton's method: $x_{k+1} = x_k - \frac{f(x_k)}{f'(x_k)}$

$$f(x) = e^x + x^2 - 4$$

$$f'(x) = e^x + 2x$$

$$x_0 = 1 - \frac{e - 3}{e + 2} = \frac{e + 2 - e + 3}{e + 2} = \frac{5}{e + 2}$$

$$x_1 = \frac{5}{e + 2} - \frac{e^{\left(\frac{5}{e+2}\right)} + \frac{25}{(e+2)^2} - 4}{e^{\left(\frac{5}{e+2}\right)} + \frac{10}{e+2}}$$

$$x_2 = x_1 - \frac{e^{x_1} + x_1^2 - 4}{e^{x_1} + 2x_1} \quad (\text{not writing all that})$$