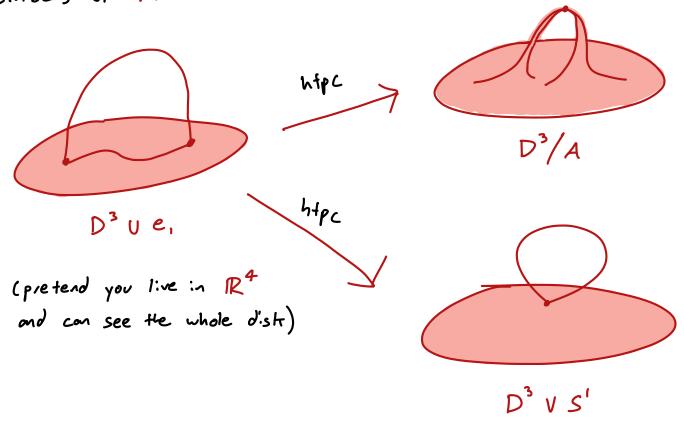
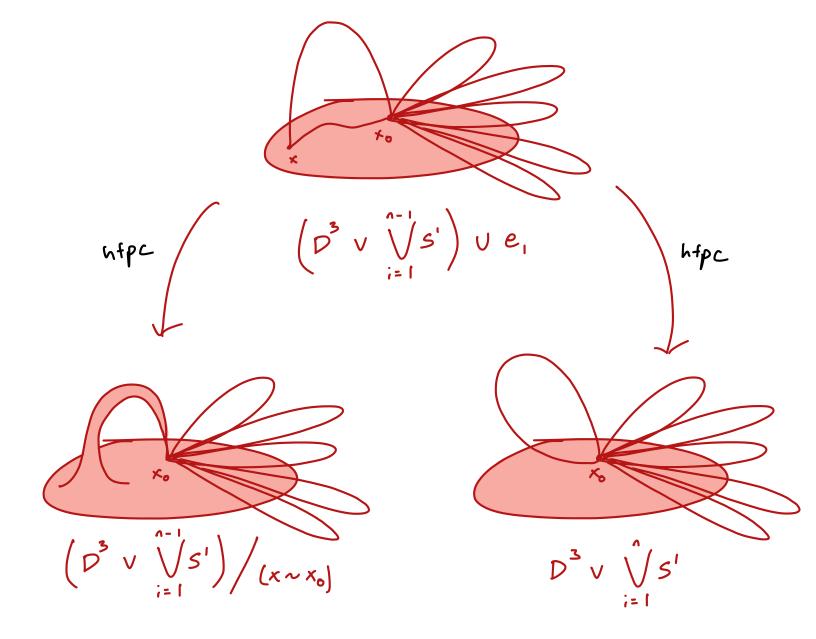
First assume |A|=2. Consider the space made by attaching a 1-cell to the points of A; it is homotopic to both D^3/A via contracting the added 1-cell, and it is also homotopic to $D^3 \vee S^1$, contracting along a path between the two members of A.



Thus $\pi_i(D^3/A) \cong \pi_i(D^3 \vee S') = \mathbb{Z}$.

Inductively assume D^3/A is homotopic to $D^3 \vee \bigvee_{i=1}^3 S^i$ for some N. Now add one $X \in D^3$ to A. As before, consider the space obtained by attaching a 1-cell to X and the weake point X_0 . Then we can confinct along this 1-cell or a path connecting X and X_0 to get the desired homotopy equivalence:



Thus D^3/A is homotopic to $D^3 \vee \bigvee_{i=1}^{|A|-1}$, and therefore $\prod_i (D^3/A)$ is isomorphic to the free group on |A|-1 generators (i.e., the (|A|-1) - fold free product of \mathbb{Z}).