19. (Fall 14 MT 1 - Chifan) Let $E = [0,1] \setminus \mathbb{Q}$. Find m(E).

Let
$$F = [0,1] \cap \mathbb{Q}$$
. Then $E \cap F = \emptyset$ and $E \cup F = [0,1]$, so:
$$m([0,1]) = 1$$

$$= m(E) + m(F)$$

$$= m(E) + 0 \text{ (as } F \text{ is countable)}$$

$$\Rightarrow m(E) = 1$$