```
In [1]: from __future__ import absolute_import
    from __future__ import division
    from __future__ import print_function

import numpy as np
    import scipy.signal as sg
    from utils import *
```

```
In [2]: # superclass of modules
        class Module:
            Module is a super class. It could be a single layer, or a multilayer perce
        ptron.
             def __init__(self):
                 self.train = True
                 return
             def forward(self, _input):
                 h = f(z); z is the input, and h is the output.
                 Inputs:
                _input: z
                 Returns:
                 output h
                 n n n
                 pass
             def backward(self, _input, _gradOutput):
                 Compute:
                 gradient w.r.t. _input
                 gradient w.r.t. trainable parameters
                 Inputs:
                _input: z
                 _gradOutput: dL/dh
                 Returns:
                 gradInput: dL/dz
                 pass
             def parameters(self):
                 Return the value of trainable parameters and its corresponding gradien
        t (Used for grandient descent)
                 Returns:
                 params, gradParams
```

```
def training(self):
    """
    Turn the module into training mode.(Only useful for Dropout layer)
    Ignore it if you are not using Dropout.
    """
    self.train = True

def evaluate(self):
    """
    Turn the module into evaluate mode.(Only useful for Dropout layer)
    Ignore it if you are not using Dropout.
    """
    self.train = False
```

```
In [3]:
        class Sequential(Module):
            Sequential provides a way to plug layers together in a feed-forward manne
        r.
            def __init__(self):
                Module.__init__(self)
                self.layers = [] # layers contain all the layers in order
            def add(self, layer):
                 self.layers.append(layer) # Add another Layer at the end
            def size(self):
                return len(self.layers) # How many layers.
            def forward(self, _input):
                Feed forward through all the layers, and return the output of the last
         Layer
                 .....
                # self._inputs saves the input of each layer
                # self._inputs[i] is the input of i-th layer
                self._inputs = [_input]
                for i in range(self.size()):
                     self._inputs.append(self.layers[i].forward(self._inputs[i]))
                # The last element of self._inputs is the output of last layer
                self._output = self._inputs[-1]
                return self. output
            def backward(self, _input, _gradOutput):
                Backpropogate through all the layers using chain rule.
                # self._gradInputs[i] is the gradient of loss w.r.t. the input of i-th
         Layer
                self._gradInputs = [None] * (self.size() + 1)
                 self._gradInputs[self.size()] = _gradOutput
```

```
for i in range(self.size(), 0, -1):
            self._gradInputs[i-1] = self.layers[i-1].backward(self._inputs[i-
1], self._gradInputs[i])
        self._gradInput = self._gradInputs[0]
        return self._gradInput
    def parameters(self):
        Return trainable parameters and its corresponding gradient in a nested
 list
        .....
        params = []
        gradParams = []
        for m in self.layers:
            _p, _g = m.parameters()
            if _p is not None:
                params.append(_p)
                gradParams.append(_g)
        return params, gradParams
    def training(self):
        Turn all the layers into training mode
        Module.training(self)
        for m in self.layers:
            m.training()
    def evaluate(self):
        Turn all the layers into evaluate mode
        Module.evaluate(self)
        for m in self.layers:
            m.evaluate()
```

```
In [4]: class Convolutional(Module):
    """
    Convolutional Layer
    """

def __init__(self, inputLength, inputDepth, filterLength, filterDepth):
        Module.__init__(self)
        # Initalization
        stdv = 1./np.sqrt(inputLength)

        self.weight = np.random.uniform(-stdv, stdv, (filterLength, inputDepth, filterDepth))
        self.gradWeight = np.ndarray((filterLength, inputDepth, filterDepth))
        self.bias = np.random.uniform(-stdv, stdv, filterDepth)
        self.gradBias = np.ndarray(filterDepth)

def forward(self, _input):
    """
        output = W * filterRegion + b convolution over input
        _input:
```

```
N x inputLength x inputDepth matrix
        inputDepth = self.weight.shape[1]
       filterDepth = self.weight.shape[2]
        _input = _input.reshape(_input.shape[0],-1,inputDepth)
       self._output = []
       for i in range(filterDepth):
            self._output.append(sg.correlate(_input, np.expand_dims(np.take(se
lf.weight,i,2),0), 'valid') + self.bias[i])
        self._output = np.array(self._output)
        self._output =
self._output.reshape(self._output.shape[1],self._output.shape[2],self._output.
hape[0])
        return self._output
   def backward(self, _input, _gradOutput):
        _input:
       N x inputLength x inputDepth matrix
       _gradOutputSize:
       N x outputLength x outputDepth matrix
       filterLength = self.weight.shape[0]
       inputDepth = self.weight.shape[1]
       filterDepth = self.weight.shape[2]
       _input = _input.reshape(_input.shape[0],-1,inputDepth)
       _gradOutput = _gradOutput.reshape(_gradOutput.shape[0],-1,filterDepth)
       for i in range(filterDepth):
            self.gradWeight[:,:,i] = sg.correlate( input, np.expand dims(np.ta
ke(_gradOutput,i,2),2), 'valid')
       self.gradBias = np.sum( gradOutput, axis=(0,1))
        self._gradInput = []
        for i in range(inputDepth):
            self._gradInput.append(sg.correlate(np.pad(_gradOutput, ((0,0),(fi
lterLength-1,filterLength-1),(0,0)), 'constant'),
np.expand_dims(np.take(self.weight,i,1),0), 'valid'))
        self._gradInput = np.array(self._gradInput)
        self._gradInput = self._gradInput.reshape(self._gradInput.shape[1],sel
f._gradInput.shape[2],self._gradInput.shape[0])
        return self._gradInput
   def parameters(self):
        Return weight and bias and their g
        return [self.weight, self.bias], [self.gradWeight, self.gradBias]
```

```
In [5]:
        class FullyConnected(Module):
            Fully connected layer
            def __init__(self, inputSize, outputSize):
                Module. init (self)
                # Initalization
                stdv = 1./np.sqrt(inputSize)
                self.weight = np.random.uniform(-stdv, stdv, (inputSize, outputSize))
                self.gradWeight = np.ndarray((inputSize, outputSize))
                self.bias = np.random.uniform(-stdv, stdv, outputSize)
                self.gradBias = np.ndarray(outputSize)
            def forward(self, _input):
                output = W * input + b
                _input:
                N x inputSize matrix
                _input = _input.reshape(_input.shape[0],-1)
                self._output = np.dot(_input, self.weight) + self.bias
                return self._output
            def backward(self, _input, _gradOutput):
                 11 11 11
                input:
                N x inputSize matrix
                _gradOutputSize:
                N x outputSize matrix
                _input = _input.reshape(_input.shape[0],-1)
                _gradOutput = _gradOutput.reshape(_gradOutput.shape[0],-1)
                self.gradWeight = np.dot(_input.T, _gradOutput)
                self.gradBias = np.sum(_gradOutput, axis=0)
                self._gradInput = np.dot(_gradOutput, self.weight.T)
                return self._gradInput
            def parameters(self):
                Return weight and bias and their a
                return [self.weight, self.bias], [self.gradWeight, self.gradBias]
```

```
In [6]: class ReLU(Module):
            ReLU activation, not trainable.
            def __init__(self):
                Module.__init__(self)
                return
            def forward(self, _input):
                output = max(0, input)
                _input:
                N x d matrix
                _input = _input.reshape(_input.shape[0],-1)
                self._output = np.maximum(0, _input)
                return self._output
            def backward(self, _input, _gradOutput):
                gradInput = gradOutput * mask
                mask = _input > 0
                _input:
                N x d matrix
                _gradOutput:
                N x d matrix
                _input = _input.reshape(_input.shape[0],-1)
                _gradOutput = _gradOutput.reshape(_gradOutput.shape[0],-1)
                self._gradInput = _gradOutput * (_input > 0)
                return self._gradInput
            def parameters(self):
                No trainable parametersm, return None
                return None, None
```

```
In [7]: class SoftMaxLoss(object):
            def __init__(self):
                return
            def forward(self, _input, _label):
                Softmax and cross entropy loss layer. Should return a scalar, since i
        t's a
                loss. (It's almost identical to what in hw2)
                _input: N x C
                _labels: N x C, one-hot
                Returns: loss (scalar)
                self._output = -np.sum(_label * (_input -
        np.log(np.sum(np.exp(_input), axis=1)).reshape(1, -1).T))
                return self._output
            def backward(self, input, label):
                self._gradInput = np.exp(_input)/np.sum(np.exp(_input), axis=1).reshap
        e(1, -1).T - _label
                return self._gradInput
In [8]: # Test softmaxloss, the relative error should be small enough
        def test_sm():
```

```
In [8]: # Test softmaxloss, the relative error should be small enough
def test_sm():
    crit = SoftMaxLoss()
    gt = np.zeros((3, 10))
    gt[np.arange(3), np.array([1,2,3])] = 1
    x = np.random.random((3,10))
    def test_f(x):
        return crit.forward(x, gt)

    crit.forward(x, gt)

    gradInput = crit.backward(x, gt)
    gradInput_num = numeric_gradient(test_f, x, 1, 1e-6)
    #print(gradInput)
    #print(gradInput_num)
    print(relative_error(gradInput, gradInput_num, 1e-8))

test_sm()
```

3.57660649424e-09

```
In [9]: # Test modules, all the relative errors should be small enough
        def test_module(model):
            model.evaluate()
            crit = TestCriterion()
            gt = np.random.random((3,10))
            x = np.random.random((3,10))
            def test_f(x):
                return crit.forward(model.forward(x), gt)
            gradInput = model.backward(x, crit.backward(model.forward(x), gt))
            gradInput_num = numeric_gradient(test_f, x, 1, 1e-6)
            print(relative_error(gradInput, gradInput_num, 1e-8))
        # Test fully connected
        model = FullyConnected(10, 10)
        test_module(model)
        # Test ReLU
        model = ReLU()
        test_module(model)
        # Test Sequential
        model = Sequential()
        model.add(FullyConnected(10, 10))
        model.add(ReLU())
        #model.add(Dropout())
        test_module(model)
```

- 4.69130962908e-09
- 2.63177896212e-10
- 2.80176673959e-09

```
In [10]: # Test gradient descent, the loss should be lower and lower
         trainX = np.random.random((10,25,15))
         model = Sequential()
         model.add(Convolutional(25,15, 6,20))
         model.add(ReLU())
         model.add(Convolutional(20,20, 11,5))
         model.add(ReLU())
         model.add(FullyConnected(50,1))
         crit = TestCriterion()
         it = 0
         state = None
         while True:
             output = model.forward(trainX)
             loss = crit.forward(output, None)
             if it % 100 == 0:
                 print(loss)
             doutput = crit.backward(output, None)
             model.backward(trainX, doutput)
             params, gradParams = model.parameters()
             sgdmom(params, gradParams, 0.0005, 0.8)
             if it > 1000:
                 break
             it += 1
```

```
0.215067533975
```

- 0.0528884357754
- 0.0257170527197
- 0.0148435453009
- 0.0121883698976
- 0.0132590955333
- 0.0125801147979
- 0.0113063602312
- 0.00979347545853
- 0.00773234396134
- 0.00824114821094

Now we start to work on real data.

```
In [11]: import MNIST_utils
    data_fn = "CLEAN_MNIST_SUBSETS.h5"

# We only consider large set this time
    print("Load large trainset.")
    Xlarge,Ylarge = MNIST_utils.load_data(data_fn, "large_train")
    print(Xlarge.shape)
    print(Ylarge.shape)

    print("Load valset.")
    Xval,Yval = MNIST_utils.load_data(data_fn, "val")
    print(Xval.shape)
    print(Yval.shape)

Load large trainset.
```

```
Load large trainset.
(7000L, 576L)
(7000L, 10L)
Load valset.
(2000L, 576L)
(2000L, 10L)
```

```
In [12]: def predict(X, model):
             Evaluate the soft predictions of the model.
             X : N x d array (no unit terms)
             model : a multi-layer perceptron
             Output:
             yhat : N x C array
                 yhat[n][:] contains the score over C classes for X[n][:]
             return model.forward(X)
         def error_rate(X, Y, model):
             Compute error rate (between 0 and 1) for the model
             model.evaluate()
             res = 1 - (model.forward(X).argmax(-1) == Y.argmax(-1)).mean()
             model.training()
             return res
         from copy import deepcopy
         def runTrainVal(X,Y,model,Xval,Yval,trainopt):
             Run the train + evaluation on a given train/val partition
             trainopt: various (hyper)parameters of the training procedure
             During training, choose the model with the lowest validation error. (early
          stopping)
             eta = trainopt['eta']
             N = X.shape[0] # number of data points in X
```

```
# Save the model with lowest validation error
   minValError = np.inf
   saved_model = None
   shuffled idx = np.random.permutation(N)
   start idx = 0
   for iteration in range(trainopt['maxiter']):
        if iteration % int(trainopt['eta_frac'] * trainopt['maxiter']) == 0:
            eta *= trainopt['etadrop']
       # form the next mini-batch
        stop idx = min(start_idx + trainopt['batch_size'], N)
        batch_idx = range(N)[int(start_idx):int(stop_idx)]
       bX = X[shuffled idx[batch idx],:]
       bY = Y[shuffled_idx[batch_idx],:]
        score = model.forward(bX)
       loss = crit.forward(score, bY)
       # print(loss)
       dscore = crit.backward(score, bY)
       model.backward(bX, dscore)
       # Update the data using
        params, gradParams = model.parameters()
        sgd(params, gradParams, eta, weight_decay = trainopt['lambda'])
        start_idx = stop_idx % N
        if (iteration % trainopt['display iter']) == 0:
            #compute train and val error; multiply by 100 for readability (mak
e it percentage points)
            trainError = 100 * error_rate(X, Y, model)
            valError = 100 * error_rate(Xval, Yval, model)
            print('{:8} batch loss: {:.3f} train error: {:.3f} val error: {:.3
f}'.format(iteration, loss, trainError, valError))
            if valError < minValError:</pre>
                saved model = deepcopy(model)
                minValError = valError
   return saved model, minValError, trainError
```

```
In [14]: # -- training options
         trainopt = {
             'eta': .001, # initial learning rate
             'maxiter': 2500, # max number of iterations (updates) of SGD
             'display_iter': 500,  # display batch loss every display_iter updates
             'batch_size': 100,
              'etadrop': .5, # when dropping eta, multiply it by this number (e.g., .5 m
         eans halve it)
              'eta_frac': .25 #
         }
         NFEATURES = Xlarge.shape[1]
         # we will maintain a record of models trained for different values of lambda
         # these will be indexed directly by lambda value itself
         trained_models = dict()
         # set the (initial?) set of lambda values to explore
         lambdas = np.array([0, 0.001, 0.01, 0.1])
         hidden sizes = np.array([10])
         for lambda_ in lambdas:
             for hidden_size_ in hidden_sizes:
                 trainopt['lambda'] = lambda_
                 model = build_model(NFEATURES, hidden_size_, 10, dropout = 0)
                 crit = SoftMaxLoss()
                 # -- model trained on large train set
                 trained_model,valErr,trainErr = runTrainVal(Xlarge, Ylarge, model, Xva
         1, Yval, trainopt)
                 trained_models[(lambda_, hidden_size_)] = {'model': trained_model, "va
         l_err": valErr, "train_err": trainErr }
                 print('train set model: -> lambda= %.4f, train error: %.2f, val error:
          %.2f' % (lambda , trainErr, valErr))
         best_trained_lambda = 0.
         best_trained_model = None
         best_trained_val_err = 100.
         for (lambda_, hidden_size_), results in trained_models.items():
             print('lambda= %.4f, hidden size: %5d, val error: %.2f' %(lambda , hidden
         size_, results['val_err']))
             if results['val_err'] < best_trained_val_err:</pre>
                 best_trained_val_err = results['val_err']
                 best_trained_model = results['model']
                 best_trained_lambda = lambda_
         print("Best train model val err:", best_trained_val_err)
         print("Best train model lambda:", best_trained_lambda)
```