

MATH 18/19: Overall analysis

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Read data

Read in the `data_math-1819.csv` file which contains the codes assigned to all items, and produce some summaries of this.

Summary of papers in the sample:

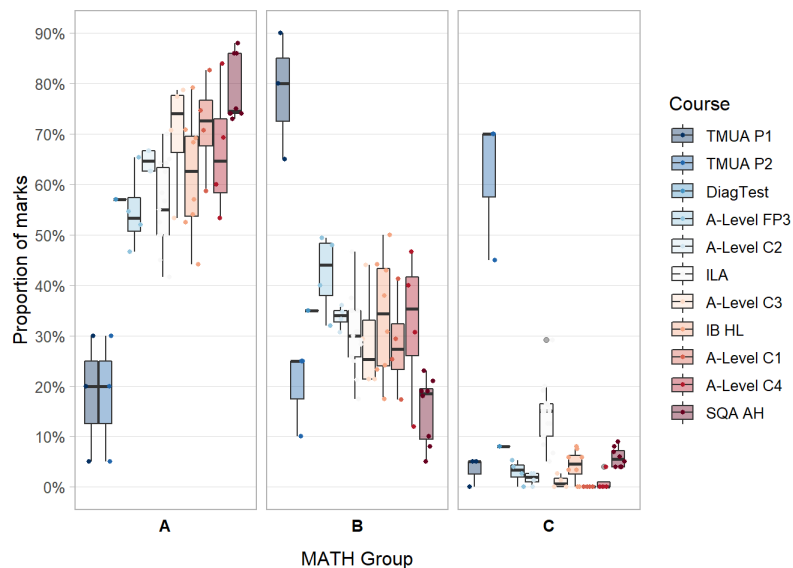
```
## `summarise()` ungrouping output (override with `.groups` argument)
```

```
## Joining, by = "Course"
```

Course	num_papers	papers	total_question	total_marks
A-Level C1	4	2014, 2015, 2016, 2017	93	300
A-Level C2	4	2014, 2015, 2016, 2017	95	300
A-Level C3	4	2014, 2015, 2016, 2017	95	300
A-Level C4	4	2014, 2015, 2016, 2017	88	300
A-Level FP3	4	2014, 2015, 2016, 2017	78	300
DiagTest	1	2018	24	100
IB HL	4	2014, 2015, 2016, 2017	232	920
ILA	8	2011, 2012, 2013, 2014, 2015, 2016, 2017, 2018	393	1760
SQA AH	8	2012, 2013, 2014, 2015, 2016, 2017, 2018, 2019	244	800
TMUA P1	3	2016, 2017, 2018	60	60
TMUA P2	3	2016, 2017, 2018	60	60
totalqs			totalmarks	
1462			5200	

Overall proportions

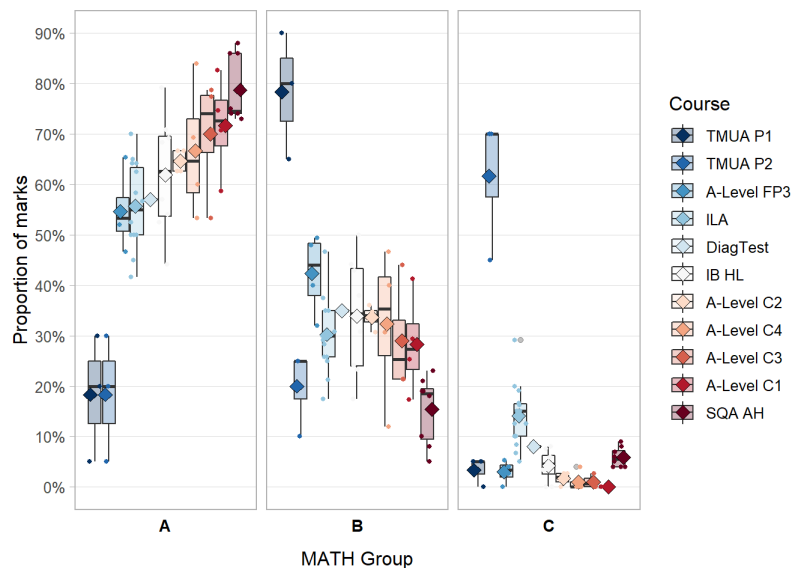
```
MATH_Group_proportions %>%
# reorder the Course factor by max % group A
mutate(
  gpAmarks = if_else(MATH_Group=="A",prop_marks,0),
  Course = reorder(Course, gpAmarks, max)
) %>%
ggplot(aes(x=1,y=prop_marks, fill=Course)) +
geom_boxplot(alpha = 0.4) +
geom_point(aes(colour=Course),
  position = position_jitterdodge(),
  size = 1) +
scale_y_continuous(labels = scales::percent_format(accuracy = 1),
  breaks = seq(0,1,0.1)) +
scale_fill_brewer(palette = "RdBu", direction = -1) +
scale_colour_brewer(palette = "RdBu", direction = -1) +
theme_light(base_size = 12)+
theme(
  panel.grid.minor = element_blank(),
  axis.text.x=element_blank(),
  axis.ticks.x=element_blank(),
  panel.grid.major.x = element_blank(),
  strip.background = element_rect(fill=NA,colour = NA),
  strip.text = element_text(size=10, face="bold", color = "black")
) +
labs(
# title = "Proportion of marks in each MATH Group",
# subtitle = "Exams are ordered by proportion of Group A marks",
  x = "MATH Group",
  y = "Proportion of marks"
) +
facet_grid( ~ MATH_Group, switch = "x") +
ggsave("figs/ABC_allpapers_ranking.pdf",width=15,height=10,units="cm",dpi=300)
```



In this version, we sort by the mean % of group A, and show the means with diamonds

```
MATH_Group_proportions %>%
# reorder the Course factor by mean % group A
mutate(
  gpAmarks = if_else(MATH_Group=="A",prop_marks,0),
  Course = reorder(Course, gpAmarks, mean)
) %>%
ggplot(aes(x=1,y=prop_marks, fill=Course)) +
geom_boxplot(alpha = 0.3) +
stat_summary(fun.y = "mean",
             geom = "point",
             shape = 23,
             size = 3,
             aes(fill = Course),
             position = position_dodge(0.8)) +
geom_point(aes(colour=Course),
           position = position_jitterdodge(),
           size = 1) +
scale_y_continuous(labels = scales::percent_format(accuracy = 1),
                   breaks = seq(0,1,0.1)) +
# scale_fill_brewer(palette = "Set1") +
# scale_colour_brewer(palette = "Set1") +
scale_fill_brewer(palette = "RdBu", direction = -1) +
scale_colour_brewer(palette = "RdBu", direction = -1) +
theme_light(base_size = 12)+
theme(
  panel.grid.minor = element_blank(),
  axis.text.x=element_blank(),
  axis.ticks.x=element_blank(),
  panel.grid.major.x = element_blank(),
  strip.background = element_rect(fill=NA,colour = NA),
  strip.text = element_text(size=10, face="bold", color = "black")
) +
labs(
  # title = "Proportion of marks in each MATH Group",
  # subtitle = "Exams are ordered by proportion of Group A marks",
  x = "MATH Group",
  y = "Proportion of marks"
) +
facet_grid( ~ MATH_Group, switch = "x") +
ggsave("figs/ABC_allpapers_boxplots.pdf",width=15,height=10,units="cm",dpi=300)
```

Warning: `fun.y` is deprecated. Use `fun` instead.

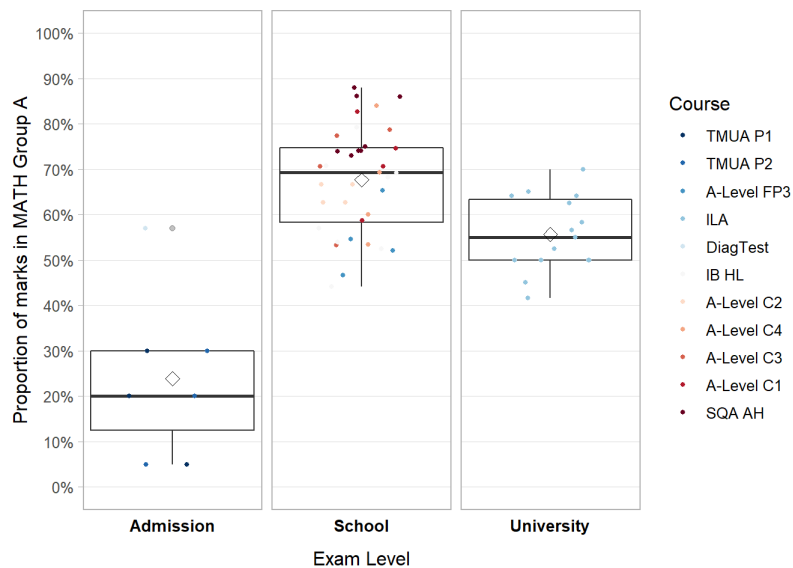


Here we group courses at different education levels

```
gpAschooluni = MATH_Group_proportions %>%
# reorder the Course factor by mean % group A
mutate(
  gpAmarks = if_else(MATH_Group=="A",prop_marks,0),
  Course = reorder(Course, gpAmarks, mean),
  CourseGroup = case_when(
    Course %in% c("TMUA P1", "TMUA P2", "DiagTest") ~ "Admission",
    Course == "ILA" ~ "University",
    TRUE ~ "School"
  )
) %>%
filter( MATH_Group == "A" ) %>%
select(Course, Year, Paper, total_marks_for_Group, total_marks_for_paper, prop_marks, CourseGroup)

gpAschooluni %>%
ggplot(aes(x=1,y=prop_marks)) +
geom_boxplot(alpha = 0.3) +
stat_summary(fun.y = "mean",
  geom = "point",
  shape = 23,
  size = 3) +
geom_point(aes(colour=Course),
  size = 1,
  position = position_jitter(0.2)) +
# geom_text(aes(Label=Course)) +
scale_y_continuous(labels = scales::percent_format(accuracy = 1),
  breaks = seq(0,1,0.1),
  limits = c(0,1)) +
# scale_fill_brewer(palette = "Set1") +
# scale_colour_brewer(palette = "Set1") +
scale_fill_brewer(palette = "RdBu", direction = -1) +
scale_colour_brewer(palette = "RdBu", direction = -1) +
theme_light(base_size = 12)+
theme(
  panel.grid.minor = element_blank(),
  axis.text.x=element_blank(),
  axis.ticks.x=element_blank(),
  panel.grid.major.x = element_blank(),
  strip.background = element_rect(fill=NA,colour = NA),
  strip.text = element_text(size=10, face="bold", color = "black")
) +
labs(
  # title = "Proportion of marks in each MATH Group",
  # subtitle = "Exams are ordered by proportion of Group A marks",
  x = "Exam Level",
  y = "Proportion of marks in MATH Group A"
) +
facet_grid( ~ CourseGroup, switch = "x") +
ggsave("figs/A_mean_school_vs_uni.pdf",width=15,height=10,units="cm",dpi=300)
```

Warning: `fun.y` is deprecated. Use `fun` instead.



Statistical comparisons

t-test comparison by level

```
gpAschool = gpAschooluni %>% filter(CourseGroup=="School") %>% select(prop_marks) %>% data.matrix
gpA_Alevel = gpAschooluni %>% filter(str_detect(Course, "A-Level")) %>% select(prop_marks) %>% data.matrix
gpAuni = gpAschooluni %>% filter(Course=="ILA") %>% select(prop_marks) %>% data.matrix
```

```
t.test(gpAschool, gpAuni)
```

```
##
## Welch Two Sample t-test
##
## data: gpAschool and gpAuni
## t = 4.1755, df = 37.021, p-value = 0.0001733
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  0.06174592 0.17816149
## sample estimates:
## mean of x mean of y
## 0.6766204 0.5566667
```

```
t.test(gpA_Alevel, gpAuni)
```

```
##
## Welch Two Sample t-test
##
## data: gpA_Alevel and gpAuni
## t = 3.0996, df = 32.957, p-value = 0.00395
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  0.03390045 0.16343289
## sample estimates:
## mean of x mean of y
## 0.6553333 0.5566667
```

Bayesian comparison

```
BESTout = BESTmcmc(gpAschool, gpAuni)
```

```
## Waiting for parallel processing to complete...done.
```

```
BESTout
```

```
## MCMC fit results for BEST analysis:
## 100002 simulations saved.
##      mean      sd    median  HDIlo    HDIup  Rhat  n.eff
## mu1    0.67727  0.02060  0.67726  0.63731  0.7185   1 58029
## mu2    0.55629  0.02424  0.55636  0.50903  0.6048   1 58749
## nu     41.76518 31.40481 33.26935 3.47672 103.9886  1 22769
## sigma1 0.11824 0.01558 0.11681 0.08931 0.1493   1 47375
## sigma2 0.08872 0.01976 0.08571 0.05540 0.1287   1 36287
##
## 'HDIlo' and 'HDIup' are the limits of a 95% HDI credible interval.
## 'Rhat' is the potential scale reduction factor (at convergence, Rhat=1).
## 'n.eff' is a crude measure of effective sample size.
```

```
summary(BESTout)
```

##	mean	median	mode	HDI%	HDIlo	HDIup	compVal	%>compVal
## mu1	0.6773	0.6773	0.6762	95	0.6373	0.7185		
## mu2	0.5563	0.5564	0.5568	95	0.5090	0.6048		
## muDiff	0.1210	0.1211	0.1211	95	0.0583	0.1840	0	100.0
## sigma1	0.1182	0.1168	0.1143	95	0.0893	0.1493		
## sigma2	0.0887	0.0857	0.0801	95	0.0554	0.1287		
## sigmaDiff	0.0295	0.0308	0.0324	95	-0.0211	0.0784	0	88.7
## nu	41.7652	33.2693	17.0551	95	3.4767	103.9886		
## log10nu	1.5070	1.5220	1.5716	95	0.8631	2.1137		
## effSz	1.1656	1.1645	1.1674	95	0.5181	1.8192	0	100.0

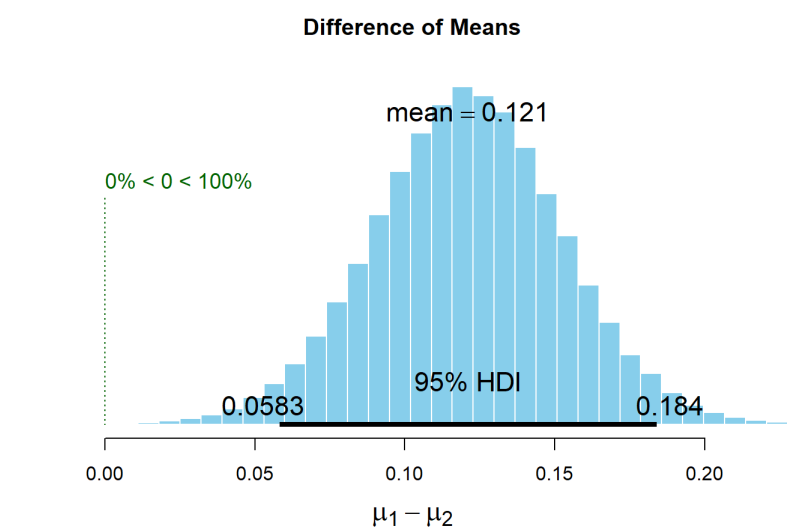
This gives the mean proportion of group A:

- for school exams, 0.68 (95% HDI [0.64, 0.72])
- for university exams, 0.56 (95% HDI [0.51, 0.60])

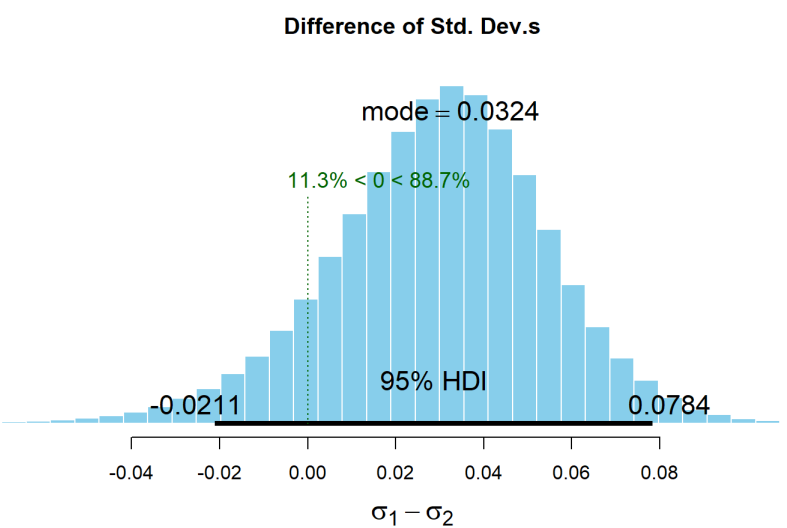
The difference between these is 0.12 (95% HDI [0.06, 0.18]).

Here are some more diagostic plots for this summary:

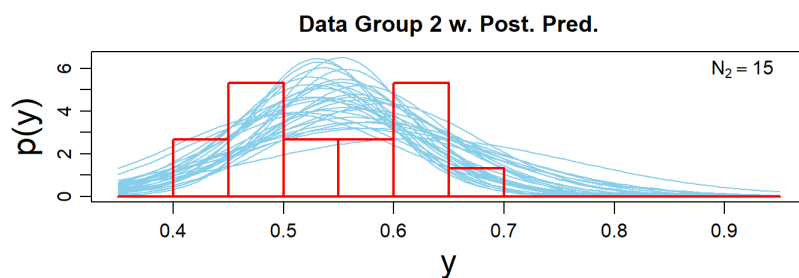
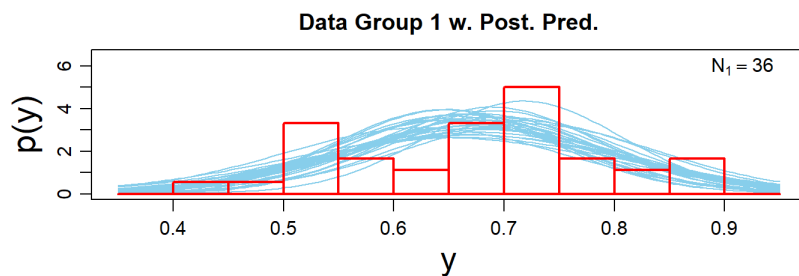
```
plot(BESTout)
```



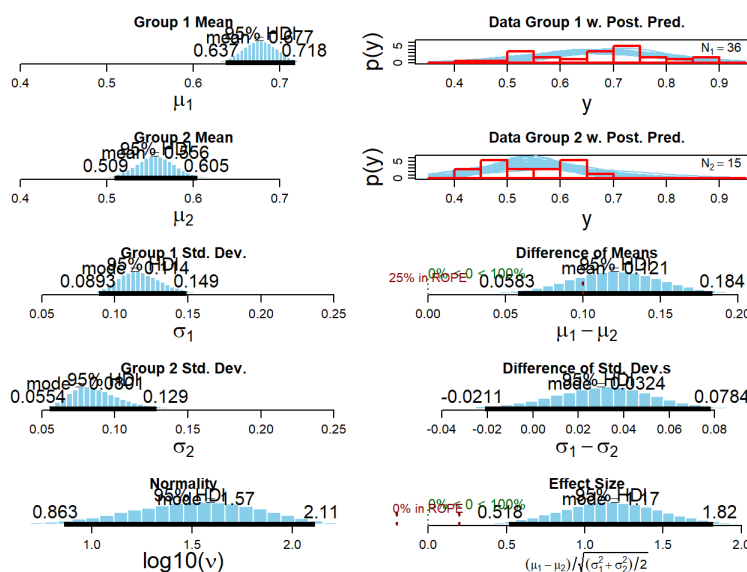
```
plot(BESTout, "sd")
```



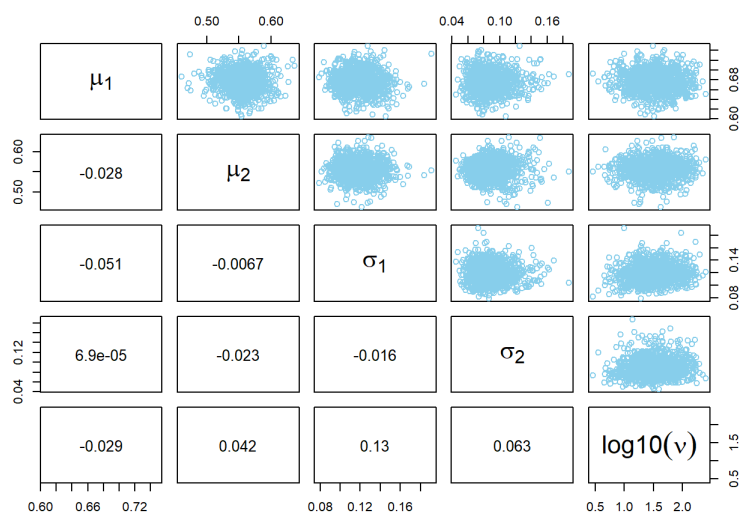
```
plotPostPred(BESTout)
```



```
plotAll(BESTout, credMass=0.95, ROPEm=c(-0.1,0.1),
        ROPEff=c(-0.2,0.2), compValm=0.5)
```



```
pairs(BESTout)
```



Looking at university versus A-Level in particular:

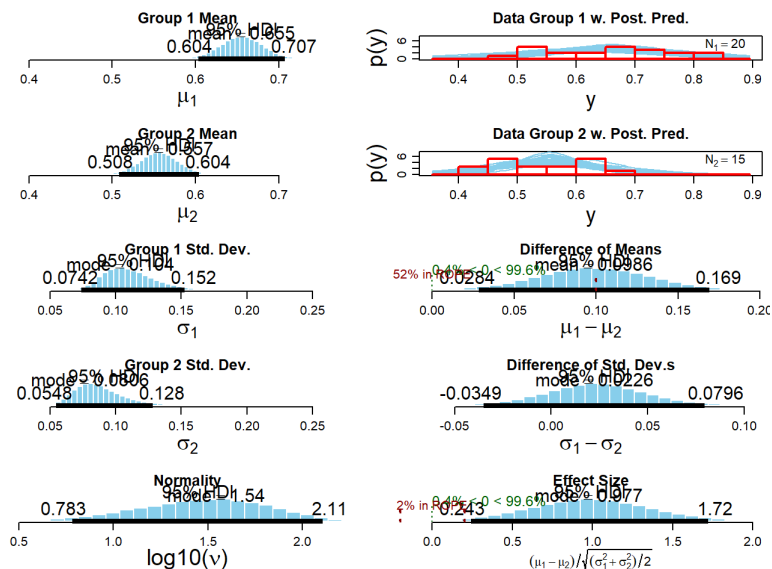
```
BESTout_Alevel = BESTmcmc(gpA_Alevel,gpAuni)
```

```
## Waiting for parallel processing to complete...done.
```

```
summary(BESTout_Alevel)
```

```
##          mean  median   mode HDI%  HDIlo  HDIup compVal %>compVal
## mu1      0.6551 0.6551 0.6572 95   0.6035 0.7073
## mu2      0.5565 0.5563 0.5547 95   0.5085 0.6043
## muDiff    0.0986 0.0985 0.0942 95   0.0284 0.1691      0      99.6
## sigma1    0.1114 0.1087 0.1035 95   0.0742 0.1524
## sigma2    0.0885 0.0854 0.0806 95   0.0548 0.1283
## sigmaDiff 0.0229 0.0229 0.0226 95  -0.0349 0.0796      0      80.6
## nu       39.2057 30.7896 14.1434 95   2.3815 100.3458
## log10nu   1.4673 1.4884 1.5428 95   0.7833 2.1080
## effSz     0.9919 0.9883 0.9773 95   0.2426 1.7235      0      99.6
```

```
plotAll(BESTout_Alevel, credMass=0.95, ROPEm=c(-0.1,0.1),
        ROPEff=c(-0.2,0.2), compValm=0.5)
```

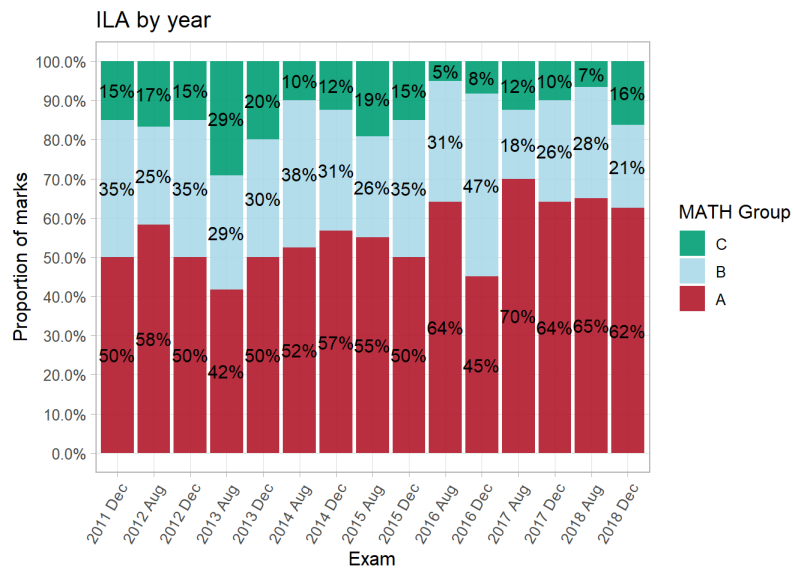


Details of each paper

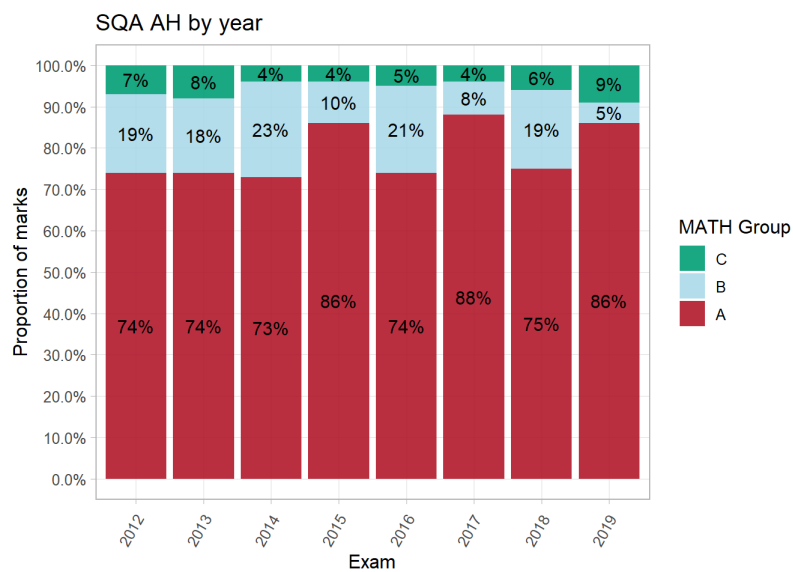
Stacked bars of ABC proportion by exam paper

```
math_stacked_bars <- function(course_name) {
  MATH_Group_proportions %>%
    filter(Course == course_name) %>%
    # compute the positions of the text labels
    # see http://t-redactyl.io/blog/2016/01/creating-plots-in-r-using-ggplot2-part-4-stacked-bar-plots.html
    dplyr::select(Course, Exam, transform, pos = cumsum(prop_marks) - (0.5 * prop_marks)) %>%
    ggplot(aes(x = Exam,
               y = prop_marks,
               fill = fct_rev(MATH_Group))) +
    geom_bar(stat="identity", alpha = 0.9) +
    geom_text(aes(x = Exam, y = 1-pos, label = paste0(sprintf("%.0f",100*prop_marks),"%")),
              size=4) +
    scale_y_continuous(labels = scales::percent,
                       breaks = seq(0,1,0.1)) +
    scale_fill_manual(values = palMATH) +
    theme_light(base_size = 12)+
    theme(
      panel.grid.minor = element_blank(),
      axis.text.x = element_text(angle = 60, hjust = 1)
    ) +
    labs(
      title = paste(course_name, "by year"),
      fill = "MATH Group",
      x = "Exam",
      y = "Proportion of marks"
    )
}
```

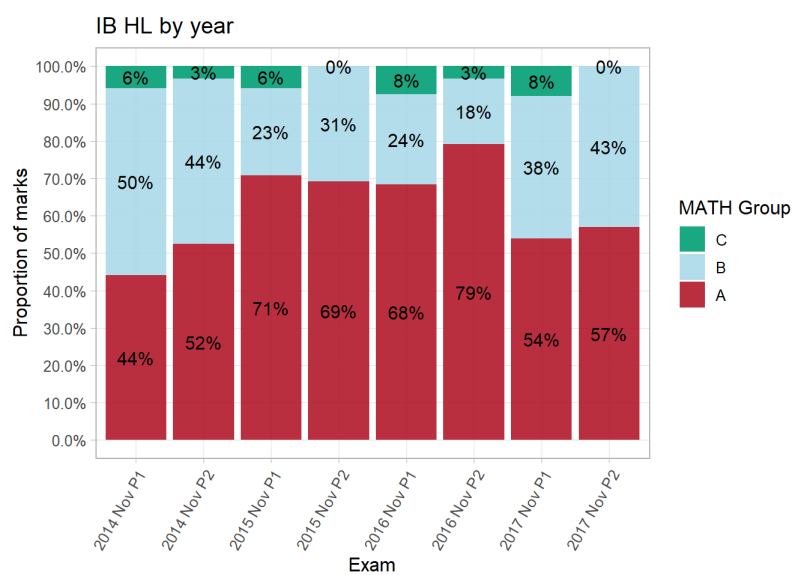
```
math_stacked_bars("ILA")
```



```
math_stacked_bars("SQA AH")
```



```
math_stacked_bars("IB HL")
```



```
#math_stacked_bars("A-Level C1-C4")
#math_stacked_bars("A-Level FP3")
```

Do them all in one big plot, using facets:


```

MATH_Group_proportions %>%
  filter(!Course %in% c("DiagTest", "TMUA")) %>%
  ddply(.(Course,Exam), transform, pos = cumsum(prop_marks) - (0.5 * prop_marks)) %>%
  ggplot(aes(x = Exam,
             y = prop_marks,
             fill = fct_rev(MATH_Group))) +
  geom_bar(stat="identity", alpha = 0.9) +
  geom_text(aes(x = Exam, y = 1-pos, label = paste0(sprintf("%.0f",100*prop_marks),"%")),
            size=2) +
  scale_y_continuous(labels = scales::percent,
                     breaks = seq(0,1,0.2)) +
  scale_fill_manual(values = palMATH) +
  theme_light(base_size = 10)+
  theme(
    panel.grid.minor = element_blank(),
    axis.text.x = element_text(size = rel(0.7), angle = 30, hjust = 1),
    strip.background = element_rect(fill=NA,colour = NA),
    strip.text = element_text(size=10, face="bold", color = "black"),
    legend.position="bottom"
  ) +
  labs(
    fill = "MATH Group",
    x = "Exam",
    y = "Proportion of marks"
  ) +
  facet_wrap( ~ Course, ncol = 2, scales = "free") +
  ggsave("figs/ABC_allpapers_facets.pdf",width=15,height=20,units="cm",dpi=300)

```



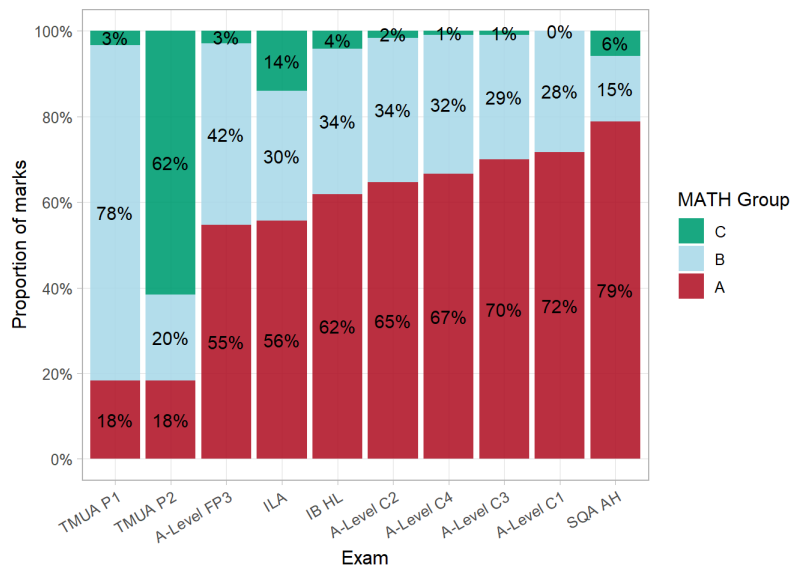
A version of Darlington 2015 Fig 2/3:

```

MATH_Group_proportions %>%
  filter(!Course %in% c("TMUA", "DiagTest")) %>%
  ungroup() %>%
  group_by(Course, MATH_Group) %>%
  summarise(
    prop_marks = mean(prop_marks),
    n = n()
  ) %>%
  ungroup() %>%
  mutate(
    gpAmarks = if_else(MATH_Group=="A", prop_marks, 0),
    # Course = paste(Course, "\n(n=", n, ")"),
    Course = (reorder(Course, gpAmarks, max))
  ) %>%
  ddply(.(Course), transform, pos = cumsum(prop_marks) - (0.5 * prop_marks)) %>%
  ggplot(aes(x = Course,
            y = prop_marks,
            fill = fct_rev(MATH_Group))) +
  geom_bar(stat="identity", alpha = 0.9) +
  geom_text(aes(x = Course, y = pos, label = paste0(sprintf("%.0f", 100*prop_marks), "%")),
            size=4) +
  scale_y_continuous(labels = scales::percent,
                     breaks = seq(0, 1, 0.2)) +
  scale_fill_manual(values = palMATH) +
  theme_light(base_size = 12) +
  theme(
    panel.grid.minor = element_blank(),
    axis.text.x = element_text(angle = 30, hjust = 1)
  ) +
  labs(
    # title = "Mean proportion of marks in each MATH Group",
    fill = "MATH Group",
    x = "Exam",
    y = "Proportion of marks"
  ) +
  ggsave("figs/ABC_school_and_ILA_means.pdf", width=15, height=10, units="cm", dpi=300)

```

```
## `summarise()` regrouping output by 'Course' (override with `.groups` argument)
```



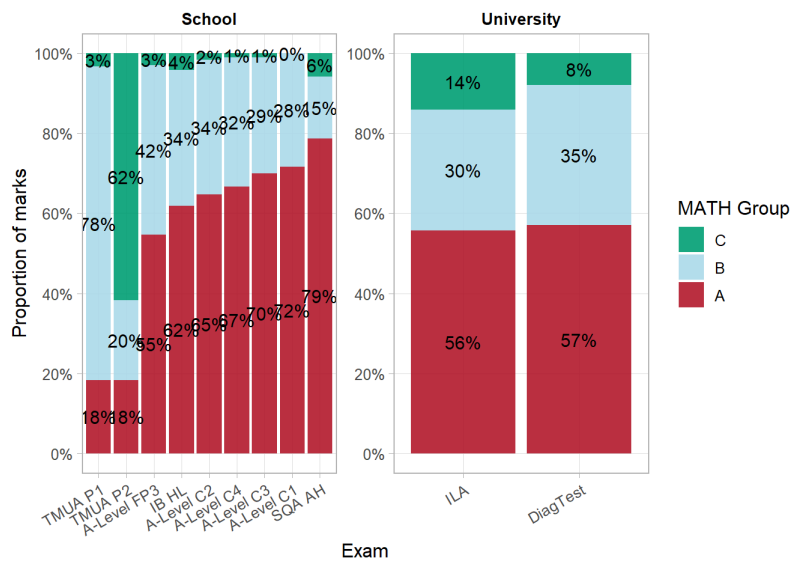
Try using facets to show school vs university:

```

MATH_Group_proportions %>%
  ungroup() %>%
  group_by(Course,MATH_Group) %>%
  summarise(
    prop_marks = mean(prop_marks),
    n = n()
  ) %>%
  ungroup() %>%
  mutate(
    gpAmarks = if_else(MATH_Group=="A",prop_marks,0),
    # Course = paste(Course,"n(n=",n,")"),
    Course = (reorder(Course, gpAmarks, max)),
    CourseGroup = if_else(Course %in% c("TMUA", "DiagTest", "ILA"), "University", "School")
  ) %>%
  dplyr(.(Course), transform, pos = cumsum(prop_marks) - (0.5 * prop_marks)) %>%
  ggplot(aes(x = Course,
    y = prop_marks,
    fill = fct_rev(MATH_Group))) +
  geom_bar(stat="identity", alpha = 0.9) +
  geom_text(aes(x = Course, y = pos, label = paste0(sprintf("%.0f",100*prop_marks,"%")),
    size=4) +
  scale_y_continuous(labels = scales::percent,
    breaks = seq(0,1,0.2)) +
  scale_fill_manual(values = palMATH) +
  facet_wrap( ~ CourseGroup, ncol = 2, scales = "free") +
  theme_light(base_size = 12)+
  theme(
    panel.grid.minor = element_blank(),
    axis.text.x = element_text(angle = 30, hjust = 1),
    strip.background = element_rect(fill=NA, colour = NA),
    strip.text = element_text(size=10, face="bold", color = "black")
  ) +
  labs(
    # title = "Mean proportion of marks in each MATH Group",
    fill = "MATH Group",
    x = "Exam",
    y = "Proportion of marks"
  ) +
  ggsave("figs/ABC_school_vs_other_means.pdf",width=15,height=10,units="cm",dpi=300)

```

```
## `summarise()` regrouping output by 'Course' (override with `.groups` argument)
```



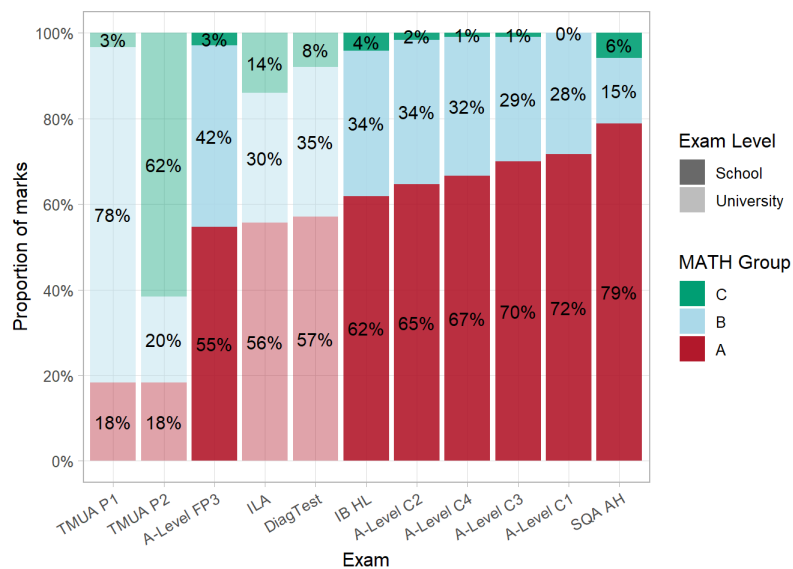
Showing the school/uni distinction using opacity:

```

MATH_Group_proportions %>%
  ungroup() %>%
  group_by(Course,MATH_Group) %>%
  summarise(
    prop_marks = mean(prop_marks),
    n = n()
  ) %>%
  ungroup() %>%
  mutate(
    gpAmarks = if_else(MATH_Group=="A",prop_marks,0),
    # Course = paste(Course,"\\n(n=",n,")"),
    Course = (reorder(Course, gpAmarks, max)),
    CourseGroup = if_else(Course %in% c("TMUA P1", "TMUA P2", "DiagTest", "ILA"), "University", "School")
  ) %>%
  ddply(.(Course), transform, pos = cumsum(prop_marks) - (0.5 * prop_marks)) %>%
  ggplot(aes(x = Course,
    y = prop_marks,
    fill = fct_rev(MATH_Group))) +
  geom_bar(stat="identity",
    aes(alpha = CourseGroup)) +
  geom_text(aes(x = Course, y = pos, label = paste0(sprintf("%.0f",100*prop_marks,"%")),
    size=4) +
  scale_y_continuous(labels = scales::percent,
    breaks = seq(0,1,0.2)) +
  scale_fill_manual(values = palMATH) +
  scale_alpha_manual("Exam Level", values = c("School" = 0.9, "University" = 0.4)) +
  theme_light(base_size = 12)+
  theme(
    panel.grid.minor = element_blank(),
    axis.text.x = element_text(angle = 30, hjust = 1)
  ) +
  labs(
    # title = "Mean proportion of marks in each MATH Group",
    fill = "MATH Group",
    x = "Exam",
    y = "Proportion of marks"
  ) +
  ggsave("figs/ABC_all_means.pdf",width=15,height=10,units="cm",dpi=300)

```

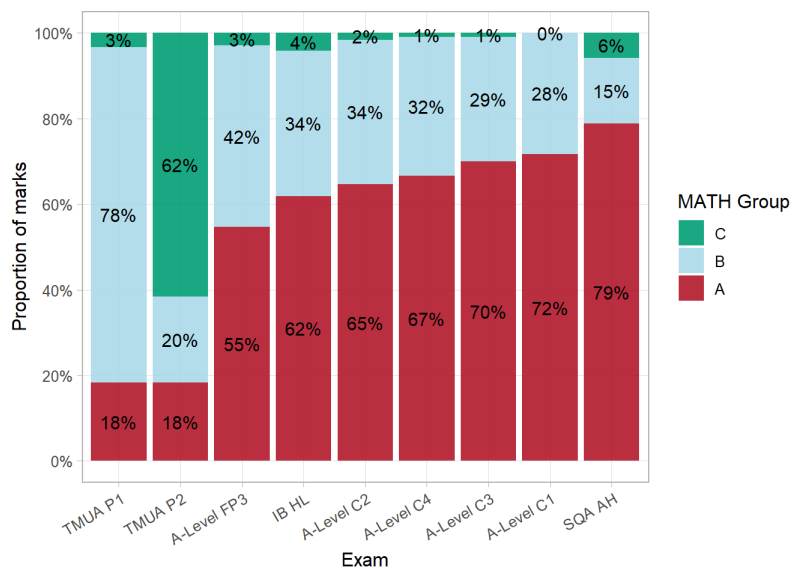
```
## `summarise()` regrouping output by 'Course' (override with `.groups` argument)
```



Focusing on school exams:

```
MATH_Group_proportions %>%
  filter(!Course %in% c("TMUA", "DiagTest", "ILA")) %>%
  ungroup() %>%
  group_by(Course, MATH_Group) %>%
  summarise(
    prop_marks = mean(prop_marks),
    n = n()
  ) %>%
  ungroup() %>%
  mutate(
    gpAmarks = if_else(MATH_Group=="A", prop_marks, 0),
    # Course = paste(Course, "\n(n=", n, ")"),
    Course = (reorder(Course, gpAmarks, max))
  ) %>%
  dplyr(.(Course), transform, pos = cumsum(prop_marks) - (0.5 * prop_marks)) %>%
  ggplot(aes(x = Course,
             y = prop_marks,
             fill = fct_rev(MATH_Group))) +
  geom_bar(stat="identity", alpha = 0.9) +
  geom_text(aes(x = Course, y = pos, label = paste0(sprintf("%.0f", 100*prop_marks), "%")),
            size=4) +
  scale_y_continuous(labels = scales::percent,
                     breaks = seq(0, 1, 0.2)) +
  scale_fill_manual(values = palMATH) +
  theme_light(base_size = 12) +
  theme(
    panel.grid.minor = element_blank(),
    axis.text.x = element_text(angle = 30, hjust = 1)
  ) +
  labs(
    # title = "Mean proportion of marks in each MATH Group",
    fill = "MATH Group",
    x = "Exam",
    y = "Proportion of marks"
  ) +
  ggsave("figs/ABC_school_means.pdf", width=15, height=10, units="cm", dpi=300)
```

```
## `summarise()` regrouping output by 'Course' (override with `.groups` argument)
```



Detailed MATH categories

Like Darlington (2014) Fig 1 - looking in detail at the MATH categories.

```
MATH_Cat_proportions = ratings %>%
  group_by(Course, Year, Paper, MATH_Group, MATH) %>%
  summarise(
    total_marks_for_Cat = sum(Marks)
  ) %>%
  ungroup() %>%
  # add in the missing "0%" entries
  complete(nesting(Course, Year, Paper), MATH, fill = list(total_marks_for_Cat = 0)) %>%
  mutate(
    # restore the MATH_Group for the "0%" entries
    MATH_Group = str_sub(MATH, 1, 1)
  ) %>%
  left_join(MATH_Group_proportions) %>%
  mutate (
    prop_marks_cat = total_marks_for_Cat / total_marks_for_Group
  ) %>%
  ungroup()
```

```
## `summarise()` regrouping output by 'Course', 'Year', 'Paper', 'MATH_Group' (override with `.groups` argument)
```

```
## Joining, by = c("Course", "Year", "Paper", "MATH_Group")
```

```
MATH_Cat_props_by_Course = MATH_Cat_proportions %>%
  group_by(Course, MATH) %>%
  summarise(
    total_Cat = sum(total_marks_for_Cat),
    total_Group = sum(total_marks_for_Group),
    prop_of_Group = total_Cat / total_Group * 100
  )
```

```
## `summarise()` regrouping output by 'Course' (override with `.groups` argument)
```

```
MATH_Cat_props_by_Course %>%
  select(-total_Cat, -total_Group) %>%
  spread(MATH, prop_of_Group) %>%
  knitr::kable(booktabs = T, digits = 0)
```

Course	A1	A2	A3	B1	B2	C1	C2	C3
A-Level C1	0	12	88	48	52	NaN	NaN	NaN
A-Level C2	0	11	89	30	70	100	0	0
A-Level C3	0	14	86	31	69	67	33	0
A-Level C4	0	13	87	19	81	100	0	0
A-Level FP3	0	3	97	11	89	100	0	0
DiagTest	0	5	95	86	14	0	100	0
IB HL	0	4	96	50	50	97	0	3
ILA	0	8	92	44	56	43	57	0
SQA AH	0	3	97	61	39	91	9	0
TMUA P1	0	0	100	43	57	50	50	0
TMUA P2	0	9	91	58	42	73	27	0

```
MATH_Cat_props_by_Course %>%
  filter( str_sub(MATH,1,1) == "A") %>%
  ungroup() %>%
  mutate(
    Course = (reorder(Course, prop_of_Group, max)),
    CourseGroup = if_else(Course %in% c("TMUA", "DiagTest", "ILA"), "University", "School"),
    MATH = fct_recode(MATH, FKFS = "A1", COMP = "A2", RUOP = "A3"),
    prop_of_Group = prop_of_Group / 100
  ) %>%
  dplyr::ddply(.(Course), transform, pos = cumsum(prop_of_Group) - (0.5 * prop_of_Group)) %>%
  ggplot(aes(x = Course,
    y = prop_of_Group,
    fill = fct_rev(MATH),
    alpha = CourseGroup)) +
  geom_bar(stat="identity") +
  geom_text(aes(x = Course,
    y = pos,
    label = if_else(prop_of_Group < 0.01,
      "",
      paste0(sprintf("%.0f", 100*prop_of_Group), "%"))
  ),
    size = 4,
    alpha = 1) +
  scale_alpha_manual("Exam Level", values = c("School" = 0.9, "University" = 0.5)) +
  scale_y_continuous(labels = scales::percent,
    breaks = seq(0,1,0.2)) +
  scale_fill_manual(values = rev(c(palMATH[3], "#d6604d", "#f4a582")))) +
  theme_light(base_size = 12)+
  theme(
    panel.grid.minor = element_blank(),
    axis.text.x = element_text(angle = 30, hjust = 1)
  ) +
  labs(
    # title = "Mean proportion of marks in each MATH Group",
    fill = "MATH Category",
    x = "Exam",
    y = "Proportion of Group A marks"
  ) +
  ggsave("figs/A_breakdown.pdf", width=15, height=10, units="cm", dpi=300)
```

