

Quantum Computing: Zero to Hero

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and

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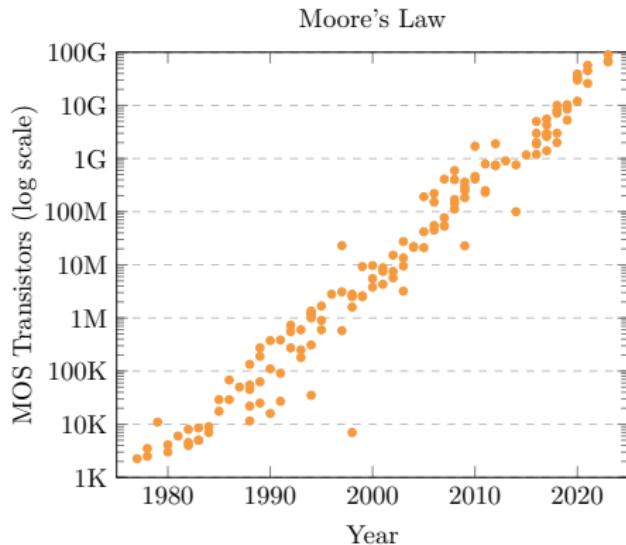
April 27, 2023

Classical Computers

- ▶ Introduction of the Turing machine by Alan Turing [1936]
- ▶ von Neumann architecture (stored-program computers) [1947]
- ▶ Invention of the transistor at Bell Labs [1947]
- ▶ Integrated circuit (IC) [1958]
- ▶ Intel 4004 microprocessor [1971]
- ▶ IBM Personal Computer (PC) [1981]
- ▶ World Wide Web invented by Berners-Lee [1989]
- ▶ NVIDIA GeForce 256 GPU [1999]
- ▶ Multi-core processors [2000s]
- ▶ IBM Watson AI [2011]
- ▶ NVIDIA A100 GPU [2020]
- ▶ GPT-4, Stable Diffusion, etc [2023]

Limitations of Classical Computers

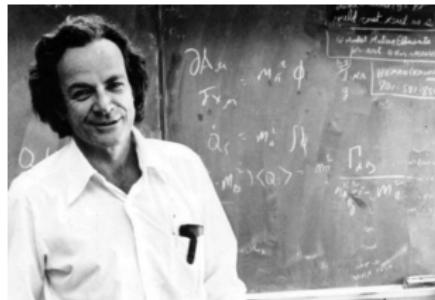
- ▶ Exponential growth of resources
- ▶ Inability to efficiently simulate quantum systems
- ▶ Limitations in solving optimization problems efficiently
- ▶ Energy consumption and heat dissipation
- ▶ Physical limitations of transistor scaling (Moore's Law)



Quantum Computing

- ▶ Manin (computable and uncomputable)
- ▶ Feynman (simulating nature)
- ▶ Benioff (quantum Turing machine)
- ▶ Deutsch (universal quantum computer)
- ▶ Shor (factoring)
- ▶ Grover (unstructured search algorithm)
- ▶ ...

“Nature isn’t classical, dammit, and if you want to make a simulation of nature, you’d better make it quantum mechanical, and by golly it’s a wonderful problem, because it doesn’t look so easy.”



Exponential Difficulty to Simulate Nature

Feynman's Insight

- ▶ Richard Feynman recognized the limitations of classical computers in simulating nature:
 - ▶ Computational complexity increases exponentially with system size.
 - ▶ Accurate simulation of quantum systems requires consideration of all possible states.

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 - ▶ Quantum systems can exist in superpositions of states.
 - ▶ Quantum entanglement leads to non-local correlations.

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- ▶ Classical computers struggle to efficiently simulate quantum systems:
 - ▶ Quantum systems can exist in superpositions of states.
 - ▶ Quantum entanglement leads to non-local correlations.
- ▶ Feynman's idea: Use quantum computers to simulate quantum systems.
 - ▶ Quantum computers operate on qubits, enabling more efficient simulations.
 - ▶ Exploit quantum parallelism and entanglement to tackle exponentially hard problems.

Hard Computational Problems

Challenges in Classical Computation

- ▶ Computational resource requirements.
 - ▶ Time complexity (# of operations required as a function of input size).
 - ▶ Space complexity(amount of memory required as a function of input size).

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 - ▶ Space complexity(amount of memory required as a function of input size).
- ▶ Example of hard problems: NP-complete problems.
 - ▶ Traveling Salesman Problem (TSP)
 - ▶ Boolean Satisfiability Problem (SAT)
 - ▶ Knapsack Problem (KP)
 - ▶ ...

Hard Computational Problems

Fresh News (yesterday!)

The screenshot shows a red header bar with the arXiv logo and navigation links for 'Search...', 'Help | Advanced'. Below it, a grey header bar displays the category 'Computer Science > Computational Complexity'. The main title 'The 2-MAXSAT Problem Can Be Solved in Polynomial Time' is prominently displayed in large black font. Below the title, the author's name 'Yangjun Chen' is shown in blue. The abstract begins with: 'By the MAXSAT problem, we are given a set V of m variables and a collection C of n clauses over V. We will seek a truth assignment to maximize the number of satisfied clauses. This problem is NP-hard even for its restricted version, the 2-MAXSAT problem by which every clause contains at most 2 literals. In this paper, we discuss a polynomial time algorithm to solve this problem. Its time complexity is bounded by O(n²m³). Hence, we provide a proof of P = NP.' The page also lists subjects ('Computational Complexity (cs.CC)'), citation information ('arXiv:2304.12517 [cs.CC]'), and a DOI link ('https://doi.org/10.48550/arXiv.2304.12517').

arXiv > cs > arXiv:2304.12517

Search...
Help | Advanced

Computer Science > Computational Complexity

[Submitted on 25 Apr 2023]

The 2-MAXSAT Problem Can Be Solved in Polynomial Time

Yangjun Chen

By the MAXSAT problem, we are given a set V of m variables and a collection C of n clauses over V . We will seek a truth assignment to maximize the number of satisfied clauses. This problem is NP-hard even for its restricted version, the 2-MAXSAT problem by which every clause contains at most 2 literals. In this paper, we discuss a polynomial time algorithm to solve this problem. Its time complexity is bounded by $O(n^2m^3)$. Hence, we provide a proof of $P = NP$.

Subjects: Computational Complexity (cs.CC)

Cite as: arXiv:2304.12517 [cs.CC]
(or arXiv:2304.12517v1 [cs.CC] for this version)
<https://doi.org/10.48550/arXiv.2304.12517>

Hard Computational Problems

Challenges in Classical Computation

- ▶ Implications of hard computational problems:
 - ▶ Limitations in optimization and decision-making tasks.
 - ▶ Security and cryptography rely on the hardness of certain problems.

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- ▶ Approaches to tackle hard computational problems:
 - ▶ Heuristics: Approximation algorithms that can provide near-optimal solutions.
 - ▶ Parallel and distributed computing: Using multiple processors to solve problems faster.

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 - ▶ Heuristics: Approximation algorithms that can provide near-optimal solutions.
 - ▶ Parallel and distributed computing: Using multiple processors to solve problems faster.
 - ▶ Quantum computing: Exploiting quantum mechanics to solve certain hard problems more efficiently.

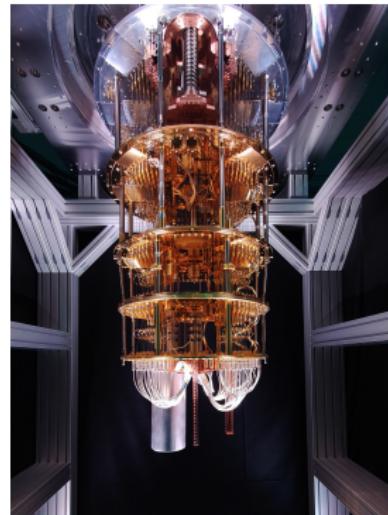
Paradigm Shift

QC is a paradigm of computation that utilizes quantum mechanics to perform calculations that are infeasible for classical computers.

Potential for **exponential** speedups!

Potential for unheard breakthroughs in science, medicine, engineering, ...

An IBM superconducting QPU



Quantum Computing: Theory 1

Church-Turing thesis

Any function “naturally to be regarded as computable” is computable by a (probabilistic) Turing machine.

Extended Church-Turing thesis

Any function naturally to be regarded as “efficiently computable” is efficiently computable by a (probabilistic) Turing machine.

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Any function “naturally to be regarded as efficiently computable” is efficiently computable by a quantum Turing machine.

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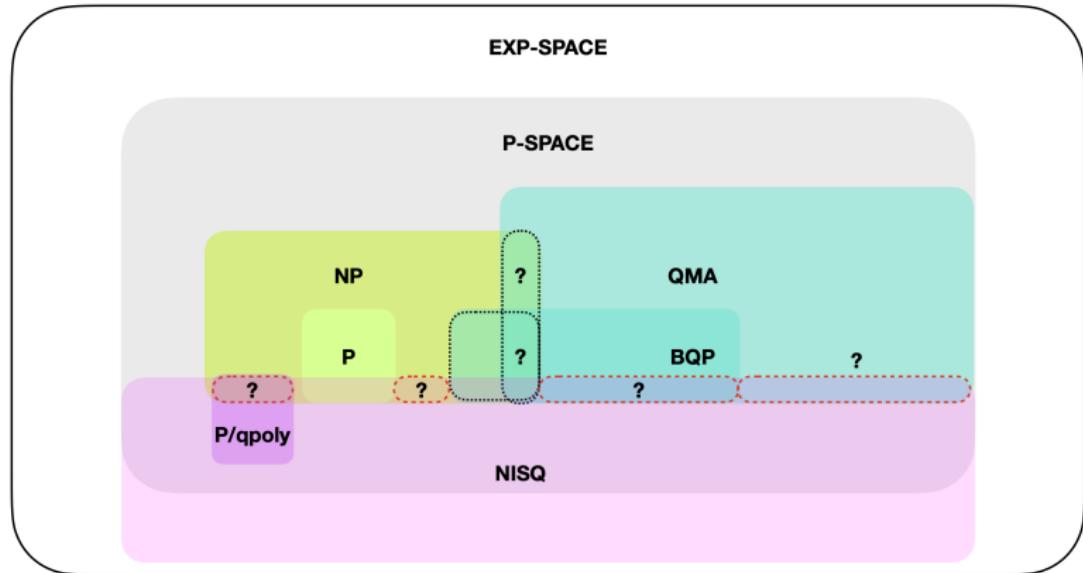
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Quantum Extended Church-Turing thesis

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What does this say about quantum computers?

Quantum Computing: Theory 2



Quantum Computing: Terminology

Quantum Supremacy

Experimental verification that a well defined computing task can be performed faster in a quantum computer than a classical computer.

Has it been achieved? Maybe.

Quantum Advantage

Experimental and repeated verification that a practical real world computing task can be performed faster in a quantum computer than a classical computer.

Has it been achieved? Probably not.

Google's Quantum Supremacy

nature

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Article | [Published: 23 October 2019](#)

Quantum supremacy using a programmable superconducting processor

[Frank Arute](#), [Kunal Arya](#), [Ryan Babbush](#), [Dave Bacon](#), [Joseph C. Bardin](#), [Rami Barends](#), [Rupak Biswas](#),
[Sergio Boixo](#), [Fernando G. S. L. Brando](#), [David A. Buell](#), [Brian Burkett](#), [Yu Chen](#), [Zijun Chen](#), [Ben Chiaro](#),
[Roberto Collins](#), [William Courtney](#), [Andrew Dunsworth](#), [Edward Farhi](#), [Brooks Foxen](#), [Austin Fowler](#), [Craig
Gidney](#), [Marissa Giustina](#), [Rob Graff](#), [Keith Guerin](#), ... [John M. Martinis](#)  + Show authors

[Nature](#) **574**, 505–510 (2019) | [Cite this article](#)

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Break

Questions?

Moving to slightly more technical territory.

Bits vs. Qubits

	Bits	Qubits
<i>Unit of information</i>	$\{0, 1\}$	\mathbb{CP}^1
<i>Operation</i>	Deterministic	Stochastic
<i>Processing</i>	Classical gates	Unitary operators
<i>Technology</i>	Semiconductor based	Large number of modalities
<i>Reversibility</i>	No	Yes

Qubits

Quantum systems are discrete. A qubit is a 2-level system described as a vector on a Hilbert space $\mathcal{H} = \mathbb{C}^2$ with basis $\{|0\rangle, |1\rangle\}$.

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$$|\psi\rangle = a|0\rangle + b|1\rangle$$

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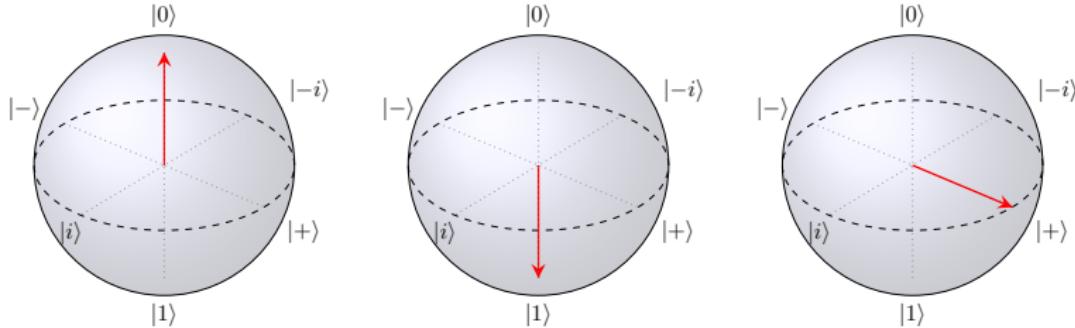
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Amplitudes are **super important**: their squares give probabilities to measure the state in either of the basis states.

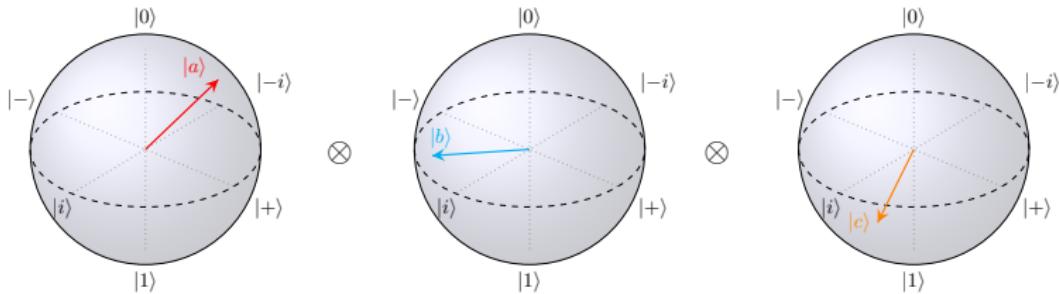
Bloch Sphere



The Bloch sphere $\cong \mathbb{CP}^1$ is an easy visualization of the state space of the qubit, the Hilbert space.

Each vector can be described by two angles, which encode the same information as the amplitude.

Multi-Qubit States



$$|\psi\rangle = |a\rangle \otimes |b\rangle \otimes |c\rangle = |abc\rangle$$

Superposition

In general a 3-qubit state is a superposition of all possible combinations (in the computational basis):

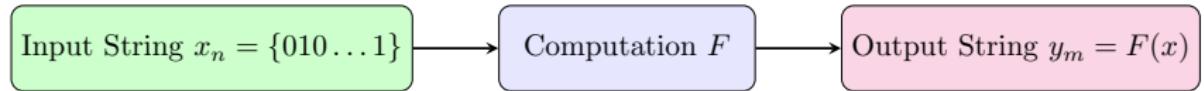
$$|\psi\rangle = \sum_i c_{ijk} |ijk\rangle$$

$$|\psi\rangle = c_{000}|000\rangle + c_{001}|001\rangle + \dots + c_{110}|110\rangle + c_{111}|111\rangle$$

This state is fully described by the $2^3 = 8$ amplitudes where

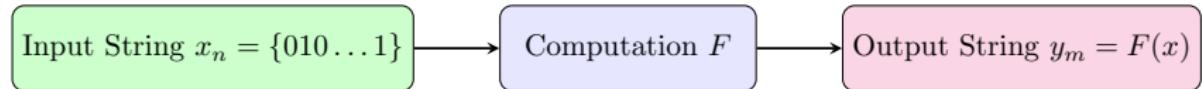
$$|c_{000}|^2 + |c_{001}|^2 + |c_{010}|^2 + |c_{011}|^2 + |c_{100}|^2 + |c_{101}|^2 + |c_{110}|^2 + |c_{111}|^2 = 1$$

Classical Computation

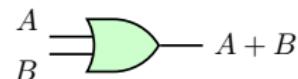
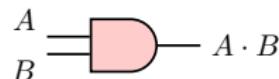
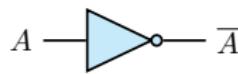


- ▶ $x \in \{0, 1\}^n$
- ▶ $y \in \{0, 1\}^m$
- ▶ $F : \{0, 1\}^n \rightarrow \{0, 1\}^m$ is the composition of logical gates

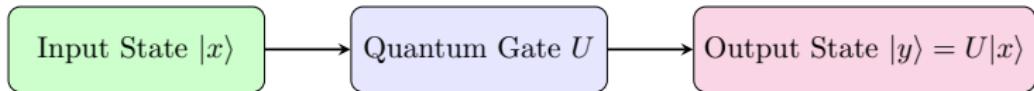
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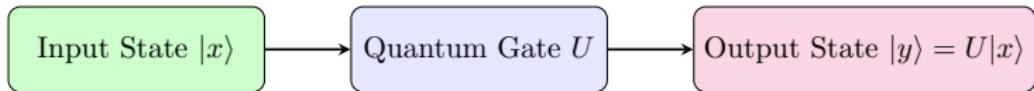


Quantum Computation



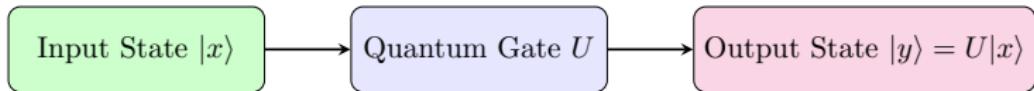
- ▶ $|x\rangle \in \mathcal{H}_{\text{in}}$, the input Hilbert space of dimension n
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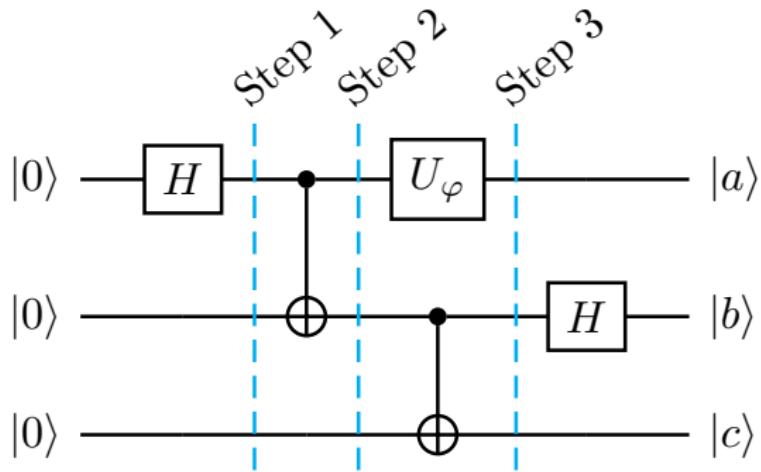
Quantum Computation



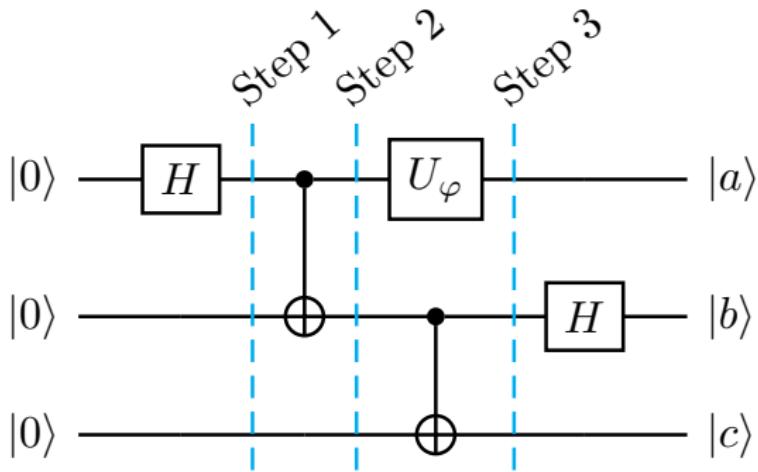
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- ▶ $U = e^{-iHt}$, for $H \in \text{Herm}(\mathbb{C}^n)$ the Hamiltonian or some other generator

$$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \quad \text{CNOT} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

Circuit Model

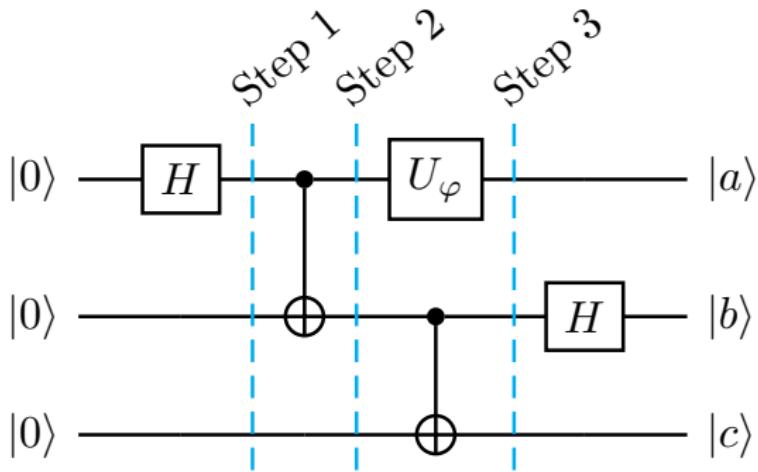


Circuit Model



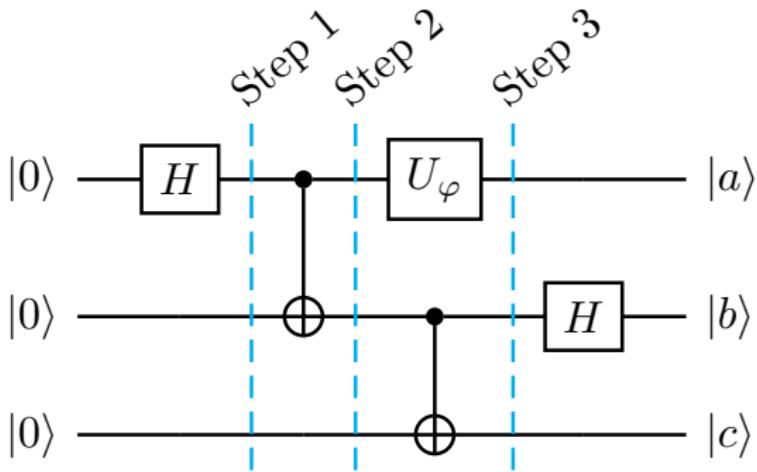
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Circuit Model



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- ▶ Obtain $|abc\rangle = U|000\rangle$

Quantum Algorithms

Out of this process, one can construct algorithms that do a lot of different things.

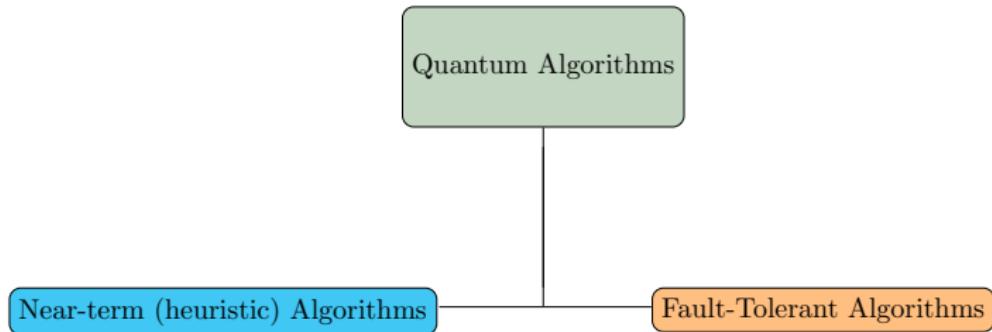
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Algorithm	Purpose	Speedup
Schor's	Factoring	exp
Quantum Simulation	Simulating Nature	exp
HHL	Solving LSs	exp
Grover's	Search	poly
QAE	Amplify prob. of desired outcome	poly
VQAs	Optimization	unknown
Quantum Annealing	Optimization	unknown

NISQ vs FTEC

- ▶ Algorithms are implemented by quantum circuits on actual hardware
- ▶ The current era of hardware is called NISQ (issues: noisy, few qubits, ...)
- ▶ We are trying to arrive to the FTEC era (millions of qubits, error correction, ...)

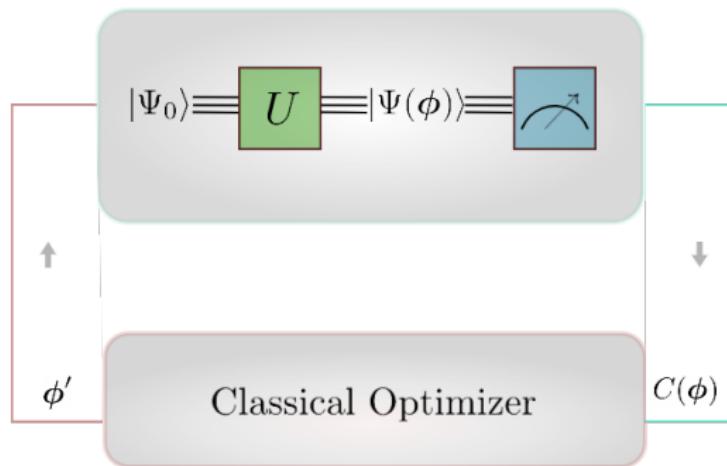


NISQ Era Algorithmic Enhancements

Currently, most people focus on NISQ compatible algorithms to be used already in real-world problems.

- ▶ **Optimization:** VQAs, Quantum Annealers, and more generally “Ising Machines”
- ▶ **Machine Learning:** Quantum Kernels, VQAs, QNNs, etc
- ▶ **Sampling:** QRNGs, Quassian Boson Sampling, Random Circuit Sampling, etc

Variational Quantum Algorithms



Variational Quantum Algorithms

- ▶ Consider some optimization problem (e.g. Knapsack):

$$\begin{aligned} \max \quad & \sum_{i=1}^n v_i x_i, \\ \text{s.t.} \quad & \sum_{i=1}^n w_i x_i \leq W, \end{aligned}$$

Variational Quantum Algorithms

- ▶ Then (if possible) formulate it as a QUBO:

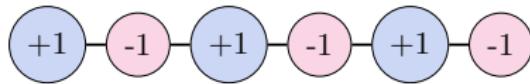
$$f(x) = \sum_i^n v_i x_i - \lambda_0 \left(\sum_i^n w_i x_i - W + \sum_{k=1}^N 2^{k-1} s_k \right)^2$$

Variational Quantum Algorithms

- ▶ Then map to an Ising Hamiltonian:

$$H(s) = \sum_i^n \left(\frac{v_i}{2} \right) \hat{s}_i + \sum_{i < j}^n \left(\frac{v_i v_j + \lambda_0 w_i w_j}{4} \right) \hat{s}_i \hat{s}_j$$

- ▶ Implement a **QAOA** certain type of VQA



NISQ Quantum Algorithms

However, more approaches exists:

Choose either:

- ▶ Quantum Annealing implementation (e.g. D-Wave)
- ▶ Digital Annealing implementation (e.g. Fujitsu)
- ▶ TensorTrain implementation (e.g. TerraQuantum)
- ▶ QAOA implementation (e.g. IBM, Quantinuum, ...)

Quantum Advantage

Applications of quantum computing:

- ▶ finance and logistic
- ▶ chemistry and material science
- ▶ automotive and aviation
- ▶ ...

McKinsey: “the four industries likely to see the earliest economic impact from quantum computing—automotive, chemicals, financial services, and life sciences—stand to potentially gain up to \$1.3 trillion in value by 2035.”

Problems

Here are (some) issues:

- ▶ FTEC computers still far ...

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Here are (some) issues:

- ▶ FTEC computers still far ...
- ▶ “hybrid” solutions (TensorTrains, Digital Annealers) not fundamentally different paradigm
- ▶ VQAs NP-Hard to train!

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Variational quantum algorithms are proposed to solve relevant computational problems on near term quantum devices. Popular versions are variational quantum eigensolvers and quantum approximate optimization algorithms that solve ground state problems from quantum chemistry and binary optimization problems, respectively. They are based on the idea of using a classical computer to train a parameterized quantum circuit. We show that the corresponding classical optimization problems are NP-hard. Moreover, the hardness is robust in the sense that, for every polynomial time algorithm, there are instances for which the relative error resulting from the classical optimization problem can be arbitrarily large assuming $P \neq NP$. Even for classically tractable systems composed of only logarithmically many qubits or free fermions, we show the optimization to be NP-hard. This elucidates that the classical optimization is intrinsically hard and does not merely inherit the hardness from the ground state problem. Our analysis shows that the training landscape can have many far from optimal persistent local minima. This means that gradient and higher order descent algorithms will generally converge to far from optimal solutions.

Problems (it's even worse?)

- ▶ Conjecture [G.K., Kungurtsev, Marecek, Zhu]:

Theorem 14 (Undecidability of VQAs). *Assuming that the [Multivariate Diophantine Reducibility](#) Conjecture 13 holds, the decision version of digitized VQA minimization (Problem 11) is undecidable for $L = 58$ layers.*

Theorem 14 then implies that there is no finite-time algorithm to solve the problem, i.e.,

Corollary 15 (Uncomputability of VQAs). *Assuming that the [Multivariate Diophantine Reducibility](#) Conjecture 13 holds, there exists no recursive function to decide digitized VQA minimization in the decision version (Problem 11) for $L = 58$ layers. Consequently, the optimization version is uncomputable for $L = 58$ layers.*

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- ▶ Conjecture [G.K., Kungurtsev, Marecek, Zhu]:

Theorem 14 (Undecidability of VQAs). *Assuming that the [Multivariate Diophantine Reducibility](#) Conjecture 13 holds, the decision version of digitized VQA minimization (Problem 11) is undecidable for $L = 58$ layers.*

Theorem 14 then implies that there is no finite-time algorithm to solve the problem, i.e.,

Corollary 15 (Uncomputability of VQAs). *Assuming that the [Multivariate Diophantine Reducibility](#) Conjecture 13 holds, there exists no recursive function to decide digitized VQA minimization in the decision version (Problem 11) for $L = 58$ layers. Consequently, the optimization version is uncomputable for $L = 58$ layers.*

- ▶ It's fine; LLMs should not work either (I guess)
- ▶ Monthly “mini-breakthroughs” on arxiv/Nature/PRL
- ▶ Conjecture [G.K., Kungurtsev, Marecek, Zhu]: VQAs can decide undecidable languages
- ▶ Slow but steady adoption by top firms

What does a bank do with quantum?

There are several (other) use cases:

- ▶ Fraud detection (QML - NISQ/FTEC)
- ▶ Collateral optimization (VQAs - NISQ)
- ▶ Portfolio optimization (VQAs - NISQ)
- ▶ Risk Management: CVA (QAE - FTEC)
- ▶ Cybersecurity (Schor - FTEC)

Quantum Option Pricing

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Option Pricing using Quantum Computers

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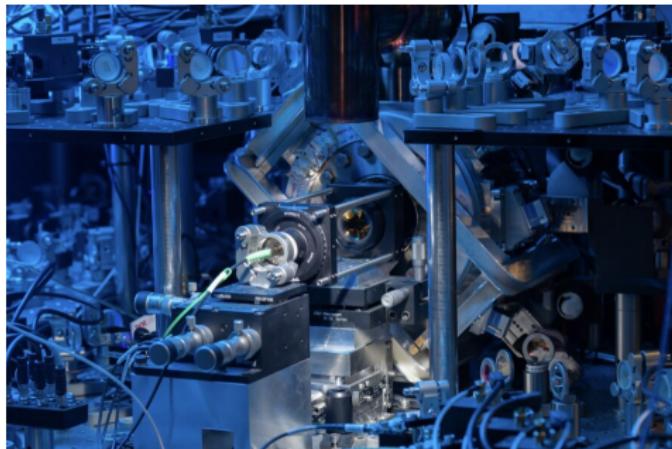
Doi: <https://doi.org/10.22331/q-2020-07-06-291>

Citation: Quantum 4, 291 (2020).

Hardware issues

One of the main problems with quantum computing is hardware.

There are **several** different modalities with many pros and cons.



Issues: scalability, noise reduction, error correction, ...

Development Kits

```
1  from qiskit import QuantumCircuit, Aer, transpile, assemble
2  from qiskit.visualization import plot_histogram, plot_bloch_multivector
3  from math import pi
4
5  def qpe_pre(circuit, qubits):
6      for qubit in range(len(qubits)):
7          circuit.h(qubit)      # Apply H-gate to all qubits
8      return circuit
9
10 def qft_rotations(circuit, n):
11     if n == 0:
12         return circuit
13     n -= 1
14     circuit.h(n)
15     for qubit in range(n):
16         circuit.u1(pi/2**(n-qubit), qubit, n)
17     qft_rotations(circuit, n)
18
19 def swap_registers(circuit, n):
20     for qubit in range(n//2):
21         circuit.swap(qubit, n-qubit-1)
22     return circuit
23
24 def qft(circuit, n):
25     qft_rotations(circuit, n)
26     swap_registers(circuit, n)
27     return circuit
28
29 n_qubits = 3
30 qc = QuantumCircuit(n_qubits)
31
32 qpe_pre(qc, range(n_qubits))
33 qft(qc, n_qubits)
34
35 qc.draw('mpl')
```

Talent Sparsity

Another problem with quantum computing is talent sparsity.

There are **several** needs across the industry

- ▶ quantum physicists,
- ▶ quantum algorithm developer,
- ▶ quantum transpilation engineers,
- ▶ software engineering,
- ▶ ...

Summary

Quantum computing is still a bet, to some extent.

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While many achievements happen and landmarks are reached, we are yet to see the **game changing application** with significant **quantum advantage**...

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While many achievements happen and landmarks are reached, we are yet to see the **game changing application** with significant **quantum advantage**...

Large institutions, governments, and corporations are convinced though. It's an exciting field that has the potential to make LLMs look like toys.

Topics not discussed

There are several “fundamental” topics that were not discussed in this talk including:

- ▶ initial quantum state preparation
- ▶ quantum optimal control and quantum SysId
- ▶ quantum compilation and circuit optimization
- ▶ important algorithms and algorithm development
- ▶ other universal models (quantum Turing machine, quantum walks, etc)
- ▶ hardware modalities and peculiarities
- ▶ quantum startups, business, VCs, etc
- ▶ ...

Thank you!

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