```
In [1]: import pandas as pd
    import statsmodels.api as sm
    from helper import ordinary_lest_squares_regression

%matplotlib inline

#HSBC and ETF data was from Nasdaq and all other columns were from Ken French https://mba.tuck.dartmouth.ec
    df = pd.read_excel("HSBC.ods", engine="odf")

In [2]: # cleaning data, data from French is already expressed in percent
    for column in ["XLF-rf", "IXG-rf", "HSBC-rf", "HSBC with dividends-rf", "HSBC- developed rf", "HSBC with dividend df[column] = pd.to_numeric(df[column], errors='coerce')*100
    df_cleaned = df.dropna()
    print(df_cleaned.info())
    df_cleaned
```

<class 'pandas.core.frame.DataFrame'>
Index: 1202 entries, 53 to 1254
Data columns (total 39 columns):

#	Column	Non-Null Count	Dtype
0	Date	1202 non-null	object
1	HSBC Close/Last	1202 non-null	object
2	Volume	1202 non-null	int64
3	0pen	1202 non-null	object
4	High	1202 non-null	object
5	Low	1202 non-null	object
6	HSBC Dividends	1202 non-null	object
7	HSBC return	1202 non-null	object
8	HSBC price return	1202 non-null	object
9	XLF Close/Last	1202 non-null	float64
10	XLF return	1202 non-null	object
11	IXG Close/Last	1202 non-null	float64
12	IXG return	1202 non-null	object
13	Mkt-RF	1202 non-null	float64
14	SMB	1202 non-null	float64
15	HML	1202 non-null	float64
16	RMW	1202 non-null	float64
17	CMA	1202 non-null	float64
18	RF	1202 non-null	float64
19	XLF-rf	1202 non-null	float64
20	IXG-rf	1202 non-null	float64
21	Banks-rf	1202 non-null	float64
22	Insur-rf	1202 non-null	float64
23	RlEst-rf	1202 non-null	float64
24	Fin -rf	1202 non-null	float64
25	Banks	1202 non-null	float64
26	Insur	1202 non-null	float64
27	RlEst	1202 non-null	float64
28	Fin	1202 non-null	float64
29	HSBC with dividends-rf	1202 non-null	float64
30	HSBC-rf	1202 non-null	float64
31	Developed Mkt-RF	1202 non-null	float64
32	Developed SMB	1202 non-null	float64
33	Developed HML	1202 non-null	float64
34	Developed RMW	1202 non-null	float64
35	Developed CMA	1202 non-null	float64
36	Developed RF	1202 non-null	float64

37 HSBC with dividends - developed rf 1202 non-null float64 38 HSBC- developed rf 1202 non-null float64

dtypes: float64(28), int64(1), object(10)

memory usage: 375.6+ KB

None

Out[2]:

]:	Date	HSBC Close/ Last	Volume	Open	High	Low	HSBC Dividends	HSBC return	HSBC price return	XLF Close/ Last	•••	HSBC with dividends- rf	HSBC-r
	<b>12/31/2024</b>	\$49.46	768225	\$49.78	\$49.86	\$49.40	0	-0.00101	-0.00101	48.33		-1.800990	-1.80099
	<b>12/30/2024</b>	\$49.51	1344573	\$49.22	\$49.66	\$49.11	0	0.004463	0.004463	48.28		-1.253662	-1.25366
	<b>55</b> 12/27/2024	\$49.29	1088110	\$49.03	\$49.32	\$49.01	0	0.000609	0.000609	48.75		-1.639099	-1.63909
	<b>56</b> 12/26/2024	\$49.26	516346	\$49.30	\$49.455	\$49.195	0	0.000203	0.000203	49.11		-1.679695	-1.67969
!	<b>57</b> 12/24/2024	\$49.25	308990	\$48.74	\$49.30	\$48.71	0	0.011501	0.011501	48.99		-0.549867	-0.54986
	•••												
12	<b>50</b> 03/30/2020	\$28.86	4859009	\$28.42	\$28.91	\$28.27	0	-0.000346	-0.000346	21.41		-0.634638	-0.63463
12	<b>51</b> 03/27/2020	\$28.87	6997786	\$28.82	\$29.50	\$28.56	0	-0.041819	-0.041819	21.01		-4.781879	-4.78187
12	<b>52</b> 03/26/2020	\$30.13	7979577	\$29.30	\$30.21	\$29.22	0	0.014478	0.014478	21.67		0.847811	0.84781
12	<b>03</b> /25/2020	\$29.70	7512773	\$29.47	\$30.42	\$29.08	0	0.003717	0.003717	20.39		-0.228253	-0.22825
12.	<b>54</b> 03/24/2020	\$29.59	7844320	\$29.32	\$30.08	\$28.837	0	0.051902	0.051902	19.85		4.590188	4.59018

1202 rows × 39 columns

correlation table

Out[3]:

	Mkt-RF	SMB	HML	RMW	CMA	XLF-rf	IXG-rf	Banks-rf	Insur-rf	RlEst-rf	Fin -
Mkt-RF	1.000000	0.241713	-0.149459	-0.231911	-0.334568	0.667645	0.665665	0.772806	0.701076	0.787788	0.87295
SMB	0.241713	1.000000	0.341334	-0.300474	0.056323	0.336009	0.320983	0.445459	0.210226	0.518404	0.36776
HML	-0.149459	0.341334	1.000000	0.402650	0.602861	0.335870	0.288290	0.398252	0.247018	0.124394	0.14859
RMW	-0.231911	-0.300474	0.402650	1.000000	0.332726	-0.025180	-0.041786	-0.058386	0.041845	-0.203812	-0.18828
СМА	-0.334568	0.056323	0.602861	0.332726	1.000000	-0.016949	-0.020420	-0.070568	0.003107	-0.182833	-0.20497
XLF-rf	0.667645	0.336009	0.335870	-0.025180	-0.016949	1.000000	0.967325	0.814004	0.680716	0.653767	0.77028
IXG-rf	0.665665	0.320983	0.288290	-0.041786	-0.020420	0.967325	1.000000	0.766868	0.642052	0.646327	0.73875
Banks-rf	0.772806	0.445459	0.398252	-0.058386	-0.070568	0.814004	0.766868	1.000000	0.737845	0.774963	0.88644
Insur-rf	0.701076	0.210226	0.247018	0.041845	0.003107	0.680716	0.642052	0.737845	1.000000	0.613500	0.73080
RlEst-rf	0.787788	0.518404	0.124394	-0.203812	-0.182833	0.653767	0.646327	0.774963	0.613500	1.000000	28008.0
Fin -rf	0.872955	0.367765	0.148594	-0.188287	-0.204975	0.770289	0.738759	0.886440	0.730809	0.800856	1.00000
HSBC with dividends- rf	0.407005	0.237129	0.311943	0.045277	0.094175	0.700079	0.761041	0.544512	0.412411	0.431036	0.48985
HSBC-rf	0.402379	0.234949	0.310128	0.045605	0.094390	0.695969	0.756837	0.541191	0.407572	0.426230	0.48559

Out[4]:		Developed Mkt-RF	Developed SMB	Developed HML	Developed RMW	Developed CMA	HSBC with dividends-rf	HSBC-rf
	Developed Mkt- RF	1.000000	-0.360447	-0.064421	-0.147379	-0.303869	-0.019487	-0.021782
	Developed SMB	-0.360447	1.000000	0.202590	-0.230002	0.142094	0.031566	0.028542
	Developed HML	-0.064421	0.202590	1.000000	-0.349174	0.774313	0.003974	0.006831
	Developed RMW	-0.147379	-0.230002	-0.349174	1.000000	-0.075813	0.001535	0.004569
	Developed CMA	-0.303869	0.142094	0.774313	-0.075813	1.000000	0.017086	0.021718
	HSBC with dividends-rf	-0.019487	0.031566	0.003974	0.001535	0.017086	1.000000	0.996183
	HSBC-rf	-0.021782	0.028542	0.006831	0.004569	0.021718	0.996183	1.000000

Both XLF and IXG with Fama-French American factors

```
In [5]: X_columns = ['Mkt-RF', 'SMB', 'HML','RMW', 'CMA', 'XLF-rf',"IXG-rf",'Banks-rf', 'Insur-rf', 'RlEst-rf','Fir

y_to_try = ["HSBC-rf",'HSBC with dividends-rf']
X = sm.add_constant(df_cleaned[X_columns])

for y_tried in y_to_try:
    print(y_tried)
    y = df_cleaned[y_tried]
    results,df_residual = ordinary_lest_squares_regression(y=y,X=X)
```

HSBC-rf

# OLS Regression Results

HSBC-rf	R-squared:	0.620
0LS	Adj. R-squared:	0.617
Least Squares	F-statistic:	176.8
Sun, 30 Mar 2025	<pre>Prob (F-statistic):</pre>	3.25e-241
18:53:34	Log-Likelihood:	-1985.9
1202	AIC:	3996.
1190	BIC:	4057.
11		
	0LS Least Squares Sun, 30 Mar 2025 18:53:34 1202 1190	OLS Adj. R-squared: Least Squares F-statistic: Sun, 30 Mar 2025 Prob (F-statistic): 18:53:34 Log-Likelihood: 1202 AIC: 1190 BIC:

Covariance Type: nonrobust

=========						========
	coef	std err	t	P> t	[0.025	0.975]
const	0.0007	0.052	0.013	0.990	-0.101	0.102
Mkt-RF	-0.2500	0.104	-2.413	0.016	-0.453	-0.047
SMB	-0.0320	0.064	-0.497	0.619	-0.158	0.094
HML	0.0029	0.081	0.036	0.971	-0.156	0.162
RMW	0.1345	0.073	1.851	0.064	-0.008	0.277
CMA	0.2209	0.091	2.430	0.015	0.043	0.399
XLF-rf	-0.7657	0.097	-7.882	0.000	-0.956	-0.575
IXG-rf	1.7667	0.094	18.876	0.000	1.583	1.950
Banks-rf	0.2032	0.074	2.756	0.006	0.059	0.348
Insur-rf	-0.1333	0.049	-2.714	0.007	-0.230	-0.037
RlEst-rf	-0.0133	0.037	-0.362	0.717	-0.086	0.059
Fin -rf	0.0319	0.072	0.441	0.659	-0.110	0.174
Omnibus:	========	======================================	======= 984 Durbir	======== n-Watson:	=======	2.150
Prob(Omnibus	s):	0.0	900 Jarque	e-Bera (JB):		2342.546
Skew:	-	-0.				0.00
Kurtosis:		9.	839 Cond.	•		15.2
=========		:=======	========		=======	=======

#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified. HSBC with dividends-rf

## OLS Regression Results

Dep. Variable: HSBC with dividends-rf R-squared: 0.626

Model: 0LS Adj. R-squared: 0.622
Method: Least Squares F-statistic: 181.0

Date:	Sun, 30 Mar 2025	<pre>Prob (F-statistic):</pre>	6.10e-245
Time:	18:53:34	Log-Likelihood:	-1966.7
No. Observations:	1202	AIC:	3957.
Df Residuals:	1190	BIC:	4018.
Df Modol.	11		

Df Model: 11 Covariance Type: nonrobust

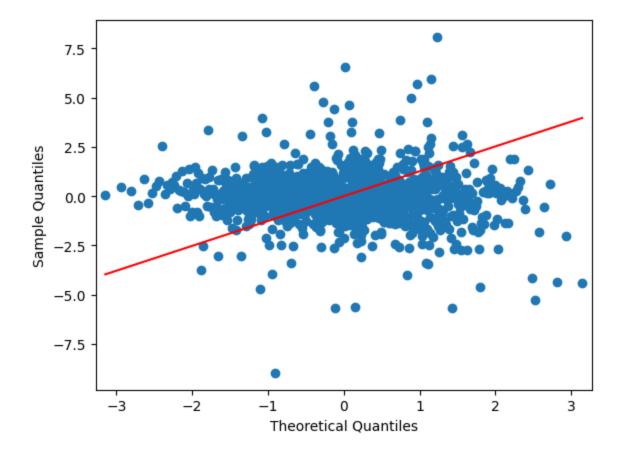
=========						=======
	coef	std err	t	P> t	[0.025	0.975]
const	0.0101	0.051	0.198	0.843	-0.090	0.110
Mkt-RF	-0.2266	0.102	-2.223	0.026	-0.427	-0.027
SMB	-0.0320	0.063	-0.505	0.613	-0.156	0.092
HML	0.0225	0.080	0.283	0.777	-0.134	0.179
RMW	0.1290	0.072	1.803	0.072	-0.011	0.269
CMA	0.2091	0.089	2.337	0.020	0.034	0.385
XLF-rf	-0.7568	0.096	-7.916	0.000	-0.944	-0.569
IXG-rf	1.7514	0.092	19.014	0.000	1.571	1.932
Banks-rf	0.1813	0.073	2.499	0.013	0.039	0.324
Insur-rf	-0.1277	0.048	-2.642	0.008	-0.223	-0.033
RlEst-rf	-0.0103	0.036	-0.283	0.777	-0.081	0.061
Fin -rf	0.0313	0.071	0.440	0.660	-0.108	0.171
Omnibus:		181.	======= 172 Durbin	 Watson:		2.159
Prob(Omnibus	s):	0.0	900 Jarque	e-Bera (JB):		2574.319
Skew:		0.0	956 Prob(J	B):		0.00
Kurtosis:		10.	169 Cond.	No.		15.2

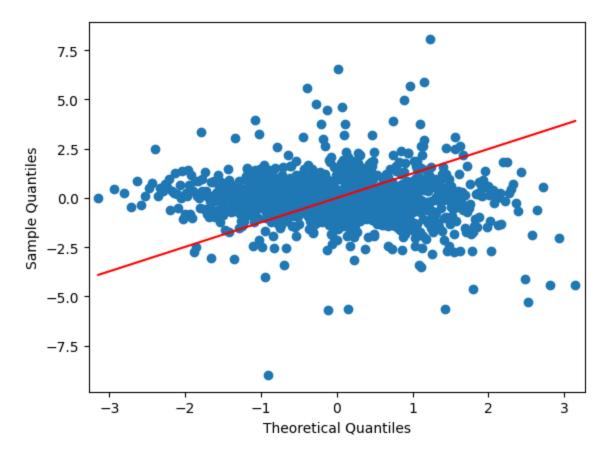
#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

/home/george/HSBC/helper.py:12: UserWarning: FigureCanvasAgg is non-interactive, and thus cannot be shown
plot.show()

/home/george/HSBC/helper.py:12: UserWarning: FigureCanvasAgg is non-interactive, and thus cannot be shown
plot.show()





```
In [6]: X_columns = ['Mkt-RF', 'SMB', 'HML','RMW', 'CMA', "IXG-rf",'Banks-rf', 'Insur-rf', 'RlEst-rf','Fin -rf']

y_to_try = ["HSBC-rf",'HSBC with dividends-rf']
X = sm.add_constant(df_cleaned[X_columns])

for y_tried in y_to_try:
    print(y_tried)
    y = df_cleaned[y_tried]
    results,df_residual = ordinary_lest_squares_regression(y=y,X=X)
```

HSBC-rf

## OLS Regression Results

Dep. Variable:	HSBC-rf	R-squared:	0.601
Model:	0LS	Adj. R-squared:	0.597
Method:	Least Squares	F-statistic:	179.1
Date:	Sun, 30 Mar 2025	<pre>Prob (F-statistic):</pre>	2.89e-229
Time:	18:53:34	Log-Likelihood:	-2016.5
No. Observations:	1202	AIC:	4055.
Df Residuals:	1191	BIC:	4111.
Df Model:	10		

Dt Model: 10 Covariance Type: nonrobust

========	========	=======	=======		=======	========
	coef	std err	t	P> t	[0.025	0.975]
const	0.0789	0.052	1.513	0.131	-0.023	0.181
Mkt-RF	-0.1276	0.105	-1.215	0.225	-0.334	0.078
SMB	-0.0268	0.066	-0.406	0.684	-0.156	0.103
HML	0.0126	0.083	0.152	0.879	-0.150	0.175
RMW	0.1211	0.074	1.626	0.104	-0.025	0.267
CMA	0.2466	0.093	2.647	0.008	0.064	0.429
IXG-rf	1.0881	0.038	28.910	0.000	1.014	1.162
Banks-rf	0.0663	0.073	0.902	0.367	-0.078	0.210
Insur-rf	-0.1919	0.050	-3.854	0.000	-0.290	-0.094
RlEst-rf	0.0066	0.038	0.176	0.861	-0.067	0.081
Fin -rf	-0.0394	0.074	-0.535	0.593	-0.184	0.105
Omnibus:	=======	======================================	.851 Durb	======= in-Watson:	=======	2.116
Prob(Omnibu	s):	0	.000 Jarq	ue-Bera (JB)	:	1994.070
Skew:	•	- 0		(JB):		0.00
Kurtosis:				. No.		13.1
========	========	========		========	:=======	========

#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified. HSBC with dividends-rf

## OLS Regression Results

Dep. Variable: HSBC with dividends-rf R-squared: 0.606
Model: 0LS Adj. R-squared: 0.603
Method: Least Squares F-statistic: 183.3
Date: Sun, 30 Mar 2025 Prob (F-statistic): 6.95e-233

Time:	18:53:34	Log-Likelihood:	-1997.5
No. Observations:	1202	AIC:	4017.
Df Residuals:	1191	BIC:	4073.

Df Model: 10 Covariance Type: nonrobust

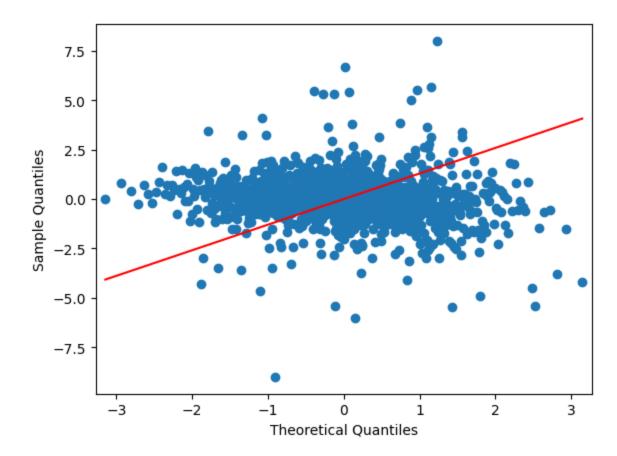
	coef	std err	t	P> t	[0.025	0.975]
const	0.0874	0.051	1.703	0.089	-0.013	0.188
Mkt-RF	-0.1056	0.103	-1.022	0.307	-0.308	0.097
SMB	-0.0269	0.065	-0.414	0.679	-0.154	0.101
HML	0.0321	0.082	0.393	0.694	-0.128	0.192
RMW	0.1157	0.073	1.578	0.115	-0.028	0.260
CMA	0.2345	0.092	2.558	0.011	0.055	0.414
IXG-rf	1.0806	0.037	29.170	0.000	1.008	1.153
Banks-rf	0.0460	0.072	0.636	0.525	-0.096	0.188
Insur-rf	-0.1856	0.049	-3.787	0.000	-0.282	-0.089
RlEst-rf	0.0095	0.037	0.255	0.799	-0.063	0.082
Fin -rf	-0.0391	0.072	-0.540	0.589	-0.181	0.103
Omnibus:		170.9	 917 Durbin			2.122
Prob(Omnibu	s):	0.0	900 Jarque	-Bera (JB):		2180.660
Skew:		0.0	927 Prob(J	B):		0.00
Kurtosis:		9.5	598 Cond.	No.		13.1

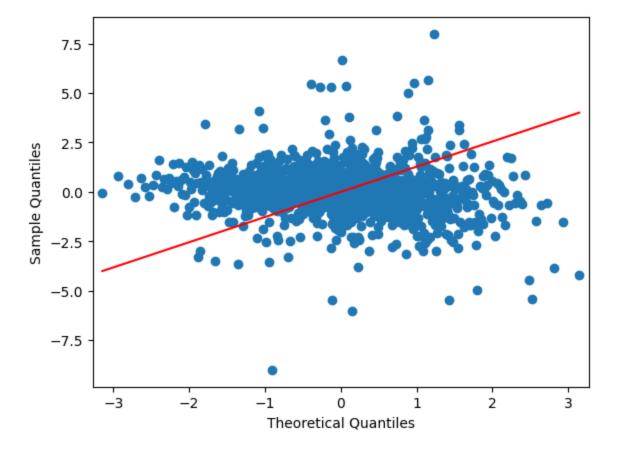
### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

/home/george/HSBC/helper.py:12: UserWarning: FigureCanvasAgg is non-interactive, and thus cannot be shown
plot.show()

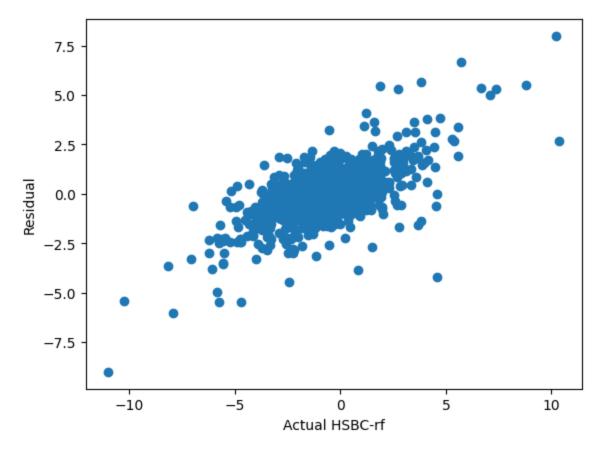
/home/george/HSBC/helper.py:12: UserWarning: FigureCanvasAgg is non-interactive, and thus cannot be shown
plot.show()





```
In [7]: from matplotlib import pyplot as plt

fig = plt.figure()
ax = fig.add_subplot()
ax.set_xlabel("Actual HSBC-rf")
ax.set_ylabel("Residual")
ax.plot(df_cleaned["HSBC-rf"],df_residual["error"],'o')
plt.show()
```



Both XLF and IXG with Fama-French Developed factors

0.071

HSBC- developed rf

# OLS Regression Results

Dep. Variable: Model: Method: Date: Time: No. Observations: Df Residuals: Df Model: Covariance Type:	HSBC- deve Least Sun, 30	HSBC- developed rf OLS		R-squared: Adj. R-squared: F-statistic: Prob (F-statistic): Log-Likelihood: AIC: BIC:		445 440 5.64 143 79.6 883.
	coef	std err	t	P> t	[0.025	0.975]
const Developed Mkt-RF Developed SMB Developed HML Developed RMW Developed CMA XLF-rf IXG-rf Banks-rf Insur-rf	-0.0030	0.053 0.117 0.135 0.175 0.207 0.112 0.108 0.065		0.000 0.790 0.980 0.635 0.120 0.307 0.000 0.000 0.000	-0.118 -0.232 -0.329 -0.615 -0.195 -1.437 1.408 0.480	-0.154 0.089 0.226 0.201 0.071 0.619 -0.997 1.831 0.735
RlEst-rf Fin -rf	-0.0788 -0.0672	0.037 0.070	-2.122 -0.956	0.034 0.339		-0.006 0.071

Omnibus:	124.260	Durbin-Watson:	1.714		
Prob(Omnibus):	0.000	Jarque-Bera (JB):	899.171		
Skew:	0.103	<pre>Prob(JB):</pre>	5.59e-196		
Kurtosis:	7.232	Cond. No.	21.2		

#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified. HSBC with dividends - developed rf

### OLS Regression Results

\_\_\_\_\_\_ Dep. Variable: HSBC with dividends - developed rf R-squared: 0.448 OLS Adj. R-squared: 0.443 Model: Least Squares F-statistic: 87.97 Method:

3/30/25, 19:12 15 of 32

Date:	Sun, 30 Mar 2025	<pre>Prob (F-statistic):</pre>	2.78e-145
Time:	18:53:34	Log-Likelihood:	-2165.0
No. Observations:	1202	AIC:	4354.
Df Residuals:	1190	BIC:	4415.
Df Model:	11		

Covariance Type: nonrobust

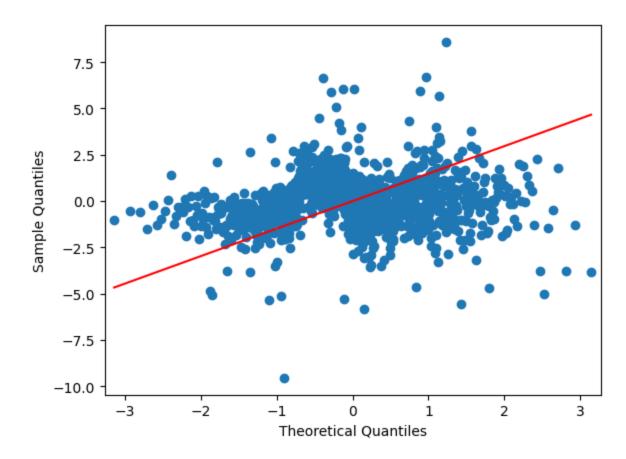
	coef	std err	t	P> t	[0.025	0.975]
const	-0.2620	0.060	-4.391	0.000	-0.379	-0.145
Developed Mkt-RF	-0.0088	0.052	-0.169	0.866	-0.111	0.093
Developed SMB	0.0162	0.115	0.140	0.888	-0.210	0.242
Developed HML	-0.0719	0.133	-0.539	0.590	-0.333	0.190
Developed RMW	-0.2905	0.173	-1.683	0.093	-0.629	0.048
Developed CMA	0.1950	0.205	0.952	0.341	-0.207	0.597
XLF-rf	-1.2098	0.111	-10.929	0.000	-1.427	-0.993
IXG-rf	1.6069	0.106	15.097	0.000	1.398	1.816
Banks-rf	0.5973	0.064	9.313	0.000	0.471	0.723
Insur-rf	-0.0104	0.052	-0.199	0.843	-0.113	0.092
RlEst-rf	-0.0736	0.037	-2.007	0.045	-0.146	-0.002
Fin -rf	-0.0627	0.069	-0.903	0.367	-0.199	0.073
Omnibus:		128.915	Durbin-Watson:		1.708	
<pre>Prob(Omnibus):</pre>		0.000	Jarque-Bera (JB):		929.661	
Skew:		0.162	Prob(JB):		1.34e-202	
Kurtosis:		7.296	Cond. No. 21.		1.2	

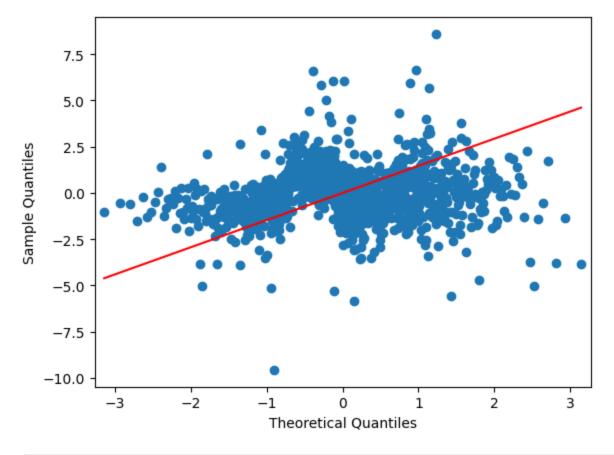
#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

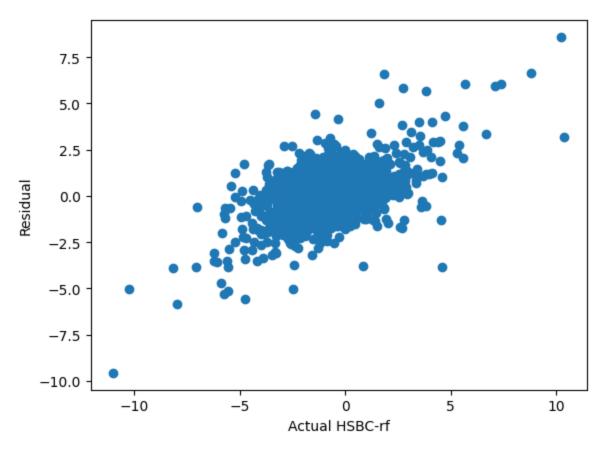
/home/george/HSBC/helper.py:12: UserWarning: FigureCanvasAgg is non-interactive, and thus cannot be shown
plot.show()

/home/george/HSBC/helper.py:12: UserWarning: FigureCanvasAgg is non-interactive, and thus cannot be shown
plot.show()

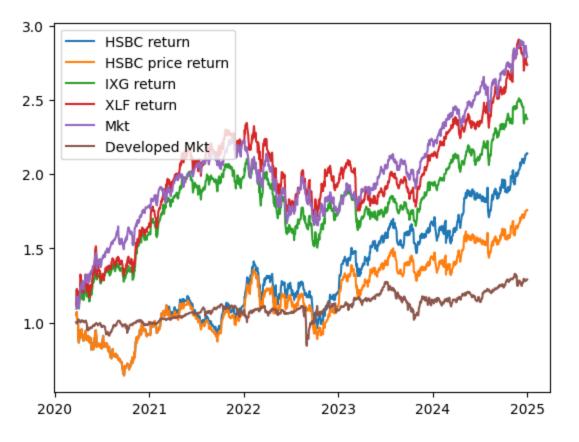




```
In [9]: fig = plt.figure()
    ax = fig.add_subplot()
    ax.set_xlabel("Actual HSBC-rf")
    ax.set_ylabel("Residual")
    ax.plot(df_cleaned["HSBC-rf"],df_residual["error"],'o')
    plt.show()
```



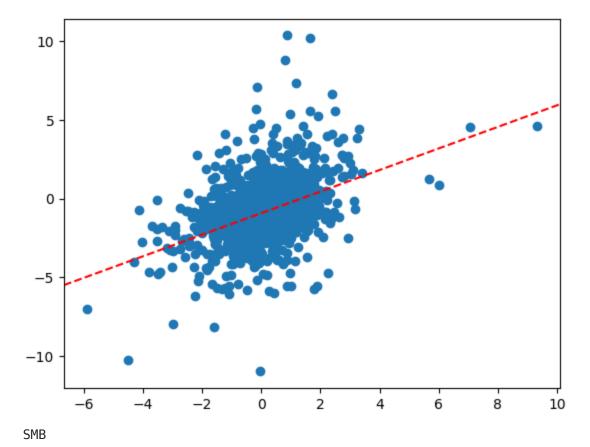
```
columns to plot = [f"cumulative {column}" for column in cumulative returns]
         df reversed["Date"] = pd.to datetime(df reversed["Date"])
         def clean label(some str):
             if "-RF" in some str:
                 some_str = some_str[:-3]
             return some str[len("cumulative "):]
         for column in columns to plot:
             plt.plot(df reversed["Date"] ,df reversed[column],label = clean label(column))
         plt.legend()
        /tmp/ipykernel 202542/934776928.py:18: SettingWithCopyWarning:
        A value is trying to be set on a copy of a slice from a DataFrame.
        Try using .loc[row indexer,col indexer] = value instead
        See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html
        #returning-a-view-versus-a-copy
          df_reversed["Date"] = pd.to_datetime(df_reversed["Date"])
Out[10]: <matplotlib.legend.Legend at 0x79e44eb7ad80>
```

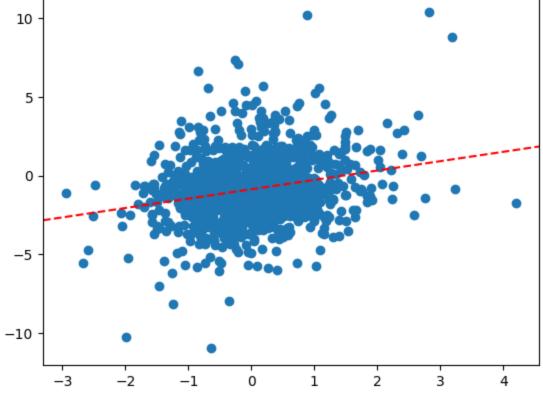


Plots of HSBC on the Y and selected factors

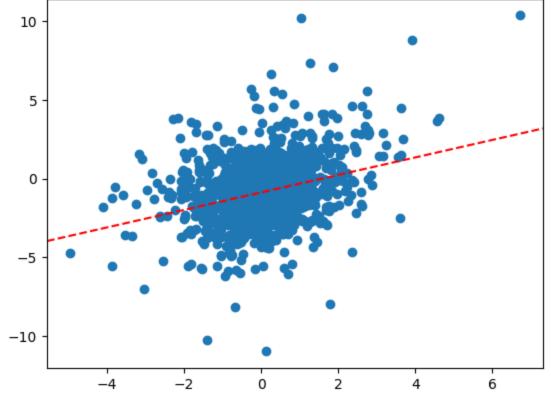
Mkt-RF

 $21 { of } 32$  3/30/25, 19:12

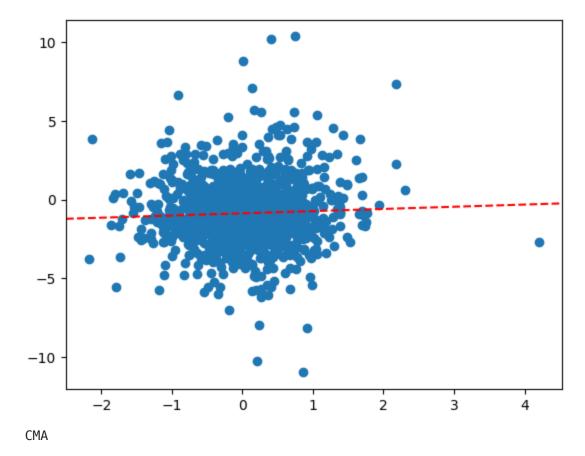


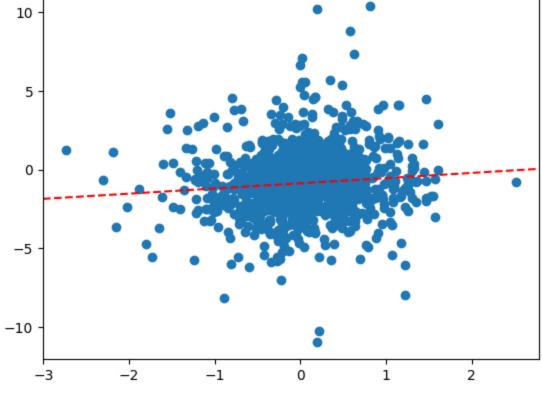


HML

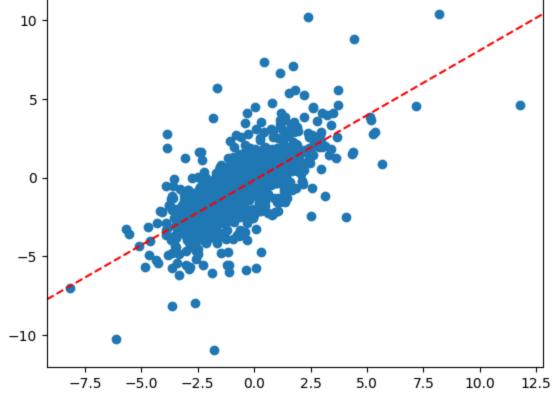


 $\mathsf{RMW}$ 

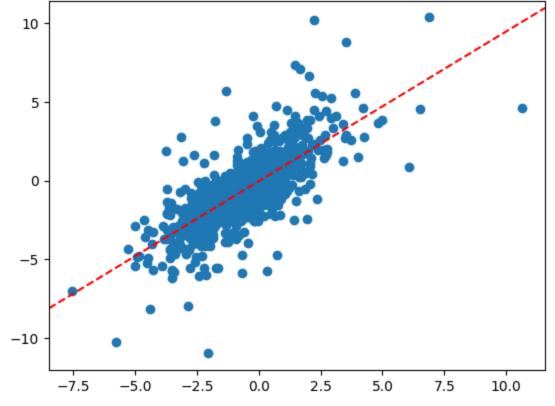




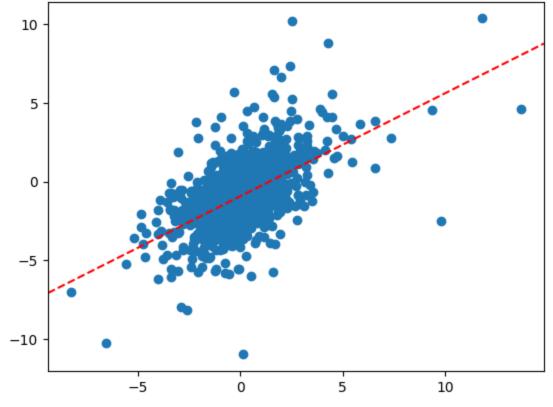
XLF-rf



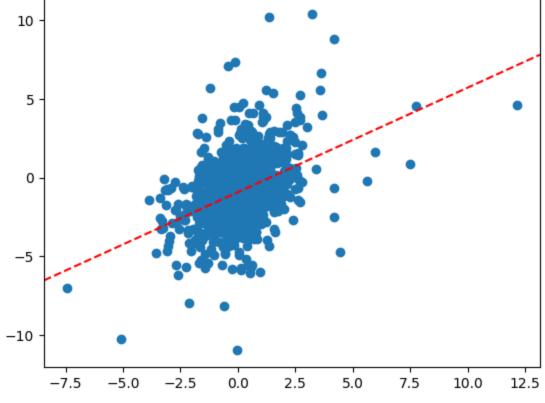
IXG-rf



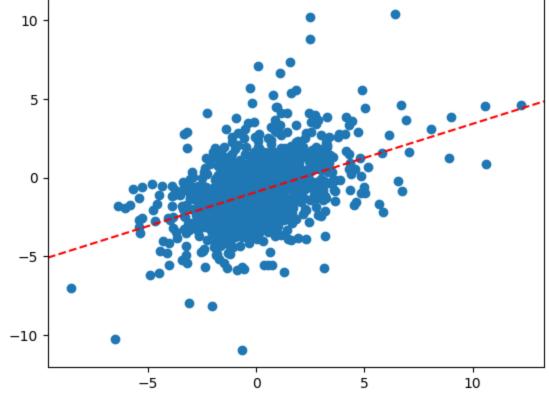
Banks-rf



Insur-rf



RlEst-rf



Fin -rf

