

```

% Question 3
clc; clear all; close all;

N = [5,10,20,40,80,160,320,640,1280];
f = [];

n = 10^4;
h = 1/(n+1);
tri = full(gallery('tridiag',n,1,-2,1));
func = @(x) (4*pi)^2*cos(4*pi*x)*h^2;
f1 = [];
x1 = [];
for i=1:n
    x1(i) = h*i;
    f1(i) = func(x1(i));
end
f1(n) = f1(n) - 2;
x1 = [0 x1 1];
x1 = x1';
u1 = tri\f1';
u1 = [0;u1;2];

for i=1:9
    n = N(i);
    h = 1/(n+1);
    tri = full(gallery('tridiag',n,1,-2,1));
    x = [];
    func = @(x) (4*pi)^2*cos(4*pi*x)*h^2;

    for j=1:n
        x(j) = h*j;
        f(j) = func(x(j));
    end
    f(n) = f(n) - 2;
    f(1) = 0;
    x = [0 x 1];
    x = x';
    u = tri\f';
    u = [0;u;2];
    E = [];

    for j=1:n
        E(j) = (u(j) - u1(j))^2;
    end
    E_sum = sum(E);
    E_final = sqrt(E_sum);
    e = E_final/n;
    E_vec(i) = E_final;
    e_vec(i) = e;
end

loglog(1./N,E_vec)
hold on
loglog(1./N,e_vec)
hold on

title('E and e vs. 1/h')
legend('E', 'e')
xlabel('1/h')
dim = [.2 .4 .3 .2];
str = 'We can see that E is order O(h) while e is O(h^2)';
annotation('textbox', dim, 'String', str, 'FitBoxToText', 'on');

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