

$$\textcircled{1} \quad u_i^* = u_i^N - \frac{k}{h} (f(u_{i+1}^N) - f(u_i^N))$$

$$u_i^{N+1} = \frac{[u_i^N - \frac{k}{h} (f(u_{i+1}^N) - f(u_i^N))] + u_i^N}{2} - \frac{k}{2h} [f(u_i^*) - f(u_{i-1}^*)]$$

$$u_i^{N+1} = u_i^N - \frac{k}{2h} [f(u_{i+1}^N) - f(u_i^N) + f(u_i^*) - f(u_{i-1}^*)]$$

$$F_i^L = [f(u_{i-1}^*) + f(u_i^N)]$$

$$F_i^R = [f(u_{i+1}^N) + f(u_i^*)]$$

$$u_i^{N+1} = u_i^N - \frac{k}{2h} [F_i^R - F_i^L]$$

This method is conservative because it finds the solution at the next time step,  $(u^{N+1})$ , using the solution from the previous step,  $(u^N)$ , combined with the difference of the numerical flux terms around the point  $[F_i^R - F_i^L]$ .