

1 e.) a) units of eigenvalues: speed,  $m/s$

b) units of  $f_1, f_2$ :  $f_1 = \frac{kg}{m^2 \cdot s}$ ,  $f_2 = \frac{kg}{m \cdot s^2}$

c) units of  $u$ :  $u_1 = kg/m^3$ ,  $u_2 = kg/m^2 \cdot s$

d) Yes, the eigenvalues depend on the state vector because they include  $u$ , which is  $u_2/u_1$ .

e)  $\lambda_2$  will always be positive as long as  $u$  is positive.

$$\lambda_1 = u - a = Ma - a = a(m-1).$$

$\lambda_1 = a(m-1)$ . We see that  $\lambda_1$  is positive when  $m \geq 1$ , and negative when  $m < 1$ . (Assuming positive velocity).