

4. $u_{i+1} = u_i + u'(x_i)h + u''(x_i)\frac{h^2}{2!}$
 $u_{i+2} = u_i + 2hu'(x_i) + 2h^2u''(x_i)$

$$u'(x_i)h = au_i + bu_{i+1} + cu_{i+2}$$

$$u'(x_i)h = au_i + b\left[u_i + u'(x_i)h + u''(x_i)\frac{h^2}{2}\right] + c\left[u_i + 2hu'(x_i) + 2h^2u''(x_i)\right]$$

$$u'(x_i)h = \cancel{1}au_i + \cancel{1}bu_i + \cancel{(b)}u'(x_i)h + \cancel{(b)}u''(x_i)\frac{h^2}{2} + \cancel{(c)}u_i + \cancel{(c)}2hu'(x_i) + \cancel{(c)}2h^2u''(x_i)$$

$$a + b + c = 0$$

$$b + 2c = 1$$

$$\frac{b}{2} + 2c = 0$$

$$a = -\frac{3}{2}, b = 2, c = -\frac{1}{2}$$