

# End of First Year Report

Draft

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## 1 Introduction

Ocean eddies are the subject of many ongoing investigations into ocean dynamics. The topic comprises a broad range of smaller-scale dynamics and relationships at varying scales. From energy transfer to blah blah \*citations\*, researchers are still trying to get a better understanding of the internal dynamics of the ocean. \*citations\*. Our main focus will be on the area of the Gulf Stream and mainly the interaction and effect of the bathymetry on the separation and subsequent path of the Gulf Stream.

### 1.1 The impact of an accurately resolved Gulf Stream

- Impact on other weather events - e.g. (Scaife *et al.*, 2011)
- Effect on other ocean processes and circulation - "blue spot of death"

The Gulf Stream is part of the AMOC and is essential to transferring heat from the Gulf of Mexico at lower latitudes towards western and northern Europe. Fundamentally it gives north-western Europe its mild climate and thus has large impacts on the weather and climate as the heat is transferred into the atmosphere. This can have wide ranging effects on weather prediction notably winter blocking (Scaife *et al.*, 2011) and \*other citation\* . Many lower resolution models render an unrealistic Gulf Stream, with the separation from the U.S. coast too far to the South, causing an inaccurate path from this point onwards. This obviously has a knock-on effect as the corresponding sea surface temperatures (SSTs) are much higher/lower than observed in the surrounding areas (Greatbatch *et al.*, 2004). The cold bias in the North West corner of the Atlantic resulting from a poorly placed Gulf Stream has become known as the "blue spot of death" (Gnanadesikan, Griffies, and Samuels, 2007) to modellers due to the inaccuracies. The Northern Recirculation Gyre (NRG) interacts with the Gulf Stream and it has been noted by (Zhang and Vallis, 2007) and (Ezer, 2016) that the representation of the Gulf Stream can have large effects on the energy modelled within the NRG . A lethargic NRG subsequently affects the \*citations\*/TODO find out about this\* and hence we can see that a poorly resolved Gulf Stream can have much wider implications throughout the model.

Haven't added citations

I'm sure I read about cyclones somewhere - find citation

check this is the right citation

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& the sub-

## 1.2 Problems and Restrictions

Higher resolution models have been shown to provide a more realistic Gulf Stream path <sup>\*citations\*</sup>, however this comes at a cost requiring more processing power and thus a higher price for the model. It is generally understood <sup>\*citations\*</sup> (Nikurashin, Vallis, and Adcroft, 2012) etc. <sup>\*</sup> that this improvement is due to the higher resolution models being able to resolve small-scale processes which are lost in the coarser resolution counterparts. (Ezer, 2016) suggests that to replicate an accurate Gulf Stream separation, the model not only needed to resolve the Gulf stream but also the northern branches of NRG, the southward slope and shelf currents. <sup>. \*citation\*</sup> It is also thought that the lack of detailed representation of the bathymetry in key areas play a large role in the unrealistic Gulf Stream path. <sup>\*citation\*</sup> posed that it is the interaction with the bathymetry and the consequential small-scale processes which cause the Gulf Stream to split off from the coast at Cape Hatteras and direct its path from there. The bathymetry itself can be represented in many different ways and the vertical coordinate system chosen has a large impact on the interaction of the ocean dynamics and the ocean floor. (Ezer, 2016) revisited a discussion on different vertical coordinate systems and their effect on the path of the Gulf Stream, though noted that the tested z-coordinate system did not include any partial or shaved cells.

Could the bathymetry cause an unresolved northern branches of NRG?

partial & shaved cells - Mike's paper?

## 2 Background

Tell a story up to where we are and what's missing.

### 2.1 Literature Review (take most from coursework). Cover the various angles including:

- Modelling & vertical grid systems - include partial cells
- Turbulence and bathymetry - understanding the smaller processes (vorticity etc.) (Tansley and Marshall, 2001) (Nikurashin, Vallis, and Adcroft, 2012)
- Possible relationships/data sets to see the history of the Gulf Stream. (Palaeo?) (Ezer, 2015)
- Include some phenomenology - e.g. bottom vortex stretching and bottom pressure torque. Maybe also the weird sandwich diagram!

Cut down lit review - parts of it will be elsewhere!! (or should be! OR Remove them from elsewhere to keep them here!!)

## 3 Lit Review as is.... Need to update it /TODOupdate!!

### 3.1 Introduction

Ocean eddies are the subject of many ongoing investigations into ocean circulation. The topic comprises a broad range of dynamics and relationships at varying scales. By interpreting data and assessing the accuracy of models, scientists aim to gain a better understanding of the processes that govern the oceans.

Vast amounts of energy are contained within the ocean and it is still not fully understood how this energy is transported or dissipated into other processes (Nikurashin, Vallis, and Adcroft, 2012). These processes which are still being questioned could provide insight into some of the areas that ocean models struggle to accurately represent.

One key area is the Gulf Stream, which despite being reasonably well represented in high resolution models, tends to be problematic in moderate and low resolution models (Zhang and Vallis, 2007). This review aims to discuss the various problems associated with modelling the Gulf Stream, with specific attention to the effect of bathymetry on its separation and subsequent path.

## 3.2 Background

The Gulf stream is part of the Atlantic Meridional Overturning Circulation (AMOC) and together with its extension, the North Atlantic Drift, carries warm water from the Gulf of Mexico, up the Florida coast, and then across to Western Europe. The resulting heat transported by the Gulf Stream contributes to the mild climate in Western Europe. Hence, understanding the Gulf Stream is important to obtain more accurate weather forecasts, as well as providing insight into the processes governing the dynamics themselves. It has been noticed that the Gulf Stream is slowing down and weakening over time (Greatbatch, Fanning, and Goulding, 1991). This could have a significant impact on European weather, as an accurately resolved Gulf Stream in climate models has been linked to improved Atlantic winter blocking (Scaife *et al.*, 2011). (Ezer, 2015) also investigated Atlantic circulation changes as a contributing factor to floods between Cape Hatteras and Cape Cod in the U.S., and sought a relationship between various currents and circulation in the North Atlantic with sea level changes on the Eastern coast of America. As observational data to determine the strength of the Gulf Stream has only been available for several decades, little is known about the evolution of the Gulf Stream over time.

A good understanding of the Gulf Stream and its contributing factors is crucial for improved climate and ocean models. The misrepresentation can not only lead to inaccurate but also false data. The warm and cold biases in sea surface temperatures (SSTs) throw off climate predictions and could be obscuring climate change predictions (?).

### 3.2.1 Gulf Stream Separation

The Gulf stream separates at Cape Hatteras, skirts the Grand Banks at Newfoundland and then heads Eastwards towards western Europe. However, in many moderate resolution climate models this separation occurs further north than observed and turns more sharply to the East, as noted in (?) and often misses off the Grand Banks, heading straight towards Europe. This can lead to what modellers refer to as the "blue spot of death" (Gnanadesikan, Griffies, and Samuels, 2007), a patch of colder than observed SSTs resulting from the lack of heat at Newfoundland normally brought up by the Gulf Stream.

The exact cause for the path of the Gulf Stream is unknown, though it has been a research topic for many years and is still a popular topic amongst researchers today. A recurring theme when looking into the separation of the Gulf Stream is the mention of bathymetry. It is thought (?) (Naveira Garabato *et al.*, 2013) (Nikurashin, Vallis, and Adcroft, 2012) that the ocean dynamics resulting from the interaction of the Gulf Stream and the deep western boundary current (DWBC) with the bathymetry in the North Atlantic could cause the turbulence required to direct the Gulf Stream along its path. A sudden change in the direction of the Gulf Stream just off the coast at South Carolina and Georgia has been attributed to the Charleston Bump, a topographical feature which raises the ocean floor, from a depth of 600m on the surrounding Blake Plateau to 200m (?). Hence it is clear that bathymetry can strongly impact the direction of ocean currents.

### 3.2.2 Small-scale Processes

It has been noted that in higher resolution models, the separation and subsequent path of the Gulf Stream is much more accurate than in the lower resolution counterparts (?) (Zhang and Vallis, 2007). This lends to the idea that the processes which affect the Gulf Stream occur on smaller scales which aren't resolved by coarser models (Naveira Garabato *et al.*, 2013) (Nikurashin, Vallis, and Adcroft, 2012). Various processes have been investigated and suggested as the main influences though it is likely that the improved Gulf Stream representation is due to multiple factors.

(Naveira Garabato *et al.*, 2013) theorised that interaction with the bathymetry creates small-scale turbulence and instabilities which could cause bathymetric steering and divert currents. If this is not being represented in coarser models, the energy behind the turbulence must be going elsewhere. (?) compared current meter readings with modelled values for kinetic energy and noticed that in some areas of the North Atlantic the total kinetic energy was being held higher in models than observed. It is discrepancies such as this which could have much wider implications. If the energy is not penetrating to the ocean floor, we cannot expect to be able to replicate the effects of the bathymetry. Perhaps by pulling this energy further down (closer to observed values), there would be more energy transfer from the larger ocean eddies to the smaller scale turbulence resulting from interaction with the bathymetry.

(Tansley and Marshall, 2001) used a simplified model of water flowing past a cylinder to highlight the importance of turbulence on fluid motion. Using a quarter-cylinder (mimicking a simplified version of Cape Hatteras) and a high Reynolds number (allowing for more turbulent flow), the model produced a jet with surrounding turbulent eddies similar to those observed in the Gulf Stream. These results were not seen with a lower Reynolds number, highlighting the importance of turbulence in forming jets like the Gulf Stream.

The turbulent mixing arising from interaction with the bathymetry could allow geostrophic eddies to transfer some of their energy to smaller processes by causing internal waves to break and contribute to enhanced mixing (Nikurashin, Vallis, and Adcroft, 2012). These effects have been seen even in cases of small-scale bathymetric roughness suggesting that it is not necessary to have large topological features to impact ocean dynamics, instead small surface differences can cause changes which lead to bigger outcomes.

(Naveira Garabato *et al.*, 2013) attribute the significant impact of small-scale bathymetry to wave drag. Although wave drag is not a large contributor to ocean dynamics, topological features on a small scales can cause wave drag which contributes ten to several tens of a percentage of the dominant source and sink terms influencing the vorticity of the ocean.

These effects of small-scale processes are not limited to the Gulf Stream, but impact on many aspects of ocean dynamics as the various currents and features affect one another. (?) speculated that amongst other things, the northern branches of the Northern Recirculation Gyre (NRG) would have to be resolved in order to produce an accurate Gulf Stream in a model. (Zhang and Vallis, 2007) determined that a significant contribution to the generation of the NRG is the bottom vortex stretching resulting from a downslope DWBC, which is in turn the result of the interaction with bathymetry as the DWBC crosses the path of the Gulf Stream. Hence, bathymetric impact can circle around to affect many aspects of ocean dynamics.

### 3.2.3 Modelling the Gulf Stream

As more scientists seek to understand ocean dynamics, more models are made and used by different researchers to simulate different processes. There are many models in use today, all with different configurations and settings. This can lead to contrasting outcomes and debate over which choice of model or model settings yields the most accurate results.

## Model Resolution

**A** long with differing numerical schemes or boundary conditions, etc. there are also many different model resolutions available. These range from coarse  $1^\circ$  models, which resolve to a scale of  $\approx 100\text{km}$ , to higher resolution  $0.25^\circ$  models, which resolve to a scale of  $\approx 25\text{km}$ , all with varying numbers of vertical levels. It is well established (Scaife *et al.*, 2011)(?) that a higher resolution ocean model tends to produce a more accurately resolved Gulf Stream. This is in part due to the small scale processes, mentioned previously, which contribute to the ocean circulation, but are not resolved in the coarser models. Unfortunately higher resolution models require additional processing power and thus additional costs. This means that the high resolutions required to resolve a realistic Gulf Stream will not be widely used for some time. Hence, the aim is to find a way to represent an accurate Gulf Stream in the lower resolution models by understanding the reasons behind it.

## Vertical Coordinate System

**O** ne of the main variabilities between different models is the handling of the vertical coordinate system. The way in which the model splits the depth of the ocean into 'levels' can have a large impact on the way the bathymetry is represented. As previously discussed, this bathymetric representation can have large impacts on the dynamics within the model. The importance and significance of the bathymetric roughness has already been discussed in this review so it is now necessary to discuss the different ways to represent this.

**T** he main coordinate systems in use are the z-coordinate system which stays true to a cartesian system of coordinates, consisting of rectangular 'blocks', which create a staircase effect when representing slopes. These z-coordinate systems can also be implemented with 'partial cells' whereby some of the cells are cut into smaller cells to 'smooth out' and more closely represent the shape of the slopes. There are also s- (or sigma-) coordinates which follow the shape of the terrain. The depth at any point is divided by the number of levels to create a consistent number of cells at all points of different thickness. These different approaches can also be combined to form hybrid coordinate systems. See Figure 1 for an illustration of some of the possible vertical coordinate systems available in the NEMO model.

**T** he main difficulty in comparing different vertical coordinate systems lies in the availability of a 'control' case for the comparison. With the wide selection of models available to researchers, it is not only the vertical coordinate system which differs but also the numerical schemes being used to resolve various processes. This could lead to false similarities or differences and cause incorrect conclusions. (?) was able to compare results from z-coordinate models and s-coordinate models while minimising any other differences between the models. Although the z-coordinate models are capable of producing an accurate Gulf Stream at high resolutions, the s-coordinate models provided a more accurate representation when restricted with coarser models. However, as (?) noted in the comparison, partial and shaved cells (whereby corners of the cells are 'shaved' off to smooth out slopes) were not used in any of these models.

## 3.3 Discussion

After evaluating the progress made so far and the themes that researchers are focusing, there are a few areas which invite further exploration.

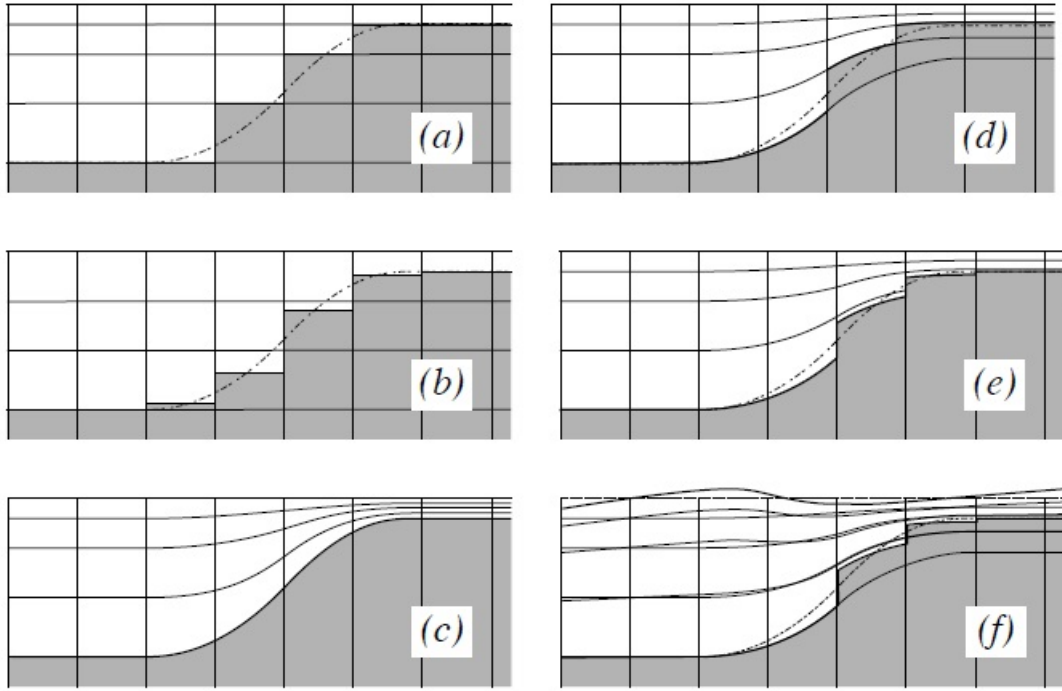


Figure 1: An illustration of different vertical coordinate systems available in NEMO. (?). (a) z-coordinate, (b) z-coordinate with partial cells, (c) s-coordinate, (d) hybrid s-z coordinate, (e) hybrid s-z coordinate with partial cell, (f) shows (e) with a non-linear free surface (which can be used with any coordinate system).

There is scope for further investigation into vertical coordinate systems. Building on the work of (?), including partial cells and hybrid coordinate schemes on model comparisons could provide interesting results of the Gulf Stream representation across different model resolutions. As the improved results in higher resolution models has highlighted the importance of small-scale processes, these kind of investigations could lead to further insight into understanding ocean dynamics.

The evolution of the Gulf Stream and its changes in direction and strength over time (Greatbatch, Fanning, and Goulding, 1991) tells an interesting story and could itself shed light on contributing factors. For example links drawn between different currents could lead to understanding of the impact they have on each other as (Ezer, 2015) suggested that Gulf Stream changes could be impacting the slope current rather than the other way around as previously suspected.

Many of the theories of smaller-scale processes come with proposed parametrisations (whether specifically included with the research or posed as future work), see (Naveira Garabato *et al.*, 2013) amongst others, and there are other schemes proposed for more general processes such as the one proposed by (?) for mesoscale eddies which fell outside the scope for this review. As researchers, we should be aiming towards a parametrisation scheme which could allow the effects of rough bathymetry (and the resulting sub-scale processes) to be taken into account without the need of a higher resolution to resolve the bathymetry itself (thus reducing the necessity and thus costs for high resolution models). However, a deeper understanding of the causes and effects involved would be required than is currently obtained.

### 3.4 Conclusion

We have discussed the ideas and challenges facing researchers when trying to understand and improve the model of the Gulf Stream. A combination of physical processes, their causes and ultimate representation in ocean models holds the key to accurately reproducing the separation and path of the Gulf Stream. This topic continues to inspire lots of research into the areas of ocean eddies, bathymetric interaction and model configurations, as more accurate simulations and higher levels of understanding lie in the future

## 4 Results

Results so far - link into Background & lead nicely into the next section.

### 4.1 Barotropic vorticity diagnostics

- Results so far
- Discussion on results and possible implications
- Results on what we're looking at and why
- Maybe brief description of JEBAR etc. to explain its use & who else has used it to show what - e.g. why are we looking at it etc?
- Should probably include model set up

## 5 Future Aims/Questions

We seek a robust & accurate Gulf Stream path. How can we improve the representation & thus understanding of the Gulf Stream?

We seek to improve the understanding and representation of the Gulf Stream in moderate resolution models. As we have discussed, there are many processes involved in the dynamics of the ocean and thus there are many different directions to turn to when seeking solutions to this problem. Here we will focus on the interactions and effects of the bathymetry while being careful not to ignore other paths this investigation may lead down.

## 5.1 Identifying key processes

- Understanding
- Representation

It is speculated *\*paper\** that interaction with the bathymetry creates small-scale turbulence and instabilities which can cause bathymetric steering and divert currents. If this is not being represented in coarser models, the energy behind the turbulence must be going elsewhere. *\*paper\** compared simulated kinetic energy over different models against measurements taken and noted that in some areas the total kinetic energy was being held higher in the ocean in the models than observed. It is discrepancies such as this which could have much wider implications. If the energy is not penetrating to the ocean floor, we cannot expect to be able to replicate the effects of the bathymetry. Perhaps pulling this energy further down (closer to observed values), we would be able to see the energy transfer from *\*\*\** to the turbulence resulting from the bathymetry.

Of course as previously discussed there are many processes which could contribute to a Gulf Stream path staying too far South. (Ezer, 2016) speculated that amongst other things, the northern branches of the NRG would have to be resolved in order to produce an accurate Gulf Stream. (Zhang and Vallis, 2007) determined that a significant contribution to the generation of the NRG is the bottom vortex stretching resulting from a downslope DWBC, which is in turn the result of the interaction with the bathymetry as the DWBC crosses the path of the Gulf Stream. Thus we see that this circles back to interaction with the bathymetry.

## 5.2 Different model formulations

- Representation of the bathymetry
- Effects of different vertical grids

The many different ocean and OGCM models available allow us to see the effects of many different schemes and parameterisations in use today. In particular the choice of vertical coordinate system has long been discussed, especially in regard to its relevance here. Obviously the representation of the topography and the way it is rendered in the model is a result of the vertical coordinate choice. (Ezer, 2016) revisited the discussion in relation to the Gulf Stream separation and used similar models to determine the most accurate results over different choices for coordinate systems. However, the z-coordinate system chosen did not include any partial or shaved cells. It is inherently obvious that using the z-coordinate system would cause the various slopes in the ocean floor to appear as steps which would significantly alter the flow around the area. . It is not so surprising perhaps that under these circumstances (Ezer, 2016) found sigma or s-coordinates to be the most realistic given that they allow for a smooth ocean floor. It is perhaps natural then to question the effect of partial or shaved cells on these findings. As NEMO allows for such a diverse range of configurations and schemes, it would be interesting to recreate these results while implementing a z-coordinate system with partial cells to allow for a new take on this review.

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### 5.3 Gulf Stream interaction with other systems

- Interaction with other currents (DWBC, etc.)
- Relationship with data sets
- Evolution of the Gulf Stream

## 6 Lines of Enquiry & Methodology

### 6.1 NEMO

- Model Resolution (Ezer, 2016)
  - simple configurations? (Tansley and Marshall, 2001)
- Representation of Bathymetry
  - Vertical Coordinate Systems
  - Partial Cells
  - Nested grids (enhancing resolution in specific areas?)

To examine the aforementioned interplay between the NRG and the path of the Gulf Stream, a simple configuration of NEMO simulating the double gyre set-up seen by the NRG north of the Gulf Stream and the subtropical(?) gyre south of the gulf stream could be used to examine the effects in an idealised model. Results from this could help to influence our investigations within the more realistic models. As (Tansley and Marshall, 2001) used the classic problem of flow past a cylinder to understand the Gulf Stream separation, we too can learn from idealised set up and by breaking the problem down to its fundamental aspects.

### 6.2 Understanding the Gulf Stream

- Turbulence (&Geostrophic turbulence)
- Vorticity and it's contributors

It has been discussed previously that a lack of energy transfer, either by lack of interaction with the bathymetry, or via some other process, could be to blame for the low levels of turbulence found in the area surrounding the separation of the Gulf Stream. As seen when (Tansley and Marshall, 2001) used a larger Reynolds number, allowing for more turbulent flow, flow passing a quarter-cylinder (akin to the coastline at Cape Hatteras), formed jet like streams with smaller eddies breaking away from it. This is akin to satellite observations of the Gulf Stream . This leads to the question which many try to answer how can we improve/enhance the turbulence in a model?

### 6.3 Gulf Stream Relationships

- Data Sets (Ezer, 2015)
  - Explore the possible links between the Gulf Stream and other data sets (e.g. coastal sea level)
- Impact of other currents (Ezer, 2015)
- Changes in the Gulf Stream (Greatbatch, Fanning, and Goulding, 1991) (Ezer, 2015)

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## Notes

- Make lit review more specific - focus it on a few key papers rather than covering a ton of them!
- Focus on phenomenology rather than model stuff
- Add a section somewhere to explain bottom pressure torque and bottom vortex stretching - maybe in diagnostics section but elsewhere too
- Maybe add in weird sandwich scales phenomenology?
- Explain vertically integrated blah blah
- Find out a use for the vertical average info.
- Maybe discuss Sverdrup vs barotropic streamfunction transport? (see P2075 bottom right blue highlighted in Vallis & Zhang 2007)
- Include how the energy is dissipated and where it goes when it hits the bottom - I think this was John T's q from my talk
- PHENOMENOLOGY
- What am I doing with the average?

## References

- Ezer, T.: 2015, Detecting changes in the transport of the Gulf Stream and the Atlantic overturning circulation from coastal sea level data: The extreme decline in 2009-2010 and estimated variations for 1935-2012. *Global and Planetary Change* **129**, 23–36. doi:10.1016/j.gloplacha.2015.03.002. <http://dx.doi.org/10.1016/j.gloplacha.2015.03.002>.
- Ezer, T.: 2016, Revisiting the problem of the Gulf Stream separation: On the representation of topography in ocean models with different types of vertical grids. *Ocean Modelling* **104**, 15–27. doi:10.1016/j.ocemod.2016.05.008.
- Gnanadesikan, A., Griffies, S.M., Samuels, B.L.: 2007, Effects in a climate model of slope tapering in neutral physics schemes. *Ocean Modelling* **16**(1-2), 1–16. ISBN 1463-5003. doi:10.1016/j.ocemod.2006.06.004.
- Greatbatch, R.J., Fanning, A.F., Goulding, A.D.: 1991, A Diagnosis of Interpentadal Circulation Changes in the North Atlantic. *JOURNAL OF GEOPHYSICAL RESEARCH* **96**023(15), 9–22. doi:10.1029/91JC02423.
- Greatbatch, R.J., Sheng, J., Eden, C., Tang, L., Zhai, X., Zhao, J.: 2004, The semi-prognostic method. *Continental Shelf Research* **24**(18), 2149–2165. doi:10.1016/j.csr.2004.07.009.
- Naveira Garabato, A.C., Nurser, A.J.G., Scott, R.B., Goff, J.A.: 2013, The Impact of Small-Scale Topography on the Dynamical Balance of the Ocean. *Journal of Physical Oceanography* **43**(3), 647–668. doi:10.1175/JPO-D-12-056.1. <http://journals.ametsoc.org/doi/abs/10.1175/JPO-D-12-056.1>.

- Nikurashin, M., Vallis, G.K., Adcroft, A.: 2012, Routes to energy dissipation for geostrophic flows in the Southern Ocean. *Nature Geoscience* **6**(1), 48–51. ISBN 1752-0894. doi:10.1038/ngeo1657. <http://www.nature.com/doifinder/10.1038/ngeo1657>.
- Scaife A.A., Copsey D., Gordon C., Harris C., Hinton T., Keeley S., O'Neill A., Roberts M., Williams K.: 2011, Improved Atlantic winter blocking in a climate model. *Geophysical Research Letters*. ISBN 0094-8276. doi:10.1029/2011GL049573. <http://0-onlinelibrary.wiley.com.lib.exeter.ac.uk/doi/10.1029/2011GL049573/epdf>.
- Tansley, C.E., Marshall, D.P.: 2001, Flow past a Cylinder on a Plane, with Application to Gulf Stream Separation and the Antarctic Circumpolar Current. *Journal of Physical Oceanography* **31**, 3274–3284. doi:10.1175/1520-0485(2001)031<3274:FPACOA>2.0.CO;2.
- Zhang, R., Vallis, G.K.: 2007, The Role of Bottom Vortex Stretching on the Path of the North Atlantic Western Boundary Current and on the Northern Recirculation Gyre. *Journal of Physical Oceanography* **37**, 2053–2080. doi:10.1175/JPO3102.1.