Consider equation (7.20).

$$F(x(t) + \eta(t)) = F(x(t)) + \int \frac{\delta F}{\delta x(s)} \eta(s) \, ds + \cdots$$
 (7.20)

For F(x(t)) = x(t) we have

$$F(x(t) + \eta(t)) = x(t) + \eta(t)$$

Then by equation (7.20) to first order

$$\eta(t) = \int \frac{\delta F}{\delta x(s)} \eta(s) \, ds$$

Hence

$$\frac{\delta F}{\delta x(s)} = \begin{cases} 1 & t = s \\ 0 & t \neq s \end{cases}$$