

7-4. Discuss why the integrated part vanishes.

The authors are referring to integration by parts in equation (7.32).

$$\int \frac{\partial F}{\partial x_k} \exp\left(\frac{i}{\hbar} S(x(t))\right) \mathcal{D}x(t) = -\frac{i}{\hbar} \int F \frac{\partial S}{\partial x_k} \exp\left(\frac{i}{\hbar} S(x(t))\right) \mathcal{D}x(t) \quad (7.32)$$

where

$$x_k = x(t_k)$$

Note that integration by parts in (7.32) uses x_k , not $x(t)$.

Let

$$u = \exp\left(\frac{i}{\hbar} S(x(t))\right) \mathcal{D}x(t)$$

$$dv = \frac{\partial F}{\partial x_k}$$

Then

$$du = \frac{i}{\hbar} \frac{\partial S}{\partial x_k} \exp\left(\frac{i}{\hbar} S(x(t))\right) \mathcal{D}x(t)$$

$$v = F$$

Integrate by parts.

$$\int u dv = uv - \int v du$$

$$= F \exp\left(\frac{i}{\hbar} S(x(t))\right) \mathcal{D}x(t) - \frac{i}{\hbar} \int F \frac{\partial S}{\partial x_k} \exp\left(\frac{i}{\hbar} S(x(t))\right) \mathcal{D}x(t)$$

The uv term vanishes due to absence of an integral over $\mathcal{D}x(t)$.