

3-1. Let the classical momentum at $x = a$ be somewhere between zero and p . Then from $p = mv$ we have the following maximum distance d .

$$d = \frac{p}{m}(t_b - t_a)$$

Hence the normalization constant C is

$$\begin{aligned} C &= \int_a^{a+d} \frac{m}{2\pi\hbar(t_b - t_a)} dx \\ &= \left. \frac{mx}{2\pi\hbar(t_b - t_a)} \right|_a^{a+d} \\ &= \frac{m(a+d)}{2\pi\hbar(t_b - t_a)} - \frac{ma}{2\pi\hbar(t_b - t_a)} \\ &= \frac{md}{2\pi\hbar(t_b - t_a)} \\ &= \frac{p}{2\pi\hbar} \end{aligned}$$

Hence diverging normalization corresponds to unrestricted momentum p .

Given

$$x + dx = \frac{p + dp}{m}(t_b - t_a)$$

we have

$$dx = \frac{dp}{m}(t_b - t_a)$$

It follows that

$$\frac{m}{2\pi\hbar(t_b - t_a)} dx = \frac{dp}{2\pi\hbar}$$