

Given the free particle kernel

$$K_0(b, a) = \left( \frac{m}{2\pi i \hbar (t_b - t_a)} \right)^{1/2} \exp \left( \frac{im(x_b - x_a)^2}{2\hbar(t_b - t_a)} \right)$$

show that

$$\frac{\partial K_0}{\partial t_b} = -\frac{i}{\hbar} \left( -\frac{\hbar^2}{2m} \frac{\partial^2 K_0}{\partial x_b^2} \right)$$

Eigenmath solution

$$K0 = \text{sqrt}(m / 2 / \text{pi} / i / \text{hbar} / (tb - ta)) * \\ \exp(i m (xb - xa)^2 / 2 / \text{hbar} / (tb - ta))$$

$$d(K0,tb) == -i / \text{hbar} (-\text{hbar}^2 / 2 / m d(K0,xb,xb))$$