The file q4.txt defines kets, operators, and a measurement function for simulating a four qbit quantum computer. See eigenmath.org/q.c for the program that generates q4.txt.

Ket vectors have 16 elements, one element for each of the 16 states represented by four qbits. Qbit order is $|q_3 q_2 q_1 q_0\rangle$. The following basis kets are defined in q4.txt.

$$|0\rangle = |0000_2\rangle = (1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)$$
$$|1\rangle = |0001_2\rangle = (0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)$$
$$|2\rangle = |0010_2\rangle = (0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)$$
$$|3\rangle = |0011_2\rangle = (0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)$$
$$\vdots$$
$$|15\rangle = |1111_2\rangle = (0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1)$$

Operators are 16×16 matrices that rotate ket vectors. (A ket always has unit length.) The following operators are defined in q4.txt.

C_{mn} Controlled not (CNOT) operator, m is the control qbit, n is the target qbit.

H_n Hadamard operator on qbit n.

X_n Pauli X (NOT) operator on qbit n.

Y_n Pauli Y operator on qbit n.

Z_n Pauli Z operator on qbit n.

Function M measures the final state by drawing a graph of the probability for each of 16 states.

$$M(\psi)$$

Quantum algorithms are expressed as sequences of operators applied to the initial state $|0\rangle$. The operator sequence should be read backwards, from right to left, although the direction makes no difference mathematically.

Deutsch-Jozsa algorithm

Let f be the oracle (16×16 matrix). Then the Deutsch-Jozsa algorithm is

$$\psi = H_2 \, H_1 \, H_0 \, f \, H_3 \, X_3 \, H_2 \, H_1 \, H_0 \, |0\rangle$$

Bernstein-Vazirani algorithm

Let f be the oracle (16×16 matrix). Then the Bernstein-Vazirani algorithm is

$$\psi = H_2 \, H_1 \, H_0 \, f \, Z_3 \, H_3 \, H_2 \, H_1 \, H_0 \, |0\rangle$$