

Canonical commutation relation in one dimension:

$$XP - PX = i\hbar$$

Let

$$X = x, \quad P = -i\hbar \frac{\partial}{\partial x}$$

Then

$$\begin{aligned}(XP - PX)\psi(x, t) &= XP\psi(x, t) - PX\psi(x, t) \\&= x \left(-i\hbar \frac{\partial}{\partial x} \psi(x, t) \right) + i\hbar \frac{\partial}{\partial x} (x\psi(x, t)) \\&= -i\hbar x \frac{\partial}{\partial x} \psi(x, t) + i\hbar \left(\frac{\partial}{\partial x} x \right) \psi(x, t) + i\hbar x \frac{\partial}{\partial x} \psi(x, t) \\&= i\hbar \psi(x, t)\end{aligned}$$

Eigenmath code:

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X(f) = x f
P(f) = -i hbar d(f,x)
X(P(psi(x,t))) - P(X(psi(x,t)))
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Result:

$$i\hbar\psi(x, t)$$