Galilean transformation

Let G be Galilean transformation operators.

$$G_1 = \frac{m}{\hbar} X_1, \quad G_2 = \frac{m}{\hbar} X_2, \quad G_3 = \frac{m}{\hbar} X_3$$

Let U be the unitary transformation

$$U = 1 - i\epsilon G_1 - \frac{1}{2}\epsilon^2 G_1^2$$

Show that to order ϵ^2

$$U^{-1}P_1U = P_1 - \epsilon m, \quad U^{-1}P_2U = P_2, \quad U^{-1}P_3U = P_3$$
 (1)

and

$$U^{-1}HU = H - \epsilon P_1 + \frac{1}{2}\epsilon^2 m \tag{2}$$

where

$$H = \frac{1}{2m} \left(P_1^2 + P_2^2 + P_3^2 \right)$$