3-8. This is the Lagrangian for a harmonic oscillator.

$$L = \frac{m}{2}\dot{x}^2 - \frac{m\omega^2}{2}x^2$$

Show that the resulting kernel is

$$K = F(T) \exp\left(\frac{im\omega}{2\hbar \sin(\omega T)} \left( (x_b^2 + x_a^2) \cos(\omega T) - 2x_b x_a \right) \right)$$

where  $T = t_b - t_a$ .

From problem 2-2 we have

$$S_{cl} = \frac{m\omega}{2\hbar \sin(\omega T)} \left( (x_b^2 + x_a^2) \cos(\omega T) - 2x_b x_a \right)$$

From equation (3.51)

$$K = F(T) \exp\left(\frac{iS_{cl}}{\hbar}\right)$$

By substitution of  $S_{cl}$ 

$$K = F(T) \exp\left(\frac{im\omega}{2\hbar \sin(\omega T)} \left( (x_b^2 + x_a^2) \cos(\omega T) - 2x_b x_a \right) \right)$$