

$$p(x) = \sqrt{2m[E - V(x)]} \quad (9.2)$$

$$T \approx e^{-2\gamma}, \quad \gamma = \frac{1}{\hbar} \int_0^a |p(x)| dx \quad (9.23)$$

Let

$$p(x) = i\sqrt{2m(V_0 - E)}, \quad |p(x)| = \sqrt{2m(V_0 - E)}$$

We have

$$\gamma = \frac{1}{\hbar} \int_{-a}^a \sqrt{2m(V_0 - E)} dx = \frac{2a}{\hbar} \sqrt{2m(V_0 - E)}$$

Hence

$$T^{-1} \approx \exp\left(\frac{4a}{\hbar} \sqrt{2m(V_0 - E)}\right) \quad (1)$$

This is the exact result from problem 2.33.

$$T^{-1} = 1 + \frac{V_0^2}{4E(V_0 - E)} \sinh^2\left(\frac{2a}{\hbar} \sqrt{2m(V_0 - E)}\right)$$

Note that

$$\sinh^2\left(\frac{2a}{\hbar} \sqrt{2m(V_0 - E)}\right) = \frac{1}{4} \exp\left(\frac{4a}{\hbar} \sqrt{2m(V_0 - E)}\right) + \frac{1}{4} \exp\left(-\frac{4a}{\hbar} \sqrt{2m(V_0 - E)}\right) - \frac{1}{2}$$

Hence for $T \ll 1$ we have

$$T^{-1} \approx \frac{V_0^2}{16E(V_0 - E)} \exp\left(\frac{4a}{\hbar} \sqrt{2m(V_0 - E)}\right)$$