6-17. Interpret equation (6.72) by explaining the meaning of each term. Then explain and verify the equation for the second-order coefficient

$$\lambda_{mn}^{(2)} = \left(-\frac{i}{\hbar}\right)^2 \int_{t_a}^{t_b} \int_{t_a}^{t_c} \sum_{j} \exp\left(-\frac{i}{\hbar} E_m(t_b - t_c)\right) V_{mj}(t_c)$$

$$\times \exp\left(-\frac{i}{\hbar} E_j(t_c - t_d)\right) V_{jn}(t_d) \exp\left(-\frac{i}{\hbar} E_n(t_d - t_a)\right) dt_d dt_c \qquad (6.74)$$

Start with equation (6.13).

$$K^{(2)}(b,a) = \left(-\frac{i}{\hbar}\right)^2 \int_{t_a}^{t_b} \int_{-\infty}^{\infty} \int_{t_a}^{t_c} \int_{-\infty}^{\infty} K_0(b,c)V(c)K_0(c,d)V(d)K_0(d,a) \times dx_d dt_d dx_c dt_c$$

Substitute K_U for K_0 . (See problem 6-1 for justification.)

$$K^{(2)}(b,a) = \left(-\frac{i}{\hbar}\right)^2 \int_{t_a}^{t_b} \int_{-\infty}^{\infty} \int_{t_a}^{t_c} \int_{-\infty}^{\infty} K_U(b,c)V(c)K_U(c,d)V(d)K_U(d,a)$$

$$\times dx_d dt_d dx_c dt_c$$

By equation (6.66) substitute sums over eigenstates for K_U .

$$K^{(2)}(b,a) = \sum_{m} \sum_{j} \sum_{n} \left(-\frac{i}{\hbar}\right)^{2} \int_{t_{a}}^{t_{b}} \int_{-\infty}^{\infty} \int_{t_{a}}^{t_{c}} \int_{-\infty}^{\infty} \phi_{m}(x_{b}) \phi_{m}^{*}(x_{c}) V(c) \phi_{j}(x_{c}) \phi_{j}^{*}(x_{d}) V(d) \phi_{n}(x_{d}) \phi_{n}^{*}(x_{a})$$

$$\times \exp\left(-\frac{i}{\hbar} E_{m}(t_{b} - t_{c})\right) \exp\left(-\frac{i}{\hbar} E_{j}(t_{c} - t_{d})\right) \exp\left(-\frac{i}{\hbar} E_{n}(t_{d} - t_{a})\right)$$

$$\times dx_{d} dt_{d} dx_{c} dt_{c}$$

By equation (6.71) substitute V_{mn} for integrals over x.

$$K^{(2)}(b,a) = \sum_{m} \sum_{j} \sum_{n} \left(-\frac{i}{\hbar}\right)^{2} \int_{t_{a}}^{t_{b}} \int_{t_{a}}^{t_{c}} \phi_{m}(x_{b}) V_{mj}(t_{c}) V_{jn}(t_{d}) \phi_{n}^{*}(x_{a})$$

$$\times \exp\left(-\frac{i}{\hbar} E_{m}(t_{b} - t_{c})\right) \exp\left(-\frac{i}{\hbar} E_{j}(t_{c} - t_{d})\right) \exp\left(-\frac{i}{\hbar} E_{n}(t_{d} - t_{a})\right)$$

$$\times dt_{d} dt_{c}$$

Finally, by equation (6.68) we obtain $\lambda_{mn}^{(2)}$.

$$\lambda_{mn}^{(2)}(t_b, t_a) = \sum_{j} \left(-\frac{i}{\hbar}\right)^2 \int_{t_a}^{t_b} \int_{t_a}^{t_c} V_{mj}(t_c) V_{jn}(t_d)$$

$$\times \exp\left(-\frac{i}{\hbar} E_m(t_b - t_c)\right) \exp\left(-\frac{i}{\hbar} E_j(t_c - t_d)\right) \exp\left(-\frac{i}{\hbar} E_n(t_d - t_a)\right)$$

$$\times dt_d dt_c$$

Here are equations (6.68) and (6.71).

$$K_V(b, a) = \sum_{m} \sum_{n} \lambda_{mn}(t_b, t_a) \phi_m(x_b) \phi_n^*(x_a)$$
 (6.68)

$$V_{mn}(t_c) = \int_{-\infty}^{\infty} \phi_m^*(x_c) V(x_c, t_c) \phi_n(x_c) \, dx_c$$
 (6.71)