Linear algebra

The dot function is used to multiply vectors, matrices, and tensors. For example, let

$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}, \quad x = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

The product Ax is computed as follows.

$$A = ((1,2),(3,4))$$

$$x = (x1,x2)$$

$$dot(A,x)$$

$$\begin{bmatrix} x_1 + 2x_2 \\ 3x_1 + 4x_2 \end{bmatrix}$$

The following example shows how to use dot and inv to solve for vector X in AX = B.

$$X = \begin{bmatrix} -\frac{5}{17} \\ \frac{41}{17} \end{bmatrix}$$

The dot function can have more than two arguments. For example, dot(A,B,C) can be used for the dot product of three tensors.

Square brackets are used for component access. Index numbering starts with 1.

$$A = ((a,b),(c,d))$$

$$A[1,2] = -A[1,1]$$

$$A$$

$$\begin{bmatrix} a & -a \\ c & d \end{bmatrix}$$

The following example demonstrates the relation $A^{-1} = (\det A)^{-1} \operatorname{adj} A$.

$$A = ((a,b),(c,d))$$

inv(A) == adj(A) / det(A)

1

Sometimes a calculation will be simpler if it can be reorganized to use \mathtt{adj} instead of \mathtt{inv} . The main idea is to try to prevent the determinant from appearing as a divisor. For example, suppose for matrices A and B you want to show that

$$A - B^{-1} = 0$$

Depending on the complexity of $\det B$, the software may not be able to find a simplification that yields zero. Should that occur, the following alternative formulation can be tried.

$$A \det B - \operatorname{adj} B = 0$$