

Use problem 3-2 and equation 3.42 to show that

$$\frac{\partial \psi}{\partial t} = -\frac{i}{\hbar} \left(-\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} \right) \quad (1)$$

From 3.42 we have

$$\psi(x, t) = \int_{-\infty}^{\infty} K_0(x, t; x_c, t_c) \psi(x_c, t_c) dx_c \quad (2)$$

Let

$$\psi(x_c, t_c) = K_0(x_c, t_c; x_a, t_a)$$

and let I be the integrand

$$I = K_0(x, t; x_c, t_c) \psi(x_c, t_c)$$

Since $\psi(x_c, t_c)$ does not depend on x or t we have by problem 3-2

$$\frac{\partial I}{\partial t} = -\frac{i}{\hbar} \left(-\frac{\hbar^2}{2m} \frac{\partial^2 I}{\partial x^2} \right)$$

Then (1) follows from (2) by linearity of differentiation.