The file q4.txt defines kets, operators, and a measurement function for simulating a four bit quantum computer. See eigenmath.org/q.c for the program that generates q4.txt.

Kets are unit vectors in \mathbb{C}^{16} . The dimension is 16 because four quantum bits have $2^4 = 16$ basis states. Quantum bit numbering is $|q_3q_2q_1q_0\rangle$. The following basis kets are defined in q4.txt.

Operators are 16×16 matrices that rotate ket vectors. (A ket always has unit length.) The following operators are defined in q4.txt.

 H_n Hadamard operator on bit n.

I Identity matrix.

 $P_{mn}(\phi)$ Controlled phase shift, m is the control bit, n is the target bit, ϕ is the phase.

Q Quantum Fourier transform.

R Inverse quantum Fourier transform.

 S_{mn} Swap bits m and n.

 X_n Pauli X (NOT) operator on bit n.

 X_{mn} Controlled not (CNOT) operator, m is the control bit, n is the target bit.

 Y_n Pauli Y operator on bit n.

 Z_n Pauli Z operator on bit n.

Function M measures the final state by drawing a graph of the probability for each of 16 states.

$$M(\psi)$$

Quantum algorithms are expressed as sequences of operators applied to the initial state $|0\rangle$. The operator sequence should be read backwards, from right to left, although the direction makes no difference mathematically.

Deutsch-Jozsa algorithm

Let $f(q_0, q_1, q_2)$ be an operator (16 × 16 matrix) that operates on q_3 in a manner consistent with a constant or balanced oracle. Then the Deutsch-Jozsa algorithm for identifying f is

$$\psi = H_2 H_1 H_0 f(q_0, q_1, q_2) H_3 X_3 H_2 H_1 H_0 |0\rangle$$

Bernstein-Vazirani algorithm

Let $f(q_0, q_1, q_2)$ be an operator (16 × 16 matrix) that operates on q_3 . Then the Bernstein-Vazirani algorithm for identifying f is

$$\psi = H_2 \ H_1 \ H_0 \ f(q_0,q_1,q_2) \ Z_3 \ H_3 \ H_2 \ H_1 \ H_0 \ |0\rangle$$