Consider a system of two electrons with the following eigenstates.

 $\begin{aligned} |0\rangle &= (1,0,0,0) & \text{no electrons} \\ |1\rangle &= (0,1,0,0) & \text{one electron in state } \phi_1 \\ |2\rangle &= (0,0,1,0) & \text{one electron in state } \phi_2 \\ |3\rangle &= (0,0,0,1) & \text{two electrons, one in state } \phi_1, \text{ one in state } \phi_2 \end{aligned}$

Then for the wavefunction basis

$$\phi_n(x) = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right)$$

and for $L = 10^{-9}$ meters we have

$$\hat{E} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0.38 \,\text{eV} & 0 & 0 \\ 0 & 0 & 1.50 \,\text{eV} & 0 \\ 0 & 0 & 0 & 6.55 \,\text{eV} \end{pmatrix}$$

Let $|\xi\rangle$ be the state vector

$$|\xi\rangle = \frac{1}{2}|0\rangle + \frac{1}{2}|1\rangle + \frac{1}{2}|2\rangle + \frac{1}{2}|3\rangle = \begin{pmatrix} 1/2\\1/2\\1/2\\1/2 \end{pmatrix}$$

The expected energy is

$$\langle \xi | \hat{E} | \xi \rangle = \frac{0 \,\text{eV}}{4} + \frac{0.38 \,\text{eV}}{4} + \frac{1.50 \,\text{eV}}{4} + \frac{6.55 \,\text{eV}}{4} = 2.11 \,\text{eV}$$

For the system we are considering, the result of a single measurement is either 0 eV, 0.38 eV, 1.50 eV, or 6.55 eV. The value 2.11 eV is the expected average across multiple measurements. Recall that a measurement causes the system to exit state $|\xi\rangle$ and enter an eigenstate $|0\rangle$, $|1\rangle$, $|2\rangle$, or $|3\rangle$ corresponding to the measured eigenvalue. The system must be put back in state $|\xi\rangle$ before the next measurement.

To use a slot machine analogy, state $|\xi\rangle$ is like the wheels spinning. Observing the system makes the wheels stop. The stopped wheels are in an eigenstate $|0\rangle$, $|1\rangle$, $|2\rangle$, or $|3\rangle$. Once they are stopped the wheels don't change, they remain in the same eigenstate. You have to pull the lever to get the wheels spinning again.