We will need equation (2.7) to determine the classical motion x(t).

$$\frac{d}{dt}\frac{\partial L}{\partial \dot{x}} = \frac{\partial L}{\partial x} \tag{2.7}$$

For the Lagrangian L given in problem 2-1 we have

$$\frac{d}{dt}\frac{\partial L}{\partial \dot{x}} = m\ddot{x} \,, \quad \frac{\partial L}{\partial x} = 0$$

By equation (2.7) we have for the classical acceleration  $\ddot{x}(t)$ 

$$\ddot{x}(t) = 0$$

Hence velocity  $\dot{x}$  is constant and equals distance divided by time.

$$\dot{x} = \frac{x_b - x_a}{t_b - t_a} \tag{1}$$

Substitute (1) into L.

$$L = \frac{m}{2} \left( \frac{x_b - x_a}{t_b - t_a} \right)^2 \tag{2}$$

Integrate (2) to obtain  $S_{cl}$ .

$$S_{cl} = \int_{t_a}^{t_b} L \, dt$$

$$= \frac{m}{2} \left( \frac{x_b - x_a}{t_b - t_a} \right)^2 t \Big|_{t_a}^{t_b} = \frac{m}{2} \frac{(x_b - x_a)^2}{t_b - t_a}$$