

The file “q4.txt” defines kets, operators, and a measurement function for simulating a four qbit quantum computer.

Each of the following operators defined in “q4.txt” is a 16×16 matrix.

Cmn Controlled not (CNOT) operator, m is the control qbit, n is the target qbit.

Hn Hadamard operator on qbit n .

Xn Pauli X (NOT) operator on qbit n .

Yn Pauli Y operator on qbit n .

Zn Pauli Z operator on qbit n .

The initial state of the quantum computer is $|0000\rangle$, i.e., the state in which all qbits are zero. Ket vectors have 16 elements, one element for each of the 16 states represented by four qbits.

$$\begin{aligned} |0000\rangle &= (1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) \\ |1000\rangle &= (0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) \\ |0100\rangle &= (0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) \\ |1100\rangle &= (0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) \\ &\vdots \\ |1111\rangle &= (0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1) \end{aligned}$$

Function M measures the final state by drawing a graph of the probability for each of 16 states.

$$M(\psi)$$

Quantum algorithms are expressed as sequences of operators applied to the initial state $|0000\rangle$. The operator sequence should be read backwards, from right to left, although the direction makes no difference mathematically.

Deutsch-Jozsa algorithm

Let f be the oracle function. Then the Deutsch-Jozsa algorithm is

$$\psi = H_2 H_1 H_0 f H_3 X_3 H_2 H_1 H_0 |0000\rangle$$

Bernstein-Vazirani algorithm

Let f be the oracle function. Then the Bernstein-Vazirani algorithm is

$$\psi = H_2 H_1 H_0 f Z_3 H_3 H_2 H_1 H_0 |0000\rangle$$