Canonical commutation relation

Canonical commutation relation in one dimension:

$$XP - PX = i\hbar$$

Let

$$X = x, \quad P = -i\hbar \frac{\partial}{\partial x}$$

Then

$$\begin{split} (XP - PX)\psi(x,t) &= XP\psi(x,t) - PX\psi(x,t) \\ &= x \left(-i\hbar \frac{\partial}{\partial x} \psi(x,t) \right) + i\hbar \frac{\partial}{\partial x} \left(x\psi(x,t) \right) \\ &= -i\hbar x \frac{\partial}{\partial x} \psi(x,t) + i\hbar \left(\frac{\partial}{\partial x} x \right) \psi(x,t) + i\hbar x \frac{\partial}{\partial x} \psi(x,t) \\ &= i\hbar \psi(x,t) \end{split}$$

Eigenmath code:

Result:

$$i\hbar\psi(x,t)$$

Another example: Show that

$$[X^2, P^2] = 2i\hbar(XP + PX)$$

Eigenmath code:

Result:

ok

(The statement check(A == B) halts if A not equal B.)