Let θ_{12} be the angular distance between $P_1=(r_1,\theta_1,\phi_1)$ and $P_2=(r_2,\theta_2,\phi_2)$. Then

$$\cos \theta_{12} = \cos \theta_1 \cos \theta_2 + \sin \theta_1 \sin \theta_2 \cos(\theta_1 - \theta_2)$$

Also

$$\cos \theta_{12} = \frac{r_1^2 + r_2^2 - r_{12}^2}{2r_1r_2}$$

where

$$r_{12}^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2$$

and

$$x_1 = r_1 \sin \theta_1 \cos \phi_1$$

$$y_1 = r_1 \sin \theta_1 \sin \phi_1$$

$$z_1 = r_1 \cos \theta_1$$

$$x_2 = r_2 \sin \theta_2 \cos \phi_2$$

$$y_2 = r_2 \sin \theta_2 \sin \phi_2$$

$$z_2 = r_2 \cos \theta_2$$