Fine structure 3

Using the following formula for the fine structure of hydrogen

$$E_{nj} = -\mu c^{2} \left[1 - \frac{1}{\sqrt{1 + \left(\frac{\alpha}{n - j - \frac{1}{2} + \sqrt{(j + \frac{1}{2})^{2} - \alpha^{2}}}\right)^{2}}} \right]$$

verify the following table of transitions.

| Transition | Wavelength (nm) |
|---|-------------------------------|
| $3_{s1/2} \rightarrow 2_{p1/2}$ $3_{s1/2} \rightarrow 2_{p3/2}$ | $656.457 \\ 656.473$ |
| $3_{p1/2} \rightarrow 2_{s1/2}$ $3_{p3/2} \rightarrow 2_{s1/2}$ | $656.457 \\ 656.452$ |
| $3_{d3/2} \rightarrow 2_{p1/2}$ $3_{d3/2} \rightarrow 2_{p3/2}$ $3_{d5/2} \rightarrow 2_{p3/2}$ | 656.452 656.468 656.466 |