Verify the following spin operator table from "Quantum Mechanics" by Susskind and Friedman.

$$
\begin{array}{ccccc}
 & |uu\rangle & |ud\rangle & |du\rangle & |dd\rangle \\[4pt]
\sigma_z & |uu\rangle & |ud\rangle & -|du\rangle & -|dd\rangle \\
\sigma_x & |du\rangle & |dd\rangle & |uu\rangle & |ud\rangle \\
\sigma_y & i|du\rangle & i|dd\rangle & -i|uu\rangle & -i|ud\rangle \\
\tau_z & |uu\rangle & -|ud\rangle & |du\rangle & -|dd\rangle \\
\tau_x & |ud\rangle & |uu\rangle & |dd\rangle & |du\rangle \\
\tau_y & i|ud\rangle & -i|uu\rangle & i|dd\rangle & -i|du\rangle
\end{array}
$$

For single spins we have

$$
|u\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \quad |d\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}
$$

For a system of two spins we use the Kronecker product of $|u\rangle$ and $|d\rangle$. Hence

$$
|uu\rangle = |u\rangle \otimes |u\rangle = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \quad |ud\rangle = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix}, \quad |du\rangle = \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}, \quad |dd\rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}
$$

The spin operators for single spins are

$$
\sigma_z = \tau_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, \quad \sigma_x = \tau_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \sigma_y = \tau_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}
$$

For a system of two spins, we again use the Kronecker product.

$$
\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \otimes I, \quad \tau_z = I \otimes \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, \quad \text{etc.}
$$

Click "Demo" to see and run the Eigenmath code.