

Template functions

Function f in $\mathbf{d}(\mathbf{f}, \mathbf{x})$ does not have to be defined, it can be a template function with just a name and an argument list. The argument list determines the result. For example, $\mathbf{d}(\mathbf{f}(\mathbf{x}), \mathbf{x})$ evaluates to itself because f depends on x . However, $\mathbf{d}(\mathbf{f}(\mathbf{x}), \mathbf{y})$ evaluates to zero because f does not depend on y .

Example 1. $f(x)$ depends on x .

```
 $\mathbf{d}(\mathbf{f}(\mathbf{x}), \mathbf{x})$ 
```

```
 $\mathbf{d}(f(x), x)$ 
```

Example 2. $f(x)$ does not depend on y .

```
 $\mathbf{d}(\mathbf{f}(\mathbf{x}), \mathbf{y})$ 
```

```
0
```

Example 3. $f(x, y)$ depends on both x and y .

```
 $\mathbf{d}(\mathbf{f}(\mathbf{x}, \mathbf{y}), \mathbf{y})$ 
```

```
 $\mathbf{d}(f(x, y), y)$ 
```

Example 4. $f()$ is shorthand for dependence on any symbol.

```
 $\mathbf{d}(\mathbf{f}(), \mathbf{t})$ 
```

```
 $\mathbf{d}(f(), t)$ 
```

As the final example shows, an empty argument list causes \mathbf{d} to evaluate to itself, regardless of the second argument.

Template functions are useful for experimenting with differential forms. For example, verify the identity

$$\nabla \cdot (\nabla \times \mathbf{F}) = 0$$

```
 $\mathbf{F} = (\mathbf{F}_x(), \mathbf{F}_y(), \mathbf{F}_z())$   
 $\mathbf{div}(\mathbf{curl}(\mathbf{F}))$ 
```

```
0
```