Consider the following anova program and its output. Note that the least significant difference test has more power than the t-test.

```
input trt $ y @@ ;
datalines;
A 6
       \mathbf{A} O
               A 2
                      A 8
                            A 11
A 4
       A 13
              A 1
                      A 8
                            A 0
B 0
       B 2
              В 3
                      B 1
                            B 18
B 4
              В 9
                            В 9
       B 14
                      B 1
C 13
       C 10
              C 18
                      C 5
                            C 23
C 12
       C 5
              C 16
                      C 1
                            C 20
proc anova;
model y = trt;
means trt / lsd ttest ;
                               Analysis of Variance
    Source
               DF
                       Sum of Squares
                                            Mean Square
                                                             F Value
                                                                          Pr > F
                         293.60000000
                                           146.80000000
    Model
                2
                                                                3.98
                                                                          0.0305
    Error
                27
                         995.10000000
                                            36.8555556
                        1288.70000000
    Total
               29
                              Coeff Var
                                             Root MSE
                R-Square
                                                             Y Mean
                0.227826
                               76.846553
                                             6.070878
                                                           7.900000
                DF
                                           Mean Square
                                                            F Value
                                                                         Pr > F
     Source
                            Anova SS
     TRT
                  2
                        293.60000000
                                          146.80000000
                                                               3.98
                                                                         0.0305
                                  Mean Response
                                                            95% CI MAX
             TRT
                       N
                                Mean Y
                                            95% CI MIN
             Α
                      10
                              5.300000
                                              1.360937
                                                              9.239063
                              6.100000
                                              2.160937
                                                             10.039063
             В
                      10
             С
                      10
                              12.300000
                                              8.360937
                                                             16.239063
                        Least Significant Difference Test
                              95% CI MIN
                                                                        Pr > |t|
  TR.T
                  Delta Y
                                             95% CI MAX
                                                            t Value
         TR.T
  Α
         В
                 -0.80000
                               -6.370677
                                               4.770677
                                                              -0.29
                                                                          0.7705
                 -7.00000
                                                              -2.58
         С
                               -12.570677
                                              -1.429323
                                                                          0.0157 *
  Α
  В
                 0.800000
                               -4.770677
                                               6.370677
                                                               0.29
                                                                          0.7705
         Α
                                                                          0.0305 *
  В
         С
                 -6.200000
                               -11.770677
                                              -0.629323
                                                              -2.28
  С
                  7.000000
                                1.429323
                                              12.570677
                                                               2.58
                                                                          0.0157 *
         Α
  С
         В
                  6.200000
                                0.629323
                                              11.770677
                                                               2.28
                                                                          0.0305 *
                                Two Sample t-Test
  TRT
         TRT
                  Delta Y
                              95% CI MIN
                                             95% CI MAX
                                                            t Value
                                                                        Pr > |t|
                                                                          0.7466
  Α
         В
                 -0.800000
                               -5.922307
                                               4.322307
                                                              -0.33
                 -7.000000
                                                              -2.60
                                                                          0.0182 *
         С
                               -12.664270
                                              -1.335730
  Α
  В
         Α
                  0.800000
                               -4.322307
                                               5.922307
                                                               0.33
                                                                          0.7466
  В
         С
                 -6.200000
                               -12.467653
                                               0.067653
                                                              -2.08
                                                                          0.0523
  С
                  7.000000
                                1.335730
                                              12.664270
                                                                          0.0182 *
         Α
                                                               2.60
  С
         В
                  6.200000
                               -0.067653
                                              12.467653
                                                               2.08
                                                                          0.0523
```

Let us take a closer look at the mean response table.

Mean Response

TRT	N	Mean Y	95% CI MIN	95% CI MAX
A	10	5.300000	1.360937	9.239063
В	10	6.100000	2.160937	10.039063
C	10	12.300000	8.360937	16.239063

Recall that the confidence interval for a treatment mean is

$$\bar{y} \pm t(1 - \alpha/2, \text{dfe}) \times \text{SE}, \quad \text{SE} = \sqrt{\frac{\text{MSE}}{n}}$$

Recall that SE is standard error and MSE (mean square error) is estimated model variance. From the analysis of variance table at the top of the output we have

Source	DF	Sum of Squares	Mean Square
Error	27	995.10000000	36.8555556

Hence

$$dfe = 27$$
, $MSE = 36.8556$

The confidence interval for the mean of treatment A can be checked by typing the following into R.

```
ybar = 5.3
n = 10
MSE = 36.8556
dfe = 27
alpha = 0.05
SE = sqrt(MSE / n)
t = qt(1 - alpha/2, dfe) * SE
ybar - t
ybar + t
```

R prints the following results.

- [1] 1.360934 [1] 9.239066
- The R results match the mean response table for treatment A.

TRT	N	Mean Y	95% CI MIN	95% CI MAX
Α	10	5.300000	1.360937	9.239063

Let us take a closer look at the first line of the least significant difference table.

Least Significant Difference Test

```
TRT TRT Delta Y 95% CI MIN 95% CI MAX t Value Pr > |t| A B -0.800000 -6.370677 4.770677 -0.29 0.7705
```

The least significant difference of two treatment means \bar{y}_A and \bar{y}_B is

LSD =
$$t(1 - \alpha/2, \text{dfe}) \times \text{SE}$$
, SE = $\sqrt{\text{MSE} \times \left(\frac{1}{n_A} + \frac{1}{n_B}\right)}$

The corresponding confidence interval is

$$\bar{y}_A - \bar{y}_B \pm \text{LSD}$$

The confidence interval in the LSD table can be checked by typing the following into R.

```
ybarA = 5.3

ybarB = 6.1

nA = 10

nB = 10

MSE = 36.8556

dfe = 27

alpha = 0.05

SE = sqrt(MSE * (1/nA + 1/nB))

LSD = qt(1 - alpha/2, dfe) * SE

ybarA - ybarB - LSD

ybarA - ybarB + LSD
```

R prints the following results.

- [1] -6.37068
- [1] 4.77068

The R results match the confidence interval in the LSD table.

```
TRT TRT Delta Y 95% CI MIN 95% CI MAX t Value Pr > |t| A B -0.800000 -6.370677 4.770677 -0.29 0.7705
```