

## 随机梯度下降法 Stochastic gradient descent

批梯度下降方法：

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$
$$\text{Repeat}\{$$
$$\quad // \text{for every } j=1, \dots, n$$
$$\theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
$$\}$$

随机梯度下降法

1. 初始化打乱训练样本
2. 代码

$$\text{Repeat}\{$$
$$\quad \text{for } i := 1, \dots, m\{$$
$$\quad // \text{for every } j=0, \dots, n$$
$$\theta_j := \theta_j - \alpha (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
$$\quad \}\}$$

- 批梯度下降：使用所有m个样本在每次迭代中
- 随机梯度下降：使用1个样本在每次迭代中
- 微型梯度下降：使用b个样本在每次迭代中

## Mini-Batch Gradient Descent 微型梯度下降

假设b=10, m=1000

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```
Repeat{ \\
\text{//for every } j=1, 11, 21, 31, \dots, 991\} \\
\theta_j := \theta_j - \alpha \frac{1}{10} \sum_{i=1}^{i+9} (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)} \\
\}
```

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$$\text{Repeat}\{$$
$$\quad // \text{for every } j=1, 11, 21, 31, \dots, 991$$
$$\theta_j := \theta_j - \alpha \frac{1}{10} \sum_{i=1}^{i+9} (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
$$\}$$
$$\text{Repeat}\{$$
$$\quad // \text{for every } j=1, 11, 21, 31, \dots, 991$$
$$\theta_j := \theta_j - \alpha \frac{1}{10} \sum_{i=1}^{i+9} (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
$$\}$$