

Destany Brown's Python Code and Solution for Homework 1

code was written using jupyter lab

the code is saved as the following files: localization_and_uncertainty.ipynb, localization_and_uncertainty.pdf, and localization_and_uncertainty.py

please also find code and solution @ my github: https://github.com/georgiabfi/robot_localization_and_uncertainty

```

In [1]: import operator
import matplotlib.pyplot as plt

def plot_color(dict1):
    #calculates color for bar graphs
    max_val=max(dict1.items(), key=operator.itemgetter(1))

    color=[]
    for key in dict1:
        if dict1[key] < max_val[1]:
            color.append('b')
        else:
            color.append('r')
    return color

#bayes filter function for calculating probability of robot's
location and for plotting bar graphs
def bayes_filter(bel_x, z,step):

    #outputs the likelihood of where the robot is before sensing a
wall or door
    if step==0:
        print("\nInitial Position: ")
        for key in bel_x:
            print(f"bel(x{step} = {key}) = ", round(bel_x[key],3))

    #initialization of variables
    #number of subplots
    nplt=4
    #subplots size
    plt.figure(figsize=(10,8))
    w=0.5
    #first subplot of the probability of the robot's position at
step =0
    plt.subplot(nplt,1,1)
    plt.title(f"bel(x{step}) ")
    plt.bar(*zip(*bel_x.items()),color=plot_color(bel_x),width=w)

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    #10% likelihood that the robot moves to the grid after the next
    grid (p2)
    second_grid=0.1
    #0% likelihood that the robot moves to the yellow grid after p3
    yellow_grid=0.0

    #state transition probability matrix
    state_trans_prob={f"x{step+1}" =
p0":[same_grid,0,0,0],f"x{step+1}" = p1":[first_grid,same_grid,0,0],
    f"x{step+1}" =
p2":[second_grid,first_grid,same_grid,0],f"x{step+1}" =
p3":[0,second_grid,first_grid,same_grid]}

    #state space matrix details
    print(f"\nAt step t={step+1}, after the control u{step+1}, the
    robot returns a measurement of z{step+1} ={z}.\n")

    print("State Transition Probability: ")
    for key in state_trans_prob:
        print(f"({key}|u{step+1},x{step}=p0, x{step}=p1,x{step}=p2,
x{step}=p3)= ",state_trans_prob[key])

    #location of door and wall
    door=['p1','p3']
    wall=['p0','p2']

    #chances of sensing a wall or door
    door_sense=
{"wall_p0":.3,"door_p1":.8,"wall_p2":.3,"door_p3":.8}
    wall_sense=
{"wall_p0":.7,"door_p1":.2,"wall_p2":.7,"door_p3":.2}

    #calculates the bel bar values for all potential locations

```

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",round(bel_bar[key[-2:]],3))

    #bel_bar plot
    plt.subplot(nplt,1,2)
    plt.title(f"bel_bar(x{step+1})")

plt.bar(*zip(*bel_bar.items()),color=plot_color(door_sense),width=w)

    sum_bel=[]
    print(f"\nProbability of the robot sensing the {z} at step =
{step+1}:")

    #plots probability of the robot detecting a door or wall
    if z == "door":
        #print("If Measurement: ", z)
        plt.subplot(nplt,1,3)
        plt.title(f"p(z{step+1}={z}|x{step+1})")

plt.bar(*zip(*door_sense.items()),color=plot_color(door_sense),width=w)
        for key in door_sense:
            print(f"p(z{step+1} = {z}|x{step+1}={key[-2:]})=",
door_sense[key])
            for key in bel_bar:

                if key in door:
                    #print("if door: ",key)
                    sum_bel.append(bel_bar[key]*.80)
                    bel_bar[key]*=.80

```

```

        #print( else measurement: , z)

    for key in wall_sense:
        print(f"p(z{step+1} = {z}|x{step+1}={key[-2:]})=",
wall_sense[key])
        for key in bel_bar:

            if key in wall:
                #print("if wall: ",key)
                sum_bel.append(bel_bar[key]*.70)
                bel_bar[key]*=.70

            else:
                #print("else wall: ",key)
                sum_bel.append(bel_bar[key]*.20)
                bel_bar[key]*=.20

print(f"\nNormalization and  $\eta$  calculation: ")

# $\eta$  (normalization value) is calculated
for i in range(len(sum_bel)):
    print(f"bel(x{step+1} = p{i}) = p(z{step+1} =
{z}|x{step+1}=p{i})*bel_bar(x{step+1} = p{i})* $\eta$  =
{round(sum_bel[i],3)}* $\eta$ ")

```

```
plt.bar(*zip(*new_bel.items()),color=plot_color(new_bel),width=w)
plt.tight_layout()
plt.show()
```

```
if z=="door":
```

```
    return new_bel
```

```
else:
```

```
    return new_bel #,df
```

```
#the robot_localization function initializes the robot's belief of  
its initial position and sets what features it can detect  
#the robot_localization function also runs the function  
bayes_filter
```

Solution for Homework 1

In [2]: `robot_localization()`

Initial Position:

$\text{bel}(x_0 = p_0) = 0.25$

$\text{bel}(x_0 = p_1) = 0.25$

$\text{bel}(x_0 = p_2) = 0.25$

$\text{bel}(x_0 = p_3) = 0.25$

At step $t=1$, after the control u_1 , the robot returns a measurement of $z_1 = \text{door}$.

State Transition Probability:

$(x_1 = p_0 | u_1, x_0=p_0, x_0=p_1, x_0=p_2, x_0=p_3) = [0.2, 0, 0, 0]$

$(x_1 = p_1 | u_1, x_0=p_0, x_0=p_1, x_0=p_2, x_0=p_3) = [0.7, 0.2, 0, 0]$

$(x_1 = p_2 | u_1, x_0=p_0, x_0=p_1, x_0=p_2, x_0=p_3) = [0.1, 0.7, 0.2, 0]$

$(x_1 = p_3 | u_1, x_0=p_0, x_0=p_1, x_0=p_2, x_0=p_3) = [0, 0.1, 0.7, 0.2]$

Calculations of bel_bar for all potential locations ($p_0 \sim p_3$):

$\text{bel_bar}(x_1=p_0) = 0.05$

$\text{bel_bar}(x_1=p_1) = 0.225$

$\text{bel_bar}(x_1=p_2) = 0.25$

$\text{bel_bar}(x_1=p_3) = 0.25$

Probability of the robot sensing the door at step = 1:

$p(z_1 = \text{door} | x_1=p_0) = 0.3$

$p(z_1 = \text{door} | x_1=p_1) = 0.8$

$p(z_1 = \text{door} | x_1=p_2) = 0.3$

$p(z_1 = \text{door} | x_1=p_3) = 0.8$

Normalization and η calculation:

$\text{bel}(x_1 = p_0) = p(z_1 = \text{door} | x_1=p_0) * \text{bel_bar}(x_1 = p_0) * \eta = 0.015 * \eta$

$\text{bel}(x_1 = p_1) = p(z_1 = \text{door} | x_1=p_1) * \text{bel_bar}(x_1 = p_1) * \eta = 0.18 * \eta$

```

bel(x1 = p2) = p(z1 = door|x1=p2)*bel_bar(x1 = p2)*η = 0.075*η
bel(x1 = p3) = p(z1 = door|x1=p3)*bel_bar(x1 = p3)*η = 0.2*η
η = 1/0.47 = 2.128

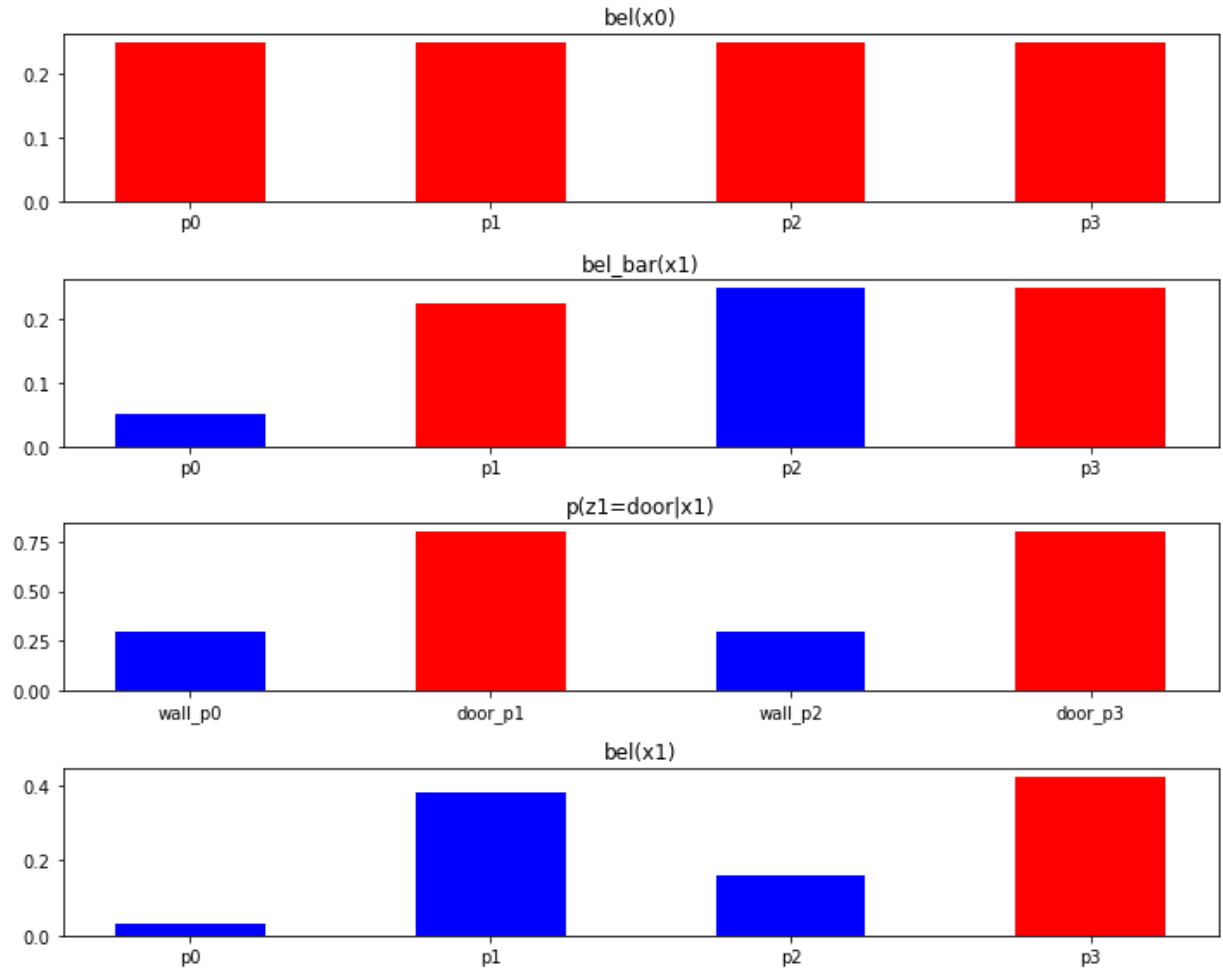
```

New updated belief of the robot's localization probability after step 1:

```

bel(x1 = p0) = 0.032
bel(x1 = p1) = 0.383
bel(x1 = p2) = 0.16
bel(x1 = p3) = 0.426

```



At step $t=2$, after the control u_2 , the robot returns a measurement of $z_2 = \text{wall}$.

State Transition Probability:

```

(x2 = p0|u2,x1=p0, x1=p1,x1=p2, x1=p3)= [0.2, 0, 0, 0]
(x2 = p1|u2,x1=p0, x1=p1,x1=p2, x1=p3)= [0.7, 0.2, 0, 0]
(x2 = p2|u2,x1=p0, x1=p1,x1=p2, x1=p3)= [0.1, 0.7, 0.2, 0]
(x2 = p3|u2,x1=p0, x1=p1,x1=p2, x1=p3)= [0, 0.1, 0.7, 0.2]

```

Calculations of bel_bar for all potential locations ($p_0 \sim p_3$):

```

bel_bar(x2=p0)= 0.006
bel_bar(x2=p1)= 0.099
bel_bar(x2=p2)= 0.303
bel_bar(x2=p3)= 0.235

```

Probability of the robot sensing the wall at step = 2:

$p(z_2 = \text{wall} | x_2 = p_0) = 0.7$
 $p(z_2 = \text{wall} | x_2 = p_1) = 0.2$
 $p(z_2 = \text{wall} | x_2 = p_2) = 0.7$
 $p(z_2 = \text{wall} | x_2 = p_3) = 0.2$

Normalization and η calculation:

$\text{bel}(x_2 = p_0) = p(z_2 = \text{wall} | x_2 = p_0) * \text{bel_bar}(x_2 = p_0) * \eta = 0.004 * \eta$
 $\text{bel}(x_2 = p_1) = p(z_2 = \text{wall} | x_2 = p_1) * \text{bel_bar}(x_2 = p_1) * \eta = 0.02 * \eta$
 $\text{bel}(x_2 = p_2) = p(z_2 = \text{wall} | x_2 = p_2) * \text{bel_bar}(x_2 = p_2) * \eta = 0.212 * \eta$
 $\text{bel}(x_2 = p_3) = p(z_2 = \text{wall} | x_2 = p_3) * \text{bel_bar}(x_2 = p_3) * \eta = 0.047 * \eta$
 $\eta = 1/0.284 = 3.527$

New updated belief of the robot's localization probability after step 2:

$\text{bel}(x_2 = p_0) = 0.016$
 $\text{bel}(x_2 = p_1) = 0.07$
 $\text{bel}(x_2 = p_2) = 0.749$
 $\text{bel}(x_2 = p_3) = 0.166$

