

Examination: I Sem. M.Tech, Ph.D (Mining Engineering)
Semester: Monsoon Semester
Subject: Mang. Decision Making NMND 501

Session: 2024-25
Max. Marks: 28
Time: 2 Hrs.

Q1. Find a minimum-cost shipping schedule for the transportation problem using VAM for basic feasible solution and MODI for the final optimal solution.

11. Coal is mined and processed at the following four mines in Kentucky, West Virginia, and Virginia. (8 marks)

<i>Location</i>	<i>Capacity (tons)</i>
A. Cabin Creek	90
B. Surry	50
C. Old Fort	80
D. McCoy	<u>60</u> 280

These mines supply the following amount of coal to utility power plants in three cities.

<i>Plant</i>	<i>Demand (tons)</i>
1. Richmond	120
2. Winston-Salem	100
3. Durham	<u>110</u> 330

The railroad shipping costs (\$1,000s) per ton of coal are shown in the following table. Because of railroad construction, shipments are now prohibited from Cabin Creek to Richmond.

<i>From</i>	<i>To</i>		
	1	2	3
A	\$ 7	\$ 10	\$ 5
B	12	9	4
C	7	3	11
D	9	5	7

- Set up the transportation tableau for this problem, determine the initial solution using VAM, and compute total cost.
- Solve using MODI.

Examination: I Sem. M.Tech, Ph.D (Mining Engineering)

Session: 2024-25

Semester: Monsoon Semester

Max. Marks: 28

Subject: Mang. Decision Making NMND 501

Time: 2 Hrs.

Q2.

Clearly show all steps and equations in solving the problem

(3 marks)

$$\begin{aligned} \text{maximize } & 8x_1 - 9x_2 + 12x_3 + 4x_4 + 11x_5 \\ \text{subject to } & 2x_1 - 3x_2 + 4x_3 + x_4 + 3x_5 \leq 1 \\ (\text{P}) \quad & x_1 + 7x_2 + 3x_3 - 2x_4 + x_5 \leq 1 \\ & 5x_1 + 4x_2 - 6x_3 + 2x_4 + 3x_5 \leq 22 \\ & x_1, x_2, x_3, x_4, x_5 \geq 0 \end{aligned}$$

1. Write down the dual (D) of the problem (P).

Q3.

(8 marks)

A mine turns out two minerals A and B, each of which is processed to two machines X and Y. A requires two hours of X and 4 hours of Y; B requires 4 hours of X and 2 hours of Y. If x is the number of A and y is the number of B produced daily, write down two inequalities in x and y, noting that neither X nor Y can work more than 24 hours a day. Assuming that all minerals produced are sold, and A yields a profit of Rs. 60/unit and B yields a profit of Rs. 100/unit, find how much of each mineral should be produced daily for maximum profit.

- a. Write the equations for linear programming
- b. SOLVE Graphically by plotting the inequalities
- c. Show the feasible region in the graph and the vertices
- d. Find the optimal point that maximizes the objective function

Q5. Answer the following: each subsection carries 2 marks

(4 marks)

- i. List any 4 benefits of the First Mile connectivity project of CIL to mining logistics
- ii. List any 4 measures taken by the Indian railways to increase coal transportation

Examination: I Sem. M.Tech, Ph.D (Mining Engineering)

Session: 2024-25

Semester: Monsoon Semester

Max. Marks: 28

Subject: Mang. Decision Making NMND 501

Time: 2 Hrs.

Q6. Use Hungarian Method to Solve

(5 marks)

(6) A company is faced with the problem of assigning six different machines M₁, M₂, M₃, M₄, M₅, and M₆ to six different jobs J₁, J₂, J₃, J₄, J₅, and J₆ respectively. The costs estimated (in hundreds of rupees) are given in the table below:

	J ₁	J ₂	J ₃	J ₄	J ₅	J ₆
M ₁	44	67	41	53	48	64
M ₂	46	69	40	45	45	68
M ₃	43	73	37	51	44	62
M ₄	50	65	35	50	46	63
M ₅	50	65	35	50	46	63
M ₆	50	65	35	50	46	63

- (i) Formulate the problem as an assignment model for the assignment of machines to jobs so that the total cost of assignment is minimum.
(ii) Find an optimal solution using the assignment algorithm. What is the total cost of assignment?